

Lab 4: Asymmetric (Public) Key

Objective: The key objective of this lab is to provide a practical introduction to public key encryption, and with a focus on RSA and Elliptic Curve methods. This includes the creation of key pairs and in the signing process.

 **Web link (Weekly activities):** <https://asecuritysite.com/esecurity/unit04>

Demo: <https://youtu.be/3n2TMpHqE18>

A RSA Encryption

A.1 We will follow a basic RSA process. If you are struggling here, have a look at the following page:

<https://asecuritysite.com/encryption/rsa>

First, pick two prime numbers:

p=
q=

Now calculate $N (p.q)$ and $\text{PHI } [(p-1).(q-1)]$:

N=
PHI =

Now pick a value of e which does not share a factor with PHI [$\text{gcd}(\text{PHI}, e) = 1$]:

e =

Now select a value of d , so that $(e.d) \pmod{\text{PHI}} = 1$:

d =

Now for a message of $M=5$, calculate the cipher as:

$C = M^e \pmod{N} =$

Now decrypt your ciphertext with:

$M = C^d \pmod{N} =$

Did you get the value of your message back ($M=5$)? If not, you have made a mistake, so go back and check.

A.2 The following defines a public key that is used with PGP email encryption:

-----BEGIN PGP PUBLIC KEY BLOCK-----
Version: GnuPG v2

```
mQENBFTzi1ABCADIEWch0yqRQmU4AyQAMj2Pn68Sqo9lTPdPcItwo9LbTdv1YCFz
w3qLlp2RORMP+Kpdi92CIhdUYHDMZFHZ3IWTBgo9+y/Np9UJ6tNGocrsq4xwz15
4vx4jJRddC7QySSh9UxDpRwf9sgqEv1pah136r95ZuyjC1EXnoNxdLJtx8PliCxc
hV/v4+KfoyzYh+HDJ4xP2bt1S07dkasYz6CA7BHYi9k4xgEwxvVytNjSPjTsQY5R
cTayXveGafuxmhSauZKiB/2TFerjEt49Y+p07tPTLX7bhMBVbUvojtT/JeUKV6vK
R82dmOd8seUvhwOHYB0JL+3S7PgFFsLo1NV5ABEBAAAG0LkJpbGwgQnVjaGFuYW4g
KE5vbmUpIDx3LmJlY2hhbmFuQG5hcGllci5hYy51az6JATKEEWECACMFA1Tzi1AC
GwMHCwkIBwMCAQYVCAIJCgSEFgIDAQIEAQIXgAAKCRDSAFZRGtdPQi13B/9KHeFb
11AxqbafFGRDEvx8UfPnEww4FFqwhcr8RLWYE8/Co1UpB/5AS2yvoymbNFMGzURb
LGf/u1LVH0a+NHQu57u8Sv+g3bBthEPH4bKaEzBYRS/dYHOx3APFYIayfm78JVRf
zdeTOOf6PaXUTRx7iscCTKn8DUD3lg/465ZX5aH3HWFFX500JSPSt0/udqjoQuAr
WA5JqB//g2GfzZe1UzH5Dz3PBbJky8GiIfLm00XSEIgaMpcv/9NjzAgjow56n3Mu
sjVkiBc+1ljw+rOo97CfJmPpmTc0vehvQv+KG0LZnp1biwVmm3vT7E6kry4gEbDu
enHPDqhsvcqTDqaduQENBFTzi1ABCACzpjgZLK/sge2rMLURUQQ6102UrS/Gi1Gc
ofq3WpNdT5hEjarwMMWn65Pb0Dj0i7vnorhL+fdb/J8b8QTiyp7i03dZvHdAhcQ5
8afvCjQtQstY8+K6kZFzQOBgyOS5rHAKHNspFq45MlnPo5aaDvP7s9mdMILITv1b
CFhcLoC60qy+JoahupJqHBqGc48/5NU4qbt6fB1AQ/H4M+6og4OozohgkQb80Hox
YbJV4sv4vYMuLd+FK0g2RdGenMM/awdqYo90qb/W2aHCCyXmhGHEEUok9jbc8cr/
xrWL0gDwlwpad8RfQwyVU/VZ3Eg3OseL4SedEmwOO
cr15XDis6dpABEBAAGJAR8E
GAECAAKFA1Tzi1ACGwwACgkQ7ABWURrXT0KZTgf9Fupkh3wv7ac5M2wwdEjt0rDx
nj9kxH99hhuTX2EHXunLH+SwLGHBq5O2sq3jfP+owEhs8/Ez0j1/fSKIqAd1z3mB
dbqWPjzPTY/m0It+ww3epOM75uwjD35PF0RkxxZmEf6SrjZD1sk0B9bRy2v9iWN9
9ZkuvCFH4vT++PognQLTUqNx0FGpD1agrG01XSctJWQXCXPfwdtbIdThBgZ4f1Z
ssAIBCaB1QkzfbPvrMzdTIP+AXg6++K9Sn09N/FRPYzjUSEmpRp+ox31wymvczcu
RmyUquF+/zNnSBVgtY1rzwai05XfuxG0WHVHPTtRyJ5pF4HSqiuvk6Z/4z3bw==
=ZrP+
```

