

**VISVESVARAYA TECHNOLOGICAL  
UNIVERSITY**

“JnanaSangama”, Belgaum -590014, Karnataka.



**LAB REPORT  
on**

**Artificial Intelligence (23CS5PCAIN)**

*Submitted by*

**Aparna Sankar (1BM23CS047)**

*in partial fulfillment for the award of the degree of*  
**BACHELOR OF ENGINEERING**  
*in*  
**COMPUTER SCIENCE AND ENGINEERING**



**B.M.S. COLLEGE OF ENGINEERING**  
(Autonomous Institution under VTU)  
**BENGALURU-560019**  
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**B.M.S. College of Engineering,**  
**Bull Temple Road, Bangalore 560019**  
(Affiliated To Visvesvaraya Technological University, Belgaum)  
**Department of Computer Science and Engineering**



**CERTIFICATE**

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Aparna Sankar (1BM23CS047)**, who is bonafide student of **B.M.S. College of Engineering**. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

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**Github Link:**

<https://github.com/1BM23CS047/AI-lab>



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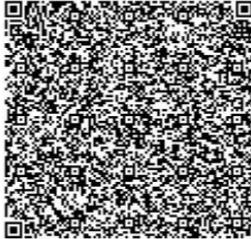
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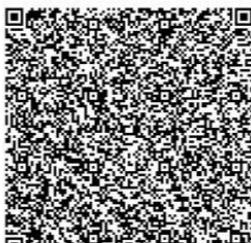
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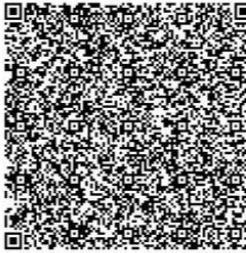
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### **Program 1**

Implement Tic – Tac – Toe Game  
Implement vacuum cleaner agent

**Tic-Tac-Toe**

**Algorithm**

## Tic - Tac - Toe Game.

Week Lab - 1

Pseudocode: Algorithm.

- start
- initialize 3x3 board with spaces that are empty
- Let computer play 'O' 'O'
- Let user play 'X' 'X'
- Let <sup>Users</sup> Humans and computer choose from row (1 - 3) and column number (1 - 3)
- When the chosen cell is free the user can enter 'X'
- If the chosen cell is not free the system should display error and the user should have to choose another cell that is free to display enter 'X'
- After that is every move display the board
- If the user wins the system should display 'you win'
- If the rows and columns are full then the system should display 'draw'

For the Computer:-

Min Max Algorithm

- call minmax(board, depth, ismaximizing = false)
- undo move
- If score > bestscore
  - let  $\frac{\text{score}}{\text{bestscore}}$  be best score
- minmax is recursively called to consider all moves to find the move of best score, that move is made by computer
- return the best move
- place 'O' in the best move cell.
- if computer wins → print "computer win"
- if board is full print 'draw'
- (G) minmax(board, depth, ismaximizing)
  - If "O" wins return 1
  - If "X" wins return -1
  - If board is full return 0
  - If ismaximizing = true
    - Let bestscore =  $-\infty$
    - For each empty cell place "O"
    - recursively call minmax with ismaximizing = false
    - undo move
    - update best cell =  $\max(\text{best\_cell}, \text{score})$
    - return the best move best-score
    - else user's turn)

place X on every possible empty space.

initialize best-score =  $+\infty$

call minmax

is maximizing = true

call minmax (board, depth, ismaximizing)

- undo move

if SCORE > best-score  
    update  
    return best-score

- minmax is recursively called to consider all moves  
- return the best move

- stop

## Code

```
import math

def print_board(board):
    for row in board:
        print(" | ".join(row))
        print("-" * 5)

def check_winner(board, player):
    for row in board:
        if all(cell == player for cell in row):
            return True
    for col in range(3):
        if all(board[row][col] == player for row in range(3)):
            return True
    if all(board[i][i] == player for i in range(3)):
        return True
    if all(board[i][2 - i] == player for i in range(3)):
        return True
    return False

def is_full(board):
    return all(cell != " " for row in board for cell in row)

def minimax(board, depth, is_maximizing, ai, human):
    if check_winner(board, ai):
        return 1
    if check_winner(board, human):
        return -1
    if is_full(board):
        return 0
    if is_maximizing:
        best_score = -float('inf')
        for row in range(3):
            for col in range(3):
                if board[row][col] == " ":
                    board[row][col] = ai
                    score = minimax(board, depth + 1, False, ai, human)
                    board[row][col] = " "
                    if score > best_score:
                        best_score = score
        return best_score
    else:
        best_score = float('inf')
        for row in range(3):
            for col in range(3):
                if board[row][col] == " ":
                    board[row][col] = human
                    score = minimax(board, depth + 1, True, ai, human)
                    board[row][col] = " "
                    if score < best_score:
                        best_score = score
        return best_score
```

```

if is_maximizing:
    best = -math.inf
    for r in range(3):
        for c in range(3):
            if board[r][c] == " ":
                board[r][c] = ai
                score = minimax(board, depth + 1, False, ai, human)
                board[r][c] = " "
                best = max(best, score)
    return best
else:
    best = math.inf
    for r in range(3):
        for c in range(3):
            if board[r][c] == " ":
                board[r][c] = human
                score = minimax(board, depth + 1, True, ai, human)
                board[r][c] = " "
                best = min(best, score)
    return best

def best_move(board, ai, human):
    best_score = -math.inf
    move = None
    for r in range(3):
        for c in range(3):
            if board[r][c] == " ":
                board[r][c] = ai
                score = minimax(board, 0, False, ai, human)
                board[r][c] = " "
                if score > best_score:
                    best_score = score
                    move = (r, c)
    return move

def tic_tac_toe():
    board = [[" " for _ in range(3)] for _ in range(3)]
    human, ai = "X", "O"

    print("Welcome to Tic-Tac-Toe!")
    print("You are X, Computer is O (Unbeatable AI)")
    print_board(board)

    while True:
        # Human move
        try:
            row = int(input("Enter row (0-2): "))

```

```

col = int(input("Enter col (0-2): "))
except ValueError:
    print("Invalid input. Try again.")
    continue

if row not in [0,1,2] or col not in [0,1,2] or board[row][col] != " ":
    print("Invalid move! Try again.")
    continue

board[row][col] = human
print_board(board)

if check_winner(board, human):
    print("X You win!")
    break
if is_full(board):
    print("It's a draw!")
    break

# Computer move
print("Computer's turn...")
row, col = best_move(board, ai, human)
board[row][col] = ai
print_board(board)

if check_winner(board, ai):
    print("O Computer wins!")
    break
if is_full(board):
    print("It's a draw!")
    break

if __name__ == "__main__":
    tic_tac_toe()

```

## Output

```
Welcome to Tic-Tac-Toe!
You are X, Computer is O (Unbeatable AI)
```

```
| |
```

```
-----
```

```
| |
```

```
-----
```

```
Enter row (0-2): 1
```

```
Enter col (0-2): 2
```

```
| |
```

```
-----
```

```
| | X
```

```
-----
```

```
| |
```

```
-----
```

```
Computer's turn...
```

```
| | 0
```

```
-----
```

```
| | X
```

```
-----
```

```
| |
```

```
-----
```

```
Enter row (0-2): 1
```

```
Enter col (0-2): 0
```

```
| | 0
```

```
-----
```

```
X | | X
```

```
-----
```

```
| |
```

```
-----
```

```
Computer's turn...
```

```
| | 0
```

```
-----
```

```
X | 0 | X
```

```
-----
```

```
| |
```

```
-----
```

```
Enter row (0-2): 0  
Enter col (0-2): 0
```

```
X |   | 0
```

```
-----
```

```
X | 0 | X
```

```
-----
```

```
 |   |
```

```
-----
```

```
Computer's turn...
```

```
X |   | 0
```

```
-----
```

```
X | 0 | X
```

```
-----
```

```
0 |   |
```

```
-----
```

```
💻 Computer wins!
```

