

# Tidy Time Series & Forecasting in R



4. Seasonality and trends

robjhyndman.com/workshop2020

#### **Outline**

- 1 Time series decompositions
- 2 Lab Session 8
- 3 Seasonal adjustment

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#### Time series decomposition

**Trend-Cycle** aperiodic changes in level over time.

Seasonal (almost) periodic changes in level due to seasonal factors (e.g., the quarter of the year, the month, or day of the week).

#### **Additive decomposition**

$$y_t = S_t + T_t + R_t$$

where  $y_t$  = data at period t

 $T_t$  = trend-cycle component at period t

 $S_t$  = seasonal component at period t

 $R_t$  = remainder component at period t

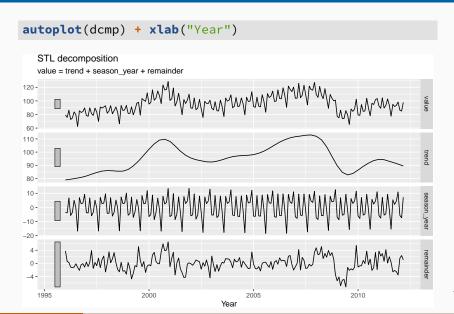
#### **STL** decomposition

- STL: "Seasonal and Trend decomposition using Loess"
- Very versatile and robust.
- Seasonal component allowed to change over time, and rate of change controlled by user.
- Smoothness of trend-cycle also controlled by user.
- Optionally robust to outliers
- Not trading day or calendar adjustments.
- Only additive.
- Take logs to get multiplicative decomposition.
- Use Box-Cox transformations to get other decompositions.

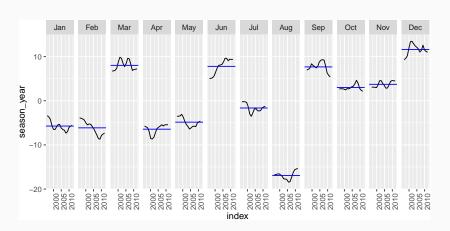
#### **Decomposition dable**

```
dcmp <- elecequip %>% STL(value ~ season(window = 7))
dcmp
```

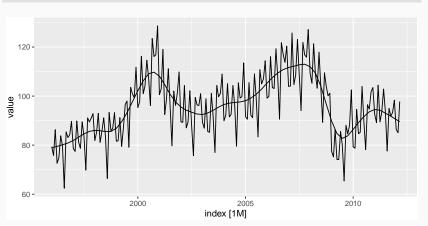
```
## # A dable:
                    195 x 6 [1M]
## # STL Decomposition: value = trend + season_year +
      remainder
## #
       index value trend season_year remainder season_adjust
##
##
       <mth> <dbl> <dbl>
                             <dbl>
                                      <dbl>
                                                  <dbl>
##
   1 1996 Jan 79.4 78.9 -3.37
                                     3.81
                                                   82.7
   2 1996 Feb 75.8 79.1
                           -3.87 0.547
                                                   79.7
##
   3 1996 Mar 86.3 79.3
                          6.73 0.301
                                                   79.6
##
   4 1996 Apr 72.6 79.5
                           -5.74
                                     -1.15
                                                   78.3
##
                                     -1.31
##
   5 1996 May 74.9
                  79.7
                            -3.53
                                                   78.4
   6 1996 Jun 83.8
                  79.9
                           5.03
                                     -1.14
                                                   78.8
##
##
   7 1996 Jul 79.8
                   80.1 -0.222
                                     -0.119
                                                   80.0
                           -16.8
##
   8 1996 Aug 62.4 80.4
                                     -1.21
                                                   79.2
   9 1996 Sep 85.4 80.6
                            6.94
                                                   78.5 6
##
                                     -2.15
## 10 1006 Oct 02 1
                   000
                            2 70
                                     _0 442
                                                   00 1
```



#### dcmp %>% gg\_subseries(season\_year)

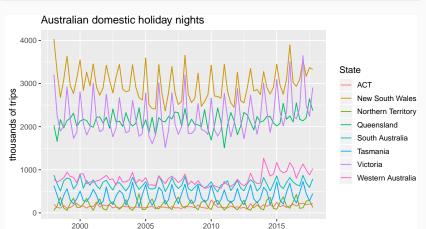


```
autoplot(elecequip, series="Data") +
autolayer(dcmp, trend, series="Trend-cycle")
```



