

# NOTES FOR CS/MATH 240, SPRING 2025

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## 1 Logic

Logic is the study of formal reasoning. A statement in logic always has a well-defined meaning.

### 1.1 Propositions and Logical Operations

#### 1.1.1 Applications of Logic

- In Mathematics, logic is used to prove theorems.
- In Computer Science, logic is used in areas such as AI and in designing digital circuits.
- In Medicine, logic precisely specifies the conditions under which a particular diagnosis applies.

#### 1.1.2 Elements of Logic

##### Propositions

A **proposition** is a statement that must be either true or false (truth value).

EXAMPLES:

- “*There are an infinite number of prime numbers.*” (Truth value: True)
- “*17 is an even number.*” (Truth value: False)

##### Proposition Variables

Variables like  $p$ ,  $q$ , and  $r$  can be used to denote propositions.

EXAMPLES:

- $p$ : January has 31 days.
- $q$ : February has 33 days.

### 1.1.3 Logical Operations

#### COMPOUND PROPOSITION

It will only be true if both  $p$  and  $q$  are true.

**Operator:**  $\wedge$  (and)

**Example:**  $p \wedge q$  (January has 31 days and February has 33 days)

**Truth Value:** False

**DISJUNCTION PROPOSITION** It will be true if either  $p$  and  $q$  are true or both true.

**Operator:**  $\vee$  (or)

**Example:**  $p \vee q$  (January has 31 days or February has 33 days)

**Truth Value:** True

#### Exclusive Or (XOR)

**Operator:**  $\oplus$

**Example:**  $p \oplus q$  (January has 31 days or February has 33 days, but not both)

**Truth Value:** True

#### Negation

**Operator:**  $\neg$

**Example:**  $\neg q$  (February has 33 days)

**Truth Value:** True