

Tidy Time Series & Forecasting in R



2. Time series graphics

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Outline

- 1 Seasonal plots
- 2 Lab Session 3
- 3 Seasonal or cyclic?
- 4 Lag plots and autocorrelation
- 5 Lab Session 4
- 6 White noise
- 7 Lab Session 5

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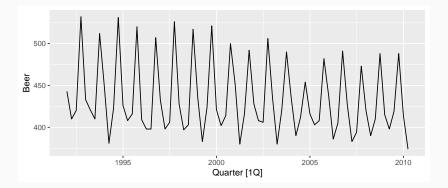
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Seasonal plots

- Data plotted against the individual "seasons" in which the data were observed. (In this case a "season" is a month.)
- Something like a time plot except that the data from each season are overlapped.
- Enables the underlying seasonal pattern to be seen more clearly, and also allows any substantial departures from the seasonal pattern to be easily identified.
- In R: gg_season()

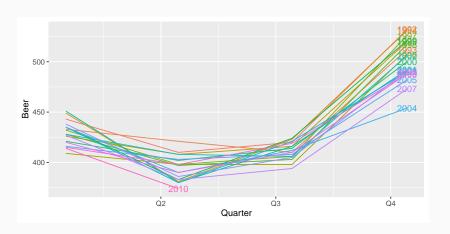
Quarterly Australian Beer Production

```
beer <- aus_production %>%
   select(Quarter, Beer) %>%
   filter(year(Quarter) >= 1992)
beer %>% autoplot(Beer)
```



Quarterly Australian Beer Production

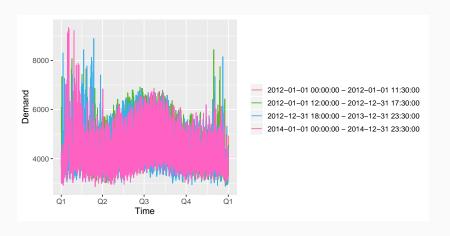
beer %>% gg_season(Beer, labels="right")



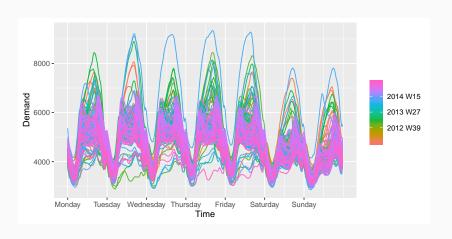
vic_elec

```
# A tsibble: 52,608 x 5 [30m]
##
      Time
                                                           Holiday
                           Demand Temperature Date
##
      <dttm>
                            <dbl>
                                         <dbl> <date>
                                                           <lgl>
##
    1 2012-01-01 00:00:00
                            4263.
                                          21.0 2012-01-01 TRUF
##
    2 2012-01-01 00:30:00
                            4049.
                                          20.7 2012-01-01 TRUE
##
    3 2012-01-01 01:00:00
                            3878.
                                          20.6 2012-01-01 TRUE
    4 2012-01-01 01:30:00
                                          20.4 2012-01-01 TRUE
##
                            4036.
    5 2012-01-01 02:00:00
                            3866.
                                          20.2 2012-01-01 TRUE
##
##
    6 2012-01-01 02:30:00
                            3694.
                                          20.1 2012-01-01 TRUF
                            3562.
                                          19.6 2012-01-01 TRUF
##
    7 2012-01-01 03:00:00
##
    8 2012-01-01 03:30:00
                            3433.
                                          19.1 2012-01-01 TRUE
    9 2012-01-01 04:00:00
                                          19.0 2012-01-01 TRUE
##
                            3359.
   10 2012-01-01 04:30:00
                                          18.8 2012-01-01 TRUE
##
                            3331.
   # ... with 52,598 more rows
```

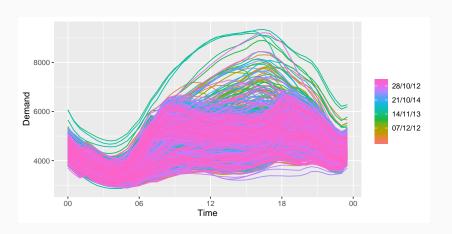
vic_elec %>% gg_season(Demand)



vic_elec %>% gg_season(Demand, period="week")



vic_elec %>% gg_season(Demand, period="day")

