Mudcard

- **Are there quantitative ways to determine how well the iid assumption holds on data?**
  - here is a good read on the topic
  - short answer is no
- **Following up to the discussion on sklearn's lack of support for support stratification where y is continuous: can you provide some insight on why (or what kind of cases) stratification would be necessary in a regression problem?**
  - PS4, problem 1c will cover this
  - it is a good idea to stratify, if the distribution of the regression target variable is heavy-tailed (e.g., exponential, log-normal)
  - if you do not stratify, some of your sets might not contain rare values from the heavy tail thus throwing off the regression model
- **In k-fold cross validation, will it make the model better if we shuffle the training/validation data before each round of training, instead of just shuffling once before taking k non-overlapping folds?**
  - that's not kfold, it's much closer to the basic split (train/validation/test)
- **If we want to predict a continuous variable, y, are imbalanced features still a concern?**
  - we don't really care about features being imbalanced
  - imbalance is important for a classification target variable
- **I am still confused on how the stratefied K fold is implemented. Is it the same process regardless of the dataset we use?**
  - yes, these splitting strategies are independent of the dataset
  - the only constraint is that the dataset needs to be IID if you want to use kfold splitting
- **A bit confused why we would want to use KFold and cross-validation as opposed to normal splitting**
  - both are equally good as long as your dataset is IID
  - use whichever you prefer in your project
  - kfold is quite often used so I wanted you to be familiar with it
- **Why do we see different random states in different models? Example - on Kaggle, we see random state = 0/10/42, etc. Apart from splitting up the dataset into different points, does the value of the random state affect the data in any other way?**
  - you will see that some ML algorithms are non-deterministic (all decision tree-based models) and you'll need a random state for those otherwise you model changes every time you rerun the cell
- **To be clear: shuffling is just randomizing the index/order of the raw data?**
  - yep, randomly rearragnes the rows

- **are test_size and train_size in the split methods pretty much specifying the same thing? I.e. does a test_size of 0.2 imply train_size 0.8?**
  - not the same thing
  - train_size = 1 - test_size
  - train size != test_size unless you want a 50-50 split
- **When using Kfold with 5 folds, should we still test the model on 10 different random states? So essentially we would be testing 50 different models?**
  - yes, that's recommended because if you use 5 folds once, that's still only one test score
- **What does this part of the k-fold splitting code mean: "for train_index, val_index in kf.split(X_other,y_other)"?**
  - print out train_index and val_index to check
- **Still a bit unclear about how stratification intuitively balances out unbalanced data sets. Just from a visualization standpoint.**
- **Can we apply stratify to balance datasets?**
  - stratification does NOT balances out an imbalanced dataset
  - if 1% of points belong to the minority class, stratification guarantees that all sets in your dataset will contain exactly 1% of the minority class
- **If train_test_split randomly separates the dataset already, why do we still need a shuffle argument for the function?**
  - experiement with the code below to figure it out

```
from sklearn.model_selection import train_test_split
import numpy as np
X, y = np.arange(20).reshape((10, 2)), range(10)
print(X,y)

X_train, X_test, y_train, y_test = train_test_split(X, y,
test_size=0.33, random_state=42,shuffle=False)

print(y_train,y_test)
```

- **could you specify why is random walk sequence not iid?**
  - D the underlying distribution changes as soon as a step is taken
- **I want to know when should I use KFolds and when can use simple train-val-test split.**
  - both are equally good if your dataset is IID
- **The baseline metric for regression was said in class to be RMSE. How is the baseline calculated?**
  - no, RMSE is not a baseline metric
  - RMSE is one metric you can use with regression datasets
  - the baseline RMSE of a regression problem can be determined if you calculate the RMSE with respect to the mean of the target variable
  - we will cover this in a few weeks
- **I understand that KFold splits for us but what exactly are we testing for, what is the test? is it a test of balance or just whatever test we code?**

    - you want to have a test set to calculate the generalization error
- **I am curious about the arguments in function, should we remember arguments or look for specific arguments using help funciotn when we need it? How is the situation when having this kind of interview?**
    - I still look up arguments all the time :)
    - some arguments stick if you use them often enough (like stratify, random_state, some plotting arguments)
    - you are not expected to know all arguments of sklearn, numpy, or pandas methods during an interview

Split non-iid data

By the end of this lecture, you will be able to

- split non-iid data based on group ID
- split non-iid time series data

The supervised ML pipeline

The goal: Use the training data (X and y) to develop a model which can accurately predict the target variable (y_new') for previously unseen data (X_new).

1. Exploratory Data Analysis (EDA): you need to understand your data and verify that it doesn't contain errors

- do as much EDA as you can!

2. Split the data into different sets: most often the sets are train, validation, and test (or holdout)

- practitioners often make errors in this step!
- you can split the data randomly, based on groups, based on time, or any other non-standard way if necessary to answer your ML question

3. Preprocess the data: ML models only work if X and Y are numbers! Some ML models additionally require each feature to have 0 mean and 1 standard deviation (standardized features)

- often the original features you get contain strings (for example a gender feature would contain 'male', 'female', 'non-binary', 'unknown') which needs to transformed into numbers
- often the features are not standardized (e.g., age is between 0 and 100) but it needs to be standardized

4. Choose an evaluation metric: depends on the priorities of the stakeholders

- often requires quite a bit of thinking and ethical considerations

5. Choose one or more ML techniques: it is highly recommended that you try multiple models

- start with simple models like linear or logistic regression
- try also more complex models like nearest neighbors, support vector machines, random forest, etc.

6. Tune the hyperparameters of your ML models (aka cross-validation)

- ML techniques have hyperparameters that you need to optimize to achieve best performance
- for each ML model, decide which parameters to tune and what values to try
- loop through each parameter combination
    - train one model for each parameter combination
    - evaluate how well the model performs on the validation set
- take the parameter combo that gives the best validation score
- evaluate that model on the test set to report how well the model is expected to perform on previously unseen data

7. Interpret your model: black boxes are often not useful

- check if your model uses features that make sense (excellent tool for debugging)
- often model predictions are not enough, you need to be able to explain how the model arrived to a particular prediction (e.g., in health care)

Examples of non-iid data

- if there is any sort of time or group structure in your data, it is likely non-iid
    - **group structure:**
        - **samples are not identically distributed, D might be different for each group**
        - a person appears multiple times in the dataset (e.g., hospital/doctor visits)
        - data is collected on multiple instrucments (e.g., equipment failure prediction)
    - **time series data**
        - **values are not independent**
        - stocks price
        - covid19 cases
        - weather data

Ask yourself these questions!

