

Scala Typesystem II

Mikhail Mutcianko, Alexey Otts

СПБГУ, СП

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Syntax recap: Advanced Features

Parameter lists

```
1 def foldLeft[B](z: B)(op: (B, A) => B): B
```

- logical grouping
- partial application
- passing implicit arguments
- assisting the typechecker

Type inference of multi-paren

Types are inferred sequentially per **each complete** parenthesis

```
1 def foo[A](x: A, f: A => Int) = ???  
2  
3  
4 object Demo {  
5   foo(1, i => i * i) // <<< error: missing parameter type  
6  
7 }
```

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```
1 def foo[A](x: A, f: A => Int) = ???
2 def bar[A](x: A)(f: A => Int) = ???
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4 object Demo {
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```
1 def foo[A](x: A, f: A => Int) = ???
2 def bar[A](x: A)(f: A => Int) = ???
3
4 object Demo {
5   foo(1, i => i * i) // <<< error: missing parameter type
6   bar(2)(i => i * i)
7 }
```

Named parameters

- arguments could be labelled with their parameter names
- order of named arguments can be rearranged
- the unnamed arguments must come first

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```
1 def printName(first: String, last: String) = ???  
2  
3 printName("John", "Smith")           // Prints "John Smith"  
4 printName(first = "John", last = "Smith") // Prints "John Smith"  
5 printName(last = "Smith", first = "John") // Prints "John Smith"  
6 printName(last = "Smith", "john")      // <<< error: positional after named argument
```


Call by-name parameters

By-name parameters are only evaluated when used. They are in contrast to by-value parameters. To make a parameter called by-name, simply prepend `=>` to its type.

- evaluated at **each** use within the function
- not the same thing as function-typed parameter
- can be used to pass blocks of code

Call by-name parameters

Example

```
1 p: () => Boolean // a function input parameter
2 p: => Boolean    // a by-name parameter
3
4
5
```

Call by-name parameters

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1 p: () => Boolean // a function input parameter
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4 myAssert(() => 5 > 3)
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1 p: () => Boolean // a function input parameter
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4 myAssert(() => 5 > 3)
5 byNameAssert(5 > 3)
```

Call by-name parameters

Example

```
1 p: () => Boolean // a function input parameter
2 p: => Boolean    // a by-name parameter
3
4 myAssert(() => 5 > 3)
5 byNameAssert(5 > 3)
```

```
1 def whileLoop(condition: => Boolean)(body: => Unit): Unit =
2   if (condition) {
3     body
4     whileLoop(condition)(body)
5   }
6
7 whileLoop (i > 0) {
8   println(i)
9   i -= 1
10 }
```

Type aliases

A type alias creates a new named type for a specific, existing type

```
1 type Word = List[Char]
2 type Sentence = List[Word]
3 type Paragraph = List[Sentence]
```

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```
1 type Word = List[Char]
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3 type Paragraph = List[Sentence]
```

Poor practice example:

```
1 type IntMaker = () => Int
2 IntMaker
```

Advanced OOP

Final keyword

In Scala `final` keyword is used to restrict inheritance

- `final val/var/def` - prohibits overriding
- `final class` - prohibits inheritance

Linearization

Scala linearization[1] is a deterministic process that puts all traits in a linear inheritance hierarchy

Linearization

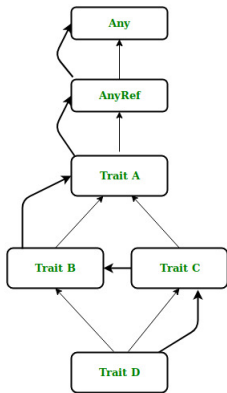
Scala linearization[1] is a deterministic process that puts all traits in a linear inheritance hierarchy

- 1 start at the first extended class or trait and write that complete hierarchy down
- 2 take the next trait and write this hierarchy down
 - remove all classes/traits from this hierarchy which are already in the linearized hierarchy
 - add the remaining traits to the bottom of the linearized hierarchy to create the new linearized hierarchy
- 3 repeat step 2 for every trait
- 4 place the class itself as the last type extending the linearized hierarchy