-----END PGP PUBLIC KEY BLOCK-----

Using the following Web page, determine the owner of the key, and the ID on the key:

<https://asecuritysite.com/encryption/pgp1>

A.3 Bob has a private RSA key of:

```
MIICXAIBAAKBgQCwgjkeoyCXm9v6VBnUi5ihQ2knkdxGDL3GXLIUU43/froeqk7q9mtxT4AnPA
adx3f2r4STZYyiQXGSHCUBZCI90dvzf6YiEM5OY2jgsmqBjf2Xkp/8HgN/XDw/wD2+zebYGLLY
td2u3Gxx9edqJ8kQcU9LaMH+fiCFQyfq9UwtjQIDAQABAoGAD7L1a6Ess+9b6G70gTANWkKJps
hVZDGB63mxKRepaJEX8sRJEqLqOYDNsC+pkK08IsfHreh4vrp9bsZuECrB10HSjwDB0S/fm3KE
wbsaaXDUAu0dQg/JBMXAKzeATreoIYJItYgwzrJ++fuquKabAZumvOnWjyBis2z103kdZ2ECQQ
Dnn3JpHirmgVdf81yBbAJaBXNIPz0CcTh1zwFAs4EvRE35n2HvUQuRhy3ahUKXsKX/bGvwzmC
206kBLTFEygVakeAwxxZnPkAAY2vuouCN5NbLZgegrAtmU+U2woa5A0fx6uXmShqxo1iDxEC71
FbNiGHBg5srsuyDj30s1oLmDVjmQJAiy7qLyOA+sCc6BtMavBgLx+bxCwFmsoZHOSX3179smTR
AJ/HY64RREisLIQ1q/yw7IWBzxQ5WTHgl1NZFjKBvQJBAL3t/vCJwRz0Ebs5FaB/8UwhhsrbtX
1GdnkojIGsmV0vHSf6poHqUiay/DV88pvhN11ZG8zHpeUhnAQccJ9ekzkCQDHHG9LYCQqTgsyY
ms//cw4sv2nuOE1UezTjUFeq01sgo+WN96b/M5gnv45/Z3xZxzJ4HOCJ/NRwxNOTeUkw+zY=
```

And receives a ciphertext message of:

```
Pob7AQZZsm1618nMwTpx3V74N45x/rTimUqet10yHq8F0dsekZgOT385J1s1HUzWCx6ZRFPFMJ
1RNYR2Yh7AkQtFLVx91YDfb/Q+SkinBIBX59ER3/fDhrVKxIN4S6h2QmMSRblh4KdVhyY6COxu
+g48Jh7TkQ2Ig93/nCpAnyQ=
```