#### **Australian holidays**

```
holidays %>% autoplot(Trips) +
  ylab("thousands of trips") + xlab("Year") +
  ggtitle("Australian domestic holiday nights")
```



Year

```
holidays %>%
   STL(Trips ~ season(window="periodic"), robust=TRUE) %>%
   autoplot()
     STL decomposition
     Trips = trend + season_year + remainder
4000 -
3000 -
2000 -
1000 -
                                                                                            State
  0 -
3000 -
                                                                                                ACT
2000 -
                                                                                                New South Wales
1000 -
                                                                                                Northern Territory
  0 -
                                                                                                Queensland
 500 -
                                                                                                South Australia
 250 -
                                                                                                Tasmania
  0 -
-250 -
                                                                                                Victoria
                                                                                                Western Australia
 500 -
                                                                                      remainder
 250 -
  0 -
-250 -
-500 -
                                                                      2015
               2000
                                 2005
                                                   2010
                                         Quarter
```

```
holidays %>%
   STL(Trips ~ season(window = 5), robust = TRUE) %>%
   autoplot()
     STL decomposition
     Trips = trend + season_year + remainder
4000 -
3000 -
2000 -
1000 -
                                                                                            State
  0 -
3000 -
                                                                                                 ACT
2000 -
                                                                                                 New South Wales
1000 -
                                                                                                 Northern Territory
  0 -
                                                                                                 Queensland
 500 -
                                                                                                 South Australia
 250 -
                                                                                                 Tasmania
  0 -
-250 -
                                                                                                 Victoria
-500 -
                                                                                                 Western Australia
 500 -
                                                                                       remainder
 250 -
  0 -
-250 -
-500 -
                                                                      2015
               2000
                                  2005
                                                    2010
                                         Quarter
```

### **STL** decomposition

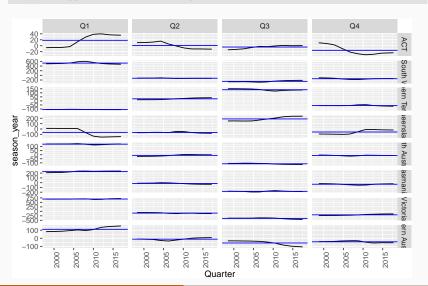
```
holidays %>%
STL(Trips ~ trend(window=15) + season(window=13),
    robust = TRUE)
```

- trend(window = ?) controls wiggliness of trend component.
- season(window = ?) controls variation on seasonal component.
- STL() chooses season(window=13) by default
- A large seasonal window is equivalent to setting window="periodic".
- Odd numbers should be used for symmetry.

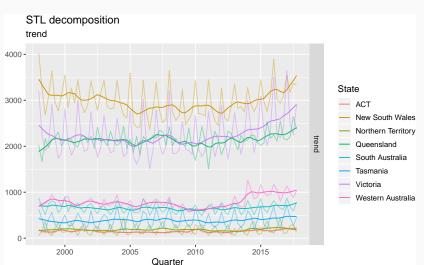
```
dcmp <- holidays %>% STL(Trips)
dcmp
```

```
## # A dable:
                    640 x 7 [10]
                     State [8]
## # Kev:
## # STL Decomposition: Trips = trend + season_year +
      remainder
## #
##
     State
             Quarter Trips trend season_year remainder
##
     <chr>
               <qtr> <dbl> <dbl>
                                    <fdb>>
                                              <dbl>
##
   1 ACT
             1998 01 196.
                           171.
                                    -6.60
                                              32.3
##
   2 ACT
             1998 02 127. 156.
                                    10.3
                                             -39.7
##
   3 ACT
             1998 03 111. 142. -13.9
                                             -17.2
             1998 04 170.
                                      9.76
                                              30.3
##
   4 ACT
                           130.
##
   5 ACT
             1999 01
                     108.
                           135.
                                    -6.35
                                             -20.7
##
   6 ACT
             1999 02
                     125.
                           148.
                                    10.5
                                             -33.9
   7 ACT
             1999 Q3
                     178.
                           166.
                                    -13.2
                                              25.5
##
##
   8 ACT
             1999 04
                     218.
                           177.
                                    8.56
                                              32.0
##
   9 ACT
             2000 01
                     158.
                           169.
                                     -6.09 -4.74
## 10 ACT
             2000 02
                     155.
                           151.
                                     10.7
                                              -7.00
```

dcmp %>% gg\_subseries(season\_year)



```
autoplot(dcmp, trend, scale_bars=FALSE) +
autolayer(holidays, alpha=0.4)
```



