$$m \coloneqq 1 \\ l \coloneqq 1 \qquad v_0 \coloneqq 2 \cdot \sqrt{g \cdot l}$$

$$v_0 \coloneqq 2 \cdot \sqrt{g \cdot l} \qquad \qquad \varphi_0 \coloneqq 0 \quad a \coloneqq l \quad k \coloneqq 0.2 \qquad \qquad v_0 \coloneqq \frac{\pi}{2} \qquad \qquad y \coloneqq \begin{bmatrix} v_0 \\ \varphi_0 \end{bmatrix} \qquad \qquad w_0 \coloneqq \sqrt{\frac{g}{l}}$$

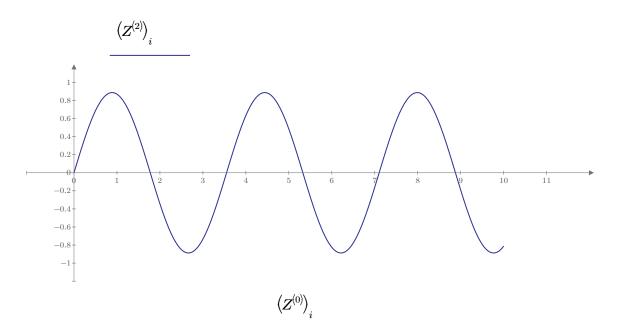
$$v_0 = \frac{\pi}{2}$$

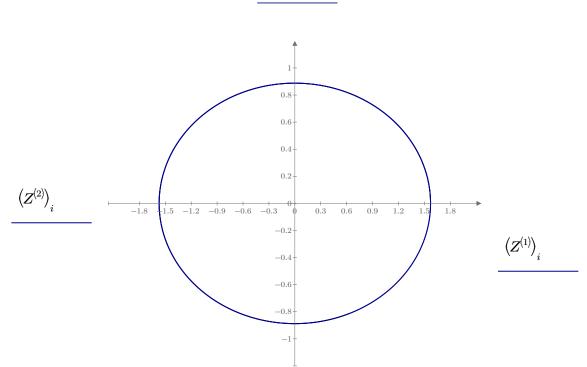
$$y\!\coloneqq\!\begin{bmatrix}v_0\\\varphi_0\end{bmatrix}$$

$$w_0 \coloneqq \sqrt{\frac{g}{l}}$$

$$D\!\left(t\,,y\right)\!\coloneqq\!\begin{bmatrix}-w_0\!\cdot\!y_{_1}\!\cdot\!1\!-\!0\!\cdot\!w_{_0}^{^2}\!\cdot\!\sin\left(y_{_1}\right)\!-\!k\!\cdot\!y_{_0}\!+\!a\!\cdot\!\sin\left(w_1\!\cdot\!t\right)\\y_{_0}\end{bmatrix}$$

$$Z \coloneqq \text{rkfixed}(y, 0, 10, 2000, D)$$
 $Z =$





 $Q = \text{rkfixed}(y, 0, 10, 20, \mathbb{R})$

$$\begin{bmatrix} 0.102 \\ 0.102 \\ 0.102 \\ 0.102 \\ 0.102 \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ 4.885 \cdot 10^{-4} \\ 9.771 \cdot 10^{-4} \\ 0.001 \end{bmatrix}$$

$$A \coloneqq \frac{1}{\sqrt{\left(w_0^2 - w^2\right)^2 + 4\left(\delta^2 \cdot w^2\right)}} = \begin{bmatrix} 0.102 \\ 0.102 \\ 0.102 \\ 0.102 \\ 0.102 \\ 0.102 \\ 0.102 \\ 0.103 \\ 0.103 \\ \vdots \end{bmatrix} \qquad \varphi \coloneqq \operatorname{atan}\left(\frac{2 \cdot \delta \cdot w}{w_0^2 - w^2}\right) = \begin{bmatrix} 0.002 \\ 0.002 \\ 0.002 \\ 0.003 \\ 0.003 \\ 0.004 \\ 0.004 \\ 0.005 \\ 0.005 \\ \vdots \end{bmatrix}$$