Using the following code:

```

from Crypto.PublicKey import RSA
from Crypto.Util import asn1
from base64 import b64decode

msg="Pob7AQZZSm1618nMwTpx3v74N45x/rTimUqETl0yHq8F0dsekZgOT385J1s1HUzWCx6ZR
FPFMJ1RNYR2Yh7AkQtFLVx91YDfb/Q+SkinBIBX59ER3/fDhrVKxIN4S6h2QmMSRb1h4KdVhyY
6c0xu+g48Jh7TkQ2Ig93/nCpAnYQ="
privatekey =
'MIICXAIBAABgQCWgjkeoyCXm9v6VBnUi5ihQ2knkdxGDL3GXLIUU43/froeqk7q9mtxT4AnP
AaDX3f2r4STZYYiqXGSHCUBZCI90dvZf6YiEM5OY2jgsmqBjf2Xkp/8HgN/XDw/wD2+zebYGLL
Ytd2u3GXx9edqJ8kQCU9LaMH+ficFQyfq9UwTjQIDAQABAoGAD7L1a6Ess+9b6G70gTANwKJp
shVZDgb63mxKRepaJEX8sRJEqLqOYDNsC+pkK08IsfHreh4vrp9bsZuECrB1OHSjwDB0S/fm3K
EwbsaaXDUAU0dQg/JBMXAKzeATreoIYJItYgwzrJ++fuquKabAZumvOnWjyBIs2z103kDz2ECQ
QDnn3JpHirmgVdf81yBbAJaXBXNIPzOCcthlzWfAs4Evre35n2HvUQuRhy3ahUKXsKX/bGvwzm
C206kbLTfEygVAKEAwXXznPkaAY2vuoUCN5NblZgegrAtmU+U2woa5A0fx6uXmShqxo1iDxEC7
1FbNIgHBg5srsuYdj3os1oLmDVjmQJAiy7qLyOA+sCc6BtmavBgLx+bxCwFmsoZHOSX3179smT
RAJ/HY64RREISLIQ1q/yw7IWBzxQ5WTHg1iNZFjKBvQJBAL3t/vCJwRz0Ebs5FaB/8Uwhhsrbt
XlGdnkOjIGsmV0vHSf6poHqUiay/DV88pvhN11ZG8zHpeUhnaQccJ9ekzkCQDHHG9LYCOqTgsy
Yms//cw4sv2nu0E1UezTjUFeq01sgO+WN96b/M5gnv45/Z3xZxzJ4HOCJ/NRwxN0tEukw+zY='

keyDER = b64decode(privatekey)
keys = RSA.importKey(keyDER)

dmsg = keys.decrypt(b64decode(msg))
print dmsg

```

What is the plaintext message that Bob has been sent?

B OpenSSL (RSA)

We will use OpenSSL to perform the following:

No	Description	Result
B.1	<p>First we need to generate a key pair with:</p> <pre>openssl genrsa -out private.pem 1024</pre> <p>This file contains both the public and the private key.</p>	<p>What is the type of public key method used:</p> <p>How long is the default key:</p> <p>How long did it take to generate a 1,024 bit key?</p> <p>Use the following command to view the keys:</p> <pre>type private.pem (or cat private.pem in Linux)</pre>
B.2	Use following command to view the output file:	What can be observed at the start and end of the file:

	<code>cat private.pem</code>	
B.3	<p>Next we view the RSA key pair:</p> <pre>openssl rsa -in private.pem -text</pre>	<p>Which are the attributes of the key shown:</p> <p>Which number format is used to display the information on the attributes:</p>
B.4	<p>Let's now secure the encrypted key with 3-DES:</p> <pre>openssl rsa -in private.pem -des3 -out key3des.pem</pre>	
B.5	<p>Next we will export the public key:</p> <pre>openssl rsa -in private.pem -out public.pem -outform PEM -pubout</pre>	View the output key. What does the header and footer of the file identify?
B.6	<p>Now we will encrypt with our public key:</p> <pre>openssl rsautl -encrypt -inkey public.pem -pubin -in myfile.txt -out file.bin</pre>	
B.7	<p>And then decrypt with our private key:</p> <pre>openssl rsautl -decrypt -inkey private.pem -in file.bin -out decrypted.txt</pre>	What are the contents of decrypted.txt