- What is the intended use of the model? What is it supposed to do/predict?
- What data do you have available at the time of prediction?

- Your split must mimic the intended use of the model only then will you accurately estimate how well the model will perform on previously unseen points (generalization error).
- two examples:
  - if you want to predict the outcome of a new patient's visit to the ER:
    - your test score must be based on patients not included in training and validation
    - your validation score must be based on patients not included in training
    - points of one patient should not be distributed over multiple sets because your generalization error will be off
  - a youtube video was released 4 weeks ago and you want to predict if it will be featured a week from now, your training data should only contain info that will available upon predictions (stuff you know 4 weeks after release)
    - split data based on youtube vid ID
    - use info that's available 4 weeks after release
    - your classification label will be whether it was featured or not 5 weeks after release

Split non-iid data

By the end of this lecture, you will be able to

- **split non-iid data based on group ID**
- split non-iid time series data

An example: seizure project

- you can read the publication here
- classification problem:
  - epileptic seizures vs. non-epileptic psychogenic seizures
- data from empatica wrist sensor
  - heart rate, skin temperature, EDA, blood volume pressure, acceleration
- data collection:
  - patients come to the hospital for a few days
  - eeg and video recording to determine seizure type
  - wrist sensor data is collected
- question:
  - Can we use the wrist sensor data to differentiate the two seizure types on new patients?

In [1]:
```
import pandas as pd
import numpy as np
```

```
df = pd.read_csv('data/seizure_data.csv')
print(df[df['patient ID'] == 32])
```

```
    patient ID            seizure_ID  ACC_mean  BVP_mean  EDA_mean    HR_mean
\
5           32  ID32__day3_arm_1_sz1  1.028539 -0.092102  0.112795  64.748167
6           32  ID32__day3_arm_1_sz1  1.027986  0.745437  0.130486  63.715667
7           32  ID32__day2_arm_1_sz0  1.002146  0.150810  0.189272  61.838500
8           32  ID32__day2_arm_1_sz0  1.005410  0.482859  1.226038  66.240833
9           32  ID32__day1_arm_1_sz0  0.997017 -0.925122  0.200990  56.103667
10          32  ID32__day1_arm_1_sz0  1.009207  1.618456  1.679754  64.668167
27          32  ID32__day1_arm_1_sz0  1.000290  0.046690  0.123165  54.289500
28          32  ID32__day1_arm_1_sz0  1.010351  0.125039  0.471180  65.060667
29          32  ID32__day2_arm_1_sz0  1.018163  0.254302  0.206010  61.875833
30          32  ID32__day2_arm_1_sz0  1.016785  1.242893  0.954649  66.216167
34          32  ID32__day3_arm_1_sz1  1.008867  0.070180  0.195966  65.995667
35          32  ID32__day3_arm_1_sz1  1.009554  0.222872  0.229909  63.871000
58          32  ID32__day3_arm_1_sz0  1.008873 -0.550857  0.177822  67.750833
79          32  ID32__day3_arm_1_sz0  1.026840  0.355953  0.205273  69.124667

    TEMP_mean  ACC_stdev   BVP_stdev  EDA_stdev  ...  BVP_50th  EDA_50th  \
5   36.944833   0.007469   36.486091   0.003905  ...     1.815  0.112710
6   36.676333   0.028190   84.964155   0.018598  ...     2.210  0.131921
7   38.600333   0.003747   64.194294   0.024278  ...     6.985  0.186026
8   39.296083   0.035257  165.665784   0.891139  ...     1.140  1.062333
9   34.656667   0.022648   77.013336   0.132008  ...     3.800  0.142159
10  34.678000   0.046047  146.515297   0.438236  ...     5.585  1.690537
27  38.467417   0.019826   51.176639   0.014530  ...     7.765  0.124259
28  38.448000   0.077142   61.205657   0.156170  ...     3.290  0.510114
29  37.681583   0.006805   40.982246   0.017099  ...     1.455  0.202632
30  37.979500   0.032493  219.277839   0.612229  ...    -5.785  1.028171
34  40.659458   0.021812   49.981175   0.013259  ...     3.480  0.198570
35  40.481333   0.048531   37.409681   0.031963  ...     0.695  0.228677
58  39.906667   0.021431   27.472002   0.003085  ...     1.955  0.178073
79  34.490167   0.008165   40.742936   0.003550  ...     3.090  0.206207

    HR_50th  TEMP_50th  ACC_75th  BVP_75th  EDA_75th  HR_75th  TEMP_75th  \
5    65.060      36.95  1.029947   16.3725  0.115591  65.8175     36.990
6    62.175      36.81  1.029947   21.1625  0.147611  66.2100     36.840
7    61.840      38.61  1.006085   43.8850  0.209086  61.9000     38.790
8    62.325      39.37  1.008872   49.4325  2.313129  71.0625     39.390
9    56.110      34.66  0.996821   35.2700  0.176739  56.6050     34.660
10   65.790      34.66  1.021497   70.4800  1.998868  67.7725     34.735
27   53.960      38.49  1.002073   39.8525  0.133226  54.7425     38.500
28   65.285      38.45  1.014302   25.4625  0.577047  69.4975     38.530
29   61.910      37.68  1.022811   29.2125  0.219282  61.9300     37.750
30   64.700      38.00  1.022811   65.5000  1.503002  69.5725     38.030
34   66.145      40.68  1.013700   13.1300  0.199852  67.0425     40.710
35   64.395      40.49  1.016106   12.9650  0.260383  65.9625     40.530
58   68.170      39.93  1.015264   17.8625  0.179354  68.5725     40.030
79   69.810      34.37  1.033260   13.4550  0.207488  70.0000     34.680

    label
5     0.0
6     0.0
7     0.0
8     0.0
9     0.0
10    0.0
27    0.0
```

```
28    0.0
29    0.0
30    0.0
34    0.0
35    0.0
58    0.0
79    0.0

[14 rows x 48 columns]
```

