Regras de Derivação - Formulário

2008/2009

Considerando que u e v são funções reais de variável real x e que $a, b, k \in \mathbb{R}$, tem-se

$$(ax+k)'=a$$

casos particulares:
$$(x)' = 1$$

$$(k)' = 0$$
 (k=const.)

$$(u \pm v)' = u' \pm v'$$

$$(u \times v)' = u' \times v + u \times v'$$

$$(k \times u)' = k \times u'$$

$$\left(\frac{u}{v}\right)' = \frac{u' \times v - u \times v'}{v^2}$$

$$(u(v))' = v' \times u'(v)$$

$$\left(\frac{u^{k+1}}{k+1}\right)'=u'u^k\ (k\neq -1)$$

$$(\ln u)' = \frac{u'}{u} \quad (u(x) > 0)$$

$$(\ln u)' = \frac{u'}{u} \quad (u(x) > 0) \qquad (\log_a u)' = \frac{u'}{u} \log_a e \ (a \in \mathbb{R}^+ \setminus \{1\}, u(x) > 0) \qquad (a^u)' = u'a^u \ln a \ (a \in \mathbb{R}^+ \setminus \{1\})$$

$$(a^u)' = u'a^u \ln a \ (a \in \mathbb{R}^+ \setminus \{1\})$$

$$(e^u)' = u' e^u$$

$$(u^{v})' = v u^{(v-1)} u' + v' u^{v} \ln u \ (u(x) > 0)$$

$$(\cos u)' = -u' \mathrm{sen}\, u$$

$$(\operatorname{sen} u)' = u' \cos u$$

$$(\operatorname{tg} u)' = \frac{u'}{\cos^2 u}$$

$$(\cot u)' = \frac{-u'}{\sin^2 u}$$

$$(\sec u)' = \frac{u' \sec u}{\cos^2 u}$$

$$(\sec u)' = \frac{u' \sec u}{\cos^2 u}$$
 $(\csc u)' = \frac{-u' \cos u}{\sec^2 u}$

$$(\arccos u)' = \frac{-u'}{\sqrt{1 - u^2}}$$

$$(\arcsin u)' = \frac{u'}{\sqrt{1 - u^2}}$$
 $(\arctan u)' = \frac{u'}{1 + u^2}$

$$(\arctan u)' = \frac{u'}{1+u^2}$$

$$(\operatorname{arccotg} u)' = \frac{-u'}{1 + u^2}$$

$$(\operatorname{ch} u)' = u' \operatorname{sh} u$$

$$(\operatorname{sh} u)' = u'\operatorname{ch} u$$

$$(\operatorname{th} u)' = \frac{u'}{\operatorname{ch}^2 u}$$

$$(\coth u)' = \frac{-u'}{\sinh^2 u}$$

$$(\coth u)' = \frac{-u'}{\sinh^2 u} \qquad (\operatorname{sech} u)' = \frac{-u' \sin u}{\cosh^2 u}$$

$$(\operatorname{cosech} u)' = \frac{-u'\operatorname{ch} u}{\operatorname{sh}^2 u}$$

$$(\operatorname{argsh} u)' = \frac{u'}{\sqrt{u^2 + 1}}$$
 $(\operatorname{argch} u)' = \frac{u'}{\sqrt{u^2 - 1}}$

$$(\operatorname{argch} u)' = \frac{u'}{\sqrt{u^2 - 1}}$$

$$(\operatorname{argth} u)' = \frac{u'}{1 - u^2}$$

$$(\operatorname{argcoth} u)' = \frac{u'}{1 - u^2}$$

Algumas fórmulas trignométricas

$$\cos{(a\pm b)}=\cos{a}\cos{b}\mp\sin{a}\sin{b}$$

$$\cos^2 a = \frac{1 + \cos(2a)}{2}$$

$$sen (a \pm b) = sen a cos b \pm sen b cos a$$

$$\sin^2 a = \frac{1 - \cos(2a)}{2}$$

$$tg(a \pm b) = \frac{tg a \pm tg b}{1 \mp tg a tg b}$$

$$tg^2 a = \frac{1 - \cos(2a)}{1 + \cos(2a)}$$

$$\cos^2 a + \sin^2 a = 1$$

$$\sec a = \frac{1}{\cos a}$$

$$\sec a = \frac{1}{\cos a} \qquad \qquad \csc a = \frac{1}{\sin a}$$