

**Anti-differentiation by the Method of Substitution**

$$\frac{d}{dx}[\sin(x^2)] =$$

$$\text{So... } \int \cos(x^2) 2x dx =$$

$$\frac{d}{dx}[\sqrt{5x^3 + 1}] =$$

$$\text{So... } \int \frac{x^2}{\sqrt{5x^3 + 1}} dx =$$

$$\frac{d}{dx}[F(g(x))] =$$

Make the change of variable substitution,  $u = g(x)$

$$\text{So... } \int F'(g(x))g'(x)dx =$$

$$1. \int x^3 \cos(x^4 + 2) dx =$$

$$2. \int \sin^3 x \cos x dx$$

$$3. \int \sqrt{2x+1} \, dx =$$

Method #1

Method #2

Method #3

$$4. \int \frac{x}{\sqrt{1-4x^2}} \, dx =$$

$$5. \int \cos(5x) \, dx =$$

$$6. \int \tan x \, dx =$$

$$7. \int \cos^3 x \, dx$$

$$8. \int \frac{x^2}{x^3+5} \, dx$$

$$9. \int \frac{x^2 + 2}{x^2 + 1} dx$$

$$10. \int \frac{\ln x}{x} dx$$

$$11. \int \frac{dx}{x\sqrt{\ln x}}$$

$$12. \int \cos x \cos(\sin x) dx$$

$$13. \int \frac{e^x}{e^x + 1} dx$$

$$14. \int \frac{\arctan x}{1 + x^2} dx$$

15.  $\int 5^x dx$

16.  $\int \tan^2 x \sec^2 x dx$

17.  $\int \frac{10\sqrt{x}}{\left(1+x^{3/2}\right)^2} dx$

18.  $\int \sin(10x)e^{\sin^2(5x)} dx$

19.  $\int \frac{x^3+1}{x^2+4} dx$

$$20. \int \frac{1}{\sqrt{1-4x^2}} dx$$

$$21. \int \frac{x^4}{x^2+1} dx$$

$$22. \int \frac{1}{x\sqrt{x^2-16}} dx$$

$$23. \int \frac{2}{\sqrt{-x^2+4x}} dx$$

24.  $\int \frac{1}{x\sqrt{x^4 - 4}} dx$

25.  $\int \frac{dx}{x^2 - 4x + 7}$

26.  $\int \frac{dx}{3x^2 + 12x + 25}$

### Other Trigonometric Anti-differentiation Techniques

27.  $\int \sin^2 x \, dx$

28.  $\int \cos^4 x \, dx$

29.  $\int \sec x \, dx$

30.  $\int \csc x \, dx$

**“Miscellaneous Substitution”**

31.  $\int \frac{1}{1 + \sqrt{3x}} dx$

32.  $\int \frac{\sqrt[3]{x}}{\sqrt[3]{x} - 1} dx$

33.  $\int \frac{\sqrt{x-2}}{x+1} dx$

34.  $\int \frac{dx}{\sqrt{x}(1+x)}$