

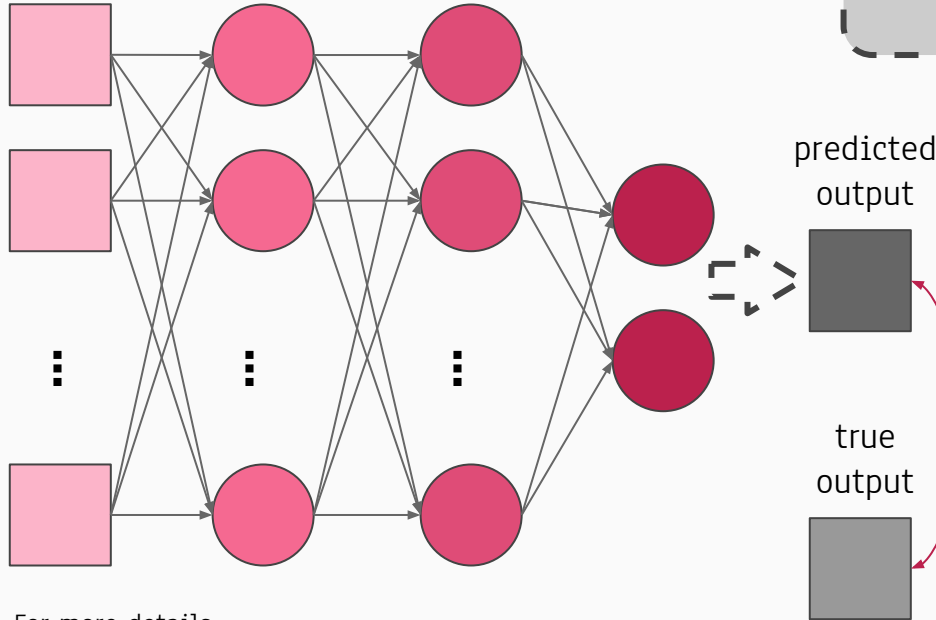


# REGRESSION LOSS FUNCTIONS



## LOSS FUNCTION

input layer      hidden layers      output layer



A loss function is a measure of **error** between the model's **predicted value** and the **actual value**.

In the context of Machine Learning:

Loss function is a method of evaluating "how well your algorithm models your dataset".

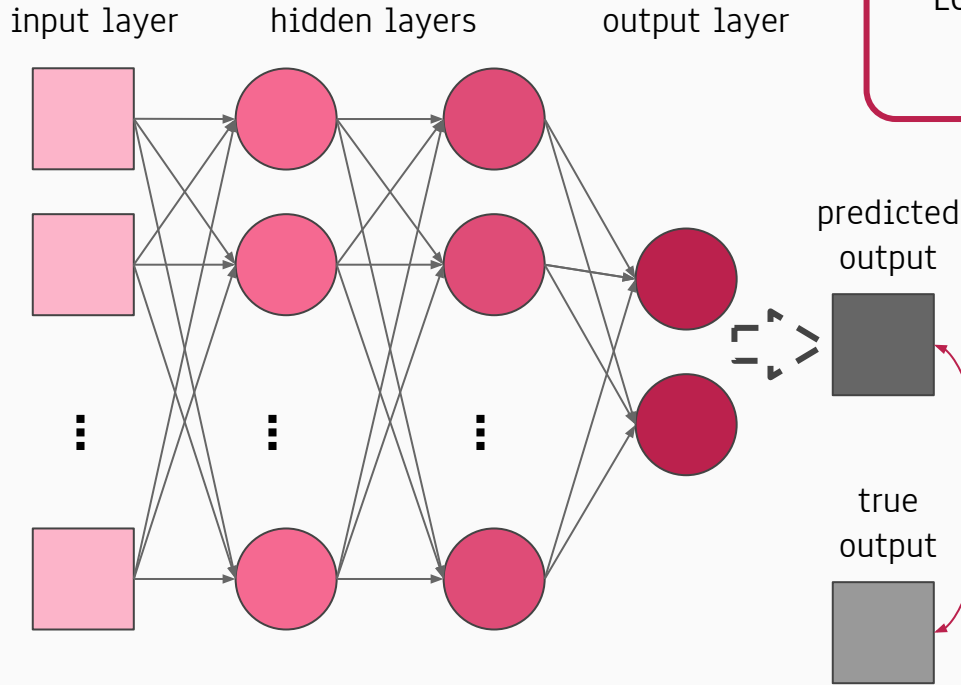
$$\text{Loss} = J(\text{pred}, \text{true})$$

It also indicates if the algorithm is **improving** the model's performance *after tuning any parameter*.