## Vacuum Cleaner

### Algorithm

## Vaccum Cleaner Algorithm

```
Function vacuum_cleaner (room-array) :  
    for each room in room-array:  
        if room is duty:  
            print "Room [label] is cleaned"  
        else  
            print "Room [label] is already clean"  
    More to next room
```

```
def vacuum_cleaner (room-array):  
    for room in room array:  
        label, status = room[0], room[1].lower()  
        print(f"Current room {label}, room[3].lower")  
        print(f"Currently in room {label}")  
        if status == "dirty":  
            print(f"Room {label} is cleaned")  
        else:  
            print(f"Room {label} is already  
cleaned")
```

```
rooms = ('A', 'duty'), ('B', 'clean'), ('C', 'clean')  
       ('D', 'duty'), ('A', 'clean'))  
vacuum_cleaner (rooms)
```

## Code

```
def vacuum_cleaner(room_array):  
    for room in room_array:  
        label, status = room[0], room[1].lower()  
        print(f"Currently in Room {label}")  
        if status == "dirty":  
            print(f"Room {label} is cleaned")  
        else:  
            print(f"Room {label} is already clean")
```

```
print("Moving to next room...\n")

# Example input: list of rooms with their status
rooms = [('A', 'dirty'), ('B', 'clean'), ('A', 'clean'), ('B', 'dirty')]
vacuum_cleaner(rooms)
```

## Output

```
Currently in Room A
Room A is cleaned
Moving to next room...
```

```
Currently in Room B
Room B is already clean
Moving to next room...
```

```
Currently in Room A
Room A is already clean
Moving to next room...
```

```
Currently in Room B
Room B is cleaned
Moving to next room...
```

## Program 2

Implement 8 puzzle problems using Depth First Search (DFS)  
Implement Iterative deepening search algorithm

## **8 Puzzle Problem**

### **Algorithm**

## Week Lab 2

- a) 8 puzzle problems using misplaced tiles and Manhattan distance and IDDFS

Initialize 8 puzzle problem using misplaced tiles and Manhattan distance

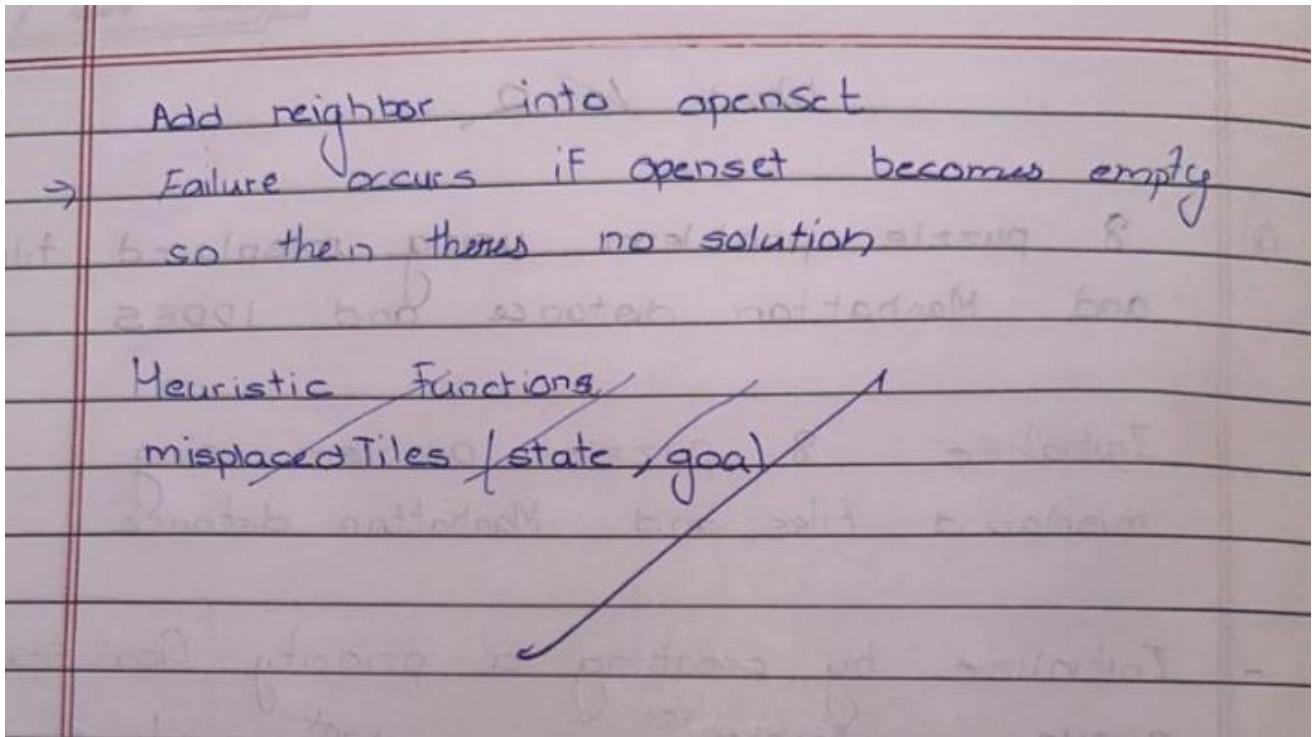
- Initialize by creating a priority queue <sup>total score so far</sup> Goal State
- $f(n) = g(n) + h(n)$  - heuristic estimate
- Set  $g(\text{start}) = 0$
- Set  $f(\text{start}) = \text{heuristic}(\text{start}, \text{goal})$
- Store parent[ $\text{start}$ ] = null
- Search loop
- insert start into openset
- Search loop while openset is not empty
- Remove the current with lowest F from openset

IF current = goal :

Return path by reconstructing from parent  
else expand current for each valid move of the blank tile.

- Generate neighbour with next move  
tentative  $g = g(\text{current}) + 1$
- IF neighbour is not in qscore or tentative  $g < g(\text{neighbor})$ :
- Update  $g(\text{neighbor}) = \text{tentative } g$
- Compute  $f(\text{neighbor}) = g(\text{neighbor}) + \text{heuristic}(\text{neighbor}, \text{goal})$

Set parent[neighbor] = current



## Code

```
import time
```

```
def find_possible_moves(state):
    index = state.index('_')
    moves = {
        0: [1, 3],
        1: [0, 2, 4],
        2: [1, 5],
        3: [0, 4, 6],
        4: [1, 3, 5, 7],
        5: [2, 4, 8],
        6: [3, 7],
        7: [6, 8, 4],
        8: [5, 7],
    }
    return moves.get(index, [])
```

```
def dfs(initial_state, goal_state, max_depth=50):
    stack = [(initial_state, [], 0)]
    visited = {tuple(initial_state)}
    states_explored = 0
    printed_depths = set()
```

```
while stack:
```

```

current_state, path, depth = stack.pop()

if depth > max_depth:
    continue

if depth not in printed_depths:
    print(f"\n--- Depth {depth} ---")
    printed_depths.add(depth)

states_explored += 1
print(f"State #{states_explored}: {current_state}")

if current_state == goal_state:
    print(f"\n Goal reached at depth {depth} after exploring {states_explored} states.\n")
    return path, states_explored

possible_moves_indices = find_possible_moves(current_state)

for move_index in reversed(possible_moves_indices): # Reverse for DFS order
    next_state = list(current_state)
    blank_index = next_state.index('_')
    next_state[blank_index], next_state[move_index] = next_state[move_index],
    next_state[blank_index]

    if tuple(next_state) not in visited:
        visited.add(tuple(next_state))
        stack.append((next_state, path + [next_state], depth + 1))

print(f"\n Goal state not reachable within depth {max_depth}. Explored {states_explored} states.\n")
return None, states_explored

# ----- TEST -----
initial_state = [1, 2, 3,
                 4, 8, '_',
                 7, 6, 5]

goal_state = [1, 2, 3,
              4, 5, 6,
              7, 8, '_']

# Measure execution time
start_time = time.time()
solution_path, explored = dfs(initial_state, goal_state, max_depth=50)
end_time = time.time()

```

```

if solution_path is None:
    print("No solution found.")
else:
    print("Solution path:")
    for step, state in enumerate(solution_path, start=1):
        print(f"Step {step}: {state}")

print("\nExecution time: {:.6f} seconds".format(end_time - start_time))
print("Total states explored:", explored)

