## Von Mises distribution

Intuitively, the Von Mises distribution[1] is a simple approximation for the normal distribution on a circle (known as the *wrapped normal distribution*). The Von Mises probability density function is defined by the following equation:

$$P(x) = \frac{e^{b\cos(x-a)}}{2\pi I_0(b)}$$

where  $I_0(x)$  is the modified Bessel function of the first kind; the Von Mises cumulative density function has no closed form.

The mean  $\mu=a$  (intuitively, the angle that the distribution clustered around), and the circular variance  $\sigma^2=1-\frac{I_1(b)}{I_0(b)}$  (intuitively, b is the "concentration" parameter). Therefore, as  $b\to 0$ , the distribution becomes uniform; as  $b\to \infty$ , the distribution becomes normal with  $\sigma^2=1/b$ .

## Von Mises-Fisher distribution

THe Von-Mises Fisher distribution is the generalization of the Von Mises distribution to n-dimensional hyperspheres. It reduces to the Von-Mises distribution with n=2. The probability density function is defined by the following equation:

$$f_p(\boldsymbol{x};\boldsymbol{\mu},\kappa) = C_p(\kappa) \exp(\kappa \boldsymbol{\mu}^T \boldsymbol{x})$$

where

$$C_p(\kappa) = \frac{\kappa^{p/2-1}}{(2\pi)^p I_{p/2-1}(\kappa)}$$

and intuitively is an approximation for the normal distribution on the hypersphere.

## References

 $[1] \begin{tabular}{lll} Eric & W. & Weisstein. & von & mises & distribution. \\ & $http://mathworld.wolfram.com/vonMisesDistribution.html. & Accessed: \\ & 2016-05-18. & \\ \end{tabular}$