

The Open University of Israel Department of Mathematics and Computer Science

IPFIM - Incremental Parallel Frequent Itemsets Mining

Thesis submitted as partial fulfillment of the requirements towards an M.Sc. degree in Computer Science

The Open University of Israel

Department of Mathematics and Computer Science

By Lev Kuznetsov

Prepared under the supervision of Prof. Ehud Gudes

March 2022

Acknowledgements

I would like to thank Prof. Gudes, my instructor, for his time and guidance in making this thesis. I would also use this acknowledgement to thanks The Open University of Israel for providing the opportunity to ... And last but certainly not least, I would like to thank my family and my wife Jenny for supporting me during that time.

Abstract

The frequent itemset mining (FIM) problem has been around pretty much since the definition of the term 'data' in the previous century. Whenever there is a collection of data, one of the basic analysis we would like to perform, is finding relations within the data. One of those basic 'relations', is to find all the sets of data that appear together in an important frequency (usually greater than a predefined threshold). The process of finding such items is called Mining, and thus the term - Frequent Itemset Mining (FIM). Frequent itemset can later reveal association rules and relations between variables. This research area in data science is applied to domains such as recommender systems (e.g. what are the set of items usually ordered together), bioinformatics (e.g. what are the genes coexpressed in a given condition), decision making, clustering, website navigation and many more.

Many algorithms were developed during time to find frequent item sets in a database, and they are mostly focused on Apriori [2] and FP-Growth [12] techniques. The later is further discussed in section TODO.

This work focuses on using tree based structure for parallel and incremental mining.

As the access to online resources grew, so does the size of the databases,. Today's databases' sizes go far beyond capabilities of a single machine. The need to provide better performance has grown and platforms for parallel computation, and the frameworks who support them, also became main stream.

We will elaborate more on these frameworks, specifically on Spark vs Hadoop in section [TODO].

Besides the size of the databases, a growing online access also increased the need for incremental updates. Such events happen with high velocity in current databases and making full recalculation may be far from optimal. To achieve this, the proposed algorithm is using a combination of two techniques. As a high-level overview, the PFP [15] algorithm is the base algorithm for parallel mining and CanTree [14] as the base structure for incremental updates. As the framework for computation, Spark was chosen [7], and will be detailed more in section [TODO].

In this paper we will also present a new approach for incremental group updates by using a greedy set-cover algorithm, where the motivation is to optimize groups for parallel calculations. However, as we will show from our experiments, the overhead of regrouping using hashmaps, is far larger than using random group deviation.

The paper is divided as following: Section 2 and 3 will review related work and background, and will provide examples for the used algorithms. Section 4 and 5 will present the IPFIM algorithm, and an improvement, based on partial frequency sort and min min threshold [TODO]. Section 6 will discuss comparison to [18]. Section 7 will present an approach for trying to optimize grouping by using greedy set-cover algorithm for optimized group mining. Section 8 will presents and discuss experimental results and section 9 will present conclusion and summarize discussion.

Contents

| 1 | Introduction | | | 1 |
|---|-------------------|--------|--|----|
| | 1.1 | | duction - Add formal definitions of FIS etc add more the issue | 1 |
| 2 | Bac | kgroun | d And Related Work | 2 |
| | 2.1 | Backg | ground | 2 |
| | | 2.1.1 | Frequent Itemset | 2 |
| | | 2.1.2 | FP-Tree and FP-Growth | 7 |
| | | 2.1.3 | Apache Spark vs Hadoop | 7 |
| | 2.2 | RELA | TED WORK | 12 |
| | | 2.2.1 | Incremental Frequent Itemsets Mining | 12 |
| | | 2.2.2 | Parallel Frequent Itemsets mining | 13 |
| | | 2.2.3 | Incremental and Parallel Frequent itemsets mining . | 14 |
| | | 2.2.4 | Song et al | 15 |
| 3 | IPFIM Algorithm 1 | | | |
| | 3.1 | IPFIM | 1 - Incremental Parallel Frequent Itemsets Mining | 18 |
| | | 3.1.1 | IPFIM Outline | 18 |
| | | 3.1.2 | Correctness | 19 |
| 4 | IPF | IM Imp | provements | 20 |
| | 4.1 | - | ovements - Need to add SetCover results and explana- | 20 |
| | | 4.1.1 | | 20 |
| | | | | |

| CONTENTS | 5 |
|----------|---|
| | |

| | | 4.1.2 | IPFIM Improved vs IPFIM - Memory | 21 |
|---|-----|----------|----------------------------------|----|
| 5 | Exp | erimen | t Preparation | 23 |
| | 5.1 | Experi | iments Preparation | 23 |
| | | 5.1.1 | Datasets | 23 |
| | | 5.1.2 | Implementation | 23 |
| | | 5.1.3 | Logging and Statistics | 24 |
| | | 5.1.4 | Infrastructure | 24 |
| | | 5.1.5 | Performance evaluation | 25 |
| | | 5.1.6 | IPFIM vs CanTree | 25 |
| 6 | Exp | erimen | ts Results | 26 |
| | 6.1 | Experi | iments and Results | 26 |
| | | 6.1.1 | Performance Evaluation | 26 |
| | | 6.1.2 | IPFIM vs PFP | 26 |
| | | 6.1.3 | improved-IPFIM vs PFP | 34 |
| | | 6.1.4 | improved-IPFIM vs Song et al | 34 |
| | | 6.1.5 | set-cover-IPFIM vs Song et al | 34 |
| 7 | Res | ults Dis | scussion | 35 |
| 8 | Con | clusion | ı | 36 |
| | 8.1 | Concl | usions | 36 |
| | | | | |

List of Figures

| 2.1 | Maximal Frequent Itemset Illustration | 4 |
|-----|--|----|
| 2.2 | Maximal Frequent Itemset Illustration | 5 |
| 2.3 | Relationship between Frequent Itemset Representations | 6 |
| 2.4 | Apriori Example | 8 |
| 2.5 | FPGrowth example | 9 |
| 2.6 | Execution time for different min-sup values, average transaction length 10 | 10 |
| 2.7 | Execution time for different min-sup values, average transaction length 30 | 11 |
| 2.8 | The CanTree after each group of transactions is added \ldots | 14 |
| 3.1 | IPFIM example | 19 |
| 4.1 | IPFIM partial frequency sort vs IPFIM cannonical sort | 21 |
| 4.2 | IPFIM pre-min, semi-frequency vs PFP | 22 |
| 6.1 | T15I5D1000N10 100 partitions | 27 |
| 6.2 | kosarak, minSup = 0.001 , PFP 100 — 1000 — 500 partitions | 27 |
| 6.3 | kosarak, minSup = 0.001, IPFIM Improved 100—1000—500 partitions | 28 |
| 6.4 | kosarak, minSup = 0.001 , partitions = $500 \dots \dots \dots$ | 28 |
| 6.5 | T15I5D10000N100, minSup = 0.0001, PFP 100—1000—500 partitions | 29 |
| 6.6 | T15I5D10000N100, minSup = 0.0001, IPFIM Improved 100—10 partitions | |