On your VM, go into the ~/.ssh folder. Now generate your SSH keys:

```
ssh-keygen -t rsa -C "your email address"
```

The public key should look like this:

```
ssh-rsa
AAAAB3NzaC1yc2EAAAADAQABAAQDLrriUNYTywuC1IW7H6yea3hMV+rm029m2f6Id
dtlImHrOXjNwYyt4Elkkc7AzOy899C3gpx0kJK45k/CLbPnrHvKLvtQ0AbzWEQpOKxI+
tw06PcqJNmTB8ITRLqIFQ++ZanjHWMw2Odew/514y1dQ8dcccOuzeGhL2Lq9dtfhSxx+
1cBLcyoSh/lQcs1HpXtpwU8JMxwJl409RQOVn3gOusp/P/0R8mz/RwkmsFsyDRLgQK+x
```

tQxbpbodpznz5lIOPwn5LnT0si7eHmL3wikTyg+QLZ3D3m44NCeNb+b0JbfaQ2ZB+lv8C30xy1xSp2sxzPZMbrZWqGSLPjgDiFIBL w.buchanan@napier.ac.uk

View the private key. What is its format?

On your Ubuntu instance setup your new keys for ssh:

```
ssh-add ~/.ssh/id_git
```

Now create a Github account and upload your public key to Github (select Settings-> **New SSH key** or **Add SSH key**). Create a new repository on your GitHub site, and add a new file to it. Next go to your Ubuntu instance and see if you can clone of a new directory:

```
git clone ssh://git@github.com/<user>/<repository name>.git
```

C OpenSSL (ECC)

Elliptic Curve Cryptography (ECC) is now used extensively within public key encryption, including with Bitcoin, Ethereum, Tor, and many IoT applications. In this part of the lab we will use OpenSSL to create a key pair. For this we generate a random 256-bit private key (*priv*), and then generate a public key point (*priv* multiplied by *G*), using a generator (*G*), and which is a generator point on the selected elliptic curve.

No	Description	Result
C.1	<p>First we need to generate a private key with:</p> <pre>openssl ecparam -name secp256k1 -genkey -out priv.pem</pre> <p>The file will only contain the private key (and should have 256 bits).</p> <p>Now use “cat priv.pem” to view your key.</p>	Can you view your key?
C.2	<p>We can view the details of the ECC parameters used with:</p> <pre>openssl ecparam -in priv.pem -text -param_enc explicit -noout</pre>	<p>Outline these values:</p> <p>Prime (last two bytes):</p> <p>A:</p> <p>B:</p> <p>Generator (last two bytes):</p>

		Order (last two bytes):
C.3	<p>Now generate your public key based on your private key with:</p> <pre>openssl ec -in priv.pem -text -noout</pre>	<p>How many bits and bytes does your private key have:</p> <p>How many bit and bytes does your public key have (Note the 04 is not part of the elliptic curve point):</p> <p>What is the ECC method that you have used?</p>

If you want to see an example of ECC, try here: <https://asecuritysite.com/encryption/ecc>

D Elliptic Curve Encryption

D.1 In the following Bob and Alice create elliptic curve key pairs. Bob can encrypt a message for Alice with her public key, and she can decrypt with her private key. Copy and paste the program from here:

<https://asecuritysite.com/encryption/elc>

Code used:

```
import OpenSSL
import pyelliptic

secretkey="password"
test="Test123"

alice = pyelliptic.ECC()
bob = pyelliptic.ECC()

print "++++Keys++++"
print "Bob's private key: "+bob.get_privkey().encode('hex')
print "Bob's public key: "+bob.get_pubkey().encode('hex')

print
print "Alice's private key: "+alice.get_privkey().encode('hex')
print "Alice's public key: "+alice.get_pubkey().encode('hex')

ciphertext = alice.encrypt(test, bob.get_pubkey())
print "\n++++Encryption++++"

print "Cipher: "+ciphertext.encode('hex')

print "Decrypt: "+bob.decrypt(ciphertext)

signature = bob.sign("Alice")
```

```
print
print "Bob verified: "+ str(pyelliptic.ECC(pubkey=bob.get_pubkey()).verify
(signature, "Alice"))
```

For a message of “Hello. Alice”, what is the ciphertext sent (just include the first four characters):

How is the signature used in this example?

