Assignment 9

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Outline

- Question
- Denote Random Variables
- Given data
- Solution(a)
- Solution(b)



Question

2-24(Papoullis):

Box 1 contains 1000 bulbs of which 10% are defective. Box 2 contains 2000 bulbs which 5% are defective. Two bulbs are picked from a randomly selected box.

- (a) Find the probability that both bulbs are defective.
- (b) Assuming that both are defective, find the probability that they came from box 1.



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Denote Random Variables

Assign events to random variables

Denote the random variables $X \in \{0, 1\}$ and $Y \in \{0\}$. Events are described in Table 1:

Variable	Event
X=0	Picking Box 1
X=1	Picking Box 2
Y=0	Picking two defective bulbs

Table 1

Given data

Represent the given data

Event	Probabilty
Pr(X=0)	0.5
Pr(X=1)	0.5
$\Pr\left(Y=0 X=0\right)$	11 1110
$\Pr(Y=0 X=1)$	99 39980

Table 2



Solution(a)

Solution

Pr(Y=0) denotes the probability that both bulbs are defective.

From Total probability theorem

$$\Pr(Y = 0) = \sum_{j=0}^{1} \Pr(X = j) \Pr(Y = 0 | X = j)$$
 (1)

$$\implies \boxed{\Pr(Y=0) \approx 0.006193} \tag{2}$$



Solution(b)

Solution

Pr(X = 0|Y = 0) denotes two bulbs are picked from box 1 assuming both are defective.

From Bayes theorem

$$\Pr(X = 0|Y = 0) = \frac{\Pr(X = 0)\Pr(Y = 0|X = 0)}{\Pr(Y = 0)}$$
(3)

$$\implies \boxed{\Pr(X=0|Y=0)\approx 0.8}$$

