# Assignment 1 - Language development in autistic and neurotypical children

Study group 9

2022-08-15

```
pacman::p_load(tidyverse, brms, cmdstanr, ggpubr)
theme_set(theme_minimal())
```

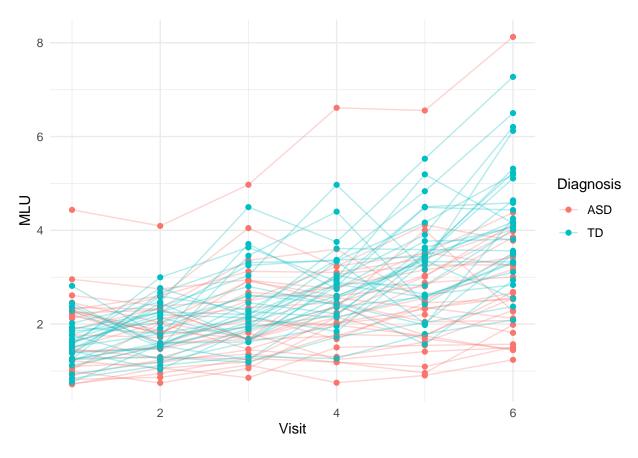
### Part 1

```
# Assign values
n <- 360
visits <- 6
mu_asd \leftarrow log(1.5)
sigma_asd \leftarrow log(1.5) - log(1.5-0.5)
mu_td <- log(1.5)
sigma_td \leftarrow log(1.5) - log(1.5-0.3)
mu_visit_asd <- 0.09</pre>
sigma_visit_asd <- 0.035
mu_visit_td <- 0.18</pre>
sigma_visit_td <- 0.025
x <- c("ASD", "TD")
# Create data frame
df \leftarrow tibble(ID = rep(1:60, each = 6)) \%\%
 mutate(Visit = rep(1:6, times = 60)) %>%
 mutate(Diagnosis = rep(x, each = 180))
# loop intercepts and slopes
for (i in seq(n)) {
 df$IndividualIntercept[df$ID == i & df$Diagnosis == "ASD"] <- rnorm(1, mu_asd, sigma_asd)
  df$IndividualIntercept[df$ID == i & df$Diagnosis == "TD"] <- rnorm(1, mu_td, sigma_td)
 df$IndividualSlope[df$ID == i & df$Diagnosis == "ASD"] <- rnorm(1, mu_visit_asd, sigma_visit_asd)
  df$IndividualSlope[df$ID == i & df$Diagnosis == "TD"] <- rnorm(1, mu_visit_td, sigma_visit_td)</pre>
## Warning: Unknown or uninitialised column: 'IndividualIntercept'.
## Warning: Unknown or uninitialised column: 'IndividualSlope'.
```

```
# Simulate MLU
for (i in seq(n)) {
  df$MLU[i] <- exp(rnorm(1, df$IndividualIntercept[i] + df$IndividualSlope[i] * (df$Visit[i] - 1), sd =
}</pre>
```

## Warning: Unknown or uninitialised column: 'MLU'.

```
# Plot
ggplot(df, aes(Visit, MLU, color = Diagnosis, group = ID)) +
geom_point() +
geom_line(alpha = 0.3)
```



```
# Check MLU
max(df$MLU)
```

## [1] 8.126249

min(df\$MLU)