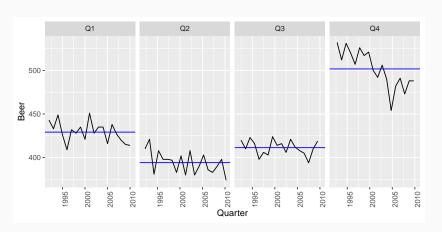


Seasonal subseries plots

- Data for each season collected together in time plot as separate time series.
- Enables the underlying seasonal pattern to be seen clearly, and changes in seasonality over time to be visualized.
- In R: gg_subseries()

Quarterly Australian Beer Production

beer %>% gg_subseries(Beer)



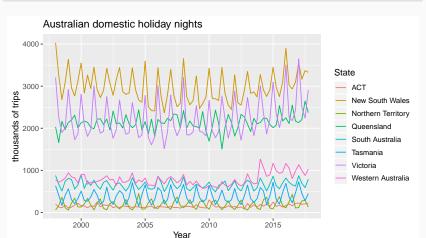
Australian holidays

```
holidays <- tourism %>%
  filter(Purpose=="Holiday") %>%
  group_by(State) %>%
  summarise(Trips = sum(Trips))
```

```
## # A tsibble: 640 x 3 [10]
## # Key: State [8]
## State Quarter Trips
##
     <chr> <qtr> <dbl>
##
   1 ACT 1998 Q1 196.
##
   2 ACT 1998 Q2 127.
##
   3 ACT 1998 Q3 111.
   4 ACT 1998 Q4 170.
##
##
   5 ACT 1999 01 108.
##
   6 ACT 1999 Q2 125.
   7 ACT
          1999 Q3 178.
##
##
  8 ACT
          1999 04 218.
##
   9 ACT
           2000 01 158.
## 10 ACT
           2000 02 155.
```

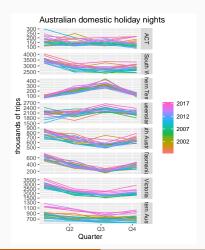
Australian holidays

```
holidays %>% autoplot(Trips) +
ylab("thousands of trips") + xlab("Year") +
ggtitle("Australian domestic holiday nights")
```



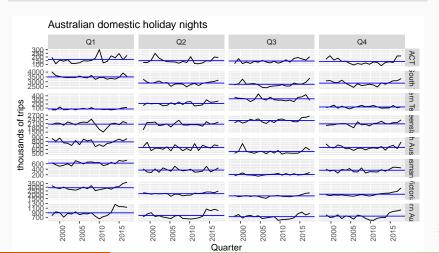
Seasonal plots

```
holidays %>% gg_season(Trips) +
  ylab("thousands of trips") +
  ggtitle("Australian domestic holiday nights")
```



Seasonal subseries plots

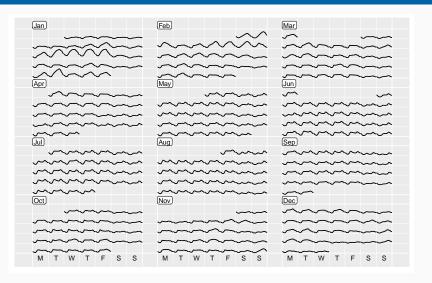
```
holidays %>%
   gg_subseries(Trips) + ylab("thousands of trips") +
   ggtitle("Australian domestic holiday nights")
```



Calendar plots

```
library(sugrrants)
vic elec %>%
  filter(year(Date) == 2014) %>%
  mutate(Hour = hour(Time)) %>%
  frame_calendar(x = Hour, y = Demand, date = Date,
    nrow = 4) \%>\%
  ggplot(aes(x = .Hour, y = .Demand, group = Date)) +
  geom_line() -> p1
prettify(p1, size = 3,
 label.padding = unit(0.15, "lines"))
```

Calendar plots



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Lab Session 3

Look at the quarterly tourism data for the Snowy Mountains

```
snowy <- filter(tourism, Region == "Snowy</pre>
```

- Use autoplot(), gg_season() and gg_subseries() to explore the data.
- What do you learn?
- Produce a calendar plot for the pedestrian data from one location and one year.