Linearization

```
1  trait A
2  trait B extends A
3  trait C extends A
4  class D extends B with C
```

Linearization

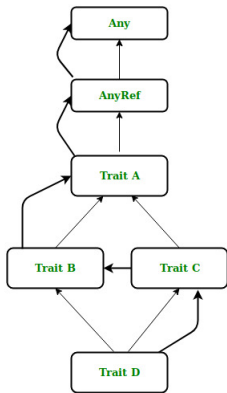


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4 class D extends B with C
```

bold — Linearization

light — Inheritance

Linearization



```
1 trait A
2 trait B extends A
3 trait C extends A
4 class D extends B with C
```

Actual hierarchy:

$D \rightarrow C \rightarrow B \rightarrow A \rightarrow \text{AnyRef} \rightarrow \text{Any}$

bold — Linearization

light — Inheritance

Abstract overrides

Scala allows invoking an abstract method of a superclass

- the meaning of `super` is not known at compile time in a single trait
- `super` calls in a trait are dynamically bound via linearization
- trait methods that need to call `super` must be annotated with `abstract override`

Abstract overrides

Example

```
1 trait IntPrinter
2   { def print(a: Int) }
3 class PrinterImpl extends IntPrinter
4   { def print(a: Int) = println(a) }
5 trait DoublingPrinter extends IntPrinter
6   { abstract override def print(a: Int) = super.print(a*2) }
7
8
```


Abstract overrides

Example

```
1 trait IntPrinter
2   { def print(a: Int) }
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7
8 (new PrinterImpl).print(3)           // prints 3
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```

Abstract overrides

Example

```
1 trait IntPrinter
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3 class PrinterImpl extends IntPrinter
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5 trait DoublingPrinter extends IntPrinter
6   { abstract override def print(a: Int) = super.print(a*2) }
7
8 (new PrinterImpl).print(3)           // prints 3
9 (new PrinterImpl with DoublingPrinter).print(3) // prints 6
```

Self type

Self-types are a way to declare that a trait must be mixed into another trait, even though it doesn't directly extend it. That makes the members of the dependency available without imports

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```
1 trait Defns { this: Aggregate => ...}  
2 trait Utils { this: Aggregate => ...}  
3  
4 object Aggregate extends Defns with Utils with ...
```

Path dependent types

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```
1 class Foo {  
2   class Bar  
3   var bar: Bar = new Bar  
4 }  
5 val a = new Foo  
6 val b = new Foo  
7 a.bar = b.bar //error: type mismatch; found: b.Bar; required: a.Bar
```

Path dependent types

In Scala, a nested type is bound to a specific *instance* of the outer type, not to the outer type itself

```
1 class Foo {  
2   class Bar  
3   var bar: Foo#Bar = new Bar  
4 }  
5 val a = new Foo  
6 val b = new Foo  
7 a.bar = b.bar // OK
```

Path dependent types

Multi-paren

```
1 case class Animal(foodName: String) {  
2   case class Food(name: String)  
3   val food = Food(foodName)  
4 }  
5  
6 def feed(animal: Animal)(food: animal.Food) = ???  
7  
8 val cat = Animal("fish")  
9 val fish = Animal("seaweed")  
10 feed(cat)(fish.food) // error: found: fish.Food, required: cat.Food
```


Compound types

- express that the type of an object is a subtype of several other types
- resulting type is an intersections of object types
- the general form is: A `with` B `with` C ... { refinement }

Compound types

```
1 trait Str { def str: String }
2 trait Count { def count: Int }
3
4 def repeat(cd: Str with Count): String =
5     Iterator.fill(cd.count)(cd.str).mkString
6
7 repeat(new Str with Count {
8     val str = "test"
9     val count = 3
10 }) // "testtesttest"
```