## [1] 0.7153566

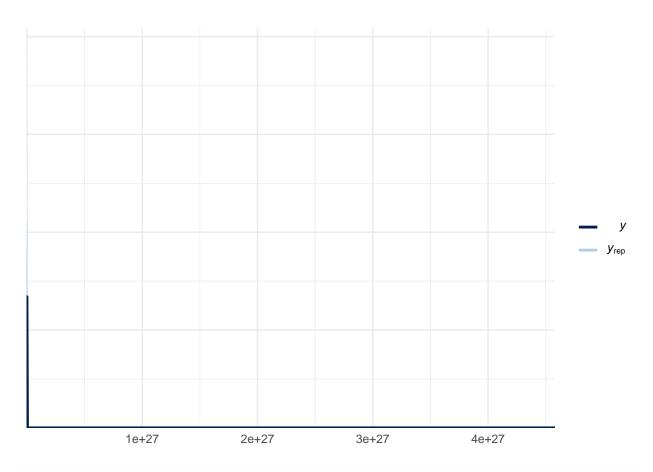
```
mean(df$MLU)
## [1] 2.467813
# Define formulas
mO \leftarrow bf(MLU \sim 1)
m1 <- bf(MLU ~ 0 + Diagnosis)
m2 <- bf(MLU ~ 0 + Diagnosis + Diagnosis:Visit)</pre>
m3 <- bf(MLU ~ 0 + Diagnosis + Diagnosis: Visit + (1 + Visit|ID))
m4 <- bf(MLU ~ 0 + Diagnosis + Diagnosis: Visit + (1 + Visit|gr(ID, by = Diagnosis)))
# Define priors
p1 <- c(
  brms::prior(normal(0, 0.1), class = b),
  brms::prior(normal(0.4, 0.1), class = b, coef = "DiagnosisASD"),
  brms::prior(normal(0.4, 0.1), class = b, coef = "DiagnosisTD"),
  brms::prior(normal(0, 0.25), class = sd, coef = Intercept, group = ID),
  brms::prior(normal(0, 0.25), class = sd, coef = Visit, group = ID)
)
get_prior(m1, data = df)
##
                                        coef group resp dpar nlpar lb ub
                   prior class
##
                   (flat)
                              b
                   (flat)
##
                              b DiagnosisASD
##
                   (flat)
                              b
                                DiagnosisTD
                                                                     0
##
    student_t(3, 0, 2.5) sigma
          source
##
##
         default
##
   (vectorized)
##
   (vectorized)
##
         default
# Fitting models
prior_fit <- brm(</pre>
  m3, data = df, prior = p1, sample_prior = "only", backend = "cmdstanr", chains = 2, cores = 2, contro
## Start sampling
## Running MCMC with 2 parallel chains...
##
## Chain 1 Iteration:
                          1 / 2000 [ 0%]
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```

(Warmup)

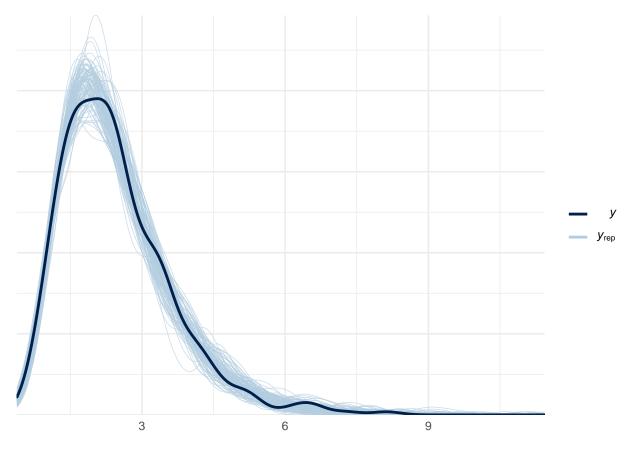
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## Chain 2 Iteration: 1000 / 2000 [ 50%]
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## Chain 2 Iteration: 1001 / 2000 [ 50%]
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## Chain 1 Iteration: 1100 / 2000 [ 55%]
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## Chain 1 Iteration: 1200 / 2000 [ 60%]
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## Chain 2 Iteration: 1100 / 2000 [ 55%]
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## Chain 2 Iteration: 1300 / 2000 [ 65%]
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## Chain 1 Iteration: 2000 / 2000 [100%]
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## Chain 2 Iteration: 2000 / 2000 [100%]
                                           (Sampling)
## Chain 1 finished in 1.5 seconds.
## Chain 2 finished in 1.5 seconds.
## Both chains finished successfully.
## Mean chain execution time: 1.5 seconds.
## Total execution time: 1.7 seconds.
model_fit <- brm(</pre>
  m3, data = df, prior = p1, sample_prior = T, backend = "cmdstanr", chains = 2, cores = 2, control = 1
## Start sampling
## Running MCMC with 2 parallel chains...
##
## Chain 1 Iteration:
                         1 / 2000 [
                                     0%]
                                           (Warmup)
## Chain 2 Iteration:
                         1 / 2000 [
                                      0%]
                                           (Warmup)
## Chain 2 Iteration: 100 / 2000 [
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                                      5%]
```

