Generative Adversarial Networks (GAN)

So far...

PixelCNNs define tractable density function, optimize likelihood of training data:

$$p_{\theta}(x) = \prod_{i=1} p_{\theta}(x_i|x_1, ..., x_{i-1})$$

VAEs define intractable density function with latent **z**:

$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

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What if we give up on explicitly modeling density, and just want ability to sample?

GANs: don't work with any explicit density function! Instead, take game-theoretic approach: learn to generate from training distribution through 2-player game

Generative Adversarial Networks

Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

Solution: Sample from a simple distribution, e.g. random noise. Learn transformation to training distribution.

Q: What can we use to represent this complex transformation?

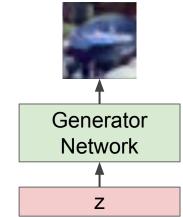
Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

Solution: Sample from a simple distribution, e.g. random noise. Learn transformation to training distribution.

Q: What can we use to represent this complex transformation?

A: A neural network!

Output: Sample from training distribution



Input: Random noise

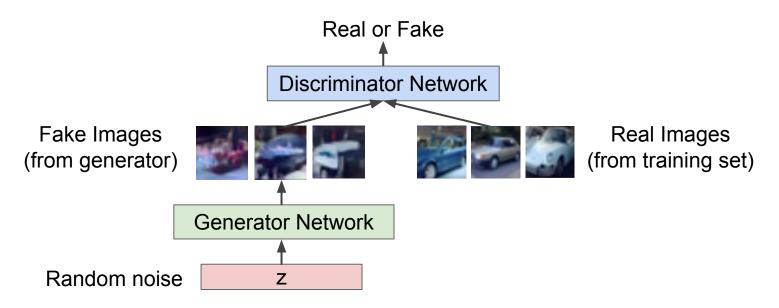
Training GANs: Two-player game

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

Training GANs: Two-player game

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Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

Train jointly in minimax game

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

Train jointly in **minimax game**

Discriminator outputs likelihood in (0,1) of real image

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$
Discriminator output for for real data x
$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$
Discriminator output for generated fake data G(z)

Training GANs: Two-player game

Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

Train jointly in minimax game

Discriminator outputs likelihood in (0,1) of real image

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$
 Discriminator output for for real data x generated fake data G(z)

- Discriminator (θ_d) wants to **maximize objective** such that D(x) is close to 1 (real) and D(G(z)) is close to 0 (fake)
- Generator (θ_g) wants to **minimize objective** such that D(G(z)) is close to 1 (discriminator is fooled into thinking generated G(z) is real)

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Minimax objective function:

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Alternate between:

Gradient ascent on discriminator

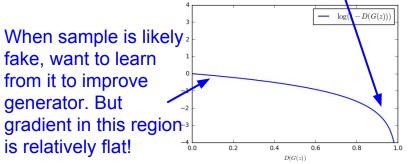
$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

In practice, optimizing this generator objective does not work well!

Oradient signal
dominated by region
where sample is
already good



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Training GANs: Two-player game

Minimax objective function:

$$\min_{\theta_a} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

Gradient ascent on discriminator

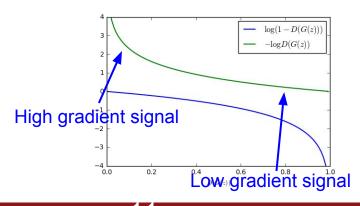
$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Instead: Gradient ascent on generator, different objective $\operatorname{log}(D, (C, (z)))$

$$\max_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(D_{\theta_d}(G_{\theta_g}(z)))$$

Instead of minimizing likelihood of discriminator being correct, now maximize likelihood of discriminator being wrong.

Same objective of fooling discriminator, but now higher gradient signal for bad samples => works much better! Standard in practice.



Training GANs: Two-player game

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Minimax objective function:

$$\min_{\theta_a} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log (1 - D_{\theta_d}(G_{\theta_g}(z))) \right] \\ \underset{\text{is an active area of}}{\text{landscapes helps training,}}$$

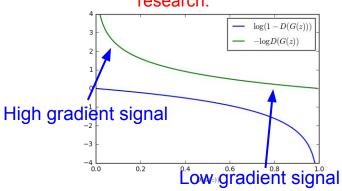
2. Instead: Gradient ascent on generator, different objective

$$\max_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(D_{\theta_d}(G_{\theta_g}(z)))$$

Instead of minimizing likelihood of discriminator being correct, now maximize likelihood of discriminator being wrong.

