# 13 imbalanced data weighting

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# 1 Kaggle Titanic survival - Dealing with imbalanced data by model weighting

A problem with machine learning models is that they may end up biased towards the majority class, and under-predict the minority class(es).

Some models (including sklearn's logistic regression) allow for classes to be weighted differently, which penalises the model more when those classes are incorrectly predicted.

Here we create a more imbalanced data set from the Titanic set, by dropping half the survivors.

We create a list of alternative weight balance between the two classes ('died' and 'survived') and the effect of class weights on a range of accuracy measures.

Note: You will need to look at the help files and documentation of other model types to find whether they have options ro change class weights. If a model type does not allow for changign weight classes then other techniques like changing classification thresholds, under-sampling, oversampling, or SMOTE should be considered (described in other notebooks).

```
[1]: # Hide warnings (to keep notebook tidy; do not usually do this)
import warnings
warnings.filterwarnings("ignore")
```

#### 1.1 Load modules

A standard Anaconda install of Python (https://www.anaconda.com/distribution/) contains all the necessary modules.

```
[2]: import numpy as np
  import pandas as pd
# Import machine learning methods
  from sklearn.linear_model import LogisticRegression
  from sklearn.model_selection import train_test_split
  from sklearn.preprocessing import StandardScaler
  from sklearn.model_selection import StratifiedKFold
```

#### 1.2 Load data

The section below downloads pre-processed data, and saves it to a subfolder (from where this code is run). If data has already been downloaded that cell may be skipped.

Code that was used to pre-process the data ready for machine learning may be found at:  $https://github.com/MichaelAllen1966/1804\_python\_healthcare/blob/master/titanic/01\_preprocessing.ipynb$ 

```
[4]: data = pd.read_csv('data/processed_data.csv')
```

The first column is a passenger index number. We will remove this, as this is not part of the original Titanic passenger data.

```
[5]: # Drop Passengerid (axis=1 indicates we are removing a column rather than a row)
# We drop passenger ID as it is not original data

data.drop('PassengerId', inplace=True, axis=1)
```

# 1.3 Artifically reduce the number of survivors (to make data set more imbalanced)

```
[6]: # Shuffle orginal data
data = data.sample(frac=1.0) # Sampling with a fraction of 1.0 shuffles data

# Create masks for filters
mask_died = data['Survived'] == 0
mask_survived = data['Survived'] == 1
```

```
# Filter data
died = data[mask_died]
survived = data[mask_survived]

# Reduce survived by half
survived = survived.sample(frac=0.5)

# Recombine data and shuffle
data = pd.concat([died, survived])
data = data.sample(frac=1.0)

# Show average of survived
survival_rate = data['Survived'].mean()
print ('Proportion survived:', np.round(survival_rate,3))
```

Proportion survived: 0.238

#### 1.4 Define function to standardise data

```
[7]: def standardise_data(X_train, X_test):
    # Initialise a new scaling object for normalising input data
    sc = StandardScaler()

# Set up the scaler just on the training set
    sc.fit(X_train)

# Apply the scaler to the training and test sets
    train_std=sc.transform(X_train)
    test_std=sc.transform(X_test)

return train_std, test_std
```