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100 / 2000 [ 5%]
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## Chain 2 Iteration:
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                       200 / 2000 [ 10%]
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## Chain 1 Iteration:
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## Chain 1 Iteration:
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## Chain 1 Iteration:
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## Chain 1 Iteration:
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                       700 / 2000 [ 35%]
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## Chain 2 Iteration:
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                                           (Warmup)
## Chain 1 Iteration:
## Chain 2 Iteration:
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## Chain 1 Iteration:
                       800 / 2000 [ 40%]
                                           (Warmup)
                       900 / 2000 [ 45%]
## Chain 2 Iteration:
                                           (Warmup)
## Chain 1 Iteration:
                       900 / 2000 [ 45%]
                                           (Warmup)
## Chain 2 Iteration: 1000 / 2000 [ 50%]
                                           (Warmup)
## Chain 2 Iteration: 1001 / 2000 [ 50%]
                                           (Sampling)
## Chain 2 Iteration: 1100 / 2000 [ 55%]
                                           (Sampling)
## Chain 1 Iteration: 1000 / 2000 [ 50%]
                                           (Warmup)
## Chain 1 Iteration: 1001 / 2000 [ 50%]
                                           (Sampling)
## Chain 2 Iteration: 1200 / 2000 [ 60%]
                                           (Sampling)
## Chain 2 Iteration: 1300 / 2000 [ 65%]
                                           (Sampling)
## Chain 1 Iteration: 1100 / 2000 [ 55%]
                                           (Sampling)
## Chain 2 Iteration: 1400 / 2000 [ 70%]
                                           (Sampling)
## Chain 1 Iteration: 1200 / 2000 [ 60%]
                                           (Sampling)
## Chain 2 Iteration: 1500 / 2000 [ 75%]
                                           (Sampling)
## Chain 1 Iteration: 1300 / 2000 [ 65%]
                                           (Sampling)
                                           (Sampling)
## Chain 2 Iteration: 1600 / 2000 [ 80%]
## Chain 1 Iteration: 1400 / 2000 [ 70%]
                                           (Sampling)
## Chain 2 Iteration: 1700 / 2000 [ 85%]
                                           (Sampling)
## Chain 2 Iteration: 1800 / 2000 [ 90%]
                                           (Sampling)
## Chain 1 Iteration: 1500 / 2000 [ 75%]
                                           (Sampling)
## Chain 2 Iteration: 1900 / 2000 [ 95%]
                                           (Sampling)
## Chain 1 Iteration: 1600 / 2000 [ 80%]
                                           (Sampling)
## Chain 2 Iteration: 2000 / 2000 [100%]
                                           (Sampling)
## Chain 2 finished in 19.9 seconds.
## Chain 1 Iteration: 1700 / 2000 [ 85%]
                                           (Sampling)
## Chain 1 Iteration: 1800 / 2000 [ 90%]
                                           (Sampling)
## Chain 1 Iteration: 1900 / 2000 [ 95%]
                                           (Sampling)
## Chain 1 Iteration: 2000 / 2000 [100%]
                                           (Sampling)
## Chain 1 finished in 22.5 seconds.
##
## Both chains finished successfully.
## Mean chain execution time: 21.2 seconds.
## Total execution time: 22.6 seconds.
# Checking priors
pp_check(prior_fit, ndraws = 100)
```



```
# Cheking fit
pp_check(model_fit, ndraws = 100)
```



```
posterior <- as_draws_df(model_fit)

plot1 <- ggplot(posterior) +
    geom_histogram(aes(prior_b_DiagnosisASD), fill = "red", color = "black", alpha = 0.3, bins = 50) +
    geom_histogram(aes(b_DiagnosisASD), fill = "green", color = "black", alpha = 0.3, bins = 50) +
    geom_histogram(aes(b_DiagnosisTD), fill = "yellow", color = "black", alpha = 0.3, bins = 50) +
    xlab("Prior-posterior update check on the intercepts")

plot2 <- ggplot(posterior) +
    geom_histogram(aes(prior_sd_ID__Intercept), fill = "red", color = "black", alpha = 0.3, bins = 50) +
    xlab("Prior-posterior update check on the intercepts")

plot3 <- ggplot(posterior) +
    geom_histogram(aes(sd_ID__Intercept), fill = "red", color = "black", alpha = 0.3, bins = 50) +
    red"    color = "black", alpha = 0.3, bins = 50) +
    red"    color = "black", alpha = 0.3, bins = 50) +
    red"    color = "black", alpha = 0.3, bins = 50) +
    red"    color = "black", alpha = 0.3, bins = 50) +
    red"    color = "black", alpha = 0.3, bins = 50) +
    red"    color = "black", alpha = 0.3, bins = 50) +
    red"    color = "black", alpha = 0.3, bins = 50) +</pre>
```

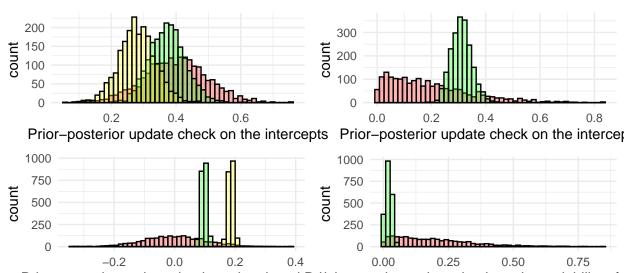
geom\_histogram(aes(sd\_ID\_\_Visit), fill = "green", color = "black", alpha = 0.3, bins = 50) +

```
xlab("Prior-posterior update check on the variability of the slope")

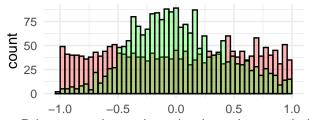
plot5 <- ggplot(posterior) +
   geom_histogram(aes(prior_cor_ID), fill = "red", color = "black", alpha = 0.3, bins = 50) +
   geom_histogram(aes(cor_ID__Intercept__Visit), fill = "green", color = "black", alpha = 0.3, bins = 50
   xlab("Prior-posterior update check on the correlation")