```

## Output

```

--- Depth 0 ---
State #1: [1, 2, 3, 4, 8, '_', 7, 6, 5]

--- Depth 1 ---
State #2: [1, 2, '_', 4, 8, 3, 7, 6, 5]

--- Depth 2 ---
State #3: [1, '_', 2, 4, 8, 3, 7, 6, 5]

--- Depth 3 ---
State #4: ['_', 1, 2, 4, 8, 3, 7, 6, 5]

--- Depth 4 ---
State #5: [4, 1, 2, '_', 8, 3, 7, 6, 5]

--- Depth 5 ---
State #6: [4, 1, 2, 8, '_', 3, 7, 6, 5]

--- Depth 6 ---
State #7: [4, '_', 2, 8, 1, 3, 7, 6, 5]

--- Depth 7 ---
State #8: ['_', 4, 2, 8, 1, 3, 7, 6, 5]

--- Depth 8 ---
State #9: [8, 4, 2, '_', 1, 3, 7, 6, 5]

```

```
--- Depth 9 ---
State #10: [8, 4, 2, 1, '_', 3, 7, 6, 5]

--- Depth 10 ---
State #11: [8, '_', 2, 1, 4, 3, 7, 6, 5]

--- Depth 11 ---
State #12: ['_', 8, 2, 1, 4, 3, 7, 6, 5]

--- Depth 12 ---
State #13: [1, 8, 2, '_', 4, 3, 7, 6, 5]

--- Depth 13 ---
State #14: [1, 8, 2, 7, 4, 3, '_', 6, 5]

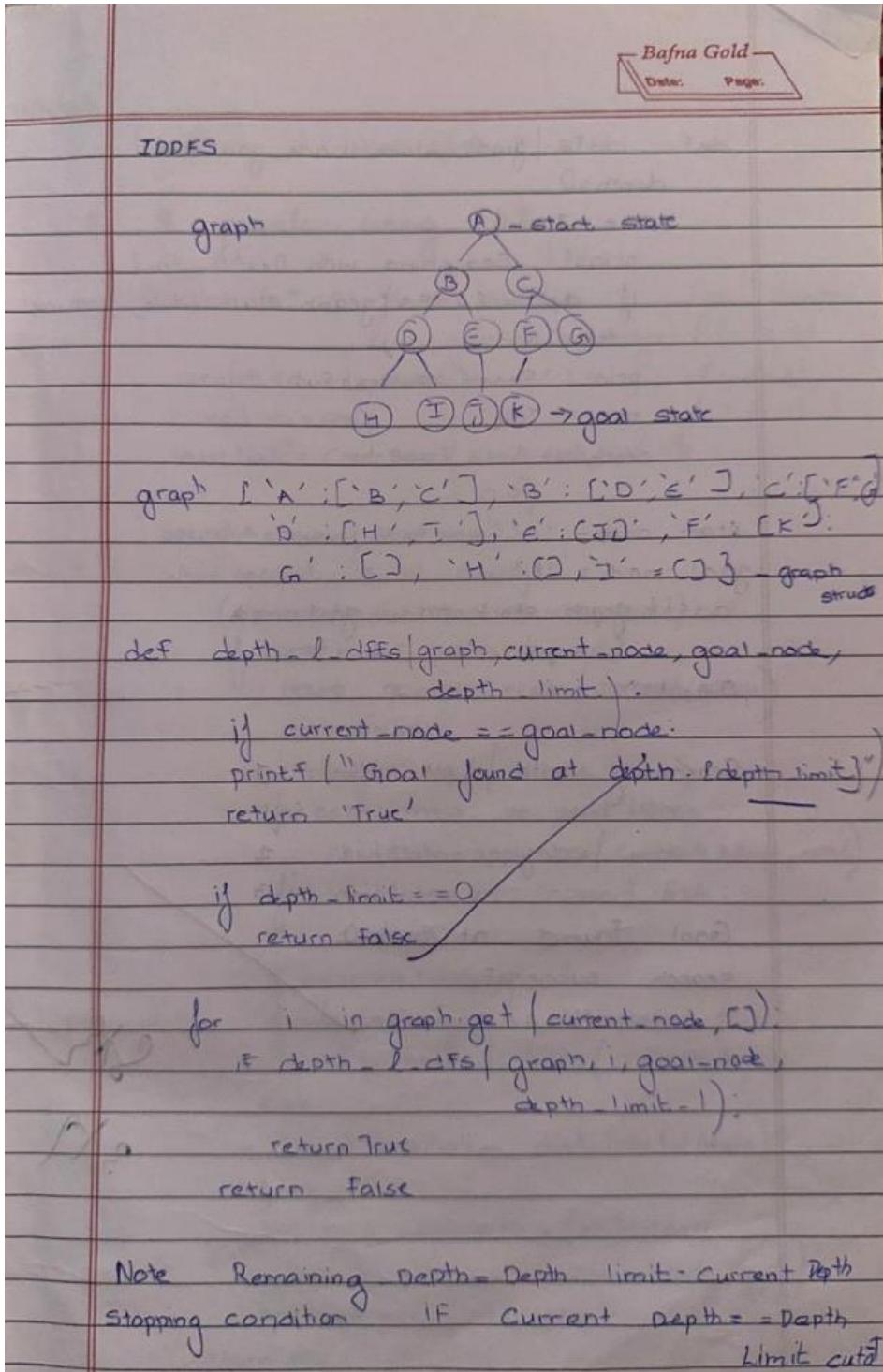
--- Depth 14 ---
State #15: [1, 8, 2, 7, 4, 3, 6, '_', 5]

--- Depth 15 ---
State #16: [1, 8, 2, 7, 4, 3, 6, 5, '_']

--- Depth 16 ---
State #17: [1, 8, 2, 7, 4, '_', 6, 5, 3]
```

IDDFS

## Algorithm



```

def idDFS(graph, start_node, goal_node)
    depth = 0
    while True:
        print("Searching with Depth limit")
        if depth == 0:
            if idDFS(graph, start_node, goal_node):
                print("Search successful!")
                return True
        depth += 1

start_node = 'A'
goal_node = 'K'
idDFS(graph, start_node, goal_node)

```

Output:

Searching with depth limit: 0

.. .. .. : 1

.. .. .. .. : 2

.. .. .. .. .. : 3

Goal found at depth 0

Search successful!

## Code

import time

```

def find_possible_moves(state):
    index = state.index('_')

    if index == 0:
        return [1, 3]
    elif index == 1:
        return [0, 2, 4]
    elif index == 2:
        return [1, 5]
    elif index == 3:
        return [0, 4, 6]
    elif index == 4:
        return [1, 3, 5, 7]
    elif index == 5:
        return [2, 4, 8]
    elif index == 6:
        return [3, 7]
    elif index == 7:
        return [4, 6, 8]
    elif index == 8:
        return [5, 7]
    return []

def depth_limited_dfs(state, goal_state, limit, path, visited):
    if state == goal_state:
        return path

    if limit <= 0:
        return None

    visited.add(tuple(state))

    for move_index in find_possible_moves(state):
        next_state = list(state)
        blank_index = next_state.index('_')
        next_state[blank_index], next_state[move_index] = next_state[move_index], next_state[blank_index]

        if tuple(next_state) not in visited:
            result = depth_limited_dfs(next_state, goal_state, limit - 1, path + [next_state], visited)
            if result is not None:
                return result
    return None

def iddfs(initial_state, goal_state, max_depth=30):
    for depth in range(max_depth):
        print(f"Searching at depth limit = {depth}")

```

```

visited = set()
result = depth_limited_dfs(initial_state, goal_state, depth, [initial_state], visited)
if result is not None:
    return result, depth
return None, max_depth

# ----- TEST -----
initial_state = [1, 2, 3,
                 4, 8, '_',
                 7, 6, 5]

goal_state = [1, 2, 3,
              4, 5, 6,
              7, 8, '_']

# Measure execution time
start_time = time.time()
solution_path, depth_reached = iddfs(initial_state, goal_state, max_depth=30)
end_time = time.time()

if solution_path is None:
    print("Goal state is not reachable within given depth limit.")
else:
    print("\n\nSolution path found:")
    for step, state in enumerate(solution_path, start=0):
        print(f"Step {step}: {state}")

print("\nExecution time: {:.6f} seconds".format(end_time - start_time))
print("Depth reached:", depth_reached)

```

## Output

```
Searching at depth limit = 0
Searching at depth limit = 1
Searching at depth limit = 2
Searching at depth limit = 3
Searching at depth limit = 4
Searching at depth limit = 5

Solution path found:
Step 0: [1, 2, 3, 4, 8, '_', 7, 6, 5]
Step 1: [1, 2, 3, 4, 8, 5, 7, 6, '_']
Step 2: [1, 2, 3, 4, 8, 5, 7, '_', 6]
Step 3: [1, 2, 3, 4, '_', 5, 7, 8, 6]
Step 4: [1, 2, 3, 4, 5, '_', 7, 8, 6]
Step 5: [1, 2, 3, 4, 5, 6, 7, 8, '_']

Execution time: 0.000194 seconds
Depth reached: 5

==== Code Execution Successful ===
```

## Program 3

Implement A\* search algorithm

### Algorithm

10/9/25  
Week 3 (contd.)

