

# Assignment 9

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**Abstract—**This document contains the solution for Assignment 9(Papoullis Text Book Chapter-2 Problems 2-24)

**2-24(Papoullis):**Box 1 contains 1000 bulbs of which 10% are defective. Box 2 contains 2000 bulbs which 5% are defective. Two bulbs are picked from a randomly selected box.

- Find the probability that both bulbs are defective.
- Assuming that both are defective, find the probability that they came from box 1.

**Solution:**

Denote the random variables  $X \in \{0, 1\}$  and  $Y \in \{0\}$  Events are described in Table I:

Variable	Event
$X=0$	Picking Box 1
$X=1$	Picking Box 2
$Y=0$	Picking two defective bulbs

TABLE I

Given data:

Event	Probability
$\Pr(X = 0)$	0.5
$\Pr(X = 1)$	0.5
$\Pr(Y = 0 X = 0)$	$\frac{11}{1110}$
$\Pr(Y = 0 X = 1)$	$\frac{99}{39980}$

TABLE II

- $\Pr(Y = 0)$  denotes the probability that both bulbs are defective.

From Total probability theorem

$$\Pr(Y = 0) = \sum_{j=0}^1 \Pr(X = j) \Pr(Y = 0|X = j) \quad (1)$$

$$\Rightarrow \boxed{\Pr(Y = 0) \approx 0.006193} \quad (2)$$

- $\Pr(X = 0|Y = 0)$  denotes two bulbs are picked from box 1 assuming both are defective. From Bayes theorem

$$\Pr(X = 0|Y = 0) = \frac{\Pr(X = 0) \Pr(Y = 0|X = 0)}{\Pr(Y = 0)} \quad (3)$$

$$\Rightarrow \boxed{\Pr(X = 0|Y = 0) \approx 0.8} \quad (4)$$