In [2]:
```
y = df['label']
patient_ID = df['patient ID']
seizure_ID = df['seizure_ID']
X = df.drop(columns=['patient ID','seizure_ID','label'])
classes, counts = np.unique(y,return_counts=True)
print('balance:',np.max(counts/len(y)))
```

```
balance: 0.6884057971014492
```

In [3]:
```
from sklearn.svm import SVC
from sklearn.metrics import accuracy_score
from sklearn.model_selection import StratifiedKFold
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
from sklearn.pipeline import make_pipeline
from sklearn.model_selection import KFold
from sklearn.model_selection import GridSearchCV
from sklearn.metrics import make_scorer

def ML_pipeline_kfold_GridSearchCV(X,y,random_state,n_folds):
    # create a test set
    X_other, X_test, y_other, y_test = train_test_split(X, y, test_size=0.2, ra
    # splitter for _other
    kf = StratifiedKFold(n_splits=n_folds,shuffle=True,random_state=random_stat
    # create the pipeline: preprocessor + supervised ML method
    scaler = StandardScaler()
    pipe = make_pipeline(scaler,SVC())
    # the parameter(s) we want to tune
    param_grid = {'svc__C': np.logspace(-3,4,num=8),'svc__gamma': np.logspace(-
    # prepare gridsearch
    grid = GridSearchCV(pipe, param_grid=param_grid,scoring = make_scorer(accur
                        cv=kf, return_train_score = True)
    # do kfold CV on _other
    grid.fit(X_other, y_other)
    return grid, grid.score(X_test, y_test)
```

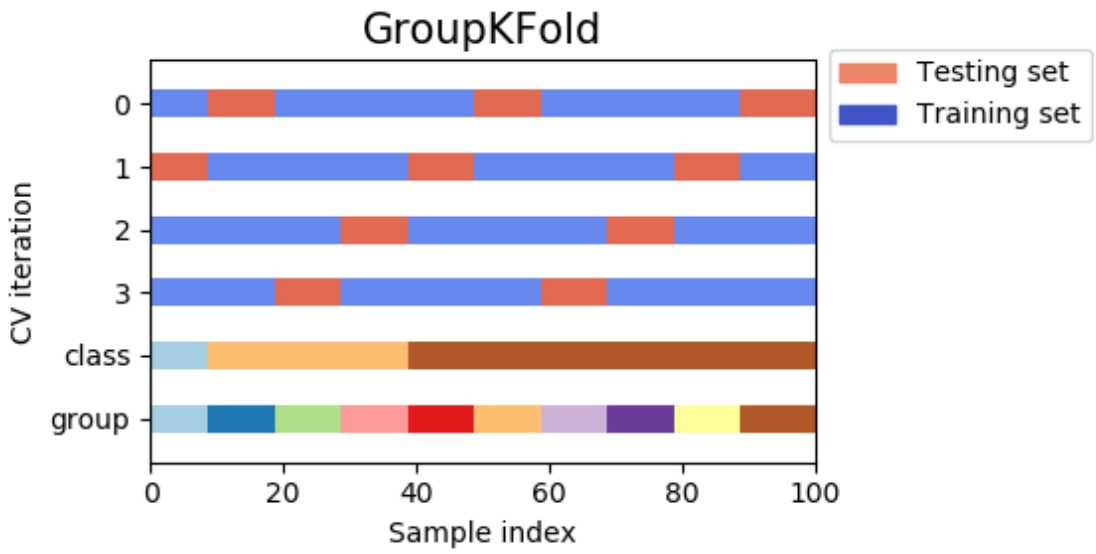
In [4]:
```
test_scores = []
for i in range(5):
    grid, test_score = ML_pipeline_kfold_GridSearchCV(X,y,i*42,5)
    print(grid.best_params_)
    print('best CV score:',grid.best_score_)
    print('test score:',test_score)
    test_scores.append(test_score)
print('test accuracy:',np.around(np.mean(test_scores),2),'+/-',np.around(np.std
```

```
{'svc__C': 1.0, 'svc__gamma': 0.01}
best CV score: 0.9227272727272726
test score: 0.9285714285714286
{'svc__C': 10.0, 'svc__gamma': 0.01}
best CV score: 0.9363636363636363
test score: 0.9285714285714286
{'svc__C': 10.0, 'svc__gamma': 0.01}
best CV score: 0.9045454545454547
test score: 0.9464285714285714
{'svc__C': 10.0, 'svc__gamma': 0.01}
best CV score: 0.9
test score: 0.9285714285714286
{'svc__C': 10.0, 'svc__gamma': 0.01}
best CV score: 0.9363636363636363
test score: 0.9107142857142857
test accuracy: 0.93 +/- 0.01
```

This is wrong! A very bad case of data leakage!

- the textbook case of information leakage!
- if we just do KFold CV blindly, the points from the same patient end up in different sets
  - when you deploy the model and apply it to data from new patients, that patient's data will be seen for the first time
- the ML pipeline needs to mimic the intended use of the model!
  - we want to split the points based on the patient ID!
  - we want all points from the same patient to be in either train/CV/test

Group-based split: GroupKFold



In [5]:
```
from sklearn.model_selection import GroupKFold
from sklearn.model_selection import GroupShuffleSplit
def ML_pipeline_groups_GridSearchCV(X,y,groups,random_state,n_folds):
    # create a test set based on groups
```

```
    splitter = GroupShuffleSplit(n_splits=1,test_size=0.2,random_state=random_s
    for i_other,i_test in splitter.split(X, y, groups):
        X_other, y_other, groups_other = X.iloc[i_other], y.iloc[i_other], grou
        X_test, y_test, groups_test = X.iloc[i_test], y.iloc[i_test], groups.il
    # check the split
#     print(pd.unique(groups))
#     print(pd.unique(groups_other))
#     print(pd.unique(groups_test))
    # splitter for _other
    kf = GroupKFold(n_splits=n_folds)
    # create the pipeline: preprocessor + supervised ML method
    scaler = StandardScaler()
    pipe = make_pipeline(scaler,SVC())
    # the parameter(s) we want to tune
    param_grid = {'svc__C': np.logspace(-3,4,num=8),'svc__gamma': np.logspace(-
    # prepare gridsearch
    grid = GridSearchCV(pipe, param_grid=param_grid,scoring = make_scorer(accur
                        cv=kf, return_train_score = True)
    # do kfold CV on _other
    grid.fit(X_other, y_other, groups=groups_other)
    return grid, grid.score(X_test, y_test)
```

