

# PRML-Assignment 2

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## 1 Problem Statement

In Figure ??,  $ABCD$  is a parallelogram,  $AE \perp DC$  and  $CF \perp AD$ . If  $AB = 16 \text{ cm}$ ,  $AE = 8 \text{ cm}$  and  $CF = 10 \text{ cm}$ , find  $AD$ . Construct the parallelogram.

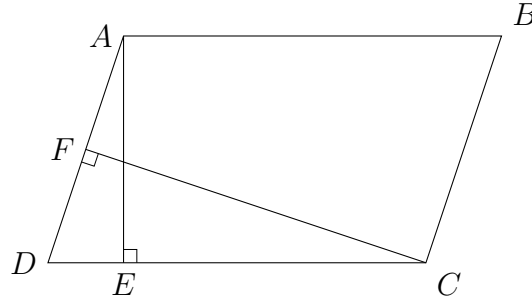


Figure 1: Parallelogram ABCD

## 2 Solution

Given,

LHS	RHS
$A - B$	$C - D$
$(A - E)^T(C - D)$	0
$(C - F)^T(A - D)$	0
$\ A - B\ $	16 cm
$\ A - E\ $	8 cm
$\ C - F\ $	10 cm

To find:  $\|AD\|$

We know that,

$$Ar(ABCD) = \|A - D\| \times \|C - F\| = \|A - E\| \times \|C - D\|$$

$$\|A - D\| \times 10 = 8 \times 16 = 128$$

$$\|A - D\| = 12.8 \text{ cm}$$

$$\|A - D\| = \|A\| = 12.8 \text{ cm}$$

To find:  $A$

Let  $\theta = \angle ADE$

$$\sin \theta = \frac{\|A-E\|}{\|A-D\|}$$

$$\theta = \sin^{-1} \left( \frac{\|A - E\|}{\|A - D\|} \right) \quad (1)$$

$$A = \|A - D\| \begin{pmatrix} \cos \theta \\ \sin \theta \end{pmatrix} \quad (2)$$

Substituting  $\|AE\|$  and  $\|AD\|$  in (??) and (??)

$$A \approx \begin{pmatrix} 10 \\ 8 \end{pmatrix} \quad (3)$$

To find:  $F$

Equation of line passing through AD:

$$\text{Direction vector, } \mathbf{m} = \begin{pmatrix} 10 \\ 8 \end{pmatrix}$$

Normal vector,

$$\Rightarrow \mathbf{n} = \begin{pmatrix} -8 \\ 10 \end{pmatrix}$$

Equation of line passing through D with normal vector n is

$$\mathbf{n}^T(\mathbf{x} - \mathbf{D}) = 0$$

$$\mathbf{n}^T \mathbf{x} = 0 \tag{4}$$

Since  $\mathbf{F}$  is foot of perpendicular from  $\mathbf{C}$  to line  $\mathbf{AD}$

$$\begin{pmatrix} m & n \end{pmatrix}^T \mathbf{F} = \begin{pmatrix} m^T \mathbf{C} \\ 0 \end{pmatrix}$$

$$\mathbf{F} = \begin{pmatrix} 10 & 8 \\ 8 & -10 \end{pmatrix}^{-1} \begin{pmatrix} 160 \\ 0 \end{pmatrix}$$

$$\mathbf{F} = \begin{pmatrix} 9.75 \\ 7.8 \end{pmatrix} \tag{5}$$

### 3 Code

<https://github.com/1ROH1TH/PRML/blob/main/9.9.2.1/codes/9.9.2.1.py>

### 4 Plot

The above code plots Figure ??.

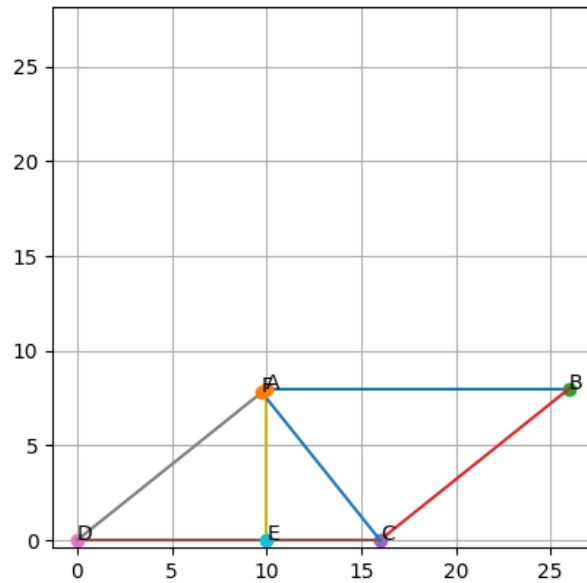


Figure 2: Parallelogram ABCD