Q 8 puzzle using A\*

- Function `a* astarSearch(startState, Goal State = [1, 2, 3], heuristicType = {Misplaced Tiles, Manhattan Dist})`

`openlist = priority Queue()`  
`closedlist = set()`

`StartNode = CreateBoard( start state, Null, 0, 0)`

`openlist.enqueue( StartNode)`

while openlist is not empty:

`current Node = openlist.dequeue()`

if current node == openlist.dequeue():  
    return reconstructPath( current Node)

`currentNode`

`closedlist.add( currentNode)`

for each move in valid moves:

`childState = applyMove( currentNode, move)`

if childstate in closed list:  
    continue

`g = currentNode.g + 1`

if heuristicType == 'Misplaced Tiles':  
    `h = misplacedTiles( childState)`

else:  
    `h = manhattan_dist( childState)`

~~`f = g + h`~~

~~`ChildNode = createNode( childState, currentNode, g, f)`~~

~~`openlist.push( childNode)`~~

`return NULL`

function reconstructPath(<sup>path</sup>node):

path = []

while node is not None &

path.append(node)

node = node.parent

return reverse(path)

1 2 3

- 4 6  
7 5 8

$g=0$

$h=3$

$F=g+h=3$

$g=1, h=4, F=5$        $g=1, h=2, f=3$        $g=1, h=1, F=5$

1 2 3

1 2 3

1 2 3

1 4 6

1 2 3

1 2 3

7 5 8

7 5 8

7 5 8

7 5 8

7 5 8

7 5 8

1 2 3

1 2 3

1 2 3

4 5 6

4 5 6

4 5 6

7 8

7 5 8

7 5 8

$g=2, h=3, f=5$

$g=2, h=3, f=5$

$g=2, h=3, f=5$

1 2 3

1 2 3

1 2 3

4 5 6

4 5 6

4 5 6

7 8

7 5 8

7 5 8

goal state

1 2 3

1 2 3

0

1 2 3

4 5 6

4 5 6

7 8

7 8 -

7 8 -

$g=3, h=0, f=5$

$g=3, h=0, f=5$

$g=3, h=0, f=5$

1 2 3

4 5 6

4 5 6

7 8

7 8 -

7 8 -

goal state

1 2 3

1 2 3

0

## Code

```
import heapq
import time

# Heuristic: Manhattan Distance
def heuristic(state, goal):
    distance = 0
    for i in range(1, 9): # tile numbers 1 to 8
        x1, y1 = divmod(state.index(i), 3)
        x2, y2 = divmod(goal.index(i), 3)
        distance += abs(x1 - x2) + abs(y1 - y2)
    return distance

# Get neighbors by sliding blank (0) up/down/left/right
def get_neighbors(state):
    neighbors = []
    i = state.index(0) # position of blank
    x, y = divmod(i, 3)
    moves = [(-1,0), (1,0), (0,-1), (0,1)]

    for dx, dy in moves:
        new_x, new_y = x + dx, y + dy
        if 0 <= new_x < 3 and 0 <= new_y < 3:
            j = new_x * 3 + new_y
            new_state = list(state)
            new_state[i], new_state[j] = new_state[j], new_state[i]
            neighbors.append(tuple(new_state))
    return neighbors

# A* Search for 8-puzzle
def astar(start, goal):
    open_set = []
    heapq.heappush(open_set, (heuristic(start, goal), 0, start))

    came_from = {}
    g_score = {start: 0}

    while open_set:
        _, cost, current = heapq.heappop(open_set)

        if current == goal:
            # Reconstruct path
            path = []
            while current in came_from:
                path.append(current)
                current = came_from[current]
            path.append(goal)
            path.reverse()
            return path

        for neighbor in get_neighbors(current):
            tentative_g_score = cost + heuristic(neighbor, goal)

            if neighbor not in came_from or tentative_g_score < g_score[neighbor]:
                came_from[neighbor] = current
                g_score[neighbor] = tentative_g_score
                f_score = g_score[neighbor] + heuristic(neighbor, goal)
                heapq.heappush(open_set, (f_score, tentative_g_score, neighbor))

    return None
```

```

        current = came_from[current]
        path.append(start)
        return path[::-1]

    for neighbor in get_neighbors(current):
        tentative_g = g_score[current] + 1
        if neighbor not in g_score or tentative_g < g_score[neighbor]:
            came_from[neighbor] = current
            g_score[neighbor] = tentative_g
            f_score = tentative_g + heuristic(neighbor, goal)
            heapq.heappush(open_set, (f_score, tentative_g, neighbor))

    return None # no solution

# ----- TEST -----
start = (1, 2, 3,
         4, 8, 0,
         7, 6, 5)

goal = (1, 2, 3,
        4, 5, 6,
        7, 8, 0)

# Measure execution time
start_time = time.time()
path = astar(start, goal)
end_time = time.time()

if path:
    print("Steps to solve ({} moves):".format(len(path)-1))
    for state in path:
        for i in range(0, 9, 3):
            print(state[i:i+3])
        print()
else:
    print("No solution found")

print("Execution time: {:.6f} seconds".format(end_time - start_time))

```

## Output

```
Steps to solve (5 moves):
```

```
(1, 2, 3)
```

```
(4, 8, 0)
```

```
(7, 6, 5)
```

```
(1, 2, 3)
```

```
(4, 8, 5)
```

```
(7, 6, 0)
```

```
(1, 2, 3)
```

```
(4, 8, 5)
```

```
(7, 0, 6)
```

```
(1, 2, 3)
```

```
(4, 0, 5)
```

```
(7, 8, 6)
```

```
(1, 2, 3)
```

```
(4, 5, 0)
```

```
(7, 8, 6)
```

```
(1, 2, 3)
```

```
(4, 5, 6)
```

```
(7, 8, 0)
```

```
Execution time: 0.000111 seconds
```

## **Program 4**

Implement Hill Climbing search algorithm to solve N-Queens problem

### **Algorithm**

9/10/25

Bafna Gold  
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Week 4

Q N Queens problem Using Hill Climbing

Function Hill-Climbing (Problem) returns local minimum

Current  $\leftarrow$  MakeNode (Problem initialState)

while True:

    next  $\leftarrow$  get best neighbor (current)

    if cost (current)  $\leq$  cost (next)

        then break

    end if

    current  $\leftarrow$  next

end while

return current

Eg) Initial State =

0	1	2	3
			Q
	Q		
		Q	
Q			

$x_0 = 3$   
 $x_1 = 1$   
 $x_2 = 2$   
 $x_3 = 0$

Cost = 2

Possible children

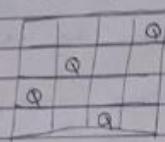
1) Swap ( $x_0, x_1$ )