Polymorphic Types

Subtype polymorphism

Subclasses of a class can define their own unique behaviors while providing a common access interface. Instances of a subclass can be passed to a base class

```
1 trait Animal { def speak }  
2 class Human extends Animal { def speak = println("foo") }  
3  
4 val animal: Animal = new Human  
5 animal.speak
```

Type parameters

Allow abstracting over types in a class or a method

- class parameters are bound on **construction**
- method parameters are bound on **invocation**

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```
1 class A[T] {  
2   def foo(t: T) = ???  
3 }  
4  
5 val a = new Foo[Int]  
6 a.foo(123)    // OK  
7 a.foo("123") // compile error: found: String, required: Int
```

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2   def foo[T](t: T) = ???  
3 }  
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5 val a = new Foo[Int]  
6 a.foo(123)    // OK  
7 a.foo("123") // OK
```

Type erasure

Scalac warning:

```
non-variable type argument Int in type pattern Seq[Int] (the  
underlying of Seq[Int]) is unchecked since it is eliminated by erasure
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Type parameters do not affect evaluation in Scala

We can assume that all type parameters and type arguments are removed before evaluating the program

Type erasure

```
1 def process(thing: Something[_]) = thing match {  
2   case _: Int           => "an int"  
3   case _: Seq[Int]      => "some ints"  
4   case _: Seq[String] => "some strings"  
5 }  
6  
7 process(123) == "an int"  
8 process(Seq(1,2,3)) == "some ints"  
9 process(Seq("1", "2", "3")) == "some ints"
```

Type erasure

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1 def process(thing: Something[_]) = thing match {  
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```

Type bounds

Type bounds limit the concrete values of the type variables and possibly reveal [more](#) information about the members of such types

- $A <: B$ means: A is a subtype of B
- $A >: B$ means: A is a supertype of B, or B is a subtype of A

Type bounds

Upper bounds

```
1 trait Animal                { def fitness: Int }
2 trait Reptile extends Animal
3 trait Mammal  extends Animal
4 trait Zebra   extends Mammal { def zebraCount: Int }
5 trait Giraffe extends Mammal
6
7 def selection[A <: Animal](a1: A, a2: A): A =
8   if (a1.fitness > a2.fitness) a1 else a2
```

Type bounds

Lower and mixed bounds

```
1 | def reptilize[A >: Reptile](stuff: A): A = ???
```

- the type parameter A that can range only over **supertypes** of Reptile
- A could be one of Reptile, Animal, AnyRef or Any

Type bounds

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```
1 | def reptilize[A >: Reptile](stuff: A): A = ???
```

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- A could be one of Reptile, Animal, AnyRef or Any

```
1 | def hide[A >: Zebra <: Animal](stuff: A): A = ???
```

- restrict A any type on the interval between Zebra and Animal

Variance

Variance is the correlation of subtyping relationships of complex types and the subtyping relationships of their component types

Scala supports variance annotations of type parameters of [generic classes](#)

```
1 class Foo[+A] // A covariant class
2 class Bar[-A] // A contravariant class
3 class Baz[A]  // An invariant class
```


Covariance

Let $C[T]$ be a parameterized type and A, B are types such that $A <: B$
and if $C[A] <: C[B]$ then C is **covariant**

```
1 class Foo[A] { def f(x: Foo[A]) = ??? }  
2  
3 val foo = new Foo[Number]  
4 foo.f(new Foo[Int]) // error: type mismatch found: Foo[Int], required: Foo[Number]
```

Covariance

Let $C[T]$ be a parameterized type and A, B are types such that $A <: B$
and if $C[A] <: C[B]$ then C is **covariant**

```
1 class Foo[+A] { def f[T <: A](x: Foo[T]) = ??? }  
2  
3 val foo = new Foo[Number]  
4 foo.f(new Foo[Int]) // OK
```

Java array variace

Early version of Java had no generics but polymorphic array algorithms were still necessary:

```
1 | boolean equalArrays (Object[] a1, Object[] a2);  
2 | void shuffleArray(Object[] a);
```

