

Ejercicio 3

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11 const A: array[0..m) x (0..n) of int
   const m, n: int
   var fil, col, sumaf, sumac: int
   var premag: bool
   {m > 0 ∧ n > 0}
   fil, sumaf, sumac := 0, 0, 0
   ; premag := false
   {P0: premag ≡ (∃ i, j | 0 ≤ i < fil ∧ 0 ≤ j < n: (∃ w | 0 ≤ w < n: A[i][w]) =
     (∃ z | 0 ≤ z < m: A[z][j])) ∧ (0 ≤ fil < m+1)} {τ0: m - fil}
   do fil < m ∧ premag ≡ false →
     sumaFila(A, m, n, fil, sumaf)
     ; col := 0
     {P1: premag ≡ (∃ j | 0 ≤ j < col: (∃ w | 0 ≤ w < n: A[fil][w]) =
       (∃ z | 0 ≤ z < m: A[z][j])) ∧ (0 ≤ col < n+1)} {τ1: n - col}
     do col < n ∧ premag ≡ false →
       sumaColumn(A, m, n, col, sumac)
       ; premag := (sumaf = sumac)
       ; col := col + 1
     od
     ; fil := fil + 1
   od
   {Q: premag ≡ (∃ i, j | 0 ≤ i < m ∧ 0 ≤ j < n: (∃ w | 0 ≤ w < n: A[i][w]) =
     (∃ z | 0 ≤ z < m: A[z][j]))}

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Procedimientos utilizados

- $\text{proc sumaFila}(\text{in } B: \text{array}[0..p) \times [0..q) \text{ of int,}$
 $\text{in } p, q, f: \text{int}; \text{out suma: int})$

$\{p > 0 \wedge q > 0\}$

$\{Q: \text{suma} = (\sum_{k | 0 \leq k < q: B[f][k]})\}$

[var $t: \text{int}$

$t, \text{suma} := 0, 0$

$\{P: (\sum_{k | 0 \leq k < t: B[f][k]) = \text{suma} \wedge (0 \leq t < q+1)\} \{cota: q-t\}$

do $t < q \rightarrow$

$\text{suma} := \text{suma} + B[f][t]$

$t := t + 1$

od

]

- $\text{proc sumaColumn}(\text{in } B: \text{array}[0..p) \times [0..q) \text{ of int,}$
 $\text{in } p, q, c: \text{int}; \text{out suma: int})$

$\{p > 0 \wedge q > 0\}$

$\{Q: \text{suma} = (\sum_{k | 0 \leq k < p: B[k][c]})\}$

[var $t: \text{int}$

$t, \text{suma} := 0, 0$

$\{P: (\sum_{k | 0 \leq k < t: B[k][c]) = \text{suma} \wedge (0 \leq t < p+1)\} \{cota: p-t\}$

do $t < p \rightarrow$

$\text{suma} := \text{suma} + B[t][c]$

$t := t + 1$

od

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