

# Exam 2013, questions and answers

Principles of Electrical Engineering (Concordia University)



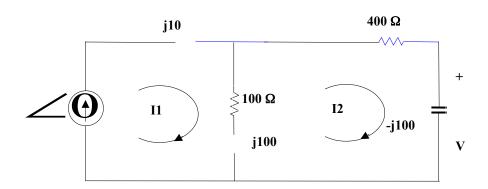
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## **Elec-275: Winter 2013 Final Exam Solution**

- 1. (a) For the time-domain circuit of Fig. 1, draw its phasor domain circuit. [Designate  $I_1$ ,  $I_2$ , and V as the phasors of  $i_1(t)$ ,  $i_2(t)$ , and v(t) respectively]. Draw this phasor circuit.
- (b) Using **mesh analysis** on this phasor circuit, determine I<sub>2</sub> and V. Use the meshes shown.
- (c) Then write the time domain expressions of  $i_2(t)$  and v(t).

# **Solution:**

(a) Phasor circuit:



- (b)  $I_1 = 0.5 \angle 0$ KVL:  $500 I_2 - (100 + j100) I_1 = 0$ ; or  $500 I_2 = (100 + j100) & 0.5 \angle 0 = 50 + j50$ . or  $I_2 = 0,1 + j0.1 = 0.1414 \angle 45$ ;  $V_2 = -j100 I_2 = 14.14 \angle -45$ .
- (c)  $i_2(t) = 0.1414 \cos(1000t + 45)$  amps;  $v_2(t) = 14.14 \cos(10000t 45)$  volts.
- 2. Using **nodal analysis** in the phasor circuit of Fig.2,
  - (a) determine the voltages  $V_2$ ,  $V_3$ , and the current I;
  - (b) draw the phasor diagrams (plot of phasors in the complex plane) of  $V_1$ ,  $V_2$ ,  $V_3$ , and I.

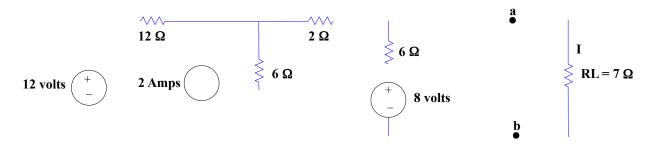
Solution:  
V1 V2 Ref = 0 V  

$$V_2 - 10^{\Omega} = 0$$
 V  
 $V_2 - 10^{\Omega} = 0$  V  
 $V_2 - 10^{\Omega} = 0$  V  
 $V_3 - 10^{\Omega} = 0$   $V_3 = 0$   $V$ 

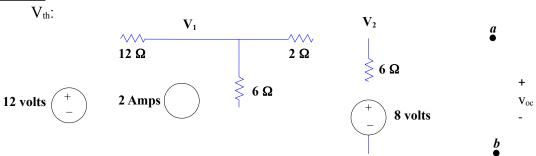
From (1) and (2):  $V_2 = 6.33 \angle 41.6$ ;  $V_3 = 5.3 \angle 24.2$ ;  $I = V_2/(j20) = 0.3165 \angle -$ 

48.4

- (b) Phasor diagrams may now be drawn.
- 3. (a) Replace the circuit to the left of **a b** of Fig. 3 by its **Thevenin** equivalent. Draw this equivalent circuit.
  - (b) Using this equivalent circuits, determine the current I through the load resistor R<sub>L</sub>.

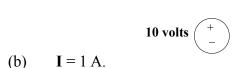


**Solution:** 



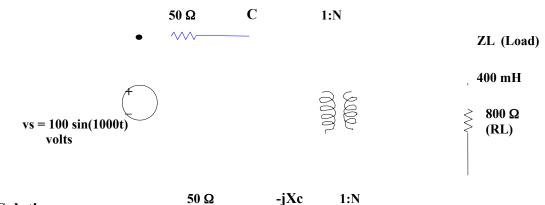
3Ω

 $\mathbf{R}_{th} = 3 \ \Omega$ . Thevenin equivalent:



- 4. An ideal transformer with a turns ratio of N in Fig. 4 is used to match the load  $Z_L$  for maximum power transfer. For that purpose, determine:
  - (a) the transformer turns ratio;