## 1.5 Define function to measure accuracy

The following is a function for multiple accuracy measures.

```
[8]: def calculate_accuracy(observed, predicted):

"""

Calculates a range of accuracy scores from observed and predicted classes.

Takes two list or NumPy arrays (observed class values, and predicted class values), and returns a dictionary of results.
```

```
1) observed positive rate: proportion of observed cases that are +ve
 2) Predicted positive rate: proportion of predicted cases that are +ve
 3) observed negative rate: proportion of observed cases that are -ve
 4) Predicted neagtive rate: proportion of predicted cases that are -ve
 5) accuracy: proportion of predicted results that are correct
 6) precision: proportion of predicted +ve that are correct
 7) recall: proportion of true +ve correctly identified
8) f1: harmonic mean of precision and recall
9) sensitivity: Same as recall
10) specificity: Proportion of true -ve identified:
11) positive likelihood: increased probability of true +ve if test +ve
12) negative likelihood: reduced probability of true +ve if test -ve
13) false positive rate: proportion of false +ves in true -ve patients
14) false negative rate: proportion of false -ves in true +ve patients
15) true postive rate: Same as recall
16) true negative rate
17) positive predictive value: chance of true +ve if test +ve
18) negative predictive value: chance of true -ve if test -ve
11 11 11
# Converts list to NumPy arrays
if type(observed) == list:
   observed = np.array(observed)
if type(predicted) == list:
   predicted = np.array(predicted)
# Calculate accuracy scores
observed_positives = observed == 1
observed_negatives = observed == 0
predicted_positives = predicted == 1
predicted_negatives = predicted == 0
true_positives = (predicted_positives == 1) & (observed_positives == 1)
false_positives = (predicted_positives == 1) & (observed_positives == 0)
true_negatives = (predicted_negatives == 1) & (observed_negatives == 1)
accuracy = np.mean(predicted == observed)
precision = (np.sum(true_positives) /
             (np.sum(true_positives) + np.sum(false_positives)))
recall = np.sum(true_positives) / np.sum(observed_positives)
sensitivity = recall
```

```
f1 = 2 * ((precision * recall) / (precision + recall))
specificity = np.sum(true_negatives) / np.sum(observed_negatives)
positive_likelihood = sensitivity / (1 - specificity)
negative_likelihood = (1 - sensitivity) / specificity
false_postive_rate = 1 - specificity
false_negative_rate = 1 - sensitivity
true_postive_rate = sensitivity
true_negative_rate = specificity
positive_predictive_value = (np.sum(true_positives) /
                             np.sum(observed_positives))
negative_predicitive_value = (np.sum(true_negatives) /
                              np.sum(observed_positives))
# Create dictionary for results, and add results
results = dict()
results['observed_positive_rate'] = np.mean(observed_positives)
results['observed_negative_rate'] = np.mean(observed_negatives)
results['predicted_positive_rate'] = np.mean(predicted_positives)
results['predicted_negative_rate'] = np.mean(predicted_negatives)
results['accuracy'] = accuracy
results['precision'] = precision
results['recall'] = recall
results['f1'] = f1
results['sensivity'] = sensitivity
results['specificity'] = specificity
results['positive_likelihood'] = positive_likelihood
results['negative_likelihood'] = negative_likelihood
results['false postive rate'] = false postive rate
results['false_negative_rate'] = false_negative_rate
results['true_postive_rate'] = true_postive_rate
results['true_negative_rate'] = true_negative_rate
results['positive_predictive_value'] = positive_predictive_value
results['negative_predicitive_value'] = negative_predicitive_value
return results
```

## 1.6 Divide into X (features) and y (lables)

We will separate out our features (the data we use to make a prediction) from our label (what we are truing to predict). By convention our features are called X (usually upper case to denote multiple features), and the label (survvive or not) y.

```
[9]: X = data.drop('Survived',axis=1) # X = all 'data' except the 'survived' column
y = data['Survived'] # y = 'survived' column from 'data'
```

### 1.7 Assess accuracy, precision, recall and f1 at different model weights

#### 1.7.1 Create a range of weights to use

Logistic regression models take weights as a dictionary in the form {label\_1:weight, label\_2:weight, etc}. Below we will create a list of alterantive weighting schemes.

```
[10]: weights = []
for weight in np.arange(0.02,0.99,0.02):
    weight_item = {0:weight, 1:1-weight}
    weights.append(weight_item)
```

## 1.8 Run our model with different weights

We will use stratified k-fold verification to assess the model performance. If you are not familiar with this please see:

https://github.com/MichaelAllen1966/1804\_python\_healthcare/blob/master/titanic/03\_k\_fold.ipynb

```
[11]: # Create NumPy arrays of X and y (required for k-fold)
X_np = X.values
y_np = y.values

# Create lists for overall results

results_accuracy = []
results_precision = []
results_recall = []
results_f1 = []
results_predicted_positive_rate = []

# Loop through list of model weights

for weight in weights:

# Create lists for k-fold results
kfold_accuracy = []
```

```
kfold_precision = []
   kfold_recall = []
   kfold_f1 = []
   kfold_predicted_positive_rate = []
    # Set up k-fold training/test splits
   number of splits = 5
   skf = StratifiedKFold(n_splits = number_of_splits)
    skf.get_n_splits(X_np, y_np)
    # Loop through the k-fold splits
   for train_index, test_index in skf.split(X_np, y_np):
        # Get X and Y train/test
       X_train, X_test = X_np[train_index], X_np[test_index]
        y_train, y_test = y_np[train_index], y_np[test_index]
        # Get X and Y train/test
       X_train_std, X_test_std = standardise_data(X_train, X_test)
        # Set up and fit model
       model = LogisticRegression(solver='lbfgs', class_weight=weight)
       model.fit(X_train_std,y_train)
        # Predict test set labels and get accuracy scores
       y_pred_test = model.predict(X_test_std)
        accuracy_scores = calculate_accuracy(y_test, y_pred_test)
       kfold_accuracy.append(accuracy_scores['accuracy'])
       kfold_precision.append(accuracy_scores['precision'])
       kfold_recall.append(accuracy_scores['recall'])
       kfold_f1.append(accuracy_scores['f1'])
       kfold_predicted_positive_rate.append(
            accuracy_scores['predicted_positive_rate'])
    # Add mean results to overall results
   results_accuracy.append(np.mean(kfold_accuracy))
   results_precision.append(np.mean(kfold_precision))
   results_recall.append(np.mean(kfold_recall))
   results fl.append(np.mean(kfold f1))
   results_predicted_positive_rate.append(
       np.mean(kfold predicted positive rate))
# Transfer results to dataframe
results = pd.DataFrame(weights)
results['accuracy'] = results_accuracy
results['precision'] = results_precision
results['recall'] = results_recall
```

```
results['f1'] = results_f1
results['predicted_positive_rate'] = results_predicted_positive_rate
```