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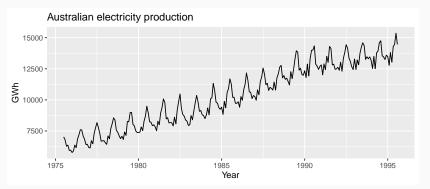
- **Trend** pattern exists when there is a long-term increase or decrease in the data.
- Seasonal pattern exists when a series is influenced by seasonal factors (e.g., the quarter of the year, the month, or day of the week).
 - Cyclic pattern exists when data exhibit rises and falls that are not of fixed period (duration usually of at least 2 years).

Time series components

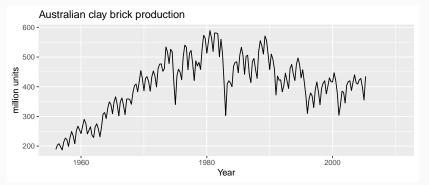
Differences between seasonal and cyclic patterns:

- seasonal pattern constant length; cyclic pattern variable length
- average length of cycle longer than length of seasonal pattern
- magnitude of cycle more variable than magnitude of seasonal pattern

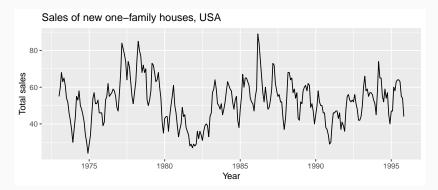
```
as_tsibble(fma::elec) %>%
filter(index >= 1980) %>%
autoplot(value) + xlab("Year") + ylab("GWh") +
ggtitle("Australian electricity production")
```



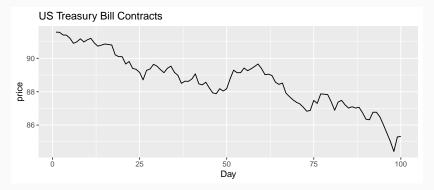
```
aus_production %>%
  autoplot(Bricks) +
  ggtitle("Australian clay brick production") +
  xlab("Year") + ylab("million units")
```



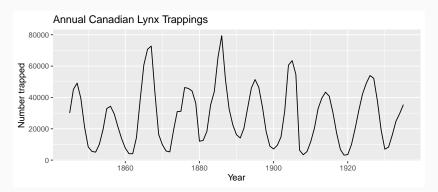
```
as_tsibble(fma::hsales) %>%
autoplot(value) +
ggtitle("Sales of new one-family houses, USA") +
xlab("Year") + ylab("Total sales")
```



```
as_tsibble(fma::ustreas) %>%
autoplot(value) +
ggtitle("US Treasury Bill Contracts") +
xlab("Day") + ylab("price")
```



```
pelt %>%
  autoplot(Lynx) +
  ggtitle("Annual Canadian Lynx Trappings") +
  xlab("Year") + ylab("Number trapped")
```



Seasonal or cyclic?

Differences between seasonal and cyclic patterns:

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Seasonal or cyclic?

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The timing of peaks and troughs is predictable with seasonal data, but unpredictable in the long term with cyclic data.

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Example: Beer production

```
new_production <- aus_production %>%
  filter(year(Quarter) >= 1992)
new_production
```

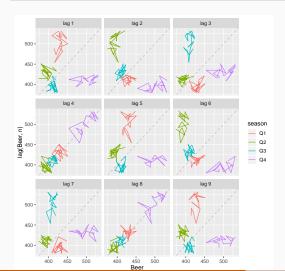
```
# A tsibble: 74 x 7 [10]
##
##
      Quarter
                Beer Tobacco Bricks Cement Electricity
                                                              Gas
        <qtr>
              <dbl>
                        <dbl>
                                <dbl>
                                        <fdb>>
                                                     <fdb> <fdb>
##
##
    1 1992 01
                         5777
                                  383
                                         1289
                                                     38332
                                                              117
                 443
##
    2 1992 02
                 410
                         5853
                                  404
                                         1501
                                                     39774
                                                              151
##
    3 1992 Q3
                 420
                         6416
                                  446
                                         1539
                                                     42246
                                                              175
```

