

# Written Homework 3

Math 111

Due January 31th at the start of class

**Textbook Exercises:**

**Section 2:** 38, 40

**Section 3:** 2, 4, 6, 10, 12, 14, 16, 18, 19, 20, 24, 26

**Exercise 1:** Let  $q(t) = 2t^2 - 20t + 48$ .

- a) Is  $q(t)$  a quadratic function?
- b) Compute the second difference between the points  $(1, 30)$ ,  $(2, 16)$ , and  $(3, 6)$ .
- c) What is the vertical axis intercept of  $q$ ? What are the horizontal axis intercepts?
- d) What is the vertex of  $q$ ?

**Exercise 2:** The rate of change of a population undergoing *logistic* growth is given by  $R(P) = kP(N - P)$ . Here,  $P$  is the population at a certain time,  $N$  is the maximum possible population (called the *carrying capacity*), and  $k$  is a positive constant. Populations that grow logistically grow quickly when the population is large, but that growth slows down as the population approaches the carrying capacity.

- a) Is  $R(P)$  a quadratic function? Explain.
- b) What are the mathematical and practical domains of  $R$ ?
- c) Find **and interpret** the vertex of  $R$ .