			Q
	Q		
		Q	
Q			

Choose this

$x_0 = 1, x_1 = 3,$

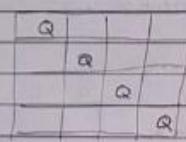
ii) Swap ( $x_0, x_2$ )



$$x_0 = 2, x_1 = 1, x_2 = 3, x_3 = 0$$

Cost = 1

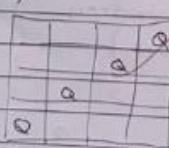
iii) Swap ( $x_0, x_3$ )



$$x_0 = 0, x_1 = 1, x_2 = 2, x_3 = 3$$

Cost = 6

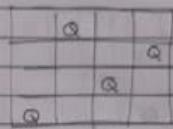
iv) Swap ( $x_1, x_2$ )



$$x_0 = 3, x_1 = 2, x_2 = 1, x_3 = 0$$

Cost = 6

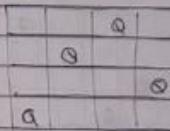
v) Swap ( $x_1, x_3$ )



$$x_0 = 3, x_1 = 0, x_2 = 2, x_3 = 1$$

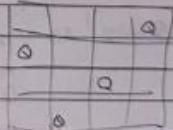
Cost = 1

vi) Swap ( $x_2, x_3$ )



$$x_0 = 3, x_1 = 1, x_2 = 0, x_3 = 2$$

vii) Selected neighbor =



$$x_0 = 1, x_1 = 3, x_2 = 2, x_3 = 0$$

Cost = 1

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<ul style="list-style-type: none"> <li>Swap (<math>x_0, x_1</math>)</li> </ul> <p><math>x_0 = 3, x_1 = 1, x_2 = 2, x_3 = 0</math> Cost = 1</p>	<ul style="list-style-type: none"> <li>Swap (<math>x_1, x_2</math>)</li> </ul> <p><math>x_0 = 0, x_1 = 3, x_2 = 2, x_3 = 1</math> Cost = 1</p>
<ul style="list-style-type: none"> <li>Swap (<math>x_0, x_2</math>)</li> </ul> <p><math>x_0 = 2, x_1 = 3, x_2 = 0, x_3 = 1</math> Cost = 2</p>	<ul style="list-style-type: none"> <li>Swap (<math>x_1, x_3</math>)</li> </ul> <p><math>x_0 = 1, x_1 = 0, x_2 = 2, x_3 = 3</math> Cost = 2</p>
<ul style="list-style-type: none"> <li>Swap (<math>x_0, x_3</math>)</li> </ul> <p><math>x_0 = 0, x_1 = 3, x_2 = 2, x_3 = 1</math> Cost = 4</p>	<p>Swap ( )</p> <p><math>x_0 = 1, x_1 = 3, x_2 = 0, x_3 = 2</math> Cost = 0</p> <p>Choose list</p>

## Code

```

import random
import math

def compute_cost(state):
    """Count diagonal conflicts for a permutation-state (one queen per row & column)."""
    conflicts = 0
    n = len(state)
    for i in range(n):
        for j in range(i + 1, n):
            if abs(state[i] - state[j]) == abs(i - j):
                conflicts += 1
    return conflicts

```

```

def random_permutation(n):
    arr = list(range(n))
    random.shuffle(arr)
    return arr

def neighbors_by_swaps(state):
    """All neighbors obtained by swapping two columns (keeps permutation property)."""
    n = len(state)
    for i in range(n - 1):
        for j in range(i + 1, n):
            nb = state.copy()
            nb[i], nb[j] = nb[j], nb[i]
            yield nb

def hill_climb_with_restarts(n, max_restarts=None):
    """Hill climbing on permutations with random restart on plateau (no revisits)."""
    visited = set()
    total_states = math.factorial(n)
    restarts = 0

    while True:
        # pick a random unvisited start permutation
        if len(visited) >= total_states:
            raise RuntimeError("All states visited — giving up (no solution found.)")

        state = random_permutation(n)
        while tuple(state) in visited:
            state = random_permutation(n)
            visited.add(tuple(state))

        # climb from this start
        while True:
            cost = compute_cost(state)
            if cost == 0:
                return state, restarts

            # find best neighbor (swap-based neighbors)
            best_neighbor = None
            best_cost = float("inf")
            for nb in neighbors_by_swaps(state):
                c = compute_cost(nb)
                if c < best_cost:
                    best_cost = c
                    best_neighbor = nb

            # if strictly better, move; otherwise it's a plateau/local optimum -> restart

```

```

if best_cost < cost:
    state = best_neighbor
    visited.add(tuple(state))
else:
    # plateau or local optimum -> restart
    restarts += 1
    if max_restarts is not None and restarts >= max_restarts:
        raise RuntimeError(f"Stopped after {restarts} restarts (no solution found).")
    break # go pick a new unvisited start

def format_board(state):
    n = len(state)
    lines = []
    for r in range(n):
        lines.append(" ".join("Q" if state[c] == r else "-" for c in range(n)))
    return "\n".join(lines)

if __name__ == "__main__":
    n = 4
    solution, restarts = hill_climb_with_restarts(n)
    print("Found solution:", solution)
    print(format_board(solution))

```

## Output

```

Found solution: [2, 0, 3, 1]
- Q - -
- - - Q
Q - - -
- - Q -

```

## Program 5

Simulated Annealing to Solve 8-Queens problem

### Algorithm

N Queens Simulated Annealing

```
current ← initial state
T ← a large positive value
while T > 0 do
    next ← a random neighbor of
        current.
    ΔE ← current.cost - next.cost
    if ΔE > 0 then
        current ← next
    else
        current ← next with probability
            p = e^(-ΔE/T)
    end if
    decrease T
end while
return current
```

### Code

```
import random
import math
```

```
def cost(state):
```

```
    attacks = 0
    n = len(state)
```

```

for i in range(n):
    for j in range(i + 1, n):
        if state[i] == state[j] or abs(state[i] - state[j]) == abs(i - j):
            attacks += 1
return attacks

def get_neighbor(state):

    neighbor = state[:]
    i, j = random.sample(range(len(state)), 2)
    neighbor[i], neighbor[j] = neighbor[j], neighbor[i]
    return neighbor

def simulated_annealing(n=8, max_iter=10000, temp=100.0, cooling=0.95):

    current = list(range(n))
    random.shuffle(current)
    current_cost = cost(current)

    temperature = temp
    cooling_rate = cooling

    best = current[:]
    best_cost = current_cost

    for _ in range(max_iter):
        if temperature <= 0 or best_cost == 0:
            break

        neighbor = get_neighbor(current)
        neighbor_cost = cost(neighbor)
        delta = current_cost - neighbor_cost

        if delta > 0 or random.random() < math.exp(delta / temperature):
            current, current_cost = neighbor, neighbor_cost
            if neighbor_cost < best_cost:
                best, best_cost = neighbor[:], neighbor_cost

        temperature *= cooling_rate

    return best, best_cost

def print_board(state):

    n = len(state)
    for row in range(n):
        line = " ".join("Q" if state[col] == row else "." for col in range(n))

```

```
print(line)
print()

n = 8
solution, cost_val = simulated_annealing(n, max_iter=20000)
print("Best position found:", solution)
print(f'Number of non-attacking pairs: {n*(n-1)//2 - cost_val}')
print("\nBoard:")
print_board(solution)
```

## Output

```
Best position found: [6, 3, 1, 7, 5, 0, 2, 4]
Number of non-attacking pairs: 28

Board:
. . . . . Q . .
. . Q . . . .
. . . . . . Q .
. Q . . . . .
. . . . . . . Q
. . . . Q . . .
Q . . . . . .
. . . Q . . .

==== Code Execution Successful ===|
```

## Program 6

Create a knowledge base using propositional logic and show that the given query entails the knowledge base or not.

### Algorithm

Week 5 - Propositional logic

① Create a knowledge base using propositional logic and query details the knowledge base

→ Algorithm  $\text{TT\_entails\_user\_input}$ )

Input:  
 $\text{KB} \leftarrow$  sentences = list of propositional sentences from user  
 $\text{query} \leftarrow$  query sentence from user

Process:  
 $\text{symbols} \leftarrow$  all unique propositional symbols appearing in KB sentences  
 $\text{return } \text{TT\_checkAll}(\text{KB sentences}, \text{query}, \text{symbols}, \text{empty model})$

→ Function  $\text{TT\_check\_all}(\text{KB}, \alpha, \text{symbols}, \text{model})$

~~If symbols is empty then  
 If PL-true? (KB, model) then  
 return PL-true? (α, model)  
 else  
 return true~~

~~else  
 $p \leftarrow \text{First}(\text{symbols})$   
 $\text{rest} \leftarrow \text{symbols} - \{p\}$~~

$\text{model\_true} = \text{model} \cup \{P = \text{true}\}$   
 $\text{model\_false} = \text{model} \cup \{P = \text{false}\}$

return  $\text{TT\_check\_all}(\text{KB}, \alpha, \text{rest}, \text{model\_true}) \text{ AND } \text{TT\_check\_all}(\text{KB}, \alpha, \text{rest}, \text{model\_false})$

→ function  $\text{PL\_true?}(\text{sentence\_set}, \text{model})$   
 for each sentence  $S$  in sentence set  
~~evaluate S  
 If S update to false under model  
 return False~~

return True

② Consider a knowledge base KB that contains the following propositional layered logic sentences:  
 $Q \rightarrow P$   
 $P \rightarrow TQ$

QVR  
 Construct a truth table that shows the value of each sentence in KB and its entailments.