Same objective of fooling discriminator, but now higher gradient signal for bad samples => works much better! Standard in practice.

Aside: Jointly training two networks is challenging, can be unstable. Choosing objectives with better loss landscapes helps training, is an active area of research.



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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Putting it together: GAN training algorithm

for number of training iterations do

for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \dots, z^{(m)}\}$ from noise prior $p_q(z)$.
- ullet Sample minibatch of m examples $\{oldsymbol{x}^{(1)},\ldots,oldsymbol{x}^{(m)}\}$ from data generating distribution $p_{\text{data}}(\boldsymbol{x})$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \dots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for

lan Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Putting it together: GAN training algorithm

for number of training iterations do

for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Sample minibatch of m examples $\{x^{(1)}, \dots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(x)$.
- Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

Recent work (e.g. Wasserstein GAN) alleviates this problem, better stability!

Some find k=1

others use k > 1,

more stable,

no best rule.

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \dots, z^{(m)}\}$ from noise prior $p_q(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

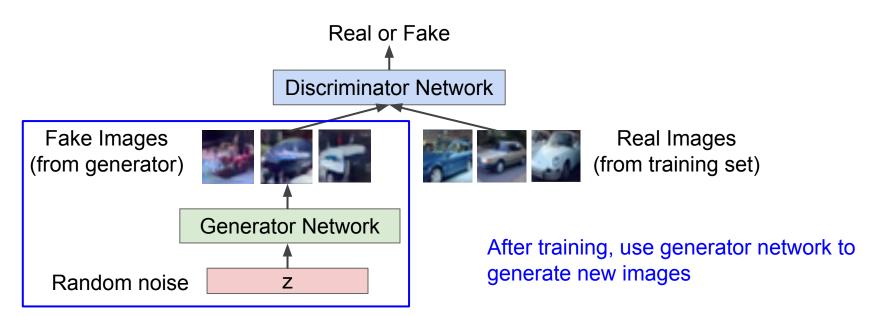
$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for

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Training GANs: Two-player game

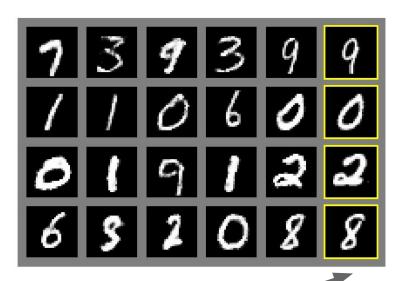
Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

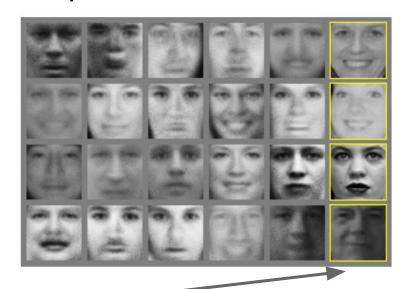


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Generative Adversarial Nets

Generated samples





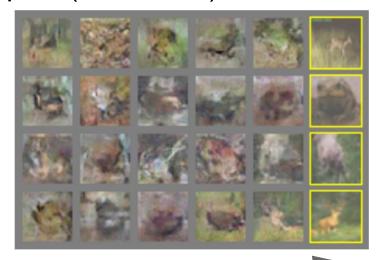
Nearest neighbor from training set

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Generative Adversarial Nets

Generated samples (CIFAR-10)