| 6./ | partitions | 30 | | | |
|----------------|--|----|--|--|--|
| 6.8 | T15I5D10000N100, minSup = 0.0001, 1000 partitions | 30 | | | |
| 6.9 | $T15I5D10000N100, minSup = 0.0001, 1000 \ partitions, Set \ cover \ vs \ IPFIM \ \dots $ | 31 | | | |
| 6.10 | T15I5D10000N100, minSup = 0.0001, PFP, Min Tree size for partitions | 31 | | | |
| 6.11 | T15I5D10000N100, minSup = 0.0001, PFP, Average Tree size for partitions | 32 | | | |
| 6.12 | T15I5D10000N100, minSup = 0.0001, PFP, Maximum Tree size for partitions | 32 | | | |
| 6.13 | T15I5D10000N100, minSup = 0.0001, Average Tree size for 1000 partitions | 33 | | | |
| 6.14 | kosarak, $minSup = 0.001$, SONG 100—1000—500 partitions. | 33 | | | |
| List of Tables | | | | | |
| 2.1 | Consider the following database: | 13 | | | |
| 2.2 | A simple example of distributed FP-Growth: | 17 | | | |

1 Introduction

1.1 Introduction - Add formal definitions of FIS etc... add more about the issue

[TODO]

Describe in the following order:

- 1. Take a lot from the abstract regarding the proposition of the algorithm.
- 2. Add the contribution description here: new algo, testing on spark...
- 3. FIS mining, also mention the usage of association rules
- 4. Apriori and FP-Growth
- problem in paralelism in both cases
- 6. problem in incremental

Mining of frequent items and association rules is a well known and studied field in Computer Science. The algorithms and solutions in this field can be roughly divided into two types - Apriori [2] and tree based solutions [14, 19, 20] Each type has benefits and limitations such as simplicity, performance, memory consumptions and scaling.

In this paper, we will describe an approach for dealing with an incrementally updated database, while avoiding candidate generation, and performing a single DB scan.

We will discuss previous related work, describe current technology and review implementation, usage and performance.

2 Background And Related Work

2.1 Background

2.1.1 Frequent Itemset

Given a set $L = \{i_1, ..., i_n\}$ called items. A set $P = \{i_1, ..., i_k\} \subseteq L$, where $k \in [1, n]$ is called a pattern (or an itemset), or a k-itemset if it contains k items.

A transaction $t = (t_{id}, Y)$ is a tuple where t_{id} is a transaction-id and Y is a pattern. If $P \subseteq Y$, it is said that t contains P or P occurs in t.

A transaction database DB over L is a set of transactions and |DB| is the size of DB, i.e. the total number of transactions in DB. The support of a pattern P in a DB, denoted as Sup(P), is the number of transactions in DB that contain P.

A pattern is called a frequent pattern if its support is no less than a user given minimum support threshold minsup ϑ , with $0 \le \vartheta \le |DB|$.

The frequent pattern mining problem, given a θ and a DB, is to discover the complete set of frequent patterns in a DB having support no less than θ .

Max and Closed Frequent Itemset

We will mention those definition, as later on in section 2.1.3, the used benchmarks are evaluating algorithms which perform Closed FIM. To better understand those definitions [9] provides good illustrations and explanations.

Max Frequent Itemset It is a frequent itemset for which none of its immediate supersets are frequent. In 2.1, the lattice is divided into two groups, red dashed line serves as the dermarcation, the itemsets above the line that are blank are frequent itemsets and the blue ones below the red dashed line are infrequent.

- 1. In order to find the maximal frequent itemset, you first identify the frequent itemsets at the border namely **d**, **bc**, **ad** and **abc**.
- 2. Then identify their immediate supersets, the supersets for **d**, **bc** are characterized by the blue dashed line and if you trace the lattice you notice that for **d**, there are three supersets and one of them, **ad** is frequent and this can't be maximal frequent, for **bc** there are two supersets namely **abc** and **bcd**, **abc** is frequent and so **bc** is NOT maximal frequent.
- 3. The supersets for **ad** and **abc** are characterized by a solid orange line, the superset for **abc** is **abcd** and being that it is infrequent, **abc** is maximal frequent. For **ad**, there are two supersets **abd** and **acd**, both of them are infrequent and so **ad** is also maximal frequent.

Closed Frequent Itemset It is a frequent itemset that is both closed and its support is greater than or equal to minsup. An itemset is closed in a data set if there exists no superset that has the same support count as this original itemset. Figure 2.2 shows the maximal, closed and frequent itemsets. The itemsets that are circled with blue are the frequent itemsets. The itemsets that are circled with the thick blue are the closed frequent itemsets. The itemsets that are circled with the thick blue and have the yellow fill are the maximal frequent itemsets. In order to determine which of the frequent itemsets are closed, all you have to do is check to see if they have the same support as their supersets, if they do they are not closed. For example **ad** is a frequent itemset but has the same support as **abd** so it is NOT a closed frequent itemset; c on the other hand is a closed frequent itemset because all of its supersets, ac, bc, and cd have supports that are less than 3. As we can see there are a total of 9 frequent itemsets, 4 of them are closed frequent itemsets and out of these 4, 2 of them are maximal frequent itemsets. This brings us to the relationship between the three representations of frequent itemsets.

Figure 2.3 demonstrates the relations between the

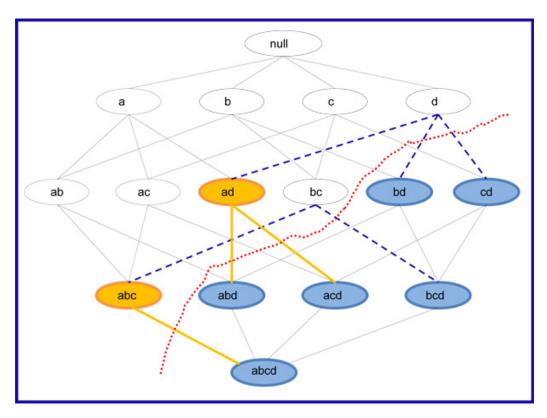


Figure 2.1: Maximal Frequent Itemset Illustration

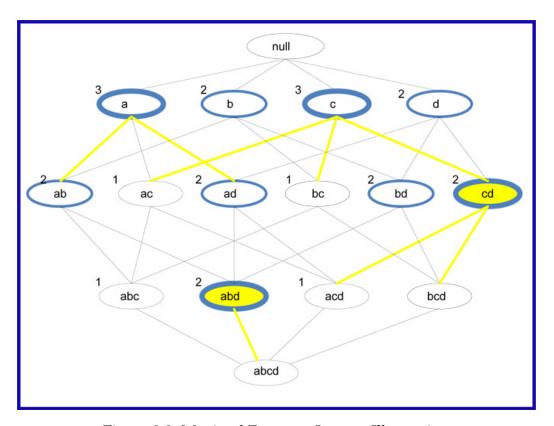


Figure 2.2: Maximal Frequent Itemset Illustration

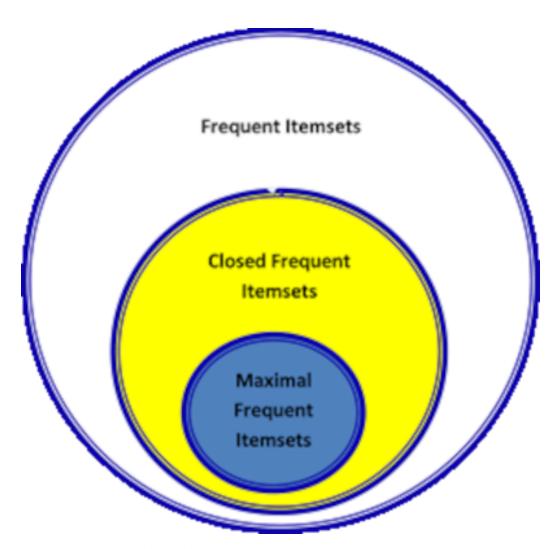


Figure 2.3: Relationship between Frequent Itemset Representations

2.1.2 FP-Tree and FP-Growth

Apriori One of the earliest and most well known algorithms for mining association rules is the Apriori algorithm [2]. This algorithm is iteratively generating candidates and pruning items with low support at each step. The correctness of this algorithm is based on the prove that if an item of length N is frequent, then all sub patterns must be frequent as well. Using that idea, an early prune of non-frequent itemsets removes many unnecessary candidates in later iterations. An example is provided in Figure 2.4. We will not expand further this algorithm, but this algorithm is intuitive and widely used. We would also mention that this algorithm main limitation is the candidate generation at every iteration, where many candidates may not be relevant and this information could have already used in previous stages.

FPGrowth In the year 2000, a tree based solution was introduced, FPGrowth algorithm and the FP-Tree structure [2]. This algorithm removes the need for candidate generation and yields better performance [11].

TODO: Add algo A small example is provided in Figure 2.5

2.1.3 Apache Spark vs Hadoop

The work by Daniele Apiletti et el. [8] is focusing on comparing different frequent itemset mining algorithms between the Apache Hadoop [4] and Apache Spark [7].

This work is performing extensive evaluation on synthetic and real world datasets and testing execution time, load balancing, and communication costs between 4 parallel itemset mining algorithm.

The participating algorithms are:

- 1. The Parallel FP-Growth implementation provided in Hadoop Mahout 0.9 [3]
- 2. The Parallel FP-Growth implementation provided in MLlib for Spark 1.3.0 [5]
- 3. The June 2015 implementation of BigFIM [21]
- 4. The version of DistEclat downloaded from [21] on September 2015

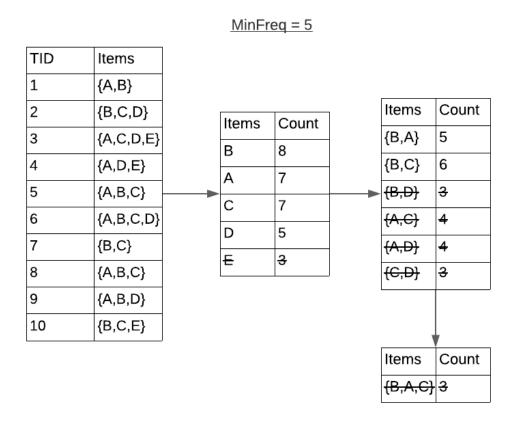


Figure 2.4: Apriori Example

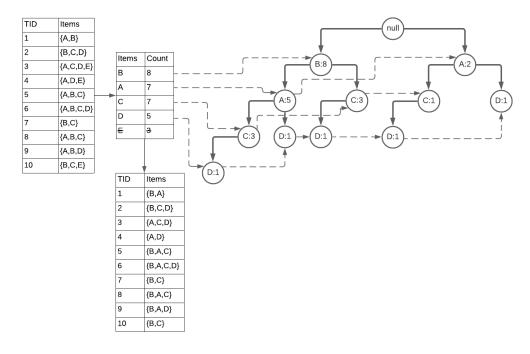


Figure 2.5: FPGrowth example

In our work we are using as the infrastructure, the PFP implementation of the MLLib [5] library in Spark, which is one of the evaluated algorithms in the article [8].

BigFIM and DistEclat are not relevant to this work.

On page 27, the article mentions that except the Spark MLLib PFP [5] algorithm, all other implementations are mining closed itemsets, and thus to obtain the same output, the execution times of Mahout PFP, BigFIM and DistEclat may increase with respect to MLlib PFP.

The evaluations in the paper were done using synthetic and real-world data. The synthetic data and real-world data The results of the paper tested a synthetic and real-world data

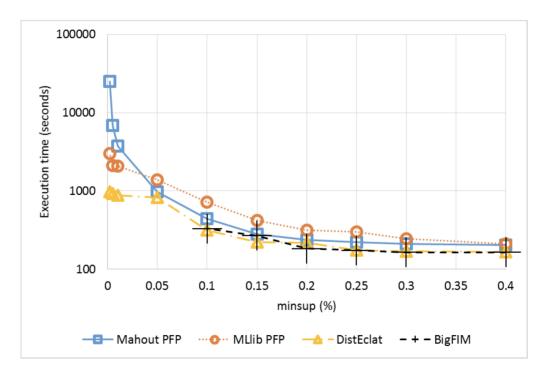


Figure 2.6: Execution time for different min-sup values, average transaction length $10\,$

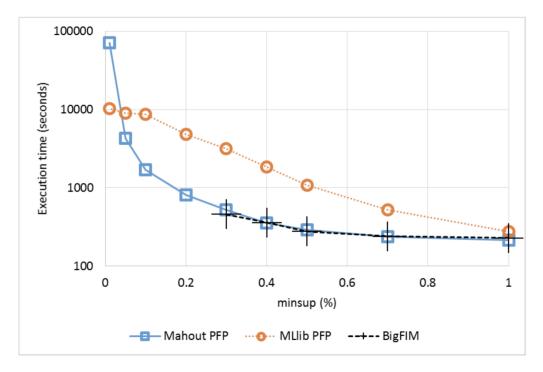


Figure 2.7: Execution time for different min-sup values , average transaction length $30\,$

2.2 RELATED WORK

2.2.1 Incremental Frequent Itemsets Mining

The definition of an Incremental update, is to recompute outputs which depend on the incoming inputs only, without recomputing the whole data.

The challenge while performing incremental updates for frequent items mining, is a non consistent frequency order. Several algorithms such as AFPIM [13], EFPIM [16] and FUFP-tree [10] are keeping an updated frequency based trees, by reordering branches where frequency has changed.

Canonical-Tree The work of [14] presented a Canonical Tree (CanTree) which preserves the frequency descending structure as in FP Growth mining, by relying on a predefined order, which will not affect the tree structure and correctness.

The predefined order, creates some nice properties, as described below:

- 1. Items are arranged according to a canonical order, which is a fixed global ordering.
- 2. The ordering of items is unaffected by the changes in frequency caused by incremental updating.
- 3. The frequency of a node in the CanTree is at least as high as the sum of frequencies of all its children.

Since CanTree preserves same feature as the FP-Tree for mining FIS, the mining is done in the same fasion as the original FP-Growth algorithm.

An example of a CanTree is presented in **Table 2.1** and **Figure 2.8**

CP-Tree The work of [19] proposes an improvement to CanTree, called CompactPattern-Tree, and discusses the memory and computation limitations of CanTree for large incremental Databases. The issues are caused due to un-efficient tree structure, and CP-Tree is proposing an improvement by periodically (using a proposed guideline) updating the order of the construction literals list (l-list) and rebuilding the trees. As mention in the original article and as seen by our experiments, the CanTree and CP-Tree has a similar tree size, and the difference for our test cases was 10% in

| | TID | Contents |
|--------------------------------------|-------|-----------------------------------|
| Original database (DB) | t_1 | a, d, b, g, e, c d, f, b, a, e |
| | t_2 | d, f, b, a, e |
| | t_3 | a |
| | t_4 | d, a, b |
| The first group of insertions (db1) | t_5 | d, a, b a, c, b c, b, a, e |
| | t_6 | |
| The second group of insertions (db2) | t_7 | a, b, c |
| | t_8 | a, b, c |

Table 2.1: Consider the following database:

tree sizes. However as seen in our results, using semi-frequency based order, improves the mining results by 10X and more for smaller minSupport values.

2.2.2 Parallel Frequent Itemsets mining

The difficulty in parallelizing FP-growth is to distribute iterations to parallel trees while still allowing correct mining. PFP [15] is solving this by dividing the DB transactions to independent trees using a Group-List, where every group consists of subgroup of the original items, and redistributing iterations in the DB based on this list. PFP [15] has the following MapReduce stages:

- Step 1: Calculate the global frequency list F-list, by MapReduce "Work Count" manner.
- Step 2: In the second job, the the map will have the following functionality:
 - 1. Sort transactions based on F-list.
 - 2. Replace items in a transaction with the appropriate group id mapped transactions.

The reducer here will build the trees in a parallel manner, based on the group id of the mapping stage.

Step 3: In the final mapping stage, every mapper will project the sub tree from a 1-item-length frequent itemset of the group, where the reducers will recursively mine those sub-trees. The parallelization

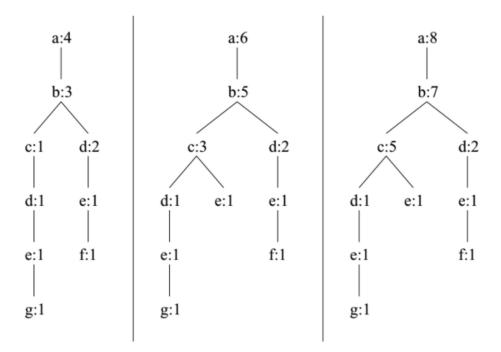


Figure 2.8: The CanTree after each group of transactions is added

in that case, can be at most equal to the number of items in the database.

A more detailed description of PFP [15] is described here **Algorithm 0**:

To better understand the distribution of transactions between groups in PFP, an example is provided in **Table 2.2**. This example shows the initial state of raw transactions, sorting them frequency based, and distributing based on a G-List of single item per group -; {C},{E},{B},{A}. Last lines demonstrate the output at line 9 **Algorithm 0** of every transaction.

2.2.3 Incremental and Parallel Frequent itemsets mining

Combining the previous 2 sections, yields an algorithm that does not rely on frequency order and uses parallelism advantages for computations of FIS. The drawbacks are also drawn from the 2 algorithms - large memory consumption for saving all items and recursively calculating FIS. As we will show later in the Improvments section, using an approach similar to [12] and maintaining a pre-min support, together with using a semi-freq-

Algorithm 1 Highlevel description of the PFP-Growth algorithm

```
1: procedure PFP-GROWTH
        F - List \leftarrow Find global frequency list
        G - list \leftarrow Define a Group items
 3:
        for each transaction T<sub>i</sub> in DB do
 4:
            t_i \leftarrow order by F-List frequency
 5:
            G - hashed - list_i \leftarrow replace every element a_i in t_i with Hash(g),
 6:
    where a_i \in g And g \in G - list
 7:
            for each Hash(g) \in G - hashed - list do
                L \leftarrow \text{find its right-most location in } t_i
 8:
                Output key'=g; value'=t_i[0]...t_i[L]
 9:
            end for
10:
        end for
11:
        Group by key' = g
12:
        For each group g, build appropriate tree
13:
        For each group g, mine the generated tree.
14:
15: end procedure
```

order as in [19], will significantly improve memory and mining runtime results.

2.2.4 Song et al.

A paper by Song et el. [18] proposes 2 techniques for building and mining frequent itemsets - IncBuildingPFP and IncMiningPFP. IncBuildingPFP presents a parallel model based on CanTree that supports incremental mining. This approach is similar to IPFIM and presented in **section 3.1**.

IncMiningPFP

As discussed by Song et el. [18] (and analysed later in this article as well), using CanTree as is, will result in memory and time limitation for relatively medium datasets (¿1M) even with large clusters (¿100G RAM). IncMiningPFP solves the problem of mining by constructing FP-Growth tree for shards with new incremental items. For other shards, the data is taken from cache.

IncMiningPFP consists of the following steps:

Step 1: Group items G-list

Step 2: For the base case, for each shard, save the FIS and construct full FP-Trees to save all transactions.

Step 3: For every Shard:

- 1. calculate and save frequency list per shard group -¿ F-list
- 2. find 1-size FIS, extract paths from FP-Trees that contain only those items and build a FP-Growth tree.
- 3. Extract full FIS from FP-Growth tree and save items in shard cache.
- Step 4: For every iteration dD, devide based on G-List and send to the appropriate shards (similar to same as the distribution stage at **Algorithm 0**).

Step 5: For every shard:

- 1. Recalculate F-list
- 2. If got new items from dD, update tree with new values
- 3. If this shard has added transactions, recalculate new FIS in similar way to initial stage and update shard cache.
- 4. Return Caches FIS.

Step 6: Reduce all previous FIS, similar to PFP.

In this paper, although the IPFIM and IncBuildingPFP are similar, in **section 4.1**, we present a different technique based on the CPTree [19] and AFPIM [13] approach.

Song et el. [18] was also tested using classic map-reduce, while here we test the performance using Spark [TODO: Add section on spark]. Spark programs iteratively run about 100 times faster than Hadoop in-memory, and 10 times faster on disk [7].

Table 2.2: A simple example of distributed FP-Growth:

| | TID | Items |
|--------------------------|---|---------|
| Original database (DB) | t_1 | A, B |
| | t_2 | E, C |
| | t_3 | E, A, C |
| | t_4 | E, C |
| | t_5 | E, C |
| | t_6 | В |
| | t_7 | A, C |
| | t_8 | E, D, C |
| | t ₉ | E, B |
| | t_{10} | E, B |
| | t_{11} | E, A, C |
| | t_{12} | E, C |
| | t_{13} | B, D, C |
| F-List: | A: 4, E: 9, B: 5, C: 9, D: 2 | |
| Support=4 | Sorted transactions = $\frac{1}{6}$ [C,E,B,A] | |
| Sorted and Filtered | t_1 | B,A |
| | t_2 | C,E |
| | t_3 | C, E, A |
| | t_4 | C,E |
| | t_5 | C,E |
| | t_6 | В |
| | t ₇ | C, A |
| | t_8 | C,E |
| | t ₉ | E, B |
| | t_{10} | E, B |
| | t ₁₁ | C, E, A |
| | t_{12} | C,E |
| | t_{13} | C, B |
| G-List | {C},{E},{B},{A} | |
| $g \in G - List$ $\{C\}$ | Transactions | FIS |
| {C} | t ₂ ,t ₃ ,t ₄ ,t ₅ ,t ₇ ,t ₈ ,t ₁₁ ,t ₁₂ ,t ₁₃ | [C] |
| {E} | t ₂ ,t ₃ ,t ₄ ,t ₅ ,t ₈ ,t ₁₁ ,t ₁₂ | [C,E] |
| | t ₉ ,t ₁₀ | [E] |
| {B} | t ₁ ,t ₆ | [B] |
| | t ₉ ,t ₁₀ | [E,B] |
| | t_{13} | [C,B] |
| $\{A\}$ | t_1 | [B,A] |
| - | t ₃ ,t ₁₁ | [C,E,A] |
| | t_7 | [C,A] |

3 IPFIM Algorithm

3.1 IPFIM - Incremental Parallel Frequent Itemsets Mining

The implementation of this algorithm strongly depends on PFP [15]. To support incremental tree updates, we are using a predefined comparison function to arrange the items insertion order, as used in CanTree [14].

3.1.1 IPFIM Outline

The combination of the previously mentioned algorithms will provide an incremental and parallel algorithm for mining FIS. **Figure 3.1** shows an example for a 2 partition calculation of CanTrees based on the partition function of $\{a6, a4, a2\} \rightarrow 0$ and $\{a5, a3, a1\} \rightarrow 1$.

The highlevel steps for the combined algorithm are:

- Step 1: Define a comparison function: compare(item1,item2)-¿bool
- Step 2: Define a Partition function: partition(item)-¿Long
- Step 3: For every increment:
 - 1. PFP: Scan transaction and sort using compare function
 - 2. PFP: Scan sorted transactions and replace using the PFP **Algorithm 0** lines 7:9
 - PFP+CanTree: Update each group partition with the transactions of the group and update the CanTree (save the partial CanTree)
 - 4. PFP: Run FP-Growth on every partitions CanTree and reduce results for final output

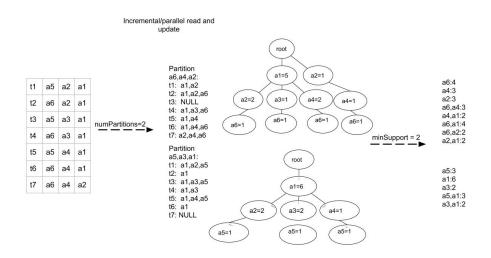


Figure 3.1: IPFIM example

3.1.2 Correctness

The correctness of IPFIM comes directly from the correctness of the 2 combined algorithms. The proof is pretty simple by using contradiction:

- 1. Assuming that the following item-set of length k, $\{t_i,...,t_{i+k-1}\}$, became frequent at iteration l, from transaction T_j , but was not part of the reported output.
- 2. According to **item 2**, transaction T_j is translated to jkey'=g; value'= $t_[0]...t_[k]$; and added to the CanTree of partition g.
- 3. If it was not added at this point, PFP is not correct, false \blacksquare
- 4. Otherwise it was added to the CanTree, but was not mined. CanTree is not correct, false ■.

Similar method is used as a proof of the other use cases - a false frequent itemset, a frequent itemset is no longer frequent etc. [?]

4 IPFIM Improvements

4.1 Improvements - Need to add SetCover results and explanations

While developing and testing the algorithm, 2 main obstacles prevented from using larger datasets and smaller minSupport:

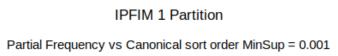
- 1. Memory Tree size.
- 2. Computation Time Tree order.

To handle these obstacles, 2 techniques were implemented. To handle the computation time, an approach similar to CPTree [19] was tested, where we defined a semi-frequency order on 1st dataset half, and used it for the rest of the iterations. New items were sorted canonically.

To handle the memory limitation, which is caused by the construction of a large tree, a partial approach of AFPIM [13] was implemented. We added a pre-min support to identify pre-frequent items. For the simplicity of the experiment, items which where not frequent in iteration i, and will become frequent after sum of j iterations, are waived. A trade-off between missing items and tree size can be controlled using the pre-min parameter.

4.1.1 IPFIM Improved vs IPFIM - Computation

Although the size of the tree was not effected by more than 10%, when using semi-frequency order, computation time was improved by 30X when running single partition, as seen in **Figure 4.1**.



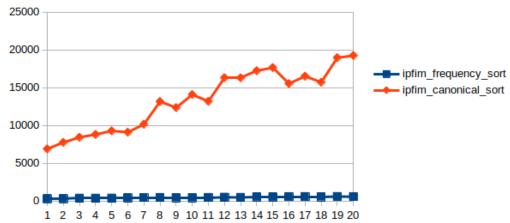


Figure 4.1: IPFIM partial frequency sort vs IPFIM cannonical sort

4.1.2 IPFIM Improved vs IPFIM - Memory

Using a partial approach of AFPIM [13], we were able to run synthetic datasets of 100M transactions and 100k unique item sets. The results, compared to PFP, for 100 partitions, min support of 0.01 and 0.003 can be seen in **Figure 4.2**. As there is only 1 dataset scan for IPFIM, and we pre-defined the semi-frequency order, the results are 10x faster even for 1st iteration, and improve to 25x for last one.

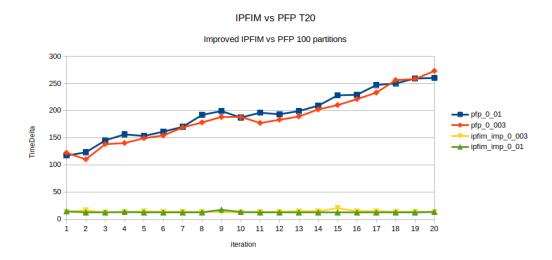


Figure 4.2: IPFIM pre-min, semi-frequency vs PFP

5 Experiment Preparation

5.1 Experiments Preparation

5.1.1 Datasets

For this article, we used 3 datasets:

- 1. Synthetic datasets of 10M transactions, and 2 magnitudes less of items, average length of 15 items. The dataset was generated using IBM Quest Synthetic Data Generator [1].
- 2. Synthetic datasets of 1M transactions, and 2 magnitudes less of items, average length of 15 items. The dataset was generated using IBM Quest Synthetic Data Generator [1].
- 3. The Kosarak dataset contains 990,000 transactions with 41,270 distinct items and an average transaction length of 8.09 items (click-stream data of a hungarian on-line news portal). This dataset was the largest used by [19].

Every dataset was divided in to 5 iterations, $I_0...I_4$, where I_0 is used as a base case with 50% of the transactions, and the remaining 50% are iterations of 12.5% (e.g. base + 4 iterations). The iterations are saved accordingly as files $f_0...f_4$.

For **PFP**, at iteration i, all files of 0...i are re-read and used as the dataset for recalculation of FIS.

5.1.2 Implementation

The implementation was done using Spark [7]. Spark contains an MLlib library, which has an implementation of the PFP algorithm [6]. For our

experiments, we leveraged that implementation and the edits required for IPFIM where minor:

- Step 1: Added support for custom sorting
- Step 2: Added support for filtering items below minMinThresholf value
- Step 3: Added support for logging and statistics

5.1.3 Logging and Statistics

To perform our evaluation of execution and memory performance, we are collecting the statistics of run time and the tree-size of trees in different partitions.

CanTree

For CanTree algorithm implementation, as can be seen From [link to IPFIM algorithm], running IPFIM with only one group, will result in the original CanTree algorithm.

Song et al.

For the algorithm developed by Song et al., we had to add a functionality to calculate the intermediate trees. This is also described in [TODO: Add link to Song diff]. The detailed implementation can be found here [TODO: add link to github?].

Set-Cover-IPFIM

To support set-cover groups, we used a greedy set-cover algorithm to find the group distribution. This group list is later passed to the partitioning of a the transactions.

5.1.4 Infrastructure

The used hardware is 4 clusters each with 20G memory and 40 cores. The provided infrastructure uses a SparkRDMA Plugin [17]. SparkRDMA provides an improvement of 3X to compared to HDFS [TODO:Add RDMA]

banchmarks]. For our experiments, since using same infrastructure, this improvement is not effecting the overall performance differences.

5.1.5 Performance evaluation

For our experiments, we will perform the evaluation of the new proposed algorithms IPFIM, improved-IPFIM and set-cover-IPFIM and compare them to the original algorithms PFP, CanTree as well as the newer Song et al.

The evaluation will review computation time at each iteration, as well as total computation improvement. We also compare the differences in tree sizes for every algorithm and test case. For every iteration we will present the median tree size to better understand the inner structures of the algorithms.

5.1.6 IPFIM vs CanTree

For CanTree [14] performance, we used IPFIM with only one group, meaning a single tree.

Synthetic Dataset

A comparison for 1M transactions (T15D1MN10K) with minSupport of 0.001, partitions of 1, 10 and 100 is seen at ??.

Kosarak Dataset

A comparison with minSupport of 0.001, partitions of 1, 10 and 100 is seen at ??.

6 Experiments Results

6.1 Experiments and Results

6.1.1 Performance Evaluation

Kosarak PFP 100—1000—500 partitions

Figure Figure 6.2

Synthetic Dataset

A comparison for 1M transactions (T15D1MN10K) with minSupport of 0.001, partitions of 1, 10 and 100 is seen at ??.

Kosarak Dataset

A comparison with minSupport of 0.001, partitions of 1, 10 and 100 is seen at ??.

6.1.2 IPFIM vs PFP

For correct PFP [15] mining, a read of all the dataset till that point needs to be performed.

Synthetic Dataset

A comparison for 10M transactions (T15D10MN100K) with minSupport of 0.001, 1K partitions is seen at ??.

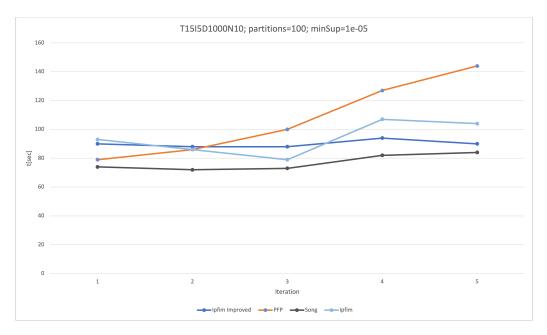


Figure 6.1: T15I5D1000N10 100 partitions

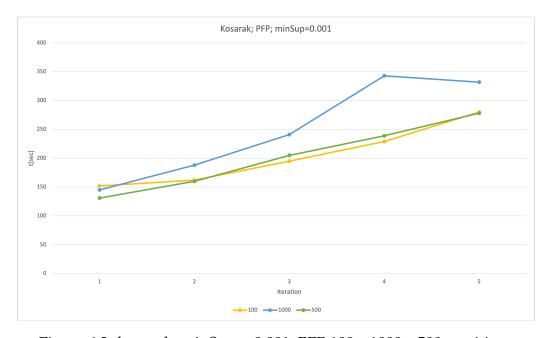


Figure 6.2: kosarak, minSup = 0.001, PFP 100—1000—500 partitions

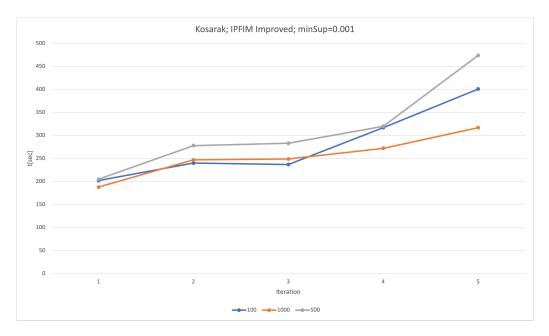


Figure 6.3: kosarak, minSup = 0.001, IPFIM Improved 100—1000—500 partitions

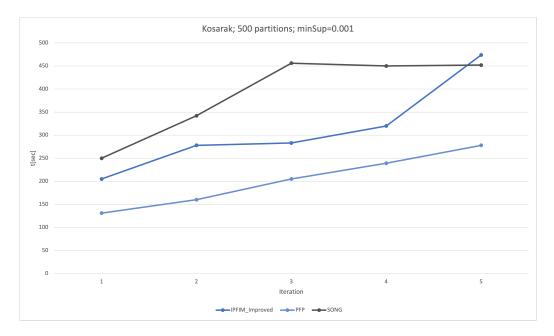


Figure 6.4: kosarak, minSup = 0.001, partitions = 500

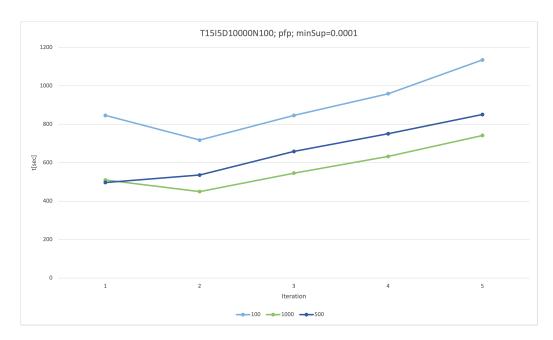


Figure 6.5: T15I5D10000N100, minSup = 0.0001, PFP 100—1000—500 partitions

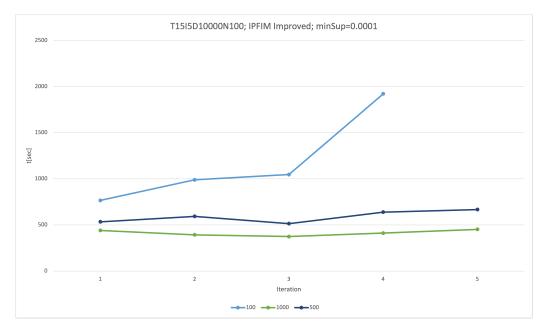


Figure 6.6: T15I5D10000N100, minSup = 0.0001, IPFIM Improved 100—1000—500 partitions

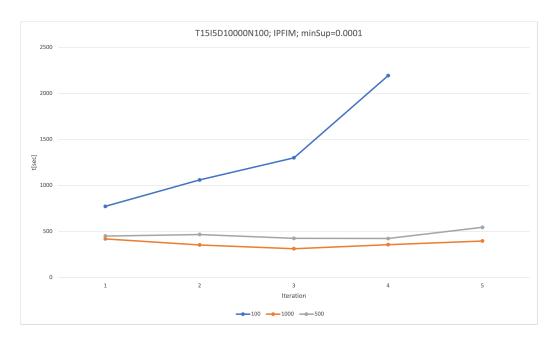


Figure 6.7: T15I5D10000N100, minSup = 0.0001, IPFIM 100—1000—500 partitions

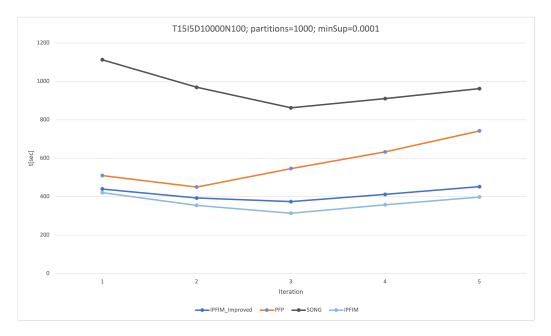


Figure 6.8: T15I5D10000N100, minSup = 0.0001, 1000 partitions

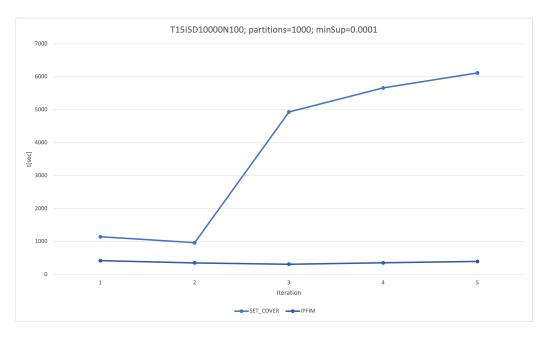


Figure 6.9: T15I5D10000N100, minSup = 0.0001, 1000 partitions, Set cover vs IPFIM

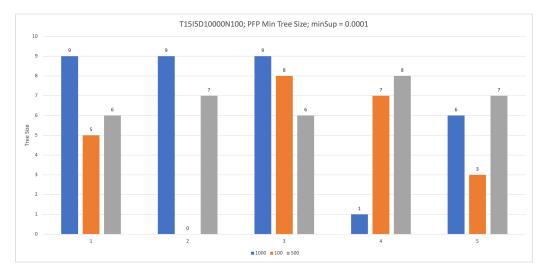


Figure 6.10: T15I5D10000N100, minSup = 0.0001, PFP, Min Tree size for partitions

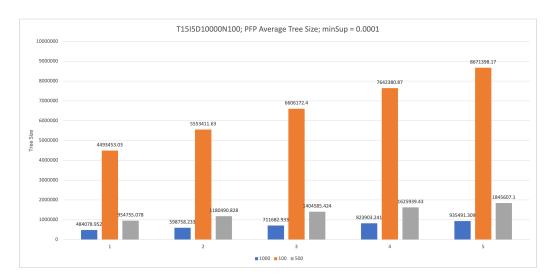
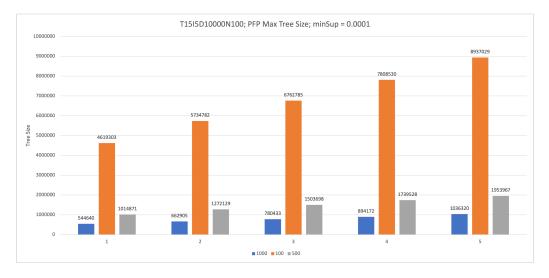


Figure 6.11: T15I5D10000N100, minSup = 0.0001, PFP, Average Tree size for partitions



Figure~6.12:~T15I5D10000N100,~minSup=0.0001,~PFP,~Maximum~Tree~size~for~partitions

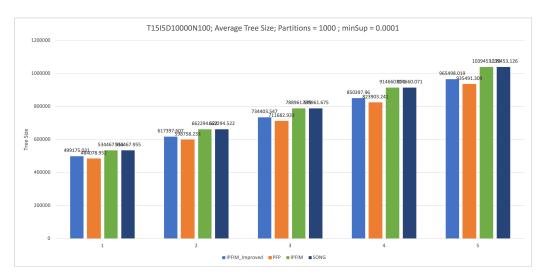


Figure 6.13: T15I5D10000N100, minSup = 0.0001, Average Tree size for 1000 partitions

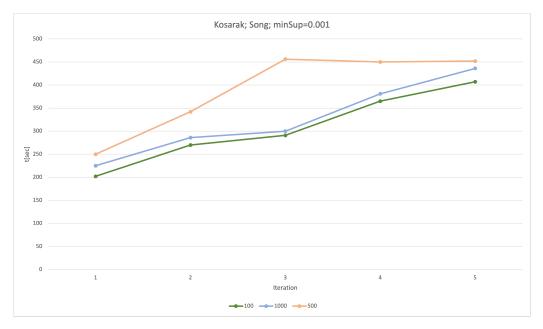


Figure 6.14: kosarak, minSup = 0.001, SONG 100—1000—500 partitions

Kosarak Dataset

A comparison with minSupport of 0.001, partitions of 10 and 100 is seen at ??.

- 6.1.3 improved-IPFIM vs PFP
- 6.1.4 improved-IPFIM vs Song et al.
- 6.1.5 set-cover-IPFIM vs Song et al.

7 Results Discussion

8 Conclusion

8.1 Conclusions

For a single computation of frequent items, the benchmark for performance and memory for IPFIM, is PFP. This is because IPFIM is using similar techniques, and FP tree is the optimal structure for this purpose (except some variations mentioned in previous sections, e.g. optimal sharding). As already mentioned in the *discussion* section, when there is a relatively equal ratio between reading a dataset and computation time of frequent item sets, IPFIM with the suggested improvements out performs PFP. However, for large FIS computation time, this advantage is negligible in total.

Using a canonical order approach, as in Cantree, was almost not practical for large data sets, nor for small min support calculations. The improvement of using a semi-frequency and pre-min support limitation, provides the best balance, and provides best performance.

For future work, it is interesting to enhance PFP to use "smart" grouping. For example trying to use greedy set cover to find groups for of frequent itemsets.

Bibliography

- [1] AGRAWAL, R., AND SRIKANT, R. Quest synthetic data generator. *IBM Almaden Research Center* (1994).
- [2] AGRAWAL, R., SRIKANT, R., ET AL. Fast algorithms for mining association rules. In *Proc. 20th int. conf. very large data bases, VLDB* (1994), vol. 1215, pp. 487–499.
- [3] APACHE. The apache mahout machine learning library,.
- [4] APACHE. The apacheTM hadoop® project develops open-source software for reliable, scalable, distributed computing.
- [5] APACHE. Mllib is apache spark's scalable machine learning library.
- [6] APACHE. Pfp mllib implementation.
- [7] APACHE. Apache spark™ is a unified analytics engine for large-scale data processing, 2020.
- [8] APILETTI, D., BARALIS, E., CERQUITELLI, T., GARZA, P., PUL-VIRENTI, F., AND VENTURINI, L. Frequent itemsets mining for big data: A comparative analysis. *Big Data Research* 9 (2017), 67–83.
- [9] COMPUTER, R. M. V. P. C. C. S. D., AND OF HOUSTON, M. S. D. U. The uh data mining hypertextbook, version 1.
- [10] HONG, T.-P., LIN, C.-W., AND WU, Y.-L. Incrementally fast updated frequent pattern trees. *Expert Systems with Applications* 34, 4 (2008), 2424–2435.
- [11] HUNYADI, D. Performance comparison of apriori and fp-growth algorithms in generating association rules. In *Proceedings of the European computing conference* (2011), pp. 376–381.

BIBLIOGRAPHY 38

[12] KOH, J.-L., AND SHIEH, S.-F. An efficient approach for maintaining association rules.

- [13] KOH, J.-L., AND SHIEH, S.-F. An efficient approach for maintaining association rules based on adjusting fp-tree structures. In *International Conference on Database Systems for Advanced Applications* (2004), Springer, pp. 417–424.
- [14] LEUNG, C.-S., KHAN, Q. I., AND HOQUE, T. Cantree: a tree structure for efficient incremental mining of frequent patterns. In *Fifth IEEE International Conference on Data Mining (ICDM'05)* (2005), IEEE, pp. 8–pp.
- [15] LI, H., WANG, Y., ZHANG, D., ZHANG, M., AND CHANG, E. Y. Pfp: parallel fp-growth for query recommendation. In *Proceedings of the 2008 ACM conference on Recommender systems* (2008), pp. 107–114.
- [16] LI, X., DENG, Z.-H., AND TANG, S. A fast algorithm for maintenance of association rules in incremental databases. In *International Conference on Advanced Data Mining and Applications* (2006), Springer, pp. 56–63.
- [17] MELLANOX. Sparkrdma plugin is a high-performance, scalable and efficient shufflemanager open-source plugin for apache spark., 2020.
- [18] SONG, Y.-G., CUI, H.-M., AND FENG, X.-B. Parallel incremental frequent itemset mining for large data. *Journal of Computer Science and Technology* 32, 2 (2017), 368–385.
- [19] TANBEER, S. K., AHMED, C. F., JEONG, B.-S., AND LEE, Y.-K. Efficient single-pass frequent pattern mining using a prefix-tree. *Information Sciences* 179, 5 (2009), 559–583.
- [20] TSAY, Y.-J., HSU, T.-J., AND YU, J.-R. Fiut: A new method for mining frequent itemsets. *Information Sciences* 179, 11 (2009), 1724–1737.
- [21] UA ADREM. Dist-eclat and bigfim implementation.