P	Q	R	$Q \rightarrow P$	$P \rightarrow TQ$	QVR
T	T	T	T	F	T
T	T	F	T	F	T
T	F	T	T	T	T
T	F	F	T	T	F
F	T	T	F	T	T
F	T	F	F	T	T
F	F	T	T	T	T
F	F	F	T	T	F

ii) Does KB entail R  
 In all models where KB is true, R = T  
 $\therefore$  KB entails R

iii) Does KB entail  $R \rightarrow P$   
 $\begin{array}{c|c|c|c}
 \text{PQR} & \text{KB} & \text{entail} & R \rightarrow P \\
 \hline
 \text{TTT} & \text{F} & \} & \text{Both false} \Rightarrow \text{KB does not entail R} \\
 \text{TTF} & \text{F} & \} & \\
 \text{FTT} & \text{F} & \} & \\
 \text{FFF} & \text{F} & \} &
 \end{array}$

ii Does KB entail  $Q \Rightarrow R$

PQR	$Q \Rightarrow P$	Always true $\Rightarrow$ KB entails $Q \Rightarrow R$
TFT	T	
FFT	T	

Q  $\Delta = A \vee B$   
 $KB = (A \vee C) \wedge (B \vee C)$

A	B	C	$A \vee C$	$B \vee C$	KB	$\Delta$
F	F	F	F	T	F	F
F	F	T	T	F	F	F
F	T	F	F	T	F	T
F	T	T	T	T	(T)	(T)
T	F	F	T	T	(T)	(T)
T	F	T	T	F	F	T
T	T	F	T	T	(T)	(T)
T	T	T	T	T	(T)	(T)

. KB entails  $\Delta$

Skr 22/11/20

## Code

```

import itertools
def evaluate_formula(formula, truth_assignment):
    eval_formula = formula
    for symbol, value in truth_assignment.items():
        eval_formula = eval_formula.replace(symbol, str(value))
    return eval(eval_formula)

def generate_truth_table(variables):
    return list(itertools.product([False, True], repeat=len(variables)))

def is_entailed(KB_formula, alpha_formula, variables):
    truth_combinations = generate_truth_table(variables)

```

```

print(f"{''.join(variables)} | KB Result | Alpha Result")
print("-" * (len(variables) * 2 + 15))
for combination in truth_combinations:
    truth_assignment = dict(zip(variables, combination))
    KB_value = evaluate_formula(KB_formula, truth_assignment)
    alpha_value = evaluate_formula(alpha_formula, truth_assignment)
    result_str = " ".join(["T" if value else "F" for value in combination])
    print(f'{result_str} | {("T" if KB_value else "F")}' + ' | {' + ('T' if alpha_value else 'F') + '}')
    if KB_value and not alpha_value:
        return False
return True

KB = "(A or C) and (B or not C)"
alpha = "A or B"
variables = ['A', 'B', 'C']

if is_entailed(KB, alpha, variables):
    print("\nThe knowledge base entails alpha.")
else:
    print("\nThe knowledge base does not entail alpha.")

```

## Output

A	B	C		KB Result		Alpha Result
<hr/>						
F	F	F		F		F
F	F	T		F		F
F	T	F		F		T
F	T	T		T		T
T	F	F		T		T
T	F	T		F		T
T	T	F		T		T
T	T	T		T		T
The knowledge base entails alpha.						

## Program 7

Implement unification in first order logic

### Algorithm

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29-10-25      Week 6 - Unification of FOL

①  $P(f(x), g(y), y)$   
 $P(f(g(z)), g(f(a)), f(a))$   
 Find  $\Theta$  (MAU)

②  $Q(x, F(x))$   
 $Q(F(y), y)$

③  $H(x, g(x))$   
 $H(g(y), g(g(z)))$

Answer

1. Compare  $x$  with  $g(z)$ ,  $\Theta_1 = \{x/g(z)\}$   
 $y$  with  $F(a)$ ,  $\Theta_2 = \{y/F(a)\}$

Substituting  $\Theta$  in  $P(F(x), g(y), y)$   
 $= P(F(g(z)), g(F(a)), f(a))$

∴ both are identical ∴ unified

$\Theta = \{x/g(z), y/F(a)\}$

2. Comparing  $x$  with  $F(y)$

Substituting  $\Theta$  in  $Q(x, F(x))$   
 $= Q(F(y), F(F(y)))$

$$f(f(y)) = y$$

it is cyclic so not unifiable

3) comparing  $n$  with  $g(y)$

$$n = g(y)$$

comparing  $g(z)$  &  $g(g(z))$

$$n = g(y)$$

$$\Theta_1 = \{ n / g(y) \}$$

$$g(x) = g(g(y))$$

If  $y = z$ ,  $g(g(y))$  can be unified but  $g(z)$

$$\Theta_2 = \{ y, z \}$$

put  $\Theta_1$  in  $H(x, g(x))$

$$\Theta(\text{MGU}) = \{ x, gy, y, z \}$$

$$= H(gy, g(g(y)))$$

$$= H(gy, g(g(z)))$$

∴ it is identical

∴ it is unifiable.

Events  
Motion  
AB Pings

of puzzle.

## Code

```
import re

def is_variable(x):
    return x[0].islower() and x.isalpha()

def parse(term):
    term = term.strip()
    if '(' not in term:
        return term
    name, args = term.split('(', 1)
    args = args[:-1] # remove closing parenthesis
    return name.strip(), [parse(a.strip()) for a in args.split(',')]

def occurs_check(var, expr):
    if var == expr:
        return True
    if isinstance(expr, tuple):
        _, args = expr
        return any(occurs_check(var, a) for a in args)
    return False

def substitute(subs, expr):
    if isinstance(expr, str):
        if expr in subs:
            return substitute(subs, subs[expr])
        return expr
    else:
        func, args = expr
        return (func, [substitute(subs, a) for a in args])

def unify(x, y, subs=None):
    if subs is None:
        subs = {}

    x = substitute(subs, x)
    y = substitute(subs, y)

    if x == y:
```

```

return subs

if isinstance(x, str) and is_variable(x):
    if occurs_check(x, y):
        return None
    subs[x] = y
    return subs

if isinstance(y, str) and is_variable(y):
    if occurs_check(y, x):
        return None
    subs[y] = x
    return subs

if isinstance(x, tuple) and isinstance(y, tuple):
    if x[0] != y[0] or len(x[1]) != len(y[1]):
        return None
    for a, b in zip(x[1], y[1]):
        subs = unify(a, b, subs)
        if subs is None:
            return None
    return subs

return None

def term_to_str(t):
    if isinstance(t, str):
        return t
    func, args = t
    return f'{func}({",".join(term_to_str(a) for a in args)})'

def pretty_print(subs):
    return ','.join(f'{v} : {term_to_str(t)}' for v, t in subs.items())

pairs = [
    ("P(f(x),g(y),y)", "P(f(g(z)),g(f(a)),f(a))"),
    ("Q(x,f(x))", "Q(f(y),y)"),
    ("H(x,g(x))", "H(g(y),g(g(z))))")
]

```

]

```
for s1, s2 in pairs:  
    print(f"\nUnifying: {s1} and {s2}")  
    result = unify(parse(s1), parse(s2))  
    if result:  
        print("=> Substitution:", pretty_print(result))  
    else:  
        print("=> Not unifiable.")
```

## Output:

```
Unifying: P(f(x),g(y),y) and P(f(g(z)),g(f(a)),f(a))  
=> Substitution: x : g(z), y : f(a)  
  
Unifying: Q(x,f(x)) and Q(f(y),y)  
=> Not unifiable.  
  
Unifying: H(x,g(x)) and H(g(y),g(g(z)))  
=> Substitution: x : g(y), y : z
```

## Program 8

Create a knowledge base consisting of first order logic statements and prove the given query using forward reasoning.