D.2 Let’s say we create an elliptic curve with $y^2 = x^3 + 7$, and with a prime number of 89, generate the first five (x,y) points for the finite field elliptic curve. You can use the Python code at the following to generate them:

https://asecuritysite.com/encryption/ecc_points

First five points:

D.3 Elliptic curve methods are often used to sign messages, and where Bob will sign a message with his private key, and where Alice can prove that he has signed it by using his public key. With ECC, we can use ECDSA, and which was used in the first version of Bitcoin. Enter the following code:

```
from ecdsa import
SigningKey,NIST192p,NIST224p,NIST256p,NIST384p,NIST521p,SECP256k1
import base64
import sys

msg="Hello"
type = 1
cur=NIST192p

sk = SigningKey.generate(curve=cur)
vk = sk.get_verifying_key()
signature = sk.sign(msg)

print "Message:\t",msg
print "Type:\t\t",cur.name
print "======"

print "Signature:\t",base64.b64encode(signature)
print "======"

print "Signatures match:\t",vk.verify(signature, msg)
```

What are the signatures (you only need to note the first four characters) for a message of “Bob”, for the curves of NIST192p, NIST512p and SECP256k1:

NIST192p:

NIST512p:

SECP256k1:

By searching on the Internet, can you find where SECP256k1 is used?

What do you observe from the different hash signatures from the elliptic curve methods?

E Inverse of a value mod N

E.1 In the RSA method, we have a value of e , and then determine d from $(d \cdot e) \pmod{\phi(N)} = 1$. But how do we use code to determine d ? Well we can use the Euclidean algorithm. The code for this is given at:

<https://asecuritysite.com/encryption/inversemod>

Using the code, can you determine the following:

Inverse of 53 (mod 120) =

Inverse of 65537 (mod 1034776851837418226012406113933120080) =

Using this code, can you now create an RSA program where the user enters the values of p , q , and e , and the program determines (e, N) and (d, N) ?

F PGP

F.1 The following is a PGP key pair. Using <https://asecuritysite.com/encryption/pgp>, can you determine the owner of the keys:

-----BEGIN PGP PUBLIC KEY BLOCK-----

Version: OpenPGP.js v4.4.5

Comment: <https://openpgpjs.org>

xk0EXEOYvQECAIpLP8wFLxzgco1mpwgzcUzT1H0icggOIyuQKsHM4XNPugzu


```
X0NeeawrJhfi+f8hDroJj5Fv8jBI0m/kwFMNTT8AEQEAAcOUYm1sbCA8Ym1s
bEBob211LmNvbT7CdQQQAQgAHwUCXEOYvQYLCQcIAwIEFQgKAGMWAgECGQEC
GwMCHgEACgkQoNSXEDYt2ZjkTAH/b6+pDfQLi6zg/Y0tHS5PPRv1323cwoay
vMcPjnWq+VfiNyXzy+UJKR1PXskzDvHMLoyVpucj1e5ChyT5LOW/ZM5NBFXD
mL0BAGDY1tSt06vVQxu3jmfLzKMAR4kLqQIuFFRCapRuHYLOjw1gJZS9p0bF
S0qS8zMEGpn9QZxkG8YECH3gHx1rvAlTABEBAAHCXwQYAQgACQUCEYOYvQIb
DAAKCRcg2xcQNi3ZmMAGaf9w/XazfELDG1W3512zw12rkWm7rk97aFrTxz5W
XwA/5gqovP0iQxklb9qpX7Rvd6rLKu7zoX7F+sQod1sCWrmWw
=cXT5
```