4 1992 04 ## 5 1993 01 6 1993 02 ## ## Q3

1993 04 127 ## 1994 01

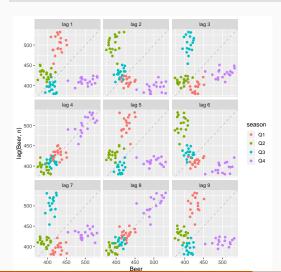
Example: Beer production

new_production %>% gg_lag(Beer)



Example: Beer production

new_production %>% gg_lag(Beer, geom='point')



Lagged scatterplots

- Each graph shows y_t plotted against y_{t-k} for different values of k.
- The autocorrelations are the correlations associated with these scatterplots.
- ACF (autocorrelation function):
 - $ightharpoonup r_1 = Correlation(y_t, y_{t-1})$
 - $ightharpoonup r_2 = Correlation(y_t, y_{t-2})$
 - $ightharpoonup r_3 = Correlation(y_t, y_{t-3})$
 - etc.
- If there is seasonality, the ACF at the seasonal lag (e.g., 12 for monthly data) will be large and positive.

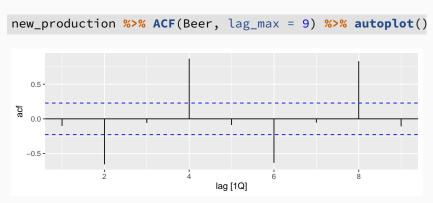
Autocorrelation

Results for first 9 lags for beer data:

```
new_production %>% ACF(Beer, lag_max = 9)
## # A tsibble: 9 x 2 [10]
     lag acf
##
## <lag> <dbl>
## 1 1Q -0.102
## 2 2Q -0.657
## 3 3Q -0.0603
## 4
       40 0.869
## 5
       50 -0.0892
## 6
       60 -0.635
## 7
       70 -0.0542
## 8
       80 0.832
```

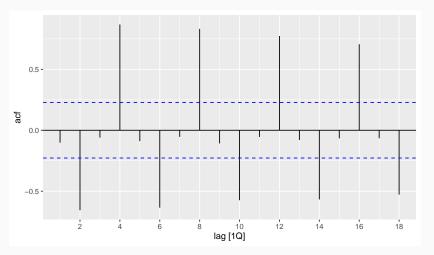
Autocorrelation

Results for first 9 lags for beer data:



ACF

new_production %>% ACF(Beer) %>% autoplot()



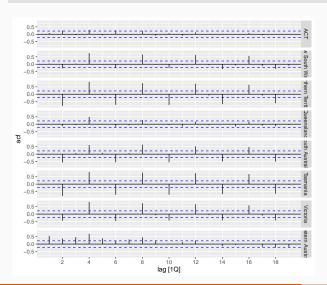
Australian holidays

holidays %>% ACF(Trips)

```
# A tsibble: 152 x 3 [10]
## # Key: State [8]
##
  State lag acf
## <chr> <lag> <dbl>
##
  1 ACT 10 0.0877
##
   2 ACT 2Q 0.252
##
   3 ACT
           30 -0.0496
##
   4 ACT
           40 0.300
##
   5 ACT 50 -0.0741
##
   6 ACT 60 0.269
   7 ACT 70 -0.00504
##
##
   8 ACT 80 0.236
##
   9 ACT 90 -0.0953
## 10 ACT 100 0.0750
## # ... with 142 more rows
```

Australian holidays

holidays %>% ACF(Trips) %>% autoplot()

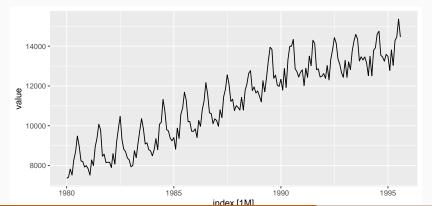


Trend and seasonality in ACF plots

- When data have a trend, the autocorrelations for small lags tend to be large and positive.
- When data are seasonal, the autocorrelations will be larger at the seasonal lags (i.e., at multiples of the seasonal frequency)
- When data are trended and seasonal, you see a combination of these effects.