Nearest neighbor from training set

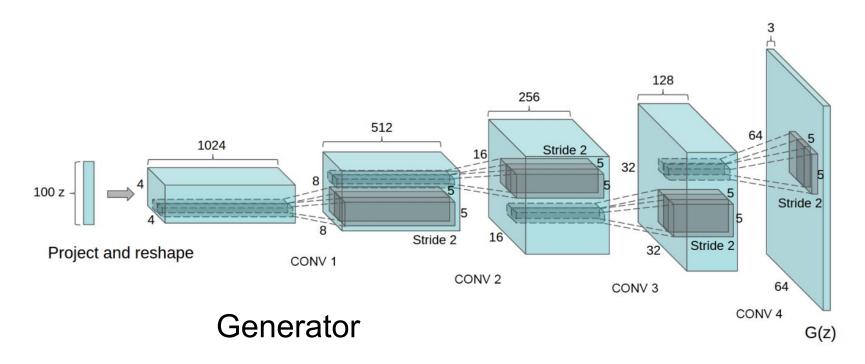
Figures copyright Ian Goodfellow et al., 2014. Reproduced with permission.

Generator is an upsampling network with fractionally-strided convolutions Discriminator is a convolutional network

Architecture guidelines for stable Deep Convolutional GANs

- Replace any pooling layers with strided convolutions (discriminator) and fractional-strided convolutions (generator).
- Use batchnorm in both the generator and the discriminator.
- Remove fully connected hidden layers for deeper architectures.
- Use ReLU activation in generator for all layers except for the output, which uses Tanh.
- Use LeakyReLU activation in the discriminator for all layers.

Radford et al, "Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks", ICLR 2016



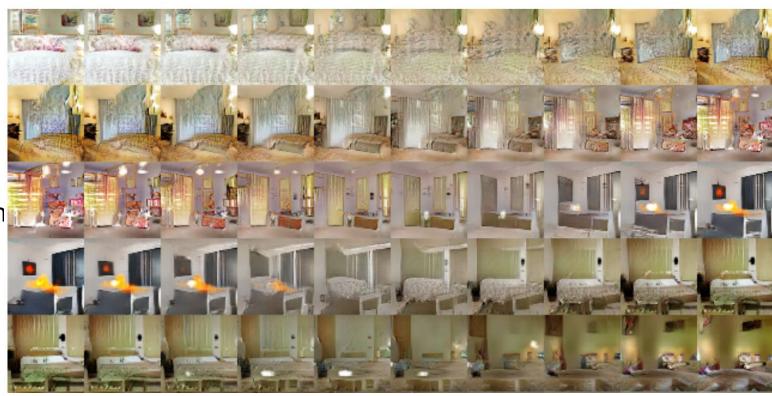
Radford et al, "Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks", ICLR 2016

Samples from the model look much better!