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#### **Lab Session 8**

Produce the following decomposition

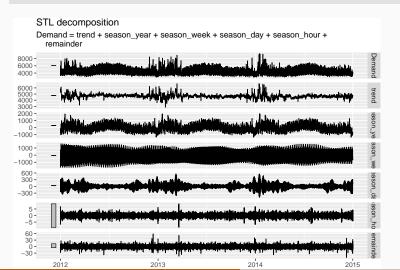
```
expsmooth::cangas %>%
  as_tsibble() %>%

STL(value ~ season(window=7) + trend(window=11)) %>%
  autoplot()
```

- What happens as you change the values of the two window arguments?
- How does the seasonal shape change over time? [Hint: Try plotting the seasonal component using gg\_season.]
- Can you produce a plausible seasonally adjusted series? [Hint: season\_adjust is one of the variables returned by STL.]

#### Multiple seasonality

#### vic\_elec %>% STL(Demand) %>% autoplot()



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# Seasonal adjustment

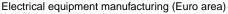
- Useful by-product of decomposition: an easy way to calculate seasonally adjusted data.
- Additive decomposition: seasonally adjusted data given by

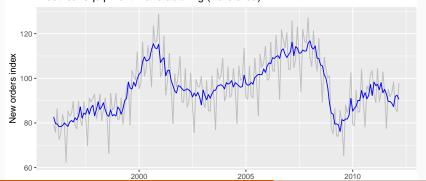
$$y_t - S_t = T_t + R_t$$

 Multiplicative decomposition: seasonally adjusted data given by

$$y_t/S_t = T_t \times R_t$$

```
dcmp <- elecequip %>% STL(value ~ season(window=7))
elecequip %>% autoplot(value, col='gray') +
   autolayer(dcmp, season_adjust, col='blue') +
   xlab("Year") + ylab("New orders index") +
   ggtitle("Electrical equipment manufacturing (Euro area)"
```





## Seasonal adjustment

- We use estimates of S based on past values to seasonally adjust a current value.
- Seasonally adjusted series reflect remainders as well as trend. Therefore they are not "smooth"" and "downturns"" or "upturns" can be misleading.
- It is better to use the trend-cycle component to look for turning points.



#### Treasurer Joe Hockey calls for answers over Australian Bureau of Statistics jobs data

By Michael Vincent and Simon Frazer

Updated 9 Oct 2014, 12:17pm

Federal Treasurer Joe Hockey says he wants answers to the problems the Australian Bureau of Statistics (ABS) has had with unemployment figures.

Mr Hockey, who is in the US to discuss Australia's G20 agenda, said last month's unemployment figures were "extraordinary".

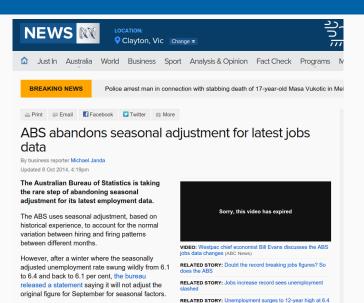
The rate was 6.1 per cent after jumping to a 12-year high of 6.4 per cent the previous month.

The ABS has now taken the rare step of abandoning seasonal adjustment for its latest employment data.



PHOTO: Joe Hockey says he is unhappy with the volatility of ABS unemployment figures. (AAP: Alan Porritt)

RELATED STORY: ABS abandons seasonal adjustment for



MAP: Australia

It will also reset the seasonal adjustment for July and August to one, meaning that these months will

# ABS jobs and unemployment figures - key questions answered by an expert

A professor of statistics at Monash University explains exactly what is seasonal adjustment, why it matters and what went wrong in the July and August figures



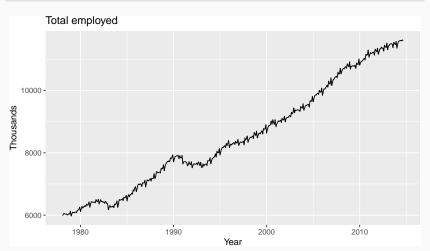
School leavers come on to the jobs market at the same time, causing a seasonal fluctuation. Photograph: Brian Snyder/Reuters

The Australian Bureau of Statistics has retracted its seasonally adjusted employment data for July and August, which recorded huge swings in the jobless rate. The ABS is also planning to review the methods it uses for seasonal adjustment to ensure its figures are as accurate as possible. Rob Hyndman, a professor of statistics at Monash University and member of the bureau's