In [6]:

```
test_scores = []
for i in range(5):
    grid, test_score = ML_pipeline_groups_GridSearchCV(X,y,patient_ID,i*42,5)
    print(grid.best_params_)
    print('best CV score:',grid.best_score_)
    print('test score:',test_score)
    test_scores.append(test_score)
print('test accuracy:',np.around(np.mean(test_scores),2),'+/-',np.around(np.std
```

```
{'svc__C': 10.0, 'svc__gamma': 0.001}
best CV score: 0.7609139784946237
test score: 0.6410256410256411
{'svc__C': 0.1, 'svc__gamma': 0.01}
best CV score: 0.6522727272727272
test score: 0.2711864406779661
{'svc__C': 10.0, 'svc__gamma': 0.001}
best CV score: 0.5720073891625616
test score: 0.9390243902439024
{'svc__C': 10.0, 'svc__gamma': 0.001}
best CV score: 0.7061742424242425
test score: 0.43243243243243246
{'svc__C': 10000.0, 'svc__gamma': 0.001}
best CV score: 0.6082407407407406
test score: 0.8901098901098901
test accuracy: 0.63 +/- 0.26
```

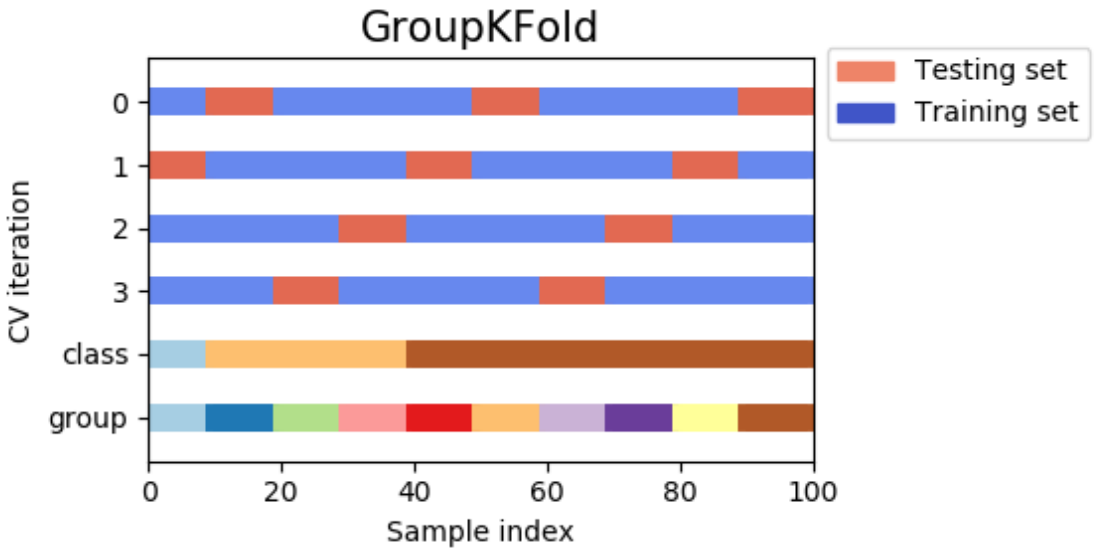
The takeaway

- an incorrect cross validation pipeline gives misleading results
  - usually the model appears to be pretty accurate
  - but the performance is poor when the model is deployed
- this can be avoided by a careful cross validation pipeline
  - think about how your model will be used

- mimic that future use in CV

Let's take a look at group splitters using toy datasets

Group-based split: GroupKFold



In [7]:
```
from sklearn.model_selection import GroupKFold
import numpy as np

X = np.ones(shape=(8, 2))
y = np.ones(shape=(8, 1))
groups = np.array([1, 1, 2, 2, 2, 3, 3, 3])

group_kfold = GroupKFold(n_splits=3)

for train_index, test_index in group_kfold.split(X, y, groups):
    print("TRAIN:", train_index, "TEST:", test_index)
```

```
TRAIN: [0 1 2 3 4] TEST: [5 6 7]
TRAIN: [0 1 5 6 7] TEST: [2 3 4]
TRAIN: [2 3 4 5 6 7] TEST: [0 1]
```