-----END PGP PUBLIC KEY BLOCK-----

-----BEGIN PGP PRIVATE KEY BLOCK-----

Version: OpenPGP.js v4.4.5

Comment: <https://openpgpjs.org>

```
xCBmBFxDmL0BAGCKSz/MHy8c4HKJTKcIM3FM05R9InIIDiMrkCrBzOFzT7oM
1F9DXmmsKyYX4vn/IQ0aIyerb/IwSNJvysBTDU0/ABEBAAH+CQMIBNTT/OPV
TJzgVF+fL0SLSNYP64QfNHav5O744y0MLV/EZT3gsBw09v4XF2SsZj6+EHbk
09gwi31BAIDgSaDsJYf7xPOhp8iEwwwrUkC+j1GpdTsGDJpeYMIsvVv8Ycam
0g7MSRSL+dYQauIgtvb3d1oLMPtuL59nVAYuIgD8HXyAH2vsEgSZSqn0kfVf
+dweqJxwFM/ux5PVKcuYsroJFBE01zas4ERfxbbwnsQGNHpdIpuex6/4EO
b1kmhOd6UT7BamubY7bcma1PBSv8PH31Jt8SzRRiawxsIDxiawxsQGhvbWUu
Y29tPsJ1BBABCAAFBQJcQ5i9BgSJBwgDagQVCAoCAXYCAQIZAQIbAwIeAQAK
CRcg2xcQNi3ZmORMAf9vr6kN9AuLrOD9jS0dLk89G/XfbdzChrK8xw+Odar5
V+I3JfNj5QkPHU9eyTM08cws7Jw1RyOV7kKHJPks7D9kx8BmBFxDmL0BAGDY
1tSt06vVQxu3jmfLzKMAR4kLqQIuFFRCapRuHYLOjw1gJZS9p0bFS0qS8zME
Gpn9QZxkG8YECH3gHx1rvAlTABEBAAH+CQMI2Gyk+BqVOgzgZX3C80JRLBRM
T4sLCHOUGlwaspe+qatOVjeEuxA5DuSs0bvMrw7mJYQZLtjNkFAT921Swfxy
gavS/bILlw3QGA0CT5mqijKr0nurKkekKBDsgjkjVbIoPLMYHfepPOju1322
Nw4V3JQ04LBh/sdgGbrnww3LhHEK4Qe70cuiert8C+S5xfG+T5RWADi5HR8u
UTYH8x1h0ZrOF7K0Wq4UcNvrUm6c35H61C1C4Zaar4JSN8fZPqVKL1HTVcL9
1pDzXxqxKjS05KXXZBh5w18EGAEIAAKFA1xDmL0CGwwACgkQoNSXEDYt2ZjA
BgH/cP12s3xCwxtvt+Zds8NdqysDO6yve2ha7cc+v18AP+YKqFT9IkMZJW/a
qV+0VXeeyru86F+xfrEKHdbAlqzMA==
=5NaF
```

-----END PGP PRIVATE KEY BLOCK-----

F.2 Using the code at the following link, generate your own key:

<https://asecuritysite.com/encryption/openpgp>

G Reflective statements

1. In ECC, we use a 256-bit private key. This is used to generate the key for signing Bitcoin transactions. Do you think that a 256-bit key is largest enough? If we use a cracker what performs 1 Tera keys per second, will someone be able to determine our private key?

2. If someone takes our elliptic curve public key, how might they determine our public key?

G What I should have learnt from this lab?

The key things learnt:

- The basics of the RSA method.
- The process of generating RSA and Elliptic Curve key pairs.
- To illustrate how the private key is used to sign data, and then using the public key to verify the signature.

Notes

To setup your Python to run Python 2.7:

```
sudo update-alternatives --set python /usr/bin/python2.7
```

To install a Python library use:

```
easy_install libname
```

or:

```
pip install libname
```