# Wrapping them plots
ggarrange(plot1, plot2, plot3, plot4, plot5, rremove("x.text"), ncol = 2, nrow = 3)</pre>
```

## Warning in as\_grob.default(plot): Cannot convert object of class themegg into a
## grob.



Prior-posterior update check on the slope birties to posterior update check on the variability of



Prior-posterior update check on the correlation

## # Model output summary(model\_fit)

```
## Family: lognormal
## Links: mu = identity; sigma = identity
## Formula: MLU ~ 0 + Diagnosis + Diagnosis:Visit + (1 + Visit | ID)
## Data: df (Number of observations: 360)
## Draws: 2 chains, each with iter = 2000; warmup = 1000; thin = 1;
```

```
##
            total post-warmup draws = 2000
##
## Group-Level Effects:
## ~ID (Number of levels: 60)
                         Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS
## sd(Intercept)
                                       0.04
                                                0.24
                                                          0.39 1.00
                                                                          523
                             0.31
## sd(Visit)
                             0.02
                                       0.01
                                                0.00
                                                          0.04 1.01
                                                                          175
## cor(Intercept, Visit)
                                       0.40
                                               -0.70
                                                          0.85 1.00
                                                                         773
                             0.02
##
                         Tail_ESS
## sd(Intercept)
                             1186
## sd(Visit)
                              456
                              780
## cor(Intercept, Visit)
## Population-Level Effects:
##
                      Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## DiagnosisASD
                           0.37
                                     0.06
                                              0.27
                                                        0.49 1.01
                                                                        542
                                                                                 944
## DiagnosisTD
                           0.28
                                     0.06
                                                        0.39 1.00
                                                                        657
                                                                                 965
                                              0.17
## DiagnosisASD: Visit
                           0.10
                                     0.01
                                               0.08
                                                        0.12 1.00
                                                                       2724
                                                                                1456
## DiagnosisTD:Visit
                           0.19
                                     0.01
                                              0.17
                                                        0.20 1.00
                                                                                1359
                                                                      2676
## Family Specific Parameters:
         Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk ESS Tail ESS
             0.19
                       0.01
                                 0.18
                                          0.21 1.00
                                                          686
                                                                  1373
## sigma
## Draws were sampled using sample(hmc). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
\# n_sim <- 100
#
# # this will help us track time
# t1 <- Sys.time()
# # here's the main event!
# s <-
    tibble(seed = 1:n_sim) %>%
    mutate(d = map(seed, generateFunc, n = 60)) %>%
    mutate(model_fit = map2(d, seed, \neg update(fit, newdata = .x, seed = .y)))
#
# t2 <- Sys.time()
#
# head(s)
#
#
# parameters <-
   s %>%
#
    mutate(treatment = map(model_fit, ~ fixef(.) %>%
#
                              data.frame() %>%
#
                              rownames_to_column("parameter"))) %>%
```

#

unnest(treatment)

# head(parameters)

```
# parameters %>%
   filter(parameter == "DiagnosisASD") %>%
#
#
   ggplot(aes(x = seed, y = Estimate, ymin = Q2.5, ymax = Q97.5)) +
#
#
    geom_hline(yintercept = c(0, .5), color = "white") +
#
   geom_pointrange(fatten = 1/2) +
#
   labs(x = "seed (i.e., simulation index)",
#
         y = expression(beta[1]))
#
# parameters %>%
   qqplot(aes(x = reorder(seed, Q2.5), y = Estimate, ymin = Q2.5, ymax = Q97.5)) +
   geom_hline(yintercept = c(0, .5), color = "white") +
#
#
   geom_pointrange(fatten = 1/2) +
#
  scale_x_discrete("reordered by the lower level of the 95% intervals", breaks = NULL) +
  ylab(expression(beta[1])) +
   coord\_cartesian(ylim = c(-.5, 1.3))
# parameters %>%
   filter(parameter == "DiagnosisASD") %>%
   mutate(check = ifelse(Q2.5 > 0, 1, 0)) \%%
#
   summarise(power = mean(check))
#
#
# s %>%
  mutate(rhat = map(model_fit, rhat)) %>%
#
#
   unnest(rhat) %>%
#
#
  ggplot(aes(x = rhat)) +
#
   geom\_histogram(bins = 20)
#
# parameters <- parameters %>%
   mutate(width = Q97.5 - Q2.5)
# parameters %>%
   ggplot(aes(x = width)) +
   geom\_histogram(binwidth = .01)
# t1 <- Sys.time()
# # here's the main event!
# s2 <-
  tibble(seed = 1:n_sim) %>%
   mutate(d = map(seed, generateFunc, n = 5)) %>%
#
   mutate(model_fit = map2(d, seed, \sim update(fit, newdata = .x, seed = .y)))
# t2 <- Sys.time()
# parameters2 <-</pre>
   s2 %>%
#
   mutate(treatment = map(model_fit, ~ fixef(.) %>%
#
                             data.frame() %>%
#
                             rownames_to_column("parameter"))) %>%
```