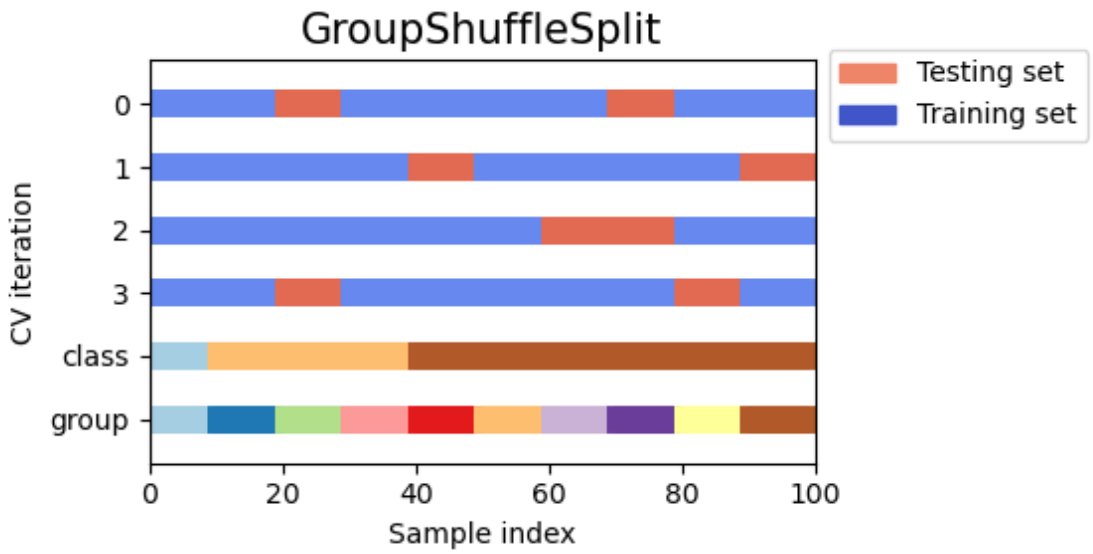
In [8]:
```
help(GroupKFold)
```

```
Help on class GroupKFold in module sklearn.model_selection._split:

class GroupKFold(_BaseKFold)
 |  GroupKFold(n_splits=5)
 |
 |  K-fold iterator variant with non-overlapping groups.
 |
 |  The same group will not appear in two different folds (the number of
 |  distinct groups has to be at least equal to the number of folds).
 |
 |  The folds are approximately balanced in the sense that the number of
 |  distinct groups is approximately the same in each fold.
 |
 |  Read more in the :ref:`User Guide <group_k_fold>`.
 |
 |  Parameters
 |  ----------
 |  n_splits : int, default=5
 |      Number of folds. Must be at least 2.
 |
 |      .. versionchanged:: 0.22
 |          ``n_splits`` default value changed from 3 to 5.
 |
 |  Notes
 |  -----
 |  Groups appear in an arbitrary order throughout the folds.
 |
 |  Examples
 |  --------
 |  >>> import numpy as np
 |  >>> from sklearn.model_selection import GroupKFold
 |  >>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
 |  >>> y = np.array([1, 2, 3, 4])
 |  >>> groups = np.array([0, 0, 2, 2])
 |  >>> group_kfold = GroupKFold(n_splits=2)
 |  >>> group_kfold.get_n_splits(X, y, groups)
 |  2
 |  >>> print(group_kfold)
 |  GroupKFold(n_splits=2)
 |  >>> for train_index, test_index in group_kfold.split(X, y, groups):
 |  ...     print("TRAIN:", train_index, "TEST:", test_index)
 |  ...     X_train, X_test = X[train_index], X[test_index]
 |  ...     y_train, y_test = y[train_index], y[test_index]
 |  ...     print(X_train, X_test, y_train, y_test)
 |  ...
 |  TRAIN: [0 1] TEST: [2 3]
 |  [[1 2]
 |   [3 4]] [[5 6]
 |   [7 8]] [1 2] [3 4]
 |  TRAIN: [2 3] TEST: [0 1]
 |  [[5 6]
 |   [7 8]] [[1 2]
 |   [3 4]] [3 4] [1 2]
 |
 |  See Also
 |  --------
 |  LeaveOneGroupOut : For splitting the data according to explicit
```

```
|      domain-specific stratification of the dataset.
|
|  Method resolution order:
|      GroupKFold
|      _BaseKFold
|      BaseCrossValidator
|      builtins.object
|
|  Methods defined here:
|
|  __init__(self, n_splits=5)
|      Initialize self.  See help(type(self)) for accurate signature.
|
|  split(self, X, y=None, groups=None)
|      Generate indices to split data into training and test set.
|
|      Parameters
|      ----------
|      X : array-like of shape (n_samples, n_features)
|          Training data, where `n_samples` is the number of samples
|          and `n_features` is the number of features.
|
|      y : array-like of shape (n_samples,), default=None
|          The target variable for supervised learning problems.
|
|      groups : array-like of shape (n_samples,)
|          Group labels for the samples used while splitting the dataset into
|          train/test set.
|
|      Yields
|      ------
|      train : ndarray
|          The training set indices for that split.
|
|      test : ndarray
|          The testing set indices for that split.
|
|  ----------------------------------------------------------------------
|  Data and other attributes defined here:
|
|  __abstractmethods__ = frozenset()
|
|  ----------------------------------------------------------------------
|  Methods inherited from _BaseKFold:
|
|  get_n_splits(self, X=None, y=None, groups=None)
|      Returns the number of splitting iterations in the cross-validator
|
|      Parameters
|      ----------
|      X : object
|          Always ignored, exists for compatibility.
|
|      y : object
|          Always ignored, exists for compatibility.
|
|      groups : object
```

```
|          Always ignored, exists for compatibility.
|
|      Returns
|      -------
|      n_splits : int
|          Returns the number of splitting iterations in the cross-validator.
|
|  ----------------------------------------------------------------------
|  Methods inherited from BaseCrossValidator:
|
|  __repr__(self)
|      Return repr(self).
|
|  ----------------------------------------------------------------------
|  Data descriptors inherited from BaseCrossValidator:
|
|  __dict__
|      dictionary for instance variables (if defined)
|
|  __weakref__
|      list of weak references to the object (if defined)
```

Group-based split: GroupShuffleSplit



In [9]:
```python
from sklearn.model_selection import GroupShuffleSplit

gss = GroupShuffleSplit(n_splits=5, train_size=.8, random_state=42)

for train_idx, test_idx in gss.split(X, y, groups):
    print("TRAIN:", train_idx, "TEST:", test_idx)
```

```
TRAIN: [2 3 4 5 6 7] TEST: [0 1]
TRAIN: [0 1 5 6 7] TEST: [2 3 4]
TRAIN: [2 3 4 5 6 7] TEST: [0 1]
TRAIN: [0 1 5 6 7] TEST: [2 3 4]
TRAIN: [2 3 4 5 6 7] TEST: [0 1]
```

Quiz 1

Go back to the GroupKFold example above. What happens when you change n_splits to 4? Why?

Why could we set the n_splits argument to 5 in GroupShuffleSplit? Check the manual of both methods to find the answer.

Explain your answer in a couple of sentences!

