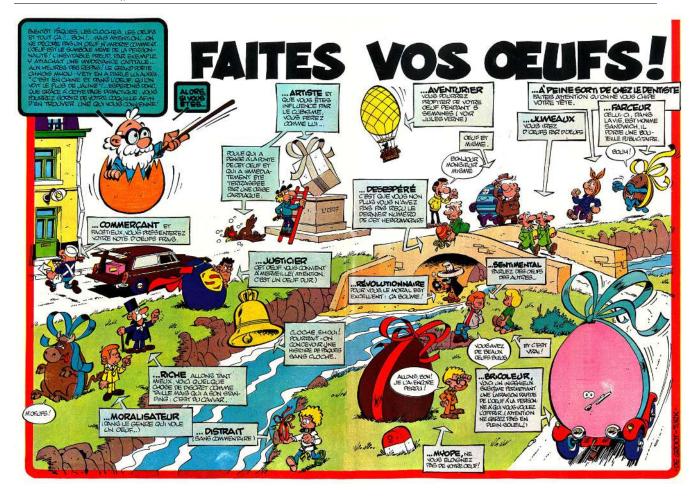
# $\begin{array}{c} {\bf Algorithmics} \\ {\bf Midterm~Exam~\#1} \end{array}$

Undergraduate  $1^{st}$  year S1# EPITA

23 avril 2019 - 13:30

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You must answer on <b>the answer sheets provided</b> . No other sheet will be collected. Keep your rough drafts.
Do not separate the sheets unless they can be re-stapled before handing them in.
The presentation is negatively marked, which means that you are marked out of 20 points and the presentation points (maximum of 2) are taken off this grade.
All Came code not indented will not be marked.
Any Caml code must be followed by its evaluation: the Caml response.
In the absence of any indication in the document, the only functions that you can use are failwith and invalid_arg (no other predefined function of CAML ).
Penciled answers will not be marked.
Duration : 2h (May the force)



## Exercise 1 (Abstract Types: Vector (errors and extension) - 6 points)

Let the algebraic abstract data type *Vector* studied in the course defined as follows.

```
TYPES
      vector
USES
     integer, element, boolean
OPERATIONS
      vect
                           integer \times integer \rightarrow vector
     modify
                           vector \times integer \times element \rightarrow vector
     nth
                           vector \times integer \rightarrow element
     isinit
                          vector \times integer \rightarrow boolean
     lowerlimit
                           vector \rightarrow integer
     upperlimit
                           vector \rightarrow integer
PRECONDITIONS
     nth(v,i) is defined if-and-only-if lower limit(v) \le i \le upper limit(v) \& isinit(v,i) = true
AXIOMS
     lowerlimit(v) \leq i \leq upperlimit(x) + nth(modify(v,i,e),i) = e
```

```
\begin{aligned} \text{lowerlimit}(v) &\leqslant i \leqslant \text{upperlimit}(x) \text{ th}(\text{modify}(v,i,e),i) = e \\ \text{lowerlimit}(v) &\leqslant i \leqslant \text{upperlimit}(v) &\leqslant \text{lowerlimit}(v) \leqslant j \leqslant \text{upperlimit}(v) &\leqslant i \neq j \\ &\Rightarrow \text{nth}(\text{modify}(v,i,e),j) = \text{nth}(v,j) \end{aligned} \begin{aligned} &\text{lowerlimit}(v) &\leqslant i \leqslant \text{upperlimit}(x) &\approx \text{lowerlimit}(v) \leqslant j \leqslant \text{upperlimit}(v) \\ &\Rightarrow \text{isinit}(\text{modify}(v,i,e),j) = \text{true} \\ &\text{lowerlimit}(v) &\leqslant i \leqslant \text{upperlimit}(v) &\approx \text{lowerlimit}(v) \leqslant j \leqslant \text{upperlimit}(v) \\ &\Rightarrow \text{isinit}(\text{modify}(v,i,e),j) = \text{isinit}(v,j) \end{aligned} \begin{aligned} &\text{lowerlimit}(\text{vect}(i,j)) = i \\ &\text{lowerlimit}(\text{vect}(i,j)) = j \\ &\text{lowerlimit}(\text{vect}(i,j)) = j \\ &\text{lowerlimit}(v) &\leqslant i \leqslant \text{upperlimit}(x) \end{aligned}
```

# WITH

```
vector v
integer i, j, k
element e
```

- 1. This definition is incorrect. Indeed, this set of axioms has two problems. For each of these problems, precise its nature, give a description and give a solution to fix it.
- 2. Now that the problems are solved, we have the algebraic type *Vector*. We suggest an extension to this type by defining a new operation: *reinitialize*. This will allow us to set a given position of the vector to its initial state (*i.e. uninitialized*). Its profile is the following:

#### **OPERATIONS**

```
reinitialize: vector \times integer \rightarrow vector
```

- (a) Precise the possible domain of definition of this operation (the preconditions).
- (b) Give the axioms allowing a complete definition of this operation.

## Exercise 2 (Insertion Sort - 7 points)

1. Write the function insert that adds an element in its place in a list sorted according to a given comparison function.

Examples of results:

```
# insert 12 [1;5;9;13;15;28] (function x -> function y -> x <= y) ;;
- : int list = [1; 5; 9; 12; 13; 15; 28]
# insert 12 [28;15;13;9;5;1] (function a -> function b -> a >= b) ;;
- : int list = [28; 15; 13; 12; 9; 5; 1]
# insert 12 [] (function a -> function b -> a >= b) ;;
- : int list = [12]
```

2. Use the function insert to write a function that sorts a list in order according to a given comparison function.

Examples of results:

```
# insertion_sort (function x -> function y -> x >= y) [12;5;47;1;23;0;48;35;3;14;9;11;8;7;65] ;;
- : int list = [65; 48; 47; 35; 23; 14; 12; 11; 9; 8; 7; 5; 3; 1; 0]

# let longer s1 s2 = String.length s1 > String.length s2 ;;
val longer : string -> string -> bool = <fun>
# insertion_sort longer ["Caml"; "C#"; "Python"; "C"; "Javascript"];;
- : string list = ["Javascript"; "Python"; "Caml"; "C#"; "C"]
```

# Exercise 3 (Association - 5 points)

Write down the function assoc k list where k is a natural and list a list of pairs (key, value) sorted in increasing order with respect to keys. We assume keys are always naturals. The function returns the value corresponding to the key k. It raises an exception if k is not a valid key or if it does not correspond to any pair.

Examples of applications:

```
# assoc 5 [(1, "one"); (2, "two"); (3, "three"); (5, "five"); (8, "eight")];;
- : string = "five"

# assoc 4 [(1, "one"); (2, "two"); (3, "three"); (5, "five"); (8, "eight")];;
Exception: Failure "not found".

# assoc (-1) [(1, "one"); (2, "two"); (3, "three"); (5, "five"); (8, "eight")];;
Exception: Invalid_argument "k not a natural".
```

#### Exercise 4 (Mystery – 2 points)

The mystery function is defined as

- 1. Give the results of the successive evaluations of the phrases on the answer sheets.
- 2. What is the return value of mystery?