#### 1.8.1 Print results

## [12]: print(results.to\_string())

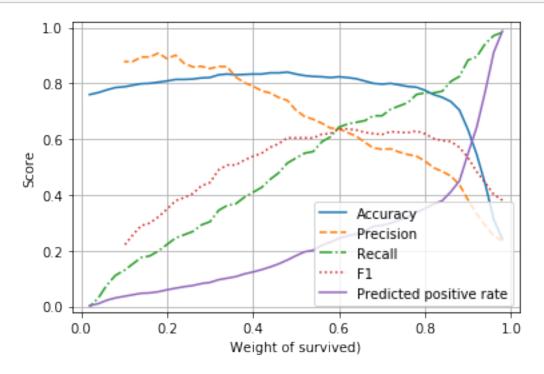
```
0
                                                      f1 predicted_positive_rate
             1
               accuracy precision
                                       recall
0
    0.02
          0.98
                0.241691
                           0.236273 0.982857
                                               0.380939
                                                                         0.987528
1
    0.04
          0.96
                0.311127
                           0.252682
                                     0.971261
                                               0.400950
                                                                         0.912556
    0.06
                0.438956
                                                                         0.770838
2
          0.94
                           0.290358
                                     0.942017
                                               0.443690
3
    0.08
          0.92
                0.545873
                           0.331241
                                     0.895126
                                               0.483374
                                                                         0.641679
4
    0.10
          0.90
                0.633336
                           0.382384
                                     0.883361
                                               0.533505
                                                                         0.548641
5
    0.12
          0.88
                0.704103
                           0.436801
                                     0.824538
                                               0.570236
                                                                         0.450057
6
    0.14
          0.86
                0.734640
                           0.467524
                                     0.806891
                                                                         0.411167
                                               0.591378
7
                0.749918
    0.16
          0.84
                           0.484329
                                     0.771765
                                               0.594673
                                                                         0.379222
8
    0.18
          0.82
                0.759650
                           0.497251
                                     0.765882
                                               0.602309
                                                                         0.366712
9
    0.20
          0.80
                0.774890
                           0.521235
                                     0.765882
                                               0.618893
                                                                         0.351473
                           0.538928
   0.22
          0.78
10
                0.785992
                                     0.760000
                                               0.628964
                                                                         0.337593
11
   0.24
          0.76
                0.788769
                           0.544896
                                     0.730756
                                               0.623032
                                                                         0.320926
12 0.26
                0.794344
                           0.553473
          0.74
                                     0.718992
                                               0.624511
                                                                         0.309796
                                                                         0.298694
13 0.28
          0.72
                0.799890
                           0.565136
                                     0.707227
                                               0.626980
14 0.30
          0.70
                0.797084
                           0.563520
                                     0.683697
                                               0.616584
                                                                         0.290370
15 0.32
          0.68
                0.799871
                           0.568079
                                     0.683697
                                               0.619561
                                                                         0.287583
   0.34
          0.66
                0.808166
                           0.588699
                                     0.666050
                                               0.624040
                                                                         0.270916
16
                0.816480
17
   0.36
          0.64
                           0.610763
                                     0.660168
                                               0.632842
                                                                         0.259824
18
   0.38
          0.62
                0.820637
                           0.623129
                                     0.654286
                                               0.636233
                                                                         0.252889
   0.40
          0.60
                0.823424
                           0.636943
                                     0.642857
                                                                         0.244585
19
                                               0.636864
                0.820676
20 0.42
          0.58
                           0.639588
                                     0.608067
                                               0.619831
                                                                         0.230705
21 0.44
          0.56
                0.823444
                           0.656934
                                     0.590420
                                               0.617513
                                                                         0.219603
22 0.46
                0.824852
          0.54
                           0.671004
                                     0.555294
                                               0.603881
                                                                         0.201528
23 0.48
          0.52
                0.827659
                           0.681178
                                     0.549580
                                               0.604690
                                                                         0.195963
24 0.50
          0.50
                0.833234
                           0.703342