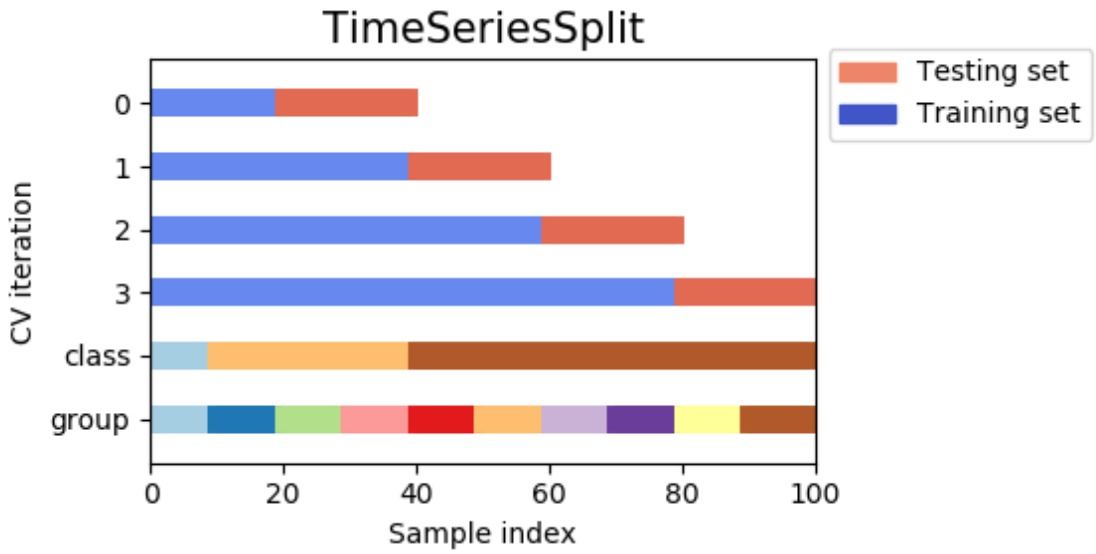
Split non-iid data

By the end of this lecture, you will be able to

- split non-iid data based on group ID
- **split non-iid time series data**

Data leakage in time series data is similar!

- do NOT use information in CV which will not be available once your model is deployed
  - don't use future information!



Time series data

- stock price, crypto price, covid-19 positive case counts, etc
- simple data structure:

| time | observation | |---------- |:----------: | | t_0 | y_0 | | t_1 | y_1 | | t_2 | y_2 | | ... | ... | | t_i | y_i | | ... | ... | | t_n-1 | y_n-1 | | t_n | y_n |

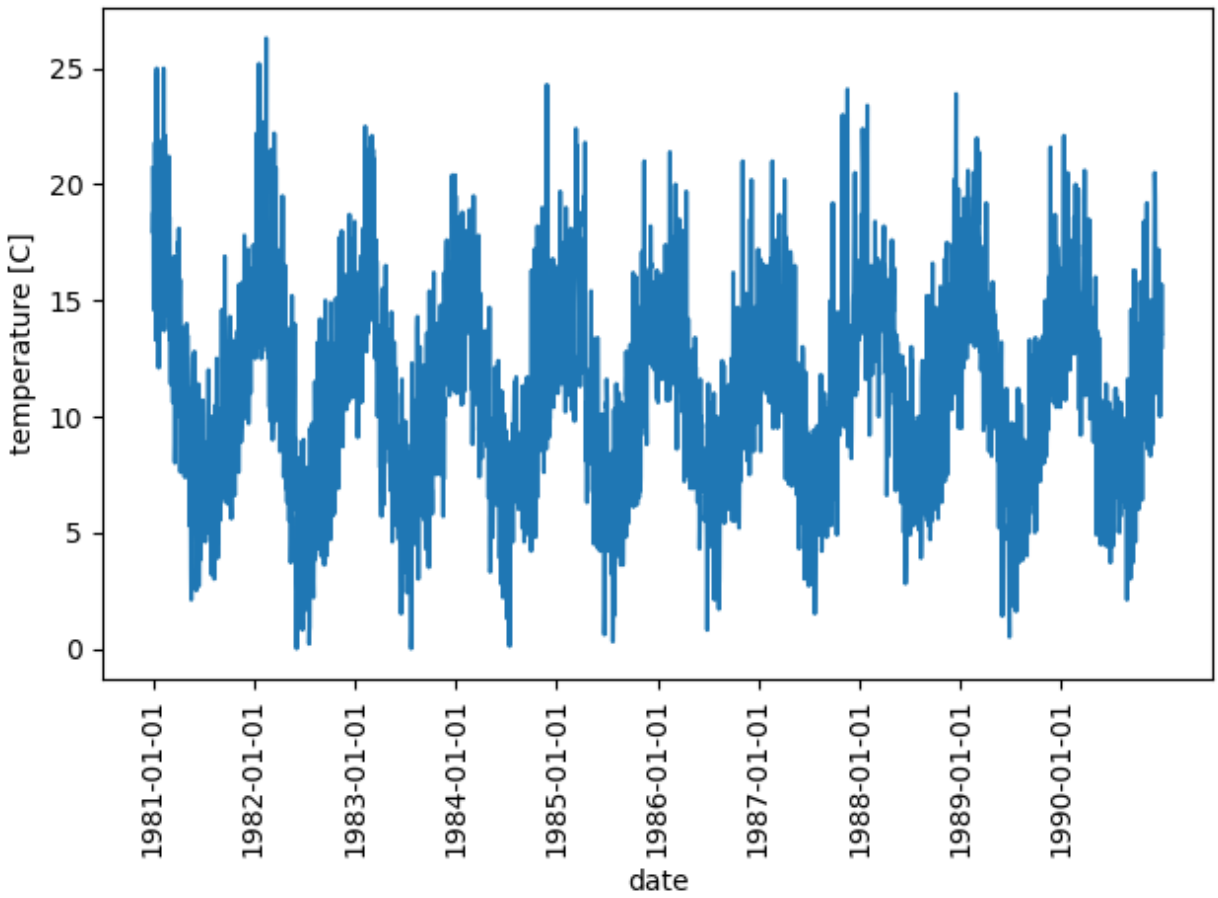
- assumption:
  - the difference between two time points (dt) is constant
  - e.g., 1 minute, 5 minutes, 1 hour, or 1 day

Autocorrelation

- the correlation of the time series data with a delayed copy of itself
- delay on the x axis, correlation coefficient on the y axis
- if delay = 0, the correlation coefficient is 1
- if the delay is short, autocorrelation can be high
- autocorrelation tends to subside for longer delays
- let's check an example