## **Algorithm**

**Forward Reasoning Algorithm:**

Function FOR-FC - ASR(KB, q) returns a substitution or false

Inputs: KB, the knowledge base, a set of F<sub>1</sub>-order definite clauses

1. the query, an atomic sentence

local variables: new, the new set of sentences inferred on each iteration

repeat until new is empty

new = {}

for each rule in KB do

(p<sub>1</sub> ∧ p<sub>2</sub> ∧ ... ∧ p<sub>n</sub> ⇒ q<sub>i</sub>) ← STANDARDIZE  
-VARIABLES(rule)

for each q such that SUBST(q, p<sub>1</sub>, ..., p<sub>n</sub>) = q'  
= SUBST(q, p<sub>1</sub>', ..., p<sub>n</sub>')

for some p<sub>1</sub>', ..., p<sub>n</sub>' in KB

q' ← SUBST(q, p<sub>i</sub>)  
if q' does not unify with some sentence already in KB  
or new then

add q' to new

Φ ← UNIFY(q', q)  
if Φ is not fail then return Φ

add new to KB

return false

**Output:**

Bafna Gold  
Date: \_\_\_\_\_ Page: \_\_\_\_\_

Query : Mortal (Arama)  
Initial facts : { 'Human (Arama)' }  
Final facts : { 'Human (Arama)', 'Mortal (Arama)' }

✓ ✓ ✓

## **Code**

```

import re

def match_pattern(pattern, fact):
    """
    Checks if a fact matches a rule pattern using regex-style variable substitution.
    Variables are lowercase words like p, q, x, r etc.
    Returns a dict of substitutions or None if not matched.
    """

    # Extract predicate name and arguments
    pattern_pred, pattern_args = re.match(r'(\w+)', pattern).groups()
    fact_pred, fact_args = re.match(r'(\w+)', fact).groups()

    if pattern_pred != fact_pred:
        return None # predicate mismatch

    pattern_args = [a.strip() for a in pattern_args.split(",")]
    fact_args = [a.strip() for a in fact_args.split(",")]

    if len(pattern_args) != len(fact_args):
        return None

    subst = {}
    for p_arg, f_arg in zip(pattern_args, fact_args):
        if re.fullmatch(r'[a-z]\w*', p_arg): # variable
            subst[p_arg] = f_arg
        elif p_arg != f_arg: # constants mismatch
            return None
    return subst

def apply_substitution(expr, subst):
    """
    Replaces all variable names in expr using the given substitution dict.
    """
    for var, val in subst.items():
        expr = re.sub(rf'\b{var}\b', val, expr)
    return expr

# ----- Knowledge Base -----

rules = [
    ("American(p)", "Weapon(q)", "Sells(p,q,r)", "Hostile(r)", "Criminal(p)"),
    ("Missile(x)", "Weapon(x)",),
    ("Enemy(x, America)", "Hostile(x)",),
    ("Missile(x)", "Owns(A, x)", "Sells(Robert, x, A)")
]

```

```

facts = {
    "American(Robert)",
    "Enemy(A, America)",
    "Owns(A, T1)",
    "Missile(T1)"
}

goal = "Criminal(Robert)"

def forward_chain(rules, facts, goal):
    added = True
    while added:
        added = False
        for premises, conclusion in rules:
            possible_substs = []
            for p in premises:
                for f in facts:
                    subst = match_pattern(p, f)
                    if subst:
                        possible_substs.append(subst)
                        break
                else:
                    break
            else:
                combined = {}
                for s in possible_substs:
                    combined.update(s)

                new_fact = apply_substitution(conclusion, combined)

                if new_fact not in facts:
                    facts.add(new_fact)
                    print(f"Inferred: {new_fact}")
                    added = True
                if new_fact == goal:
                    return True
    return goal in facts

print("Goal achieved:", forward_chain(rules, facts, goal))

```

## Output

```
Inferred: Weapon(T1)
Inferred: Hostile(A)
Inferred: Sells(Robert, T1, A)
Inferred: Criminal(Robert)
Goal achieved: True
```

## Program 9

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution

## **Algorithm**

12-11-23      Bajna Gold  
Date: \_\_\_\_\_ Page: \_\_\_\_\_

Week 7

Convert a given first order logic statement into Conjunctive Normal Form (CNF)

procedure TO-CNF( $F$ ):

# Step 1: Eliminate implications and biconditionals, for each subformula in  $F$ :

if subformula is  $(A \rightarrow B)$ :  
    replace with  $(\neg A \vee B)$

if subformula is  $(A \leftrightarrow B)$ :  
    replace with  $((\neg A \vee B) \wedge (\neg B \vee A))$

# Step 2: Move negations inward while there exists a negation applied to a compound formula:

apply De Morgan's laws:  
 $\neg(A \wedge B) \rightarrow (\neg A \vee \neg B)$   
 $\neg(A \vee B) \rightarrow (\neg A \wedge \neg B)$

push  $\neg$  through quantifiers:

$\forall x P(x) \rightarrow \exists x \neg P(x)$   
 $\exists x P(x) \rightarrow \forall x \neg P(x)$

remove <sup>double</sup> ^ negations:

$\neg(\neg A) \rightarrow A$

# Step 3: Standardize variables for each quantified variable  $x$  in  $F$ :

if variable name repeats:  
    rename it to a unique variable

# Step 4: Skolemize / remove existential quantifiers

For each  $\exists x$  in F:

if  $\exists x$  is inside  $\forall y_1, \forall y_2, \dots, \forall y_n$

replace  $x$  with a new skolem

Function  $F(y_1, y_2, \dots, y_n)$

else:

replace  $x$  with a new skolem constant

remove  $\exists$  quantifier

# Step 5: Drop universal quantifiers

remove all  $\forall$  quantifiers (all variables now

implicitly universal)

# Step 6: Distribute V over A

repeat until no distribution is possible

apply rules:

$$(A \vee (B \wedge C)) \rightarrow ((A \vee B) \wedge (A \vee C))$$

$$((A \wedge B) \vee C) \rightarrow ((A \vee C) \wedge (B \vee C))$$

# Step 7: Simplify

remove duplicate literals in clauses

remove tautological clauses (where A and  $\neg A$  appear

together)

return F

Output:

Function  $(A \rightarrow (B \vee C)) \wedge \neg (D \rightarrow E)$

Output:  $(\neg A \vee B \vee C) \wedge \neg D \wedge \neg E$

## Code

```
from copy import deepcopy
```

```
def print_step(title, content):
```

```
    print(f"\n{'='*45}\n{title}\n{'='*45}")
```

```
    if isinstance(content, list):
```

```
        for i, c in enumerate(content, 1):
```

```
            print(f'{i}. {c}')
```

```

else:
    print(content)

KB = [
    ["¬Food(x)", "Likes(John,x)"],
    ["Food(Apple)"],
    ["Food(Vegetable)"],
    ["¬Eats(x,y)", "Killed(x)", "Food(y)"],
    ["Eats(Anil,Peanuts)"],
    ["Alive(Anil)"],
    ["¬Alive(x)", "¬Killed(x)"],
    ["Killed(x)", "Alive(x)"]
]
QUERY = ["Likes(John,Peanuts)"]

def negate(literal):
    if literal.startswith("¬"):
        return literal[1:]
    return "¬" + literal

def substitute(clause, subs):
    new_clause = []
    for lit in clause:
        for var, val in subs.items():
            lit = lit.replace(var, val)
        new_clause.append(lit)
    return new_clause

def unify(lit1, lit2):
    """Small unifier for patterns like Food(x) and Food(Apple)."""
    if "(" not in lit1 or "(" not in lit2:
        return None
    pred1, args1 = lit1.split("(")
    pred2, args2 = lit2.split("(")
    args1 = args1[:-1].split(",")
    args2 = args2[:-1].split ","
    if pred1 != pred2 or len(args1) != len(args2):
        return None
    subs = {}
    for a, b in zip(args1, args2):
        if a == b:
            continue
        if a.islower():
            subs[a] = b
        elif b.islower():
            subs[b] = a

```

```

    else:
        return None
    return subs

def resolve(ci, cj):
    """Return list of (resolvent, substitution, pair)."""
    resolvents = []
    for li in ci:
        for lj in cj:
            if li == negate(lj):
                new_clause = [x for x in ci if x != li] + [x for x in cj if x != lj]
                resolvents.append((list(set(new_clause)), {}, (li, lj)))
            else:
                # same predicate, opposite sign
                if li.startswith("¬") and not lj.startswith("¬") and li[1:].split("(")[0] == lj.split("(")[0]:
                    subs = unify(li[1:], lj)
                    if subs:
                        new_clause = substitute([x for x in ci if x != li] + [x for x in cj if x != lj], subs)
                        resolvents.append((list(set(new_clause)), subs, (li, lj)))
                elif lj.startswith("¬") and not li.startswith("¬") and lj[1:].split("(")[0] == li.split("(")[0]:
                    subs = unify(lj[1:], li)
                    if subs:
                        new_clause = substitute([x for x in ci if x != li] + [x for x in cj if x != lj], subs)
                        resolvents.append((list(set(new_clause)), subs, (li, lj)))
    return resolvents

def resolution(kb, query):
    clauses = deepcopy(kb)
    negated_query = [negate(q) for q in query]
    clauses.append(negated_query)
    print_step("Initial Clauses", clauses)

    steps = []
    new = []
    while True:
        pairs = [(clauses[i], clauses[j]) for i in range(len(clauses))
                  for j in range(i + 1, len(clauses))]
        for (ci, cj) in pairs:
            for r, subs, pair in resolve(ci, cj):
                if not r:
                    steps.append({
                        "parents": (ci, cj),
                        "resolvent": r,
                        "subs": subs
                    })
        print_tree(steps)
        print("\n✓ Empty clause derived — query proven.")