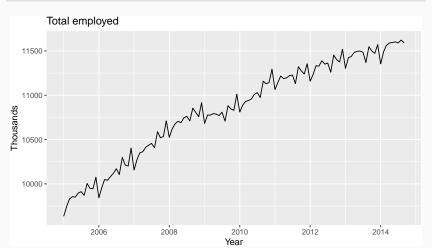
#### employed

```
# A tsibble: 440 x 4 [1M]
##
          Time Month Year Employed
         <mth> <ord> <dbl>
                                <dbl>
##
##
    1 1978 Feb Feb
                       1978
                                5986.
    2 1978 Mar Mar
##
                       1978
                                6041.
                                6054.
##
    3 1978 Apr Apr
                       1978
##
    4 1978 May May
                       1978
                                6038.
    5 1978 Jun Jun
                       1978
                                6031.
##
    6 1978 Jul Jul
##
                       1978
                                6036.
##
    7 1978 Aug Aug
                       1978
                                6005.
##
    8 1978 Sep Sep
                       1978
                                6024.
##
    9 1978 Oct Oct
                       1978
                                6046.
##
   10 1978 Nov Nov
                       1978
                                6034.
   # ... with 430 more rows
```

```
employed %>%
  autoplot(Employed) +
  ggtitle("Total employed") + ylab("Thousands") + xlab("Year")
```



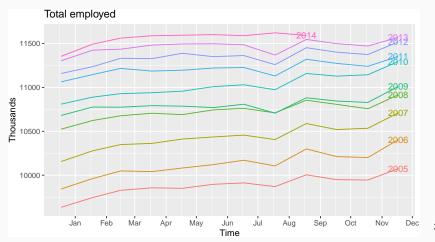
```
employed %>% filter(Year >= 2005) %>%
  autoplot(Employed) +
  ggtitle("Total employed") + ylab("Thousands") + xlab("Year")
```



```
employed %>% filter(Year >= 2005) %>%

gg_season(Employed, label='right') +

ggtitle("Total employed") + ylab("Thousands")
```

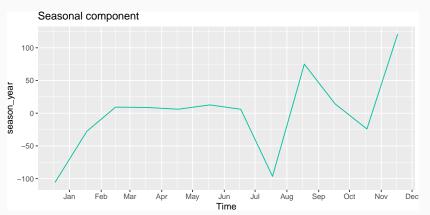


```
employed %>%
  mutate(diff = difference(Employed)) %>%
  filter(Month == "Sep") %>%
  ggplot(aes(y= diff, x = 1)) +
  geom_boxplot() + coord_flip() +
  ggtitle("Sep - Aug: total employed") +
  xlab("") + ylab("Thousands") +
  scale_x_continuous(breaks=NULL, labels=NULL)
```

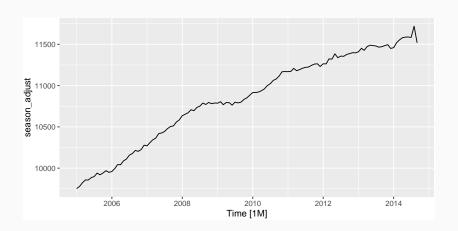


```
dcmp <- employed %>%
   filter(Year >= 2005) %>%
   STL(Employed ~ season(window = 11), robust = TRUE)
autoplot(dcmp)
     STL decomposition
      Employed = trend + season_year + remainder
11500 -
                                                                                             Employed
11000 -
10500 -
10000 -
11500 -
11000 -
                                                                                             trend
10500 -
10000 -
  100 -
  50 -
   0 -
 -50 -
 -100 -
  100 -
                                                                                             remainder
   50 -
   0 -
  -50 -
 -100 -
                                  2008
                  2006
                                                  2010
                                                                 2012
                                                                                 2014
                                               Time
```

```
dcmp %>%
  filter(year(Time) == 2013) %>%
  gg_season(season_year) +
  ggtitle("Seasonal component") +
  guides(colour="none")
```



```
dcmp %>% as_tsibble %>% autoplot(season_adjust)
```



- August 2014 employment numbers higher than expected.
- Supplementary survey usually conducted in August for employed people.
- Most likely, some employed people were claiming to be unemployed in August to avoid supplementary questions.
- Supplementary survey not run in 2014, so no motivation to lie about employment.
- In previous years, seasonal adjustment fixed the problem.
- The ABS has now adopted a new method to avoid the bias.