

Name: \_\_\_\_\_

Homework 2 | Math 341 | Cruz Godar

*Due Wednesday of Week 3 at the start of class*

Complete the following problems and submit them as a pdf to Canvas. 8 points are awarded for thoroughly attempting every problem, and I'll select three problems to grade on correctness for 4 points each. Enough work should be shown that there is no question about the mathematical process used to obtain your answers.

## Section 1

1. Suppose every 5 years, an average of 5

## Section 2

In problems 2–7, find the eigenvalues and eigenvectors of  $A$  and the algebraic and geometric multiplicity of the eigenvalues. Then diagonalize  $A$  if possible, using block diagonalization with at most  $2 \times 2$  blocks if necessary.

2.  $A = \begin{bmatrix} -8 & 10 \\ -5 & 7 \end{bmatrix}.$

3.  $A = \begin{bmatrix} -1 & -1 \\ 10 & 5 \end{bmatrix}.$

4.  $A = \begin{bmatrix} -4 & -6 & 12 \\ 9 & 11 & -18 \\ 3 & 3 & -4 \end{bmatrix}.$

5.  $A = \begin{bmatrix} -10 & 4 & -4 \\ -13 & 4 & -10 \\ 1 & 0 & 2 \end{bmatrix}$

6.  $A = \begin{bmatrix} 11 & -6 & -4 & -8 \\ -4 & 1 & -12 & -4 \\ -12 & 6 & 3 & 8 \\ 20 & -10 & 0 & -11 \end{bmatrix}.$

7.  $A = \begin{bmatrix} 10 & 6 & -7 & 12 \\ -4 & -3 & 4 & -12 \\ 7 & 6 & -4 & 12 \\ -1 & 0 & 1 & 3 \end{bmatrix}.$

8. Let  $A = BDB^{-1}$  be a diagonalized  $n \times n$  matrix, so that the columns of  $B$  are eigenvectors of  $A$ . Use this factorization to describe the eigenvectors of  $A^T$  (remember that transposing a product reverses the order of the factors).

9. Give an example of an invertible  $3 \times 3$  matrix that is not diagonalizable, and an example of a diagonalizable  $3 \times 3$  matrix that is not invertible.