Radford et al, **ICLR 2016**

Interpolating between random points in laten space

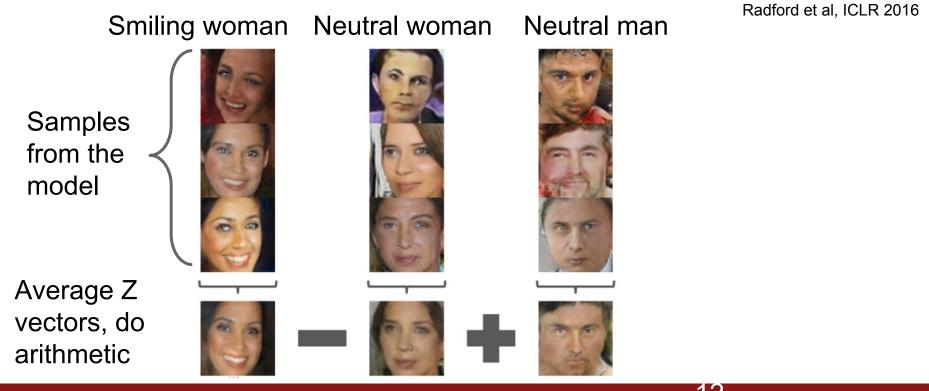


Radford et al, **ICLR 2016**

Samples from the model

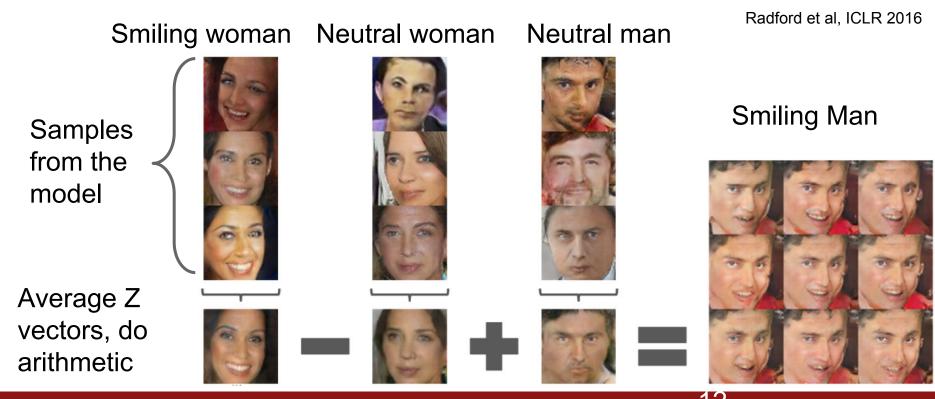
Smiling woman Neutral woman Neutral man Ne

Radford et al, ICLR 2016



 $\frac{12}{2}$ M

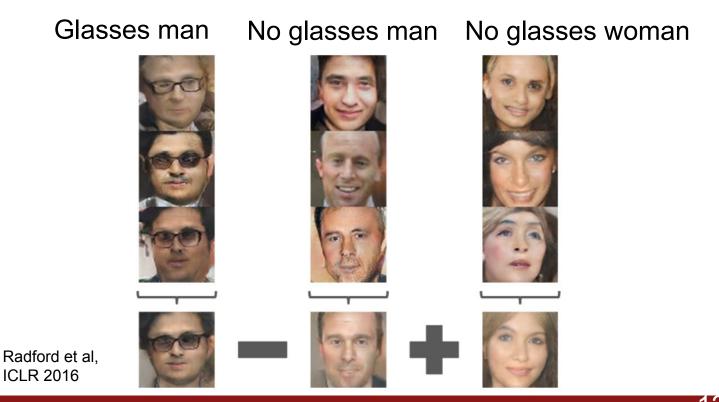
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Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 12 -

May 15, 2018





¹² May 15, 2018

"The GAN Zoo"

- GAN Generative Adversarial Networks
- · 3D-GAN Learning a Probabilistic Latent Space of Object Shapes via 3D Generative-Adversarial Modeling
- acGAN Face Aging With Conditional Generative Adversarial Networks
- AC-GAN Conditional Image Synthesis With Auxiliary Classifier GANs
- AdaGAN AdaGAN: Boosting Generative Models
- AEGAN Learning Inverse Mapping by Autoencoder based Generative Adversarial Nets
- AffGAN Amortised MAP Inference for Image Super-resolution
- · AL-CGAN Learning to Generate Images of Outdoor Scenes from Attributes and Semantic Layouts
- ALI Adversarially Learned Inference
- AM-GAN Generative Adversarial Nets with Labeled Data by Activation Maximization
- · AnoGAN Unsupervised Anomaly Detection with Generative Adversarial Networks to Guide Marker Discovery
- . ArtGAN ArtGAN: Artwork Synthesis with Conditional Categorial GANs
- · b-GAN b-GAN: Unified Framework of Generative Adversarial Networks
- Bayesian GAN Deep and Hierarchical Implicit Models
- BEGAN BEGAN: Boundary Equilibrium Generative Adversarial Networks
- BiGAN Adversarial Feature Learning
- BS-GAN Boundary-Seeking Generative Adversarial Networks
- · CGAN Conditional Generative Adversarial Nets
- CaloGAN CaloGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters with Generative Adversarial Networks
- · CCGAN Semi-Supervised Learning with Context-Conditional Generative Adversarial Networks
- · CatGAN Unsupervised and Semi-supervised Learning with Categorical Generative Adversarial Networks
- CoGAN Coupled Generative Adversarial Networks