```
# unnest(treatment)
#

# parameters2 %>%
# ggplot(aes(x = reorder(seed, Q2.5), y = Estimate, ymin = Q2.5, ymax = Q97.5)) +
# geom_hline(yintercept = c(0, .5), color = "white") +
# geom_pointrange(fatten = 1/2) +
# scale_x_discrete("reordered by the lower level of the 95% intervals", breaks = NULL) +
# ylab(expression(beta[1])) +
# <math>coord_cartesian(ylim = c(-.5, 1.3))
# # parameters2 %>%
# filter(parameter == "DiagnosisASD") %>%
# mutate(check = ifelse(Q2.5 > 0, 1, 0)) %>%
# summarise(power = mean(check))
```

#### Part 2

```
# Load data
real_df <- read_csv("data_clean.csv")</pre>
## Rows: 372 Columns: 22
## -- Column specification ----
## Delimiter: ","
## chr (3): Ethnicity, Diagnosis, Gender
## dbl (19): Child.ID, Visit, Age, ADOS, MullenRaw, ExpressiveLangRaw, Socializ...
## i Use 'spec()' to retrieve the full column specification for this data.
## i Specify the column types or set 'show_col_types = FALSE' to quiet this message.
# Run through analysis pipeline
# Filter CHI MLU
real_df <- real_df %>%
 filter(CHI MLU != 0) %>%
 filter(CHI_MLU != "na")
# Define formula
r_m0 <- bf(CHI_MLU ~ 0 + Diagnosis + Diagnosis:Visit + (1 + Visit|Child.ID))
# Define priors
p2 <- c(
  brms::prior(normal(0, 0.1), class = b),
  brms::prior(normal(0.4, 0.1), class = b, coef = "DiagnosisASD"),
  brms::prior(normal(0.4, 0.1), class = b, coef = "DiagnosisTD"),
  brms::prior(normal(0, 0.25), class = sd, coef = Intercept, group = Child.ID),
  brms::prior(normal(0, 0.25), class = sd, coef = Visit, group = Child.ID)
# Fitting priors
real_prior_fit <- brm(</pre>
```

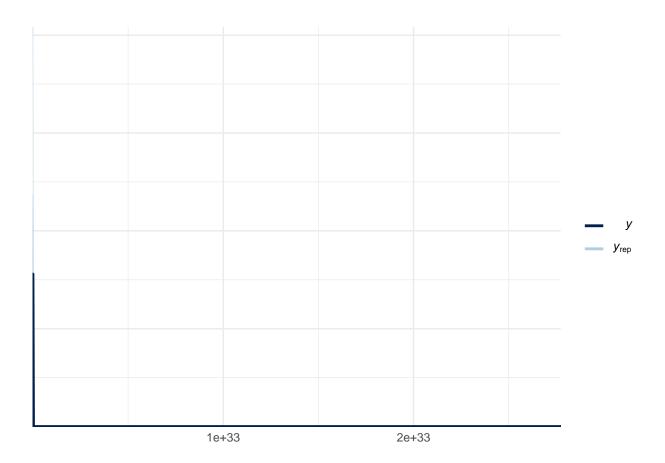
```
r_m0, data = real_df, prior = p2, sample_prior = "only", backend = "cmdstanr", chains = 2, cores = 2,
## Start sampling
## Running MCMC with 2 parallel chains...
## Chain 1 Iteration:
                         1 / 2000 [
                                      0%]
                                           (Warmup)
## Chain 2 Iteration:
                         1 / 2000 Γ
                                      0%7
                                           (Warmup)
## Chain 2 Iteration:
                       100 / 2000 [
                                      5%]
                                           (Warmup)
## Chain 2 Iteration:
                       200 / 2000 [ 10%]
                                           (Warmup)
                       300 / 2000 [ 15%]
## Chain 2 Iteration:
                                           (Warmup)
                       400 / 2000 [ 20%]
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## Chain 2 Iteration:
## Chain 1 Iteration:
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## Chain 2 Iteration:
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## Chain 2 Iteration:
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## Chain 2 Iteration: 1000 / 2000 [ 50%]
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## Chain 2 Iteration: 1001 / 2000 [ 50%]
                                           (Sampling)
                                           (Warmup)
## Chain 1 Iteration: 500 / 2000 [ 25%]
## Chain 1 Iteration:
                       600 / 2000 [ 30%]
                                           (Warmup)
## Chain 1 Iteration:
                       700 / 2000 [ 35%]
                                           (Warmup)
## Chain 2 Iteration: 1100 / 2000 [ 55%]
                                           (Sampling)
                       800 / 2000 [ 40%]
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## Chain 1 Iteration:
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## Chain 1 Iteration: 1001 / 2000 [ 50%]
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## Chain 1 Iteration: 1100 / 2000 [ 55%]
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## Chain 2 Iteration: 1400 / 2000 [ 70%]
## Chain 1 Iteration: 1300 / 2000 [ 65%]
                                           (Sampling)
## Chain 1 Iteration: 1400 / 2000 [ 70%]
                                           (Sampling)
## Chain 2 Iteration: 1500 / 2000 [ 75%]
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                                           (Sampling)
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## Chain 2 Iteration: 1700 / 2000 [ 85%]
## Chain 1 Iteration: 1700 / 2000 [ 85%]
                                           (Sampling)
## Chain 2 Iteration: 1800 / 2000 [ 90%]
                                           (Sampling)
## Chain 1 Iteration: 1800 / 2000 [ 90%]
                                           (Sampling)
                                           (Sampling)
## Chain 2 Iteration: 1900 / 2000 [ 95%]
## Chain 1 Iteration: 1900 / 2000 [ 95%]
                                           (Sampling)
## Chain 1 Iteration: 2000 / 2000 [100%]
                                           (Sampling)
## Chain 2 Iteration: 2000 / 2000 [100%]
                                           (Sampling)
## Chain 1 finished in 1.7 seconds.
## Chain 2 finished in 1.7 seconds.
```