For more details :

<https://medium.com/@zeeshanmulla/cost-activation-loss-function-neural-network-deep-learning-what-are-these-91167825a4de>

## SYNONYMS OF LOSS FUNCTION



Loss function, cost function, objective function or error function are synonyms and can be used interchangeably .

Loss is nothing but a prediction error of an ML model. Sometimes a loss function or cost function is computed for a single training sample; at other times it is computed for a mini-batch of the training set.

$$\text{Loss} = J(\text{pred}, \text{true})$$

If pred is very far off from true, the loss value will be **very high**.

If both values are almost similar, the loss value will be **very low**.

## TYPES OF LOSS FUNCTION

### REGRESSION

- Predict continuous and numerical value.
- E.g., predicting the appropriate price of a product, predicting the number of sales each day, height of a person

Mean Squared Error Loss  
Mean Squared Logarithmic Error Loss  
Mean Absolute Error Loss

### CLASSIFICATION

- Predict a categorical outcome (number of classes)
- E.g., objects in an image, topics in emails, suitable products to advertise

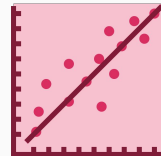
#### BINARY CLASSIFICATION

Binary Cross-Entropy  
Hinge Loss  
Squared Hinge Loss

#### MULTI-CLASS CLASSIFICATION

Multi-Class Cross-Entropy  
Sparse Multiclass Cross-Entropy  
Kullback Leibler Divergence

# COMMON LOSS FUNCTIONS FOR REGRESSION



## Mean Squared Error Loss (MSE)

MSE is calculated as the average of the squared differences between the predicted and actual values.

- *Mathematically, MSE is the preferred loss function if the distribution of the target variable is Gaussian, and the target value doesn't have any outliers.*
- *The squaring of errors means that larger mistakes result in higher error than smaller mistakes.*

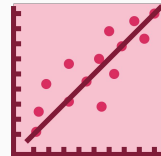
## Mean Absolute Error Loss (MAE)

MAE is calculated as the average of the absolute difference between the actual and predicted values.

- *MAE is appropriate if the data samples have properties of Gaussian distribution and have a tendency towards outliers.*

Outliers are the large or small values far from the mean value of all the observation. Simply, an outlier is an extremely high or extremely low value in a dataset.

# COMMON LOSS FUNCTIONS FOR REGRESSION



## Mean Squared Error Loss (MSE)

MSE is calculated as the average of the squared differences between the predicted and actual values.

## Mean Absolute Error Loss (MAE)

MAE is calculated as the average of the absolute difference between the actual and predicted values.

### Steps for computing MSE:

1. Take the difference between your model's predictions and the actual value
2. Square the difference
3. Compute the average of the squared differences.

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - \hat{y}_i|$$

### Legend:

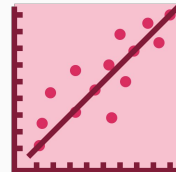
$i$  - index of sample

$\hat{y}$  - predicted value

$y$  - expected value

$n$  - number of samples in dataset

# ANOTHER LOSS FUNCTION FOR REGRESSION



## Mean Squared Logarithmic Error Loss (MSLE)

MSLE calculates the natural logarithm of each of the predicted values, then calculate the mean squared error.

- *The MSLE is smoother than MSE and will not be so strongly affected by the occasional wildly incorrect prediction.*
- *As a loss measure, it may be more appropriate when the model is predicting unscaled quantities; (unscaled input variables of data may have different units e.g. feet, kilometers, and hours).*

$$MSLE = \frac{1}{n} \sum_{i=1}^n (\log(y_i + 1) - \log(\hat{y}_i + 1))^2$$