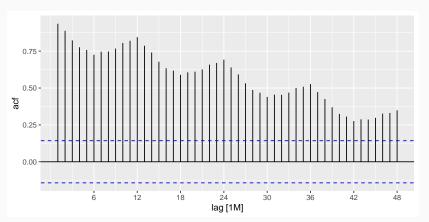
Aus monthly electricity production

```
elec2 <- as_tsibble(fma::elec) %>%
  filter(year(index) >= 1980)
elec2 %>% autoplot(value)
```



Aus monthly electricity production

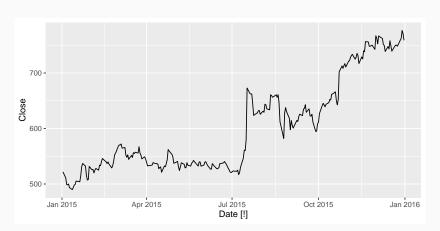
```
elec2 %>% ACF(value, lag_max=48) %>%
autoplot()
```



```
google_2015 <- gafa_stock %>%
  filter(Symbol == "G00G", year(Date) == 2015) %>%
  select(Date, Close)
google_2015
```

```
## # A tsibble: 252 x 2 [!]
##
     Date
            Close
##
     <date> <dbl>
##
   1 2015-01-02 522.
##
   2 2015-01-05 511.
##
   3 2015-01-06
                 499.
##
   4 2015-01-07 498.
##
   5 2015-01-08
                 500.
##
   6 2015-01-09
                 493.
```

google_2015 %>% autoplot(Close)



```
google_2015 %>%
   ACF(Close, lag_max=100)
# Error: Can't handle tsibble of irregular interval.
```

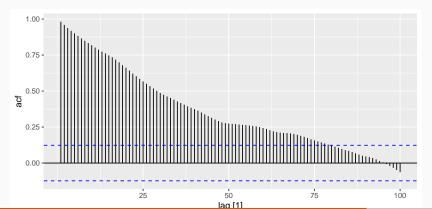
```
google_2015 %>%
 ACF(Close, lag_max=100)
# Error: Can't handle tsibble of irregular interval.
google_2015
## # A tsibble: 252 x 2 [!]
     Date Close
##
     <date> <dbl>
##
## 1 2015-01-02 522.
##
   2 2015-01-05 511.
##
   3 2015-01-06 499.
```

```
google_2015 <- google_2015 %>%
  mutate(trading_day = row_number()) %>%
  update_tsibble(index=trading_day, regular=TRUE)
google_2015
```

```
## # A tsibble: 252 x 3 [1]
##
     Date
            Close trading_day
##
     <date> <dbl>
                            <int>
##
   1 2015-01-02 522.
##
   2 2015-01-05 511.
                                3
##
   3 2015-01-06
                 499.
##
   4 2015-01-07
                 498.
                                4
                 500.
                                5
##
   5 2015-01-08
##
   6 2015-01-09
                 493.
                                6
```

```
google_2015 %>%

ACF(Close, lag_max=100) %>%
autoplot()
```



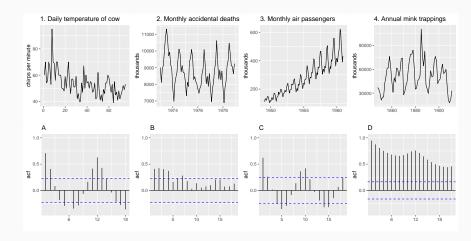
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Lab Session 4

We have introduced the following functions: gg_lag and ACF. Use these functions to explore the four time series: Beer from aus_production, Lynx from pelt, Close from gafa_stock, Demand from vic_elec. Can you spot any seasonality, cyclicity and trend? What do you learn about the series?