- (b) the value of the capacitor **C**;
- the power absorbed by the load. (c)



**Solution:** 

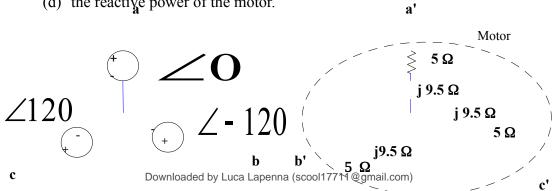


(a): 
$$N^{2} = \frac{800}{50} = 16$$

$$X_{c} = \frac{400}{16} = 25 = \frac{1}{1000 \times C};$$
(b) 
$$C = 40 \,\mu\text{F.}$$

$$(\frac{50}{\sqrt{2}})^{2} = 25$$
(c) 
$$\mathbf{P} = \frac{(\frac{50}{\sqrt{2}})^{2}}{50} = 25 \quad \text{watts.}$$

- 5. A three-phase 60 Hz power supply is connected to a three-phase motor as shown in Fig. 5. Find:
  - (a) the power factor
  - (b) the apparent power of the motor
  - (c) the real power of the motor
  - (d) the reactive power of the motor.



## **Solution:**

Using single phase circuit:  $Z_L = 5 + j9.5 = 10.735$   $\angle$  62.24

(a) **P.F.** =  $\cos 62.24 = 0.4657$ .

(b) 
$$S = \frac{V_{rms}^2}{Z^i} = \frac{120^2}{10.735 \angle -62.24} = 1341.4 \angle 62.24$$
  
Total power = 3 S = 4024.2  $\angle$  62.24  
**Apparent power** = 4024.2 VA

- (c) **Real power**= 1874.34 W
- (d) Reactive power = 3561 VAR.
- 6. For the magnetic circuit of Fig.6:
  - Air gap cross sectional area = 2 cm 6 2 cm (for both gaps)
  - Air gap lengths:

$$l_{g1} = 2 \text{ mm}$$
$$l_{g2} = 4 \text{ mm}$$

- Neglect the reluctance of the magnetic metallic structure (compared to those of the air gaps), as well as the fringing effect.
- The magnetizing coil has 100 turns and carries a current of 0.5 amps.
- (a) Determine, for each air gap:
  - (i) the reluctance  $\mathbf{R}$ :
  - (ii) the flux  $\phi$ .
- (b) Find
  - (i) the flux density  $\mathbf{B}$  for air gap-1 only;
  - (ii) the field intensity **H** for air gap-1 only.
- (c) Find the equivalent reluctance seen by the magnetomotive force **NI**. **Solution:**

$$A = 4$$
  $\stackrel{?}{\iota}$   $10^{-4}$  m<sup>2</sup>.

#### Elec-275: Final 2013 Solution

(a) Air gap 1: (i) 
$$\mathbf{R}_1 = \frac{2 \times 10^{-3}}{4 \pi \times 10^{-7} \times 4 \times 10^{-4}} = 3.98 \times 10^6$$
 A-turns/Wb;

(ii) 
$$q_1 = \frac{NI}{R_1} = \frac{50}{3.98 \times 10^6} = 12.566 \times 10^{-6}$$
 Wb.

- Air gap 2: (i)  $\mathbf{R}_2 = 7.98$  &  $10^6$  A-turns/Wb;
  - (ii)  $\phi_2 = 6.283$  6 10<sup>-6</sup> Wb.

- (c)  $R_{eq} = R_1 \parallel R_2 = 2.65 \text{ A-turn/Wb}.$
- - (b) At full-load:  $I_a = 50 2 = 48$  amps;  $E_b = 240 48$  6 0.4 = 220.8 volts.

(c) Speed = 
$$\omega_m = \frac{220.8}{1.138} \times \frac{60}{2\pi} = 1852.35$$
 rpm.

- (d) Torque =  $(K_a \phi) I_a = 1.138$  6 48 = 54.637 N-m
- (e) Power= Torque i speed = 54.637 i  $\frac{1852.35}{60} \times 2\pi$  = 10,598.4 W = 14.2 HP.