```

```

        return True
    if r not in clauses and r not in new:
        new.append(r)
        steps.append({
            "parents": (ci, cj),
            "resolvent": r,
            "subs": subs
        })
    if all(r in clauses for r in new):
        print_step("No New Clauses", "Query cannot be proven ✗")
        print_tree(steps)
        return False
    clauses.extend(new)

def print_tree(steps):
    print("\n" + "="*45)
    print("Resolution Proof Trace")
    print("="*45)
    for i, s in enumerate(steps, 1):
        p1, p2 = s["parents"]
        r = s["resolvent"]
        subs = s["subs"]
        subs_text = f" Substitution: {subs}" if subs else ""
        print(f" Resolve {p1} and {p2}")
        if subs_text:
            print(subs_text)
        if r:
            print(f" ⇒ {r}")
        else:
            print(" ⇒ {} (empty clause)")
    print("-"*45)

def main():
    print_step("Knowledge Base in CNF", KB)
    print_step("Negated Query", [negate(q) for q in QUERY])
    proven = resolution(KB, QUERY)
    if proven:
        print("\n✓ Query Proven by Resolution: John likes peanuts.")
    else:
        print("\n✗ Query cannot be proven from KB.")

if __name__ == "__main__":
    main()

```

## Output

```
Unifying: P(f(x),g(y),y)  and  P(f(g(z)),g(f(a)),f(a))
          ))
=> Substitution: x : g(z), y : f(a)

Unifying: Q(x,f(x))  and  Q(f(y),y)
=> Not unifiable.

Unifying: H(x,g(x))  and  H(g(y),g(g(z)))
=> Substitution: x : g(y), y : z

==== Code Execution Successful ===
```

## **Program 10**

Implement Alpha-Beta Pruning

### **Algorithm**

2-11-25

Date: \_\_\_\_\_ Page: \_\_\_\_\_

## Alpha beta Search

### Algorithm

Function ALPHA-BETA-SEARCH(state) returns an action  
 $v \leftarrow \text{MAX-VALUE}(\text{state}, -\infty, +\infty)$   
return the action in ACTIONS(state) with value v

Function MAX-VALUE(state,  $\alpha, \beta$ ) returns a utility value  
if TERMINAL TEST(state) then return UTILITY(state)

$v \leftarrow -\infty$

for each  $a$  in ACTIONS(state) do

$v \leftarrow \text{MAX}(v, \text{MIN-VALUE}(\text{RESULT}(s, a), \alpha, \beta))$

if  $v > \beta$  then return  $v$

$\alpha \leftarrow \text{MAX}(\alpha, v)$

return  $v$

Function MIN-VALUE(state,  $\alpha, \beta$ ) returns a utility value  
if terminal TEST(state) then return UTILITY(state)

$v \leftarrow +\infty$

for each action  $a$  in ACTIONS(state) do

$v \leftarrow \text{MIN}(v, \text{MAX-VALUE}(\text{RESULT}(s, a), -\infty, \beta))$

if  $v < \alpha$  then return  $v$

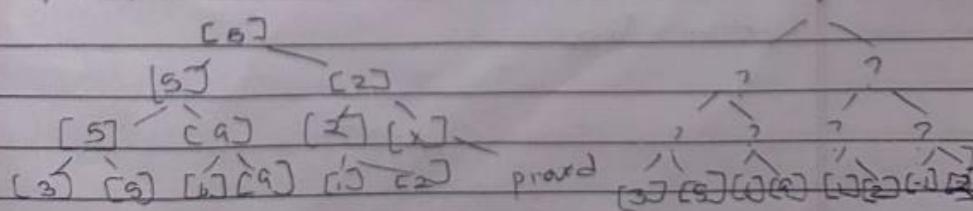
$\beta \leftarrow \text{MIN}(\beta, v)$

return  $v$

### Output

Leaf Node Values: [3, 5, 6, 9, 1, 2, 0, -1]

Optimal Value: 5



## Code

```
def unify(a, b):
    """Very simple unification for small terms like ('line', [X,O,X])"""
    if a == b:
        return {}
    if isinstance(a, str) and a.islower(): # variable
        return {a: b}
    if isinstance(b, str) and b.islower():
        return {b: a}
    if isinstance(a, tuple) and isinstance(b, tuple):
        if a[0] != b[0] or len(a[1]) != len(b[1]):
            return None
        subs = {}
        for x, y in zip(a[1], b[1]):
            s = unify(x, y)
            if s is None:
                return None
            subs.update(s)
        return subs
    return None

# Winning triples (rows, cols, diagonals)
WIN_TRIPLES = [(0,1,2),(3,4,5),(6,7,8),(0,3,6),(1,4,7),(2,5,8),(0,4,8),(2,4,6)]

def winner(board):
    pattern = ('line', ['X','X','X'])
    for i,j,k in WIN_TRIPLES:
        term = ('line', [board[i], board[j], board[k]])
        if unify(term, pattern):
            return 'X'
        if unify(term, ('line',['O','O','O'])):
            return 'O'
    return None

def is_full(board): return all(c != '_' for c in board)

def evaluate(board):
    w = winner(board)
    if w == 'X': return 1
    if w == 'O': return -1
    if is_full(board): return 0
    return None
```

```

def alpha_beta(board, player, alpha=-float('inf'), beta=float('inf')):
    val = evaluate(board)
    if val is not None:
        return val, None

    moves = [i for i,c in enumerate(board) if c == '_']
    best_move = None
    if player == 'X':
        max_eval = -float('inf')
        for m in moves:
            new_board = board[:]
            new_board[m] = 'X'
            eval_, _ = alpha_beta(new_board, 'O', alpha, beta)
            if eval_ > max_eval:
                max_eval, best_move = eval_, m
            alpha = max(alpha, eval_)
            if beta <= alpha: break
        return max_eval, best_move
    else:
        min_eval = float('inf')
        for m in moves:
            new_board = board[:]
            new_board[m] = 'O'
            eval_, _ = alpha_beta(new_board, 'X', alpha, beta)
            if eval_ < min_eval:
                min_eval, best_move = eval_, m
            beta = min(beta, eval_)
            if beta <= alpha: break
        return min_eval, best_move

def print_board(b):
    for i in range(0,9,3):
        print(''.join(b[i:i+3]))
    print()

# --- Example usage ---
board = ['_']*9
score, move = alpha_beta(board, 'X')
print("Best first move for X:", move)
board[move] = 'X'
print_board(board)

```

## Output

```
You are X. AI is O.          AI is thinking...
|   |
+---+---+
|   |
+---+---+
|   |
Enter your move (0-8): 7      | o | x
+---+---+
| o |
+---+---+
x |   |
|   |
Enter your move (0-8): 2      | o | x
+---+---+
|   | x
+---+---+
|   |
+---+---+
|   |
AI is thinking...              | o |
+---+---+
| o |
+---+---+
x | x | o
Enter your move (0-8): 6      Enter your move (0-8): 0
+---+---+
|   | x
+---+---+
| o |
+---+---+
x |   |
|   |
Enter your move (0-8): 6      AI is thinking...
+---+---+
|   | x
+---+---+
| o |
+---+---+
x |   |
|   |

```

```
Enter your move (0-8): 5      X | o | x
+---+---+
0 | o | x
+---+---+
X | X | o
Result: Draw
```