In [10]:
```
import pandas as pd
import matplotlib.pyplot as plt
import matplotlib
import numpy as np

df = pd.read_csv('data/daily-min-temperatures.csv')
print(df.shape)
print(df.head())

plt.plot(df['Temp'])
plt.xticks(np.arange(len(df['Date']))[::365],df['Date'].iloc[::365],rotation=90
plt.xlabel('date')
plt.ylabel('temperature [C]')
plt.tight_layout()
plt.show()
```

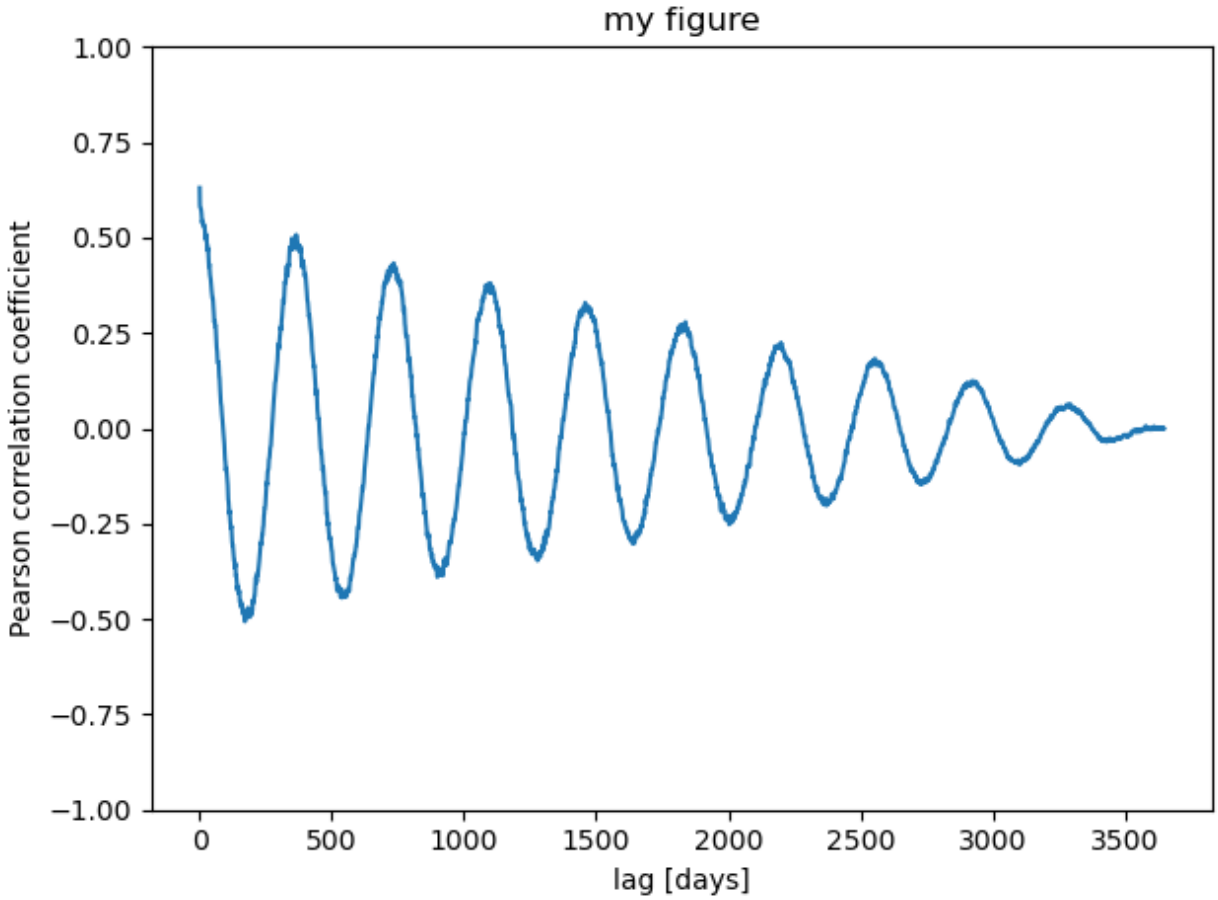
```
(3650, 2)
         Date  Temp
0  1981-01-01  20.7
1  1981-01-02  17.9
2  1981-01-03  18.8
3  1981-01-04  14.6
4  1981-01-05  15.8
```

