Calculation of methane production from manometric measurements

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Description

This document describes calculations for manometric measurment of biogas. Two methods are commonly used and both are described here: one based on normalized $\mathrm{CH_4}$ concentrations (method 1) and one that explicitly includes estimation of $\mathrm{CH_4}$ in the bottle headspace (method 2). Expected results from the two methods are identical; differences are due only to error in measurement of biogas composition or headspace volume. Both methods are available through the cumbg() function in the biogas package [1] and through the web application OBA (https://biotransformers.shinyapps.io/oba1/) and can be easily added to, e.g., a spreadsheet template.

1 Standardization of measured gas volume

Both methods use the same approach for standardization of gas volume. Dry biogas volume in a bottle's headspace before and after venting is calculated by correcting for water vapor, temperature, and pressure. First the volume of headspace gas is converted to dry conditions at standard pressure:

$$V_{dry} = V_{headspace}(P_{meas} - P_{H_2O})/101.325 \,\text{kPa}$$
(1)

where P_{meas} is the measured headspace pressure and P_{H_2O} the water vapor partial pressure (both in kPa). Eq. (1) is an expression of Boyle's law. The value of P_{H_2O} is assumed to be the saturation vapor pressure prior to venting, and can be calculated using, e.g., the Magnus-form equation given below (Eq. 21 in [2]):

$$P_{H_2O} = 0.61094e^{(17.625T/(243.04+T))}$$
 (2)

where T is temperature in °C. Immediately after venting, when water vapor has been lost through venting but water evaporation has not yet led to equilibrium,

it is reasonable to assume that the mixing ratio of water is the same as it was prior to venting. Assuming saturation prior to venting and an insignificant change in temperature, this is equivalent to taking relative humidity as the ratio of post- to pre-venting absolute pressure (always < 1.0). Volume is then further standardized to 273.15 K by application of Charles's law:

$$V_{std} = V_{dry} 273.15 \,\mathrm{K}/T_{meas}$$
 (3)

where V_{std} is the standardized volume of gas within a bottle's headspace at the time of pressure measurement.

Interval biogas production is calculated as:

$$V_{biogas,i} = V_{std,pre,i} - V_{std,post,i-1} \tag{4}$$

where all V is standardized gas volume in a bottle's headspace, pre and post refer to before and after venting, respectively, i indicates the current interval and i-1 the previous one.

2 Calculation of CH₄ production

2.1 Method 1

In the first method, biogas is assumed to consist of only $\mathrm{CH_4}$ and $\mathrm{CO_2}$ at the time of production (i.e., as produced by the microbial community) and $\mathrm{CH_4}$ production is calculated from vented (removed) biogas only. This method is described in [3]. Coupled with the assumption that all gas production is biogas (Eq. 4), this provides the simplest approach for calculating $\mathrm{CH_4}$ production.

First, concentrations of CH_4 and CO_2 are adjusted so they sum to 1.0:

$$x_{CH_4,n} = x_{CH_4}/(x_{CH_4} + x_{CO_2}) (5)$$

where x_{CH_4} and x_{CO_2} are the measured CH_4 and CO_2 concentrations as volume (mole) fraction (possibly including a correction for water vapor—this has no effect here) and $x_{CH_4,n}$ is the normalized CH_4 volume fraction.

Methane production in an interval i is then calculated as

$$V_{CH_4,i} = x_{CH_4,n} V_{biogas,i} \tag{6}$$

Cumulative production is taken as the cumulative sum of interval values.

2.2 Method 2

Method 2 relies on fewer assumptions, but requires the true concentration of CH_4 (volume fraction) of CH_4 within the bottle headspace, with correction only for water vapor. Here, CH_4 production in an interval has two components: a vented part that is naturally interval, and a residual headspace part, that is naturally cumulative:

$$V_{CH_4,i} = V_{CH_4,v,i} + (V_{CH_4,HSR,i} - V_{CH_4,HSR,i-1})$$
(7)

where the subscript v indicates vented volume and HSR= residual headspace volume (post-venting).

Vented CH_4 is calculated from:

$$V_{CH_4,v,i} = x_{CH_4,n,i} V_{biogas,i} \tag{8}$$

Head space CH_4 is calculated from:

$$V_{CH_4,HSR,i} = x_{CH_4,n,i} V_{post,i} \tag{9}$$

Cumulative production is taken as the cumulative sum of interval values.

References

- [1] Hafner, S.D., Koch, K., Carrere, H., Astals, S., Weinrich, S., Rennuit, C. 2018 Software for biogas research: Tools for measurement and prediction of methane production. SoftwareX 7: 205-210
- [2] Alduchov, O.A., Eskridge, R.E. 1996 Improved Magnus form approximation of saturation vapor pressure. Journal of Applied Meteorology 35: 601-609
- [3] Richards, B.K., Cummings, R.J., White, T.E., Jewell, W.J. 1991 Methods for kinetic-analysis of methane fermentation in high solids biomass digesters. Biomass and Bioenergy 1: 65-73