                                     0.531933
                                                                         0.182016
                                               0.604176
25 0.52
          0.48
                0.840188
                           0.738762
                                     0.514286
                                               0.604974
                                                                         0.166728
26 0.54
          0.46
                0.837458
                           0.749111
                                     0.479328
                                               0.583324
                                                                         0.152829
27
   0.56
          0.44
                0.837468
                           0.765044
                                     0.455798
                                               0.570581
                                                                         0.141689
28 0.58
          0.42
                0.833301
                           0.773304
                                     0.426723
                                               0.549245
                                                                         0.131966
29 0.60
          0.40
                0.833321
                           0.789706
                                     0.409244
                                                                         0.123633
                                               0.538430
                                     0.391597
30 0.62
          0.38
                0.831932
                           0.802381
                                               0.524652
                                                                         0.116689
31
   0.64
          0.36
                0.830533
                           0.822318
                                     0.368067
                                               0.507092
                                                                         0.106937
32 0.66
          0.34
                0.833301
                           0.859412
                                     0.362185
                                               0.507141
                                                                         0.101391
33 0.68
          0.32
                0.830514
                           0.860721
                                     0.344538
                                               0.489440
                                                                         0.095845
34 0.70
          0.30
                0.820820
                           0.852708
                                     0.303866
                                                                         0.086152
                                               0.444136
          0.28
35 0.72
                0.819451
                           0.860985
                                     0.292269
                                               0.432262
                                                                         0.081985
36 0.74
          0.26
                0.815294
                           0.858939
                                     0.268739
                                               0.404819
                                                                         0.075031
37 0.76
          0.24
                0.813905
                           0.871667
                                     0.256975
                                               0.390043
                                                                         0.070864
```

```
38 0.78 0.22 0.813924
                         0.900866 0.245378 0.379396
                                                                  0.065308
39 0.80 0.20 0.808388
                         0.888492 0.222185 0.348680
                                                                  0.059772
40 0.82 0.18 0.804202
                         0.908333 0.198824 0.321220
                                                                  0.052827
41 0.84 0.16 0.800016
                         0.894286 0.181176 0.298791
                                                                  0.048641
42 0.86 0.14 0.798627
                         0.894286 0.175294 0.289615
                                                                  0.047252
43 0.88 0.12 0.793071
                         0.877778 0.151933 0.255388
                                                                  0.041697
44 0.90 0.10 0.787535
                         0.877778 0.128739 0.216873
                                                                  0.036160
45 0.92 0.08 0.784766
                             NaN 0.111261
                                                NaN
                                                                  0.030614
46 0.94 0.06 0.776423
                             NaN 0.076303
                                                NaN
                                                                  0.022271
47 0.96 0.04 0.766711
                             NaN 0.029412
                                                NaN
                                                                  0.009761
48 0.98 0.02 0.759727
                             NaN 0.000000
                                                                  0.002778
                                                NaN
```

#### 1.8.2 Plot results

```
[13]: import matplotlib.pyplot as plt
      %matplotlib inline
      chart_x = results[1]
      plt.plot(chart_x, results['accuracy'],
               linestyle = '-',
               label = 'Accuracy')
      plt.plot(chart_x, results['precision'],
               linestyle = '--',
               label = 'Precision')
      plt.plot(chart x, results['recall'],
               linestyle = '-.',
               label = 'Recall')
      plt.plot(chart_x, results['f1'],
               linestyle = ':',
               label = 'F1')
      plt.plot(chart_x, results['predicted_positive_rate'],
               linestyle = '-',
               label = 'Predicted positive rate')
      plt.xlabel('Weight of survived)')
      plt.ylabel('Score')
      plt.xlim(-0.02, 1.02)
      plt.ylim(-0.02, 1.02)
      plt.legend(loc='lower right')
      plt.grid(True)
```

plt.show()



# 1.9 Observations

- Accuracy is maximised when classes are equally weighted.
- When weights are equal the minority class ('survived') is underpredicted.
- A weight of 0.6 for survived (c.f. 0.4 for non-survived) balances precision and recall and correctly estimates the proportion of passengers who survive.
- There is a marginal reduction in overall accuracy in order to balance accuracy of the classes.