- · Context-RNN-GAN Contextual RNN-GANs for Abstract Reasoning Diagram Generation
- C-RNN-GAN C-RNN-GAN: Continuous recurrent neural networks with adversarial training
- CS-GAN Improving Neural Machine Translation with Conditional Sequence Generative Adversarial Nets
- CVAE-GAN CVAE-GAN: Fine-Grained Image Generation through Asymmetric Training
- · CycleGAN Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks
- DTN Unsupervised Cross-Domain Image Generation
- . DCGAN Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks
- · DiscoGAN Learning to Discover Cross-Domain Relations with Generative Adversarial Networks
- . DR-GAN Disentangled Representation Learning GAN for Pose-Invariant Face Recognition
- DualGAN DualGAN: Unsupervised Dual Learning for Image-to-Image Translation
- · EBGAN Energy-based Generative Adversarial Network
- f-GAN f-GAN: Training Generative Neural Samplers using Variational Divergence Minimization
- FF-GAN Towards Large-Pose Face Frontalization in the Wild
- GAWWN Learning What and Where to Draw
- GeneGAN GeneGAN: Learning Object Transfiguration and Attribute Subspace from Unpaired Data
- Geometric GAN Geometric GAN
- GoGAN Gang of GANs: Generative Adversarial Networks with Maximum Margin Ranking
- GP-GAN GP-GAN: Towards Realistic High-Resolution Image Blending
- IAN Neural Photo Editing with Introspective Adversarial Networks
- iGAN Generative Visual Manipulation on the Natural Image Manifold
- IcGAN Invertible Conditional GANs for image editing
- ID-CGAN Image De-raining Using a Conditional Generative Adversarial Network
- . Improved GAN Improved Techniques for Training GANs
- InfoGAN InfoGAN: Interpretable Representation Learning by Information Maximizing Generative Adversarial Nets
- LAGAN Learning Particle Physics by Example: Location-Aware Generative Adversarial Networks for Physics Synthesis
- LAPGAN Deep Generative Image Models using a Laplacian Pyramid of Adversarial Networks

https://github.com/hindupuravinash/the-gan-zoo

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See also: https://github.com/soumith/ganhacks for tips and tricks for trainings GANs

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https://github.com/hindupuravinash/the-gan-zoo

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May 15, 2018

Better training and generation



LSGAN, Zhu 2017.



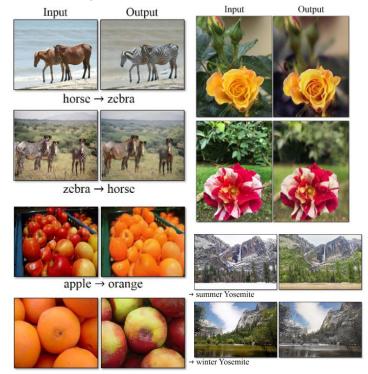
Wasserstein GAN, Arjovsky 2017. Improved Wasserstein GAN, Gulrajani 2017.





Progressive GAN, Karras 2018.

Source->Target domain transfer



CycleGAN. Zhu et al. 2017.

Text -> Image Synthesis

this small bird has a pink breast and crown, and black almost all black with a red primaries and secondaries.

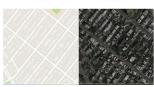
this magnificent fellow is crest, and white cheek patch.





Reed et al. 2017. Many GAN applications





Pix2pix. Isola 2017. Many examples at https://phillipi.github.io/pix2pix/

GANs

Don't work with an explicit density function Take game-theoretic approach: learn to generate from training distribution through 2-player game

Pros:

- Beautiful, state-of-the-art samples!

Cons:

- Trickier / more unstable to train
- Can't solve inference queries such as p(x), p(z|x)

Active areas of research:

- Better loss functions, more stable training (Wasserstein GAN, LSGAN, many others)
- Conditional GANs, GANs for all kinds of applications

Recap

Generative Models

- PixeIRNN and PixeICNN Explicit density model, optimizes exact likelihood, good samples. But inefficient sequential generation.
- Variational Autoencoders (VAE) Optimize variational lower bound on likelihood. Useful latent representation, inference queries. But current sample quality not the best.
- Generative Adversarial Networks (GANs) Game-theoretic approach, best samples!
 But can be tricky and unstable to train,
 no inference queries.

Recap

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Also recent work in combinations of these types of models! E.g. Adversarial Autoencoders (Makhanzi 2015) and PixelVAE (Gulrajani 2016)

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Recap

Generative Models

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Next time: Visualizing and understanding networks