```
##
## Both chains finished successfully.
## Mean chain execution time: 1.7 seconds.
## Total execution time: 1.8 seconds.
# Fitting model
real_model_fit1 <- brm(</pre>
  r_m0, data = real_df, prior = p2, sample_prior = T, backend = "cmdstanr", chains = 2, cores = 2, cont
## Start sampling
## Running MCMC with 2 parallel chains...
## Chain 1 Iteration:
                         1 / 2000 [ 0%]
                                           (Warmup)
## Chain 2 Iteration:
                         1 / 2000 [
                                      0%]
                                           (Warmup)
## Chain 2 Iteration:
                       100 / 2000 [
                                      5%]
                                           (Warmup)
                       100 / 2000 [
## Chain 1 Iteration:
                                      5%]
                                           (Warmup)
## Chain 2 Iteration:
                       200 / 2000 [ 10%]
                                           (Warmup)
## Chain 2 Iteration:
                       300 / 2000 [ 15%]
                                           (Warmup)
## Chain 1 Iteration: 200 / 2000 [ 10%]
                                           (Warmup)
## Chain 2 Iteration: 400 / 2000 [ 20%]
                                           (Warmup)
## Chain 1 Iteration: 300 / 2000 [ 15%]
                                           (Warmup)
## Chain 2 Iteration: 500 / 2000 [ 25%]
                                           (Warmup)
## Chain 1 Iteration: 400 / 2000 [ 20%]
                                           (Warmup)
## Chain 2 Iteration: 600 / 2000 [ 30%]
                                           (Warmup)
## Chain 2 Iteration: 700 / 2000 [ 35%]
                                           (Warmup)
## Chain 1 Iteration: 500 / 2000 [ 25%]
                                           (Warmup)
## Chain 2 Iteration: 800 / 2000 [ 40%]
                                           (Warmup)
## Chain 1 Iteration:
                       600 / 2000 [ 30%]
                                           (Warmup)
                       900 / 2000 [ 45%]
## Chain 2 Iteration:
                                           (Warmup)
                       700 / 2000 [ 35%]
                                           (Warmup)
## Chain 1 Iteration:
## Chain 2 Iteration: 1000 / 2000 [ 50%]
                                           (Warmup)
## Chain 1 Iteration: 800 / 2000 [ 40%]
                                           (Warmup)
## Chain 2 Iteration: 1001 / 2000 [ 50%]
                                           (Sampling)
## Chain 2 Iteration: 1100 / 2000 [ 55%]
                                           (Sampling)
## Chain 1 Iteration: 900 / 2000 [ 45%]
                                           (Warmup)
## Chain 1 Iteration: 1000 / 2000 [ 50%]
                                           (Warmup)
## Chain 2 Iteration: 1200 / 2000 [ 60%]
                                           (Sampling)
## Chain 1 Iteration: 1001 / 2000 [ 50%]
                                           (Sampling)
## Chain 2 Iteration: 1300 / 2000 [ 65%]
                                           (Sampling)
## Chain 1 Iteration: 1100 / 2000 [ 55%]
                                           (Sampling)
## Chain 1 Iteration: 1200 / 2000 [ 60%]
                                            (Sampling)
## Chain 2 Iteration: 1400 / 2000 [ 70%]
                                           (Sampling)
## Chain 1 Iteration: 1300 / 2000 [ 65%]
                                           (Sampling)
## Chain 2 Iteration: 1500 / 2000 [ 75%]
                                           (Sampling)
## Chain 1 Iteration: 1400 / 2000 [ 70%]
                                           (Sampling)
## Chain 2 Iteration: 1600 / 2000 [ 80%]
                                           (Sampling)
## Chain 1 Iteration: 1500 / 2000 [ 75%]
                                           (Sampling)
## Chain 2 Iteration: 1700 / 2000 [ 85%]
                                            (Sampling)
## Chain 1 Iteration: 1600 / 2000 [ 80%]
                                           (Sampling)
## Chain 2 Iteration: 1800 / 2000 [ 90%]
                                           (Sampling)
## Chain 1 Iteration: 1700 / 2000 [ 85%]
                                           (Sampling)
```

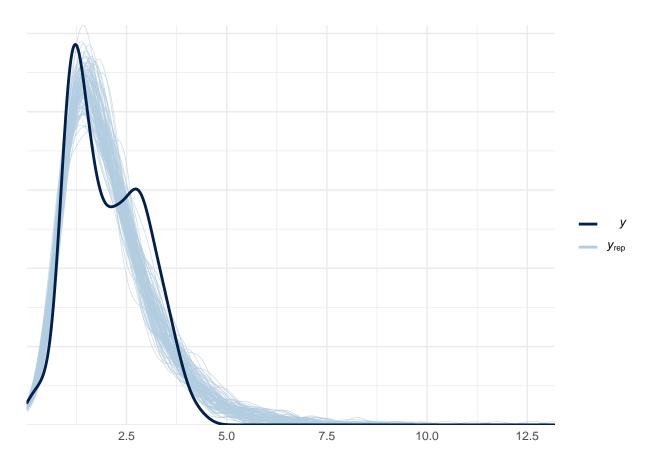
```
## Chain 2 Iteration: 1900 / 2000 [ 95%] (Sampling)
## Chain 1 Iteration: 1800 / 2000 [ 90%] (Sampling)
## Chain 2 Iteration: 2000 / 2000 [100%] (Sampling)
## Chain 2 finished in 11.4 seconds.
## Chain 1 Iteration: 1900 / 2000 [ 95%] (Sampling)
## Chain 1 Iteration: 2000 / 2000 [100%] (Sampling)
## Chain 1 finished in 12.1 seconds.
##
## Both chains finished successfully.
## Mean chain execution time: 11.7 seconds.
## Total execution time: 12.1 seconds.
```

### # Check priors

pp\_check(real\_prior\_fit, ndraws = 100)



