# **Assignment 9**

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## **Outline**

- Question
- Denote Random Variables
- Given data
- Solution(a)
- Solution(b)



#### Question

## 2-24(Papoullis):

Box 1 contains 1000 bulbs of which 10% are defective. Box 2 contains 2000 bulbs which 5% are defective. Two bulbs are picked from a randomly selected box.

- (a) Find the probability that both bulbs are defective.
- (b) Assuming that both are defective, find the probability that they came from box 1.



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## **Denote Random Variables**

## Assign events to random variables

Denote the random variable  $X \in \{0, 1, 2\}$ . Events are described in Table 1:

Variable	Event
X=0	Picking Box 1
X=1	Picking Box 2
X=2	Picking two defective bulbs

Table 1

## Given data

## Represent the given data

Event	Probabilty
Pr(X=0)	0.5
Pr(X=1)	0.5
$\Pr\left(X=2 X=0\right)$	11 1110
$\Pr\left(X=2 X=1\right)$	99 39980

Table 2



# Solution(a)

#### Solution

Pr(X = 2) denotes the probability that both bulbs are defective.

From Total probability theorem

$$\Pr(X = 2) = \sum_{j=0}^{1} \Pr(X = j) \Pr(X = 2|X = j)$$
 (1)

$$\implies \left| \Pr(X = 2) \approx 0.006193 \right| \tag{2}$$



# Solution(b)

#### Solution

Pr(X = 0|X = 2) denotes two bulbs are picked from box 1 assuming both are defective.

From Bayes theorem

$$\Pr(X = 0|X = 2) = \frac{\Pr(X = 0)\Pr(X = 2|X = 0)}{\Pr(X = 2)}$$
(3)

$$\implies \boxed{\Pr(X=0|X=2)\approx 0.8} \tag{4}$$

