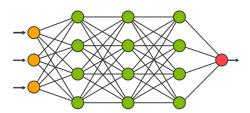
Introduction to Neural Networks

ML Instruction Team, Fall 2022

CE Department Sharif University of Technology



Problem: OverFitting in a Neural Network

- Why does overfitting happen in a neural network?
 - ▶ There are Too many free parameters.

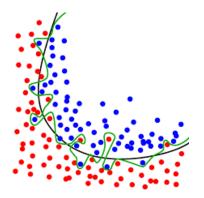


Figure: OverFitting in a neural network. source

Solution 1: L1/L2 Regularization

- It is like a linear regression regularizer.
- Sum the regularizer term for every layer weight!

$$L = \frac{1}{N} \sum_{i=1}^{N} L(\phi(x_i), y_i) + \lambda \sum_{i,j,k} R(W_{j,k}^{(i)})$$

L1/L2 Regularization

■ L1/L2 regularizer functions (review)

$$L1: R(w) = |w|$$

$$L2: R(w) = w^2$$

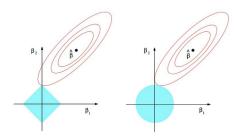


Figure: L1/L2 regularizers' solution diagram source

You can also combine the two different regularizers (Elastic Net).

$$R(w) = \beta w^2 + |w|$$



Solution 2: Early Stopping

Stop the training procedure when the validation error is minimum.

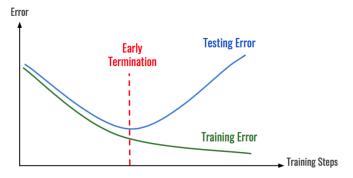
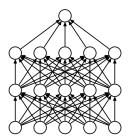


Figure: Early-Stopping diagram. source

Solution 3: Dropout

Training

- In each forward pass, randomly set some neurons to zero.
- The probability of dropping out for each neuron is a hyperparameter; 0.5 is common.



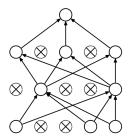


Figure: Behavior of dropout at training time. source

Dropout

- How can this possibly be a good idea?
 - ▶ It prevents the co-adaptation of features



Figure: Discrimination of neurons at training time. [1]

Dropout

- How can this possibly be a good idea?
 - ▶ It trains a large ensemble of models that share parameters.
 - \triangleright A fully connected layer with 4096 neurons has $2^4096 \sim 10^1233$ possible masks! There are only 10^82 atoms in the universe!

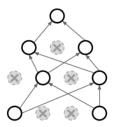


Figure: Behavior of dropout at training time. [1]

Dropout: Test Time

Dropout makes our output random at training time.

$$y = f_W(x, \underbrace{z}_{\text{random mask}})$$

We want to average out the randomness at test time,

$$y = f(x) = E_z[f(x,z)] = \int p(z)f(x,z)dz$$

But this integral seems complicated.

Dropout: Test Time

We want to approximate the integral for a superficial layer.

$$y = f(x) = E_z[f(x, z)] = \int p(z)f(x, z)dz$$

$$\begin{split} E_{train}[a] &= \frac{1}{4}(w_1x + w_2y + \frac{1}{4}(w_1x + 0y) \\ &+ \frac{1}{4}(0x + w_2y) + \frac{1}{4}(0x + 0y) \\ &= \frac{1}{2}(w_1x + w_2y) \\ E_{test}[a] &= w_1x + w_2y \\ \Rightarrow E_{test}[a] &= \underbrace{0.5}_{\text{dropout probability}} E_{train}[a] \end{split}$$

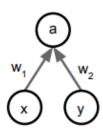


Figure: Simple neural network. [1]

Problem: Vanishing/Exploding Gradients

// Todo

- beginning of learning -> He/ELU
- during learning -> still exists

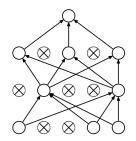


Figure: Behavior of dropout at training time. Source

Solution: Batch Norm Layer

It is used for normalizing the data.

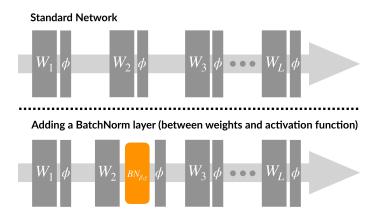


Figure: The suggested place to put a BatchNorm layer. source

Batch Norm: Training

First, it zero-centers and normalizes the batch.

$$\mu_B := \frac{1}{N_B} \sum x_B^{(i)}$$

$$\sigma_B^2 := \frac{1}{N_B} \sum (x_B^{(i)} - \mu_B)^2$$

$$\hat{x_B}^{(i)} = \frac{x_B^{(i)} - \mu_B}{\sqrt{\sigma_B^2 + \epsilon}}$$

Then, scales and shifts the batch with two learnable parameters γ , β .

$$y_B^{(i)} = \gamma \hat{x_B}^{(i)} + \beta$$



Batch Norm: Testing

- To zero-center and normalize the input, we need the average and variance of the whole data.
- Those parameters can be acquired during the training.
- Therefore we need two more trainable parameters.

$$\mu_D := \frac{1}{N} \sum x^{(i)}$$

$$\sigma_D^2 := \frac{1}{N} \sum_{i} (x^{(i)} - \mu)^2$$

Batch Norm: Performance

Normalizing the data improves the convergence speed by a considerable amount.

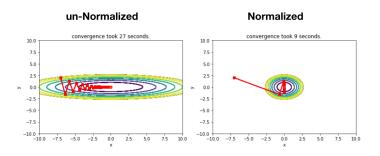


Figure: BatchNorm performance. Convergence speed is increased by 200%. source

Batch Norm: Pros

- Vanishing/Exploding gradient problem is reduced by a considerable amount.
- You can use even saturating activation functions.
- The network is much less sensitive to the initial weight.
- We're able to use larger learning rates, which speeds up the training.
- It also acts as a regularizer.
 - ▶ There is no need for other regularizer techniques.

Batch Norm: Cons

- It increases model parameters and prediction latency.
 - After the training procedure, we can mix the BatchNorm layer with its previous layer to hold the prediction latency.

$$y^{(i)} = Wx^{(i)} + b'$$

$$y^{(i)} = \frac{x'^{(i)} - \mu}{\sqrt{\sigma^2 + \epsilon}} + \beta$$

$$\Rightarrow \qquad W' := \frac{1}{\sqrt{\sigma^2 + \epsilon}} W$$

$$b' := \beta + \frac{b - \mu}{\sqrt{\sigma^2 + \epsilon}}$$

Thank You!

Any Question?

References



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