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```
1 | boolean equalArrays (Object[] a1, Object[] a2);  
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```

```
1 | Zebra[] zebras = new Zebra[]{ new Zebra() } // Array containing 1 `Zebra`  
2 | Mammal[] mammals = zebras // Allowed because arrays are covariant in Java  
3 | mammals[0] = new Giraffe() // Allowed because a `Giraffe` is a subtype of `Mammal`  
4 | Zebra zebra = zebras[0] // Get the first `Zebra` ... which is actually a `Giraffe`!
```

Java array variance

ArrayStoreException

To mitigate invalid array type storage issue Java has introduced
ArrayStoreException [4]

```
1 | Object x[] = new String[3];  
2 | x[0] = new Integer(0); // ArrayStoreException is thrown
```

Scala collections variance

- immutable Scala collections are **covariant**
- mutable Scala collections are **invariant**
- Array in Scala is **invariant**

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- Array in Scala is **invariant**

```
1 | val zebras: Array[Zebra] = Array(new Zebra)
2 | val mammals: Array[Mammal] = zebras //error: found: Array[Zebra], required: Array[Mammal]
3 | mammals(0) = new Giraffe
4 | val zebra: Zebra = zebras(0)
```

Scala collections variance

- immutable Scala collections are **covariant**
- mutable Scala collections are **invariant**
- Array in Scala is **invariant**

```
1 val zebras: List[Zebra] = List(new Zebra)
2 val mammals: List[Mammal] = zebras
3 val something = mammals :+ new Giraffe
4 val zebra: Zebra = zebras.tail.head // OK
```


Scala function variance

If $A2 \leq A1$ and $B1 \leq B2$ then $A1 \Rightarrow B1 \leq A2 \Rightarrow B2$

So functions are contravariant in argument type(s) and covariant in result type

```
1 | trait Function1[-T, +U] {  
2 |     def apply(x: T): U  
3 | }
```

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So functions are contravariant in argument type(s) and covariant in result type

```
1 trait Function1[-T, +U] {  
2   def apply(x: T): U  
3 }
```

```
1 class Foo[+A] { def f(x: Foo[A]) = ??? }  
2 //           ^  
3 // error: covariant type A occurs in contravariant position in type Foo[A] of value x
```

Variance checks

The Scala compiler will check that there are no problematic combinations when compiling a class with variance annotations. Roughly:

- covariant type parameters can only appear in method results
- contravariant type parameters can only appear in method parameters
- invariant type parameters can appear anywhere

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- covariant type parameters can only appear in method results
- contravariant type parameters can only appear in method parameters
- invariant type parameters can appear anywhere
- covariant type parameters may appear in lower bounds of method type parameters
- contravariant type parameters may appear in upper bounds of method

Type members

Abstract types, such as traits and abstract classes, can in turn have abstract type members. This means that the concrete implementations define the actual types.

```
1 trait Buffer {  
2   type T  
3   val element: T  
4   def copyFrom(t: T)  
5 }  
6 abstract class SeqBuffer extends Buffer {  
7   type U  
8   type T <: Seq[U]  
9   def length = element.length  
10 }
```

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```
1 trait Buffer {  
2   type T  
3   val element: T  
4   def copyFrom(t: T)  
5 }  
6 class IntSeqBuffer extends Buffer {  
7   override type T = Seq[Int]  
8   def length = element.length  
9   def copyFrom(t: Seq[Int]) = ???  
10 }
```

Practice:
Testing

- [1] <https://www.scala-lang.org/files/archive/spec/2.11/05-classes-and-objects.html#class-linearization>
- [2] <http://lampwww.epfl.ch/~amin/dot/fpdt.pdf>
- [3] <https://stackoverflow.com/questions/12935731/any-reason-why-scala-does-not-explicitly-support-dependent-types/12937819#12937819>
- [4] <https://docs.oracle.com/javase/7/docs/api/java/lang/ArrayStoreException.html>