$$v_0 = 2 \cdot \sqrt{g \cdot l}$$
 $\varphi_0 = 2 \cdot \sqrt{g \cdot l}$

$$\varphi_0 := 0 \quad a := l \quad k := 0.2$$

=1

$$v_0 = \frac{\pi}{2}$$

$$y \coloneqq \begin{bmatrix} v_0 \\ \varphi_0 \end{bmatrix}$$

$$w_0 \coloneqq \sqrt{w_0}$$

 $m \coloneqq 1$

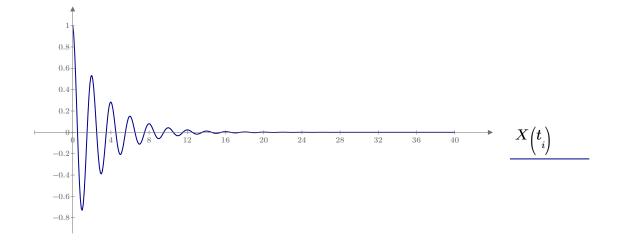
$$R(t,y) \coloneqq \begin{bmatrix} \frac{-g}{l} \cdot y_1 \cdot 0 - 1 \cdot w_0 \cdot \sin(y_1) - k \cdot y_0 + a \cdot \sin(w_1) \\ y_0 \end{bmatrix}$$

$$(A^{(i)})_{j} := \frac{A0}{m \cdot \sqrt{\left(w0^{2} - w_{j}^{2}\right)^{2} + 4 b_{i}^{2} \cdot w_{j}^{2}}}$$

$$f = 0, 0.1..40 =$$

$$d \coloneqq 0.1 \qquad w0 \coloneqq \sqrt{\frac{g}{l}} \qquad w \coloneqq w0 \qquad \text{ } f \coloneqq 0$$

$$A0 \coloneqq l \qquad b \coloneqq d \cdot w0 \qquad X(t) \coloneqq A0 \cdot e^{-b \cdot t} \cdot \cos(w \cdot t + f)$$



$$n = 1000$$

$$m:=3$$
 $step:=\frac{m}{n}$ 0 0.003 0.006 0.006

$$m := 3$$
 $step := \frac{m}{n}$
 $k := 0, step ... m = \begin{bmatrix} 0 \\ 0.003 \\ 0.006 \\ \vdots \end{bmatrix}$
 $z(t) := 3 \cdot \frac{t}{m}$ $z(k) = \begin{bmatrix} 0 \\ 0.003 \\ 0.006 \\ \vdots \end{bmatrix}$

$$A_1 \coloneqq \left\| \begin{matrix} j \leftarrow 0 \\ \text{while } j \leq n \end{matrix} \right\| \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_2 \coloneqq \left\| \begin{matrix} j \leftarrow 0 \\ \text{while } j \leq n \end{matrix} \right\| \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix} \right\| A_2 = \left\| \begin{matrix} j \leftarrow 0 \\ m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{30}^{\ 2} \cdot w_j^{\ 2}} \end{matrix}$$

$$A_{9} \coloneqq \begin{vmatrix} j \leftarrow 0 \\ \text{while } j \leq n \\ \\ \left(A\right)_{j} \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^{2} - w_{j}^{2}\right)^{2} + 4 b_{50}^{2} \cdot w_{j}^{2}}} \end{vmatrix} A_{10} \coloneqq \begin{vmatrix} j \leftarrow 0 \\ \text{while } j \leq n \\ \\ \left(A\right)_{j} \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^{2} - w_{j}^{2}\right)^{2} + 4 b_{100}^{2} \cdot w_{j}^{2}}} \end{vmatrix}$$

$$A_5 \coloneqq \left\| \begin{matrix} j \leftarrow 0 \\ \text{while } j \leq n \end{matrix} \right\| \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{15}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \coloneqq \left\| \begin{matrix} j \leftarrow 0 \\ \text{while } j \leq n \end{matrix} \right\| \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| \left\| \begin{matrix} j \leftarrow j + 1 \end{matrix} \right\| A_6 \coloneqq \left\| \begin{matrix} j \leftarrow 0 \end{matrix} \right\| \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \coloneqq \left\| \begin{matrix} j \leftarrow j + 1 \end{matrix} \right\| A_6 \coloneqq \left\| \begin{matrix} j \leftarrow 0 \end{matrix} \right\| A_6 \coloneqq \left\| \begin{matrix} j \leftarrow 0 \end{matrix} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\| A_6 \mapsto \left(A \right)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^{\ 2} \right)^2 + 4 \ b_{20}^{\ 2} \cdot w_j^{\ 2}}} \right\|$$

$$A_{10} \coloneqq \begin{vmatrix} j \leftarrow 0 \\ \text{while } j \leq n \end{vmatrix}$$

$$\begin{vmatrix} (A)_j \leftarrow \frac{A0}{m \cdot \sqrt{\left(w0^2 - w_j^2\right)^2 + 4 b_{100}^{-2} \cdot w_j^2}}$$

