

1. In Trig last year you learned that the period of the function $y = 3\cos(12x)$ is $\frac{\pi}{6}$ and that the amplitude is 3. Explain how both of these connect to the graph of $r = 3\cos(12\theta)$ in polar. [3]

The amplitude, 3, represents the height of the rectangular wave & length of the polar petal. period.
In both of them, it is the distance of rotation needed to make a full wave or petal.
amp 3 ✓ period $\frac{\pi}{6}$ -1

$$\text{Amp} \rightarrow \frac{2\pi}{12} = \frac{\pi}{6}$$

↑
period 2

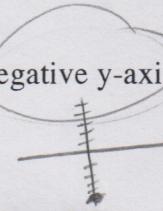
2. Consider the polar rose $r = 5\sin(15\theta)$

- ✓ a) How many visible petals will there be? 15 [2]

- ✓ b) Will there be a petal along the positive y axis, negative y-axis, both or neither? negative y [2]

$$r = 5\sin(15 \cdot \frac{\pi}{2})$$

$$= 5\sin(\frac{15\pi}{2}) = 5\sin\frac{3\pi}{2} = -5$$



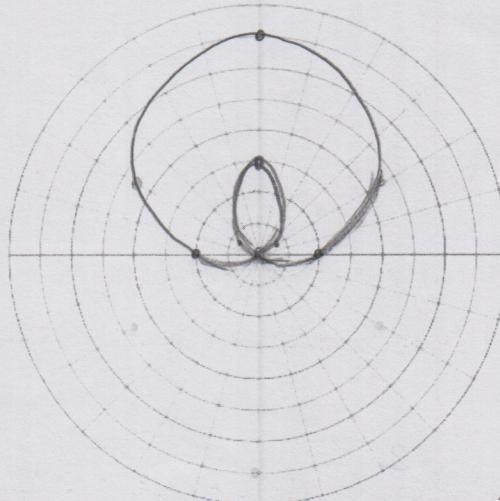
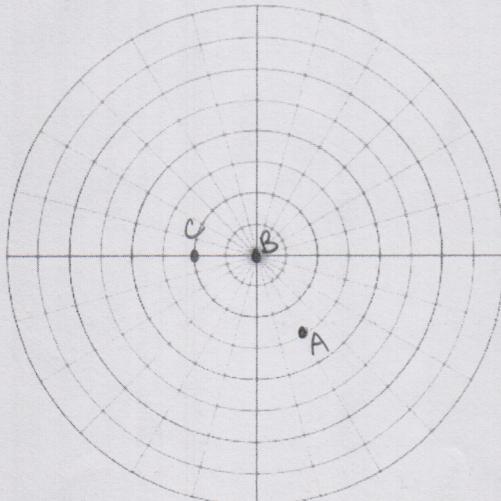
(-5, $\frac{\pi}{2}$) and ($5, \frac{3\pi}{2}$)
are the same point

$$\begin{aligned} r &= 5\sin(15 \cdot \frac{3\pi}{2}) \\ &= 5\sin(\frac{45\pi}{2}) \\ &= 5\sin\frac{\pi}{2} \\ &= 5 \end{aligned}$$

- ✓ c) The line of symmetry for the first petal in Quadrant I, is at $\theta = \frac{\pi}{30}$ [2]

- ✓ 3. On the polar graph paper below left plot and label the 3 points: [3]

$$A: (-3, -\frac{4\pi}{3}) \quad B: (0, \frac{\pi}{3}) \quad C: (-2, 0)$$



- ✓ 4. Above right, accurately graph $r = -2 + 5\sin\theta$. [5]

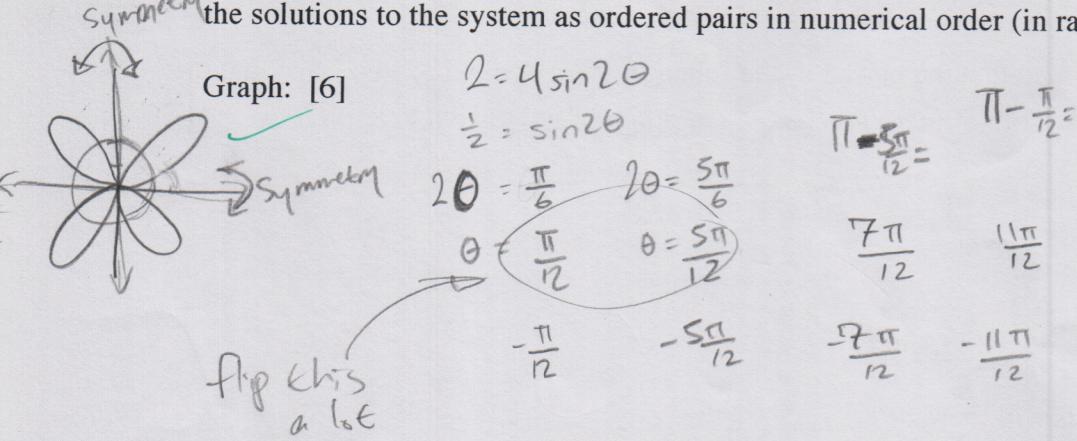
$$r = -2 + 5\sin(\frac{3\pi}{2})$$

$$-7 = -2 + -5$$

$$\begin{aligned} -2 + 5\sin\frac{\pi}{6} \\ -2 + 5\sin\frac{\pi}{2} \\ -2 + 5\sin\frac{5\pi}{6} \\ -2 + \frac{5}{2} \\ -\frac{9}{2} \end{aligned}$$

$$\begin{aligned} -2 + 5\sin(-\frac{\pi}{6}) \\ -2 + 5\sin(-\frac{1}{2}) \\ -2 + -\frac{5}{2} \\ -\frac{9}{2} \end{aligned}$$

5. Roughly graph the system of equations $r = 2$ and $r = 4\sin 2\theta$ below, and clearly state all of the solutions to the system as ordered pairs in numerical order (in radians). Show all work.



Solutions: $(2, \frac{\pi}{12}), (2, \frac{5\pi}{12}), (2, \frac{7\pi}{12}), (2, \frac{11\pi}{12}), (2, \frac{13\pi}{12}), (2, \frac{17\pi}{12}),$
 $(2, \frac{19\pi}{12}), (2, \frac{23\pi}{12})$ ✓

6. Convert the point $(-5, -5)$ into polar coordinates in radians. [2]

$$(\sqrt{(-5)^2 + (-5)^2}, \tan^{-1}(\frac{-5}{-5}))$$

$$\boxed{(5\sqrt{2}, \frac{5\pi}{4})} \quad \checkmark$$

7. Convert the point $(r, \theta) = (-2, 5\pi/6)$ into simplified rectangular form. [2]

$$(-2 \cos \frac{5\pi}{6}, -2 \sin \frac{5\pi}{6})$$

$$(-2 \cdot -\frac{\sqrt{3}}{2}, -2 \cdot \frac{1}{2})$$

$$\boxed{(\sqrt{3}, -1)} \quad \checkmark$$

8. Convert the hyperbola $r^2 = 20/\sin 2\theta$ into rectangular. [3]

$$r^2 = \frac{20}{\sin 2\theta}$$

$$r^2 = \frac{20}{2\cos\theta \sin\theta}$$

$$r^2 \cos\theta \sin\theta = 20$$

$$\begin{aligned} xy &= 20 \\ \boxed{y = \frac{20}{x}} \quad -1 \end{aligned}$$

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