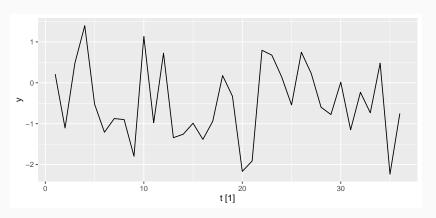
Which is which?



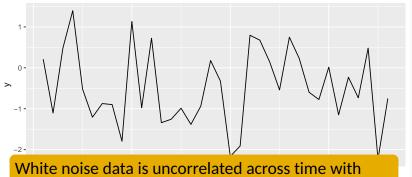
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```
wn <- tsibble(t=seq(36), y=rnorm(36), index=t)
wn %>% autoplot(y)
```



```
wn <- tsibble(t=seq(36), y=rnorm(36), index=t)
wn %>% autoplot(y)
```

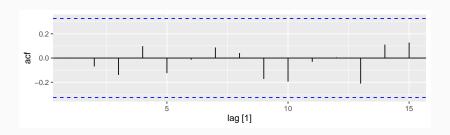


White noise data is uncorrelated across time with zero mean and constant variance.

(Technically, we require independence as well.)

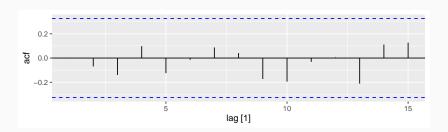
wn **%>% ACF**(y)

r ₁	r ₂	r ₃	r ₄	r ₅	r ₆	r ₇	r ₈	r ₉	r ₁₀
-0.001	-0.070	-0.140	0.098	-0.125	-0.014	0.087	0.041	-0.173	-0.195

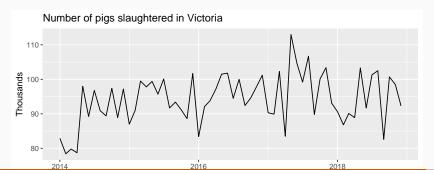


wn **%>% ACF**(y)

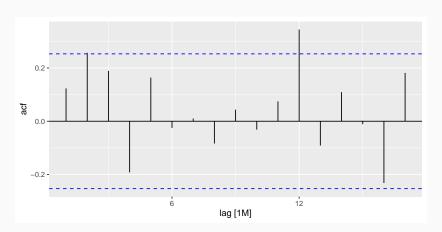
r ₁	r ₂	r ₃	r ₄	r ₅	r ₆	r ₇	r ₈	r ₉	r ₁₀
-0.001	-0.070	-0.140	0.098	-0.125	-0.014	0.087	0.041	-0.173	-0.195



- Sample autocorrelations for white noise series.
- Expect each autocorrelation to be close to zero.
- Blue lines show 95% critical values.



pigs %>% ACF(Count) %>% autoplot()



Monthly total number of pigs slaughtered in the state of Victoria, Australia, from January 2014 through December 2018 (Source: Australian Bureau of Statistics.)

Monthly total number of pigs slaughtered in the state of Victoria, Australia, from January 2014 through December 2018 (Source: Australian Bureau of Statistics.)

- Difficult to detect pattern in time plot.
- ACF shows significant autocorrelation for lag 2 and 12.
- Indicate some slight seasonality.

Monthly total number of pigs slaughtered in the state of Victoria, Australia, from January 2014 through December 2018 (Source: Australian Bureau of Statistics.)

- Difficult to detect pattern in time plot.
- ACF shows significant autocorrelation for lag 2 and 12.
- Indicate some slight seasonality.

These show the series is **not a white noise series**.

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Lab Session 5

You can compute the daily changes in the Google stock price in 2018 using

```
dgoog <- gafa_stock %>%
  filter(Symbol == "GOOG", year(Date) >= 2018) %>%
  mutate(trading_day = row_number()) %>%
  update_tsibble(index=trading_day, regular=TRUE) %>%
  mutate(diff = difference(Close))
```

Does diff look like white noise?