NOTES FOR CS/MATH 240, SPRING 2025

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1 Logic

Logic is the study of formal reasoning. A statement in logic always has a well-defined meaning.

1.1 Propositions and Logical Operations

1.1.1 Applications of Logic

- In Mathematics, logic is used to prove theorems.

- In Computer Science, logic is used in areas such as AI and in designing digital circuits.

- In Medicine, logic precisely specifies the conditions under which a particular diagnosis applies.

1.1.2 Elements of Logic

Propositions

A **proposition** is a statement that must be either true or false (truth value).

EXAMPLES:

- *"There are an infinite number of prime numbers."*   (Truth value: True)

- *"17 is an even number."*   (Truth value: False)

Proposition Variables

Variables like p, q, and r can be used to denote propositions.

EXAMPLES:

- p: January has 31 days.

- q: February has 33 days.

1.1.3 Logical Operations

COMPOUND PROPOSITION

It will only be true if both p and q are true.

Operator: $\wedge$ (and)
Example: $p \wedge q$ (January has 31 days and February has 33 days)
Truth Value: False

Disjunction Proposition

It will be true if either p and q are true or both true.

Operator: $\vee$ (or)
Example: $p \vee q$ (January has 31 days or February has 33 days)
Truth Value: True

Exclusive Or (XOR)

Operator: $\oplus$
Example: $p \oplus q$ (January has 31 days or February has 33 days, but not both)
Truth Value: True

Negation

Operator: $\neg$
Example: $\neg q$ (February has 33 days)
Truth Value: True