```
# Check model
pp_check(real_model_fit1, ndraws = 100)
```



```
real_plot5 <- ggplot(posterior2) +</pre>
  geom_histogram(aes(prior_cor_Child.ID), fill = "red", color = "black", alpha = 0.3, bins = 50) +
  geom_histogram(aes(cor_Child.ID__Intercept__Visit), fill = "green", color = "black", alpha = 0.3, bin
  xlab("Prior-posterior update check on the correlation")
# Wrapping plots
ggarrange(real_plot1, real_plot2, real_plot3, real_plot4, real_plot5, rremove("x.text"), ncol = 2, nrow
## Warning in as_grob.default(plot): Cannot convert object of class themegg into a
## grob.
    150
                                                    200
                                                 conut 200 100
    100
    50
                                                      0
      0
       0.0
                 0.2
                                      0.6
                                                         0.00
                                                                  0.25
                                                                             0.50
                                                                                       0.75
                           0.4
    Prior-posterior update check on the intercepts  Prior-posterior update check on the intercept
                                                    1000
    400
 conut 200
                                                     750
                                                 count
                                                     500
                                                     250
                                                       0
      0
                -0.2
                                                                  0.25
                                                                          0.50
                          0.0
                                    0.2
                                             0.4
                                                         0.00
                                                                                  0.75
                                                                                           1.00
  Prior-posterior update check on the slope by Priisit-posterior update check on the variability of
    250
    200
 150
100
    50
      0
                -0.5
                          0.0
                                  0.5
    Prior-posterior update check on the correlation
# Model output
summary(real_model_fit1)
    Family: lognormal
##
     Links: mu = identity; sigma = identity
## Formula: CHI_MLU ~ 0 + Diagnosis + Diagnosis: Visit + (1 + Visit | Child.ID)
##
      Data: real_df (Number of observations: 349)
##
     Draws: 2 chains, each with iter = 2000; warmup = 1000; thin = 1;
```

total post-warmup draws = 2000

##

##