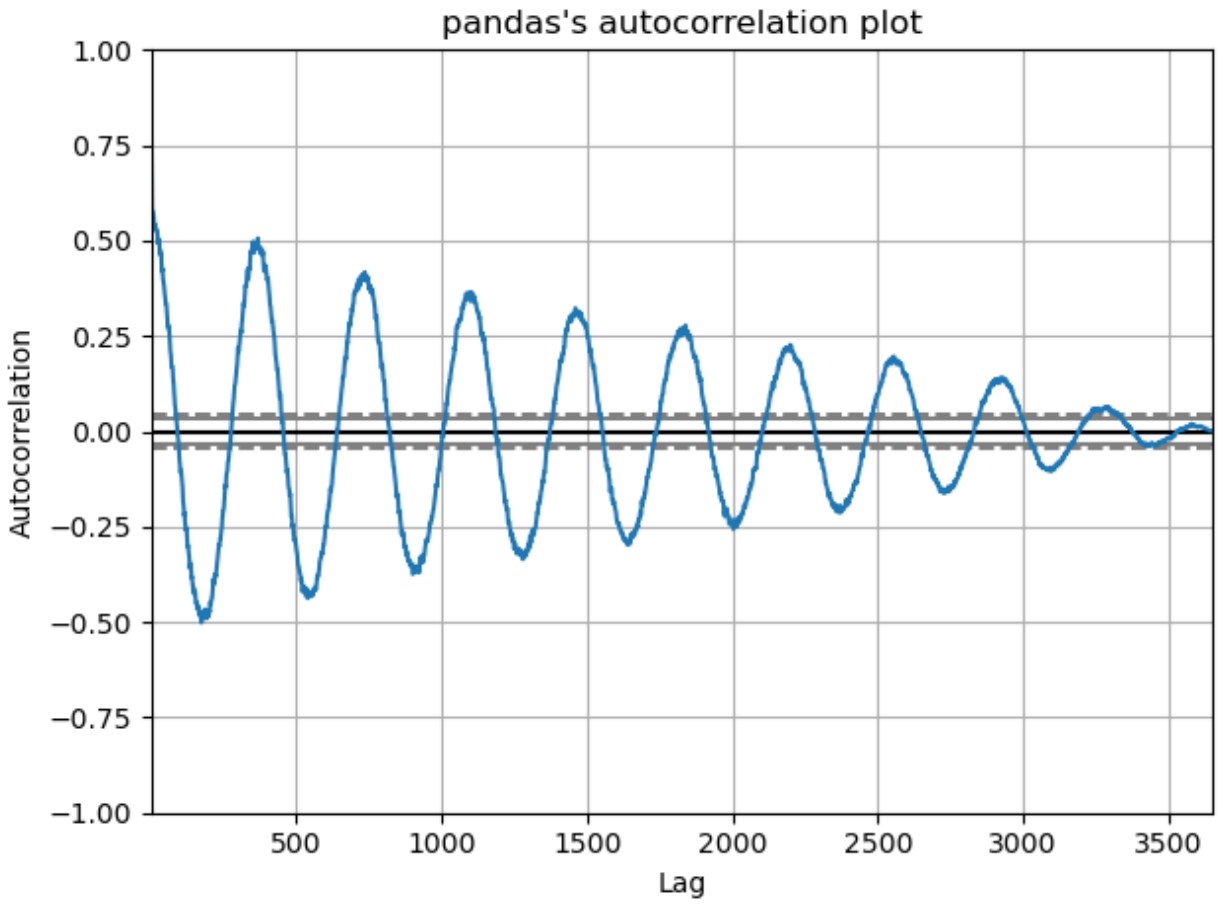


In [11]:
```
# let's create an autocorrelation plot

lags = np.arange(3650)
corr_coefs = np.zeros(3650)

for i in np.arange(len(lags)):
    x = df['Temp'].iloc[i:-1].reset_index(drop=True) # recent observations
    y = df['Temp'].iloc[:-i-1].reset_index(drop=True) # lag-shifted observation
    # the shapes must be the same
    if x.shape != y.shape:
        raise ValueError('shape mismatch!')
    # Pearson correlation multiplied by the fraction of time series used
    corr_coefs[i] = x.corr(y,method='pearson')*x.shape[0]/df['Temp'].shape[0]
print(corr_coefs[:10])

plt.plot(lags[2:],corr_coefs[2:])
plt.ylim([-1,1])
plt.xlabel('lag [days]')
plt.ylabel('Pearson correlation coefficient')
plt.title('my figure')
plt.tight_layout()
plt.show()

# a one-liner
pd.plotting.autocorrelation_plot(df['Temp'])
plt.title("pandas's autocorrelation plot")
plt.tight_layout()
plt.show()
```

```
[0.99972603 0.77446147 0.63057611 0.58570362 0.5780733  0.57758888
 0.57542059 0.57472479 0.56812066 0.56190417]
```

```
/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.10/site-packages/numpy/li
b/function_base.py:2821: RuntimeWarning: Degrees of freedom <= 0 for slice
  c = cov(x, y, rowvar, dtype=dtype)
/Users/azsom/opt/anaconda3/envs/data1030/lib/python3.10/site-packages/numpy/li
b/function_base.py:2680: RuntimeWarning: divide by zero encountered in true_di
vide
  c *= np.true_divide(1, fact)
```





Autoregression: create an iid feature matrix using lag features

- goal:
  - predict what y will be dt in the future
- the target variable and lag features:

| feature_1 | feature_2 | ... | feature_m-1 | feature m | target variable| |---------- |:---------- ---: |:---:|:----------: |:--------: |:----------: | | y_0 | y_1 | ... | y_m-1 | y_m | y_m+1| | y_1 | y_2 | ... | y_m | y_m+1 | y_m+2| | ... | ... | ... | ... | ... | ... | | y_i-m | y_i-m+1 | ... | y_i-2 | y_i-1 | y_i | | ... | ... | ... | ... | ... | ... | | y_n-m | y_n-m+1 | ... | y_n-2 | y_n-1 | y_n |

- the features are shifted with respect to the original observation with a dt lag
- this feature matrix is now iid and can be split with any of the methods we covered in the previous lecture

In [12]:
```
y = df['Temp']
X = pd.concat([df['Temp'].shift(3),df['Temp'].shift(2),df['Temp'].shift(1)],axi
X.columns = ['lag 3 days','lag 2 days','lag 1 day']
print(X.tail(10))
print(y.tail(10))
```

```
      lag 3 days  lag 2 days  lag 1 day
3640        14.7        15.4       13.1
3641        15.4        13.1       13.2
3642        13.1        13.2       13.9
3643        13.2        13.9       10.0
3644        13.9        10.0       12.9
3645        10.0        12.9       14.6
3646        12.9        14.6       14.0
3647        14.6        14.0       13.6
3648        14.0        13.6       13.5
3649        13.6        13.5       15.7
3640    13.2
3641    13.9
3642    10.0
3643    12.9
3644    14.6
3645    14.0
3646    13.6
3647    13.5
3648    15.7
3649    13.0
Name: Temp, dtype: float64
```

Things to consider

- lag between the target variable and feature m can be more if you want to predict the observation multiple dt's in the future
- you might also have multiple time series to work with (prices of multiple stock, covid cases in multiple countries, etc)
  - all of those need to be shifted by the same lag relative to the target variable
- due to autocorrelation, the features closer in time to the target variable tend to be more predictive
- how many features should you use?
  - treat the number of features as a hyperparameter

Special scenarios

- what if dt is not consant and/or each time series have its own non-uniform time?
  - for example you try to predict crypto prices based on stock prices
    - stock prices are available once per hour
    - crypto prices are only available when a trade happens (i.e., some tokens are traded rarely)
- interpolate to a uniform time grid
  - try linear and non-linear interpolation techniques to figure out what works best
  - check out scipy for more info
  - cubic spline interpolation usually works well
- you might have a mix of time series and non-time series features
  - cvs customer purchase history

- you know what a customer bought and when - time series part
- you have info on the customer (gender, race, address, etc) - non-time series part

Mud card

In [ ]: