

(9)

(123)

Q. When we want to store a -ve number.

First we are going to convert it into binary string of that number if it was positive and then we are going to find the ~~the~~ 2^s complement.

$$i) \therefore 13 \rightarrow \underline{0} \dots \underline{1} \cdot \underline{\frac{1}{0}} \underline{1}$$

\uparrow 31st. bit

$$1^s \text{ complement of } 13 \rightarrow \underline{1} \dots \underline{0} \underline{0} \underline{1} \underline{0}$$

Add 1 for making it ~~the~~ 2^s complement

$$\cancel{2^s} \text{ complement of } 13 \rightarrow$$

$$\boxed{1} \dots \underline{0} \underline{0} \underline{1} \underline{1}$$

\downarrow

-ve.

2^s complement of 13.

★ Largest value that you can store as an integer \rightarrow .

$$\underline{0} \quad \underline{1} \cdot \underline{1} \quad \dots \quad \underline{1} \cdot \underline{1}$$

\uparrow last bit \uparrow 1st bit

$$= 2^{30} + 2^{29} + 2^{28} + \dots 2^0 \\ = 2^{31} - 1 = \text{Int} - \text{Bias}$$

(8)

112

$$\text{ii) } \frac{13}{2^2} = 3$$

$$\text{iii) } \frac{13}{2^4} = 0.$$

→ Why this formula perfectly fits?

$$13 \rightarrow 1101.$$

$$\begin{aligned} \cdot 1101 &\rightarrow 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 \\ &+ 1 \times 2^0 \end{aligned}$$

$$1.3 >> 1.$$

$$\cdot 110 \rightarrow 1 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$$

The second binary is obtained by dividing the 1st binary by two.

How does the computer ~~stores~~^{differentiates} positive and negative number.

The computer stores number in 32 bit ^{or less} signed integer. Inside the 31st bit is used to store the sign.

$$1 \rightarrow -\text{ve} \quad 0 \rightarrow +\text{ve}.$$



31st bit
(sign).

$$0 = 0 \quad 0 \quad 1 \quad 1 \quad 0 \quad 1 \rightarrow 13$$

(7).

212

~~0 1 1 0 1~~ → see we are going to remove this 1

~~0 1 1 0~~ = 13 >> 1.
 ↓
 6. (integer)

ii) $n = 13 \gg 2$

~~0 1 1 0 1~~
 ↓
 0 1 1. → 3. (integer).

iii) $n = 13 \gg 4$

~~0 1 1 0 1~~
 ↓
 0 0. → 0 (integer)

Formula for right shift operator →

$$n \gg k = \left(\frac{n}{2^k} \right)$$

i) $13 \gg 1$

$$\frac{13}{2^1} = 6.$$

(6)

② Or Operator \rightarrow .

1 true means true
all false means false.

a) $n = 13 \mid 7$

number
represent n

$$\begin{array}{r} 1 \\ 0 \\ \hline 1 & 0 & 1 \\ 1 & 1 & 1 \\ \hline 1 & 1 & 1 & 1 \end{array} \quad \begin{array}{l} 13 \\ 7 \\ 19 \end{array}$$

③ X O R Operator \rightarrow .

no. of 1s \rightarrow odd. $\rightarrow 1$.
no. of 1s \rightarrow even $\rightarrow 0$.

a) $n = 13 \wedge 7$

number
repres n

$$\begin{array}{r} 0 . 1 \quad 1 \quad 0 \quad 1 \\ 0 \quad 0 \quad 1 \quad 1 \quad 1 \\ \hline 0 . 0 1 . \quad 0 \quad 1 \quad 0 \end{array} \quad \begin{array}{l} 13 \\ 7 \\ 10 \end{array}$$

(4)

Shift Operators \rightarrow .

a) Right shift operator \rightarrow ($>>$)

i). $n = 13. >> 1$

13 shift by 1

5:

(b) 2^s complement of 7.

$$\begin{array}{r} (0 \ 0 \ 0)_2 \\ \cancel{(0 \ 0 \ 1)}_2 \\ \hline (0 \ 0 \ 1)_2 \end{array}$$

1's complement
Add 1.
2^s complement

Operators

① And Operator → .

- And operator means all true is true.
- One False is false.
- True represents 1 and false represents 0.

(a) $m = 13 \& 7$

$$13 \rightarrow (1 \ 1 \ 0 \ 1)_2 \quad 7 \rightarrow (1 \ 1 \ 1)_2$$

$$\begin{array}{r} 1 \ 1 \ \textcircled{0} \ 1 \\ \textcircled{0} \ 1 \ 1 \ 1 \\ \hline 1 \ 0 \ 1 \ 0 \ 1 \end{array}_2$$

represents
of 5.)

if there is
(0,1) or (0,0)
it will be
considered as 0.

if there is (1,1) then it will be 1.

4.

(1.^s complement)

a) 1^s complement of 13.

$$(13) \rightarrow (1\ 1\ 0\ 1)_2$$

↓ flip all the bits

$$(0\ 0\ 1\ 0)_2$$

Flip all the bits means flipping all the zeroes to one and all the ones to zeroes.

b) 1^s complement of 7.

$$(7) \rightarrow (1\ 1\ 1)_2$$

↓ flip all the bits

$$(0\ 0\ 0)_2$$

(2.^s complement)

Step - 1) Find the 1^s. complement,
Step 2). Add 1 to it.

a) 2^s complement of 13

$$\begin{array}{r} (0\ 0\ 1\ 0)_2 \\ (0\ 0\ 0\ 1) \\ \hline (0\ 0\ 1\ 1)_2 \end{array}$$

1^s complement
Add 1
→ 2^s complement

③

• Zeros are stored in place of the remaining bits.

And when we are printing the value, the computer converts binary format into a number. (decimal).

Computer always converts the number into the binary and then stores it. almost short.

For integers 32 bits is used & we will mostly come across this.

A long int is that signed integral type. that is atleast 32 bits

A long long is a signed integral type. is atleast 64 bits.

The concepts of short int can be applied to long long bits. as they are same.

2

3. 2 1 0 ←

$$\textcircled{c} \quad (1101)_2 \rightarrow (13)_{10}$$

Start from the right and move onto the left.

number \times base ^(index) for each number in the binary equivalent from left to right

$$1 \times 2^0 + 0 \times 2^1 + 1 \times 2^2 + 1 \times 2^3$$

$$1 + 0 + 4 + 8 = (13)_{10}$$

$$\textcircled{d} \quad (11\cancel{1})_2 \rightarrow (7)_{10}$$

~~$$1 \times 2^0 + 1 \times 2^1 + 1 \times 2^2$$~~

$$1 + 2 + 4 = 7$$

When we are writing a number on computer such as 13, it doesn't store the number as 13 instead it stores ~~13~~ in the form 1101. But whenever a computer stores a number it stores in 32 bits (int)

0 0 0 0 - - - 1 1 0 1 . ~~4 bits~~
 28 bits 4 bits

①

Bit Manipulation



Binary Number Conversion
(1's & 2's Complement)

②

$$(7)_{10} \rightarrow (111)_2$$

7 to the
Base 10
(Decimal Number)

Binary
Format

2 7	1 ↑	Remainder of 7/2.
2 3	1 ↑	Remainder of 3/2
2 1	1 ↑	Remainder as 1 is not divisible by 2.

Consider the remainders as strings
and add them in upward direction.

$$"1" + "1" + "1" = 111$$

111 is the Binary Format of $(7)_{10}$

$$(13)_{10}$$

\rightarrow

$$(1101)_2$$

2 13	1 ↑
2 6	0
2 3	1

$$\begin{aligned} "1" + "1" + "0" + "1" \\ = 1101 \end{aligned}$$