```
## Group-Level Effects:
## ~Child.ID (Number of levels: 61)
##
                        Estimate Est. Error 1-95% CI u-95% CI Rhat Bulk ESS
## sd(Intercept)
                             0.36
                                       0.05
                                                0.27
                                                          0.46 1.00
                                                                         658
## sd(Visit)
                             0.13
                                       0.01
                                                0.11
                                                          0.16 1.01
                                                                         211
## cor(Intercept, Visit)
                                       0.13
                                               -0.72
                                                         -0.22 1.01
                            -0.51
                                                                         117
                        Tail ESS
## sd(Intercept)
                             1251
## sd(Visit)
                              444
## cor(Intercept, Visit)
                              413
## Population-Level Effects:
                      Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## DiagnosisASD
                                     0.06
                           0.30
                                              0.18
                                                        0.43 1.00
                                                                       856
                                                                                1353
## DiagnosisTD
                           0.26
                                     0.06
                                              0.14
                                                        0.38 1.01
                                                                       908
                                                                                1358
## DiagnosisASD:Visit
                           0.01
                                     0.02
                                             -0.03
                                                        0.06 1.00
                                                                       348
                                                                                 678
                                     0.02
                                                                                 703
## DiagnosisTD: Visit
                           0.15
                                              0.10
                                                        0.19 1.00
                                                                       355
##
## Family Specific Parameters:
         Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk ESS Tail ESS
                                          0.30 1.00
## sigma
             0.27
                       0.01
                                 0.25
                                                          774
                                                                  1269
## Draws were sampled using sample(hmc). For each parameter, Bulk_ESS
## and Tail ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
# Defining formulas
# ind m1 <- bf(CHI MLU ~ 0 + Diagnosis + Diagnosis: Visit + Diagnosis: verbalIQ1 + Diagnosis: nonVerbalIQ1
# env_m2 <- bf(CHI_MLU ~ 0 + Diagnosis + Diagnosis:Visit + Diagnosis:MOT_MLU + Diagnosis:types_MOT + Di
# ind_env_m3 <- bf(CHI_MLU ~ 0 + Diagnosis + Diagnosis:Visit + Diagnosis:verbalIQ1 + Diagnosis:nonVerba
#
#
# # Fitting models
# real_model_fit2 <- brm(</pre>
   ind_m1, data = real_df, prior = p2, sample_prior = T, backend = "cmdstanr", chains = 2, cores = 2,
#
# pp_check(real_model_fit2, ndraws = 100)
#
# real_model_fit3 <- brm(</pre>
    env_m2, data = real_df, prior = p2, sample_prior = T, backend = "cmdstanr", chains = 2, cores = 2,
# pp check(real model fit3, ndraws = 100)
# real_model_fit4 <- brm(</pre>
   ind_env_m3, data = real_df, prior = p2, sample_prior = T, backend = "cmdstanr", chains = 2, cores =
#
# pp_check(real_model_fit4, ndraws = 100)
```

```
# # Add criterions to models
#
# real model fit loo1 <- add criterion(real model fit1, criterion = "loo")
#
# real model fit loo2 <- add criterion(real model fit2, criterion = "loo")
#
# real_model_fit_loo3 <- add_criterion(real_model_fit3, criterion = "loo")
# real_model_fit_loo4 <- add_criterion(real_model_fit4, criterion = "loo")</pre>
# # Compare models on information criterion
#
\#\ loo\_compare(real\_model\_fit\_loo1,\ real\_model\_fit\_loo2,\ real\_model\_fit\_loo3,\ real\_model\_fit\_loo4)
#
\# loo_model_weights(real_model_fit_loo1, real_model_fit_loo2, real_model_fit_loo3, real_model_fit_loo4)
# # Split in k folds
# kfold1 <- kfold(real_model_fit1, folds = "stratified", group = "Child.ID", K = 5, save_fits = TRUE)
#
# kfold2 <- kfold(real_model_fit2, folds = "stratified", group = "Child.ID", K = 5, save_fits = TRUE)
# kfold3 <- kfold(real_model_fit3, folds = "stratified", group = "Child.ID", K = 5, save_fits = TRUE)
#
# kfold4 <- kfold(real_model_fit4, folds = "stratified", group = "Child.ID", K = 5, save_fits = TRUE)
#
#
#
# # Define loss function
# rmse <- function(y,yrep) {</pre>
  yrep_mean <- colMeans(yrep)</pre>
#
    sqrt(mean((yrep_mean-y)^2))
# }
#
# # Predict responses and evaluate the loss
# kfp1 <- kfold_predict(kfold1)</pre>
# rmse1 <- rmse(kfp1$y, kfp1$yrep)</pre>
# kfp2 <- kfold_predict(kfold2)</pre>
# rmse2 <- rmse(kfp2$y, kfp2$yrep)</pre>
# kfp3 <- kfold_predict(kfold3)</pre>
# rmse3 <- rmse(kfp3$y, kfp3$yrep)</pre>
# kfp4 <- kfold_predict(kfold4)</pre>
# rmse4 < - rmse(kfp4$y, kfp4$yrep)
# # Plotting rmse for cross-validation
#
# rmse_plot <- tibble(</pre>
# model = c("fit1", "fit2", "fit3", "fit4"),
    rmse = c(rmse1, rmse2, rmse3, rmse4)
# )
```

#

```
# ggplot(rmse_plot, aes(model, rmse)) +
# geom_point(size = 5)
```