The University Interscholastic League Number Sense Test • HS A • 2019

Tumbe	di Selise Test • 115 /1 • 201)			
		Final		
Contestant's Number		2nd		
		1st		
Read directions carefully D before beginning test	O NOT UNFOLD THIS SHEET UNTIL TOLD TO BEGIN		Score	Initials
Directions: Do not turn this page until the person cond 80 problems. Solve accurately and quickly as many as SOLVED MENTALLY. Make no calculations with each problem. Problems marked with a (*) require a five percent of the exact answer will be scored correct; The person conducting this contest should explain	you can in the order in which they appear. ALL paper and pencil. Write only the answer in tapproximate integral answers; any answer to a all other problems require exact answers.	L PROBLEM the space prov	IS ARE 'ided at the	TO BE e end of
	STOP WAIT FOR SIGNAL!			
(1) 111 — 209 + 219 =	(18) 11129 ÷ 6 has a remair	ıder of		
(2) 201 + 911 — 129 =				
(3) 209 × 11 =	*(20) 902111 ÷ 2019 =			
$(4) 29^2 = \underline{\hspace{1cm}}$	(21) 1993 × 7 + 49 =			
(5) $15 + 24 + 33 + 42 + 51 =$	(22) 15% of 60 is 25% of _			
(6) $\frac{3}{8} = $ % (dec	cimal) (23) The product of the root	ts of $2x^2 - 3$	3x - 4 =	0 is
(7) 45 + 67 + 89 =	(24) $(3^3 + 6 \times 9) \div 4$ has a	remainder (of	
$(8) \ 90 \div 3\frac{1}{3} = \underline{\hspace{1cm}}$	(25) $1600 = [2(16 + k)]^2$. Fin	nd k ≥ 0 .		
(9) MMXIX =	(26) 15 × 52 =			
*(10) 111 + 2019 + 902 + 9102 =	(27) If $f(x) = x^3 - 3x^2$ then	f(5) =		
(11) If 1 gram = .04 oz., 1200 grams =	and a positive difference	_		
$(12) \ \frac{7}{2(5^3)} = \underline{\qquad} (dec$	(29) 56 ₈ =			
(13) $6\frac{1}{8} - 2\frac{3}{4} =$ (mixed num	mber) $*(30) \sqrt{111209} =$			
$(14) \sqrt[3]{2197} = \underline{}$	a + b + c =	$x^2 + bx + c$	then	
$(15) \ 35 + 30 \div 25 \times (20 - 15) = \underline{\hspace{1cm}}$	(32) The set {p,0,w,e,r} has			
$(16) \ 56^2 - 64^2 = 8 \times \underline{\hspace{1cm}}$	(33) The sum of the positive	integral div	visors of	40 is
(17) The smallest prime number greater than 47 is				

- $(34) 52 \times 58 =$
- (35) The discriminant of $x^2 4x + 2$ is _____
- (36) A nonagon has how many sides?
- (37) How many positive integers less than 36 are relatively prime to 36?
- (38) $6\frac{1}{8} \div 1\frac{3}{4} =$ ______ (mixed number)
- (39) If $2^{2x} = 32$, then x =_____
- *(40) 142.857 × 138 =
- (41) The x-intercept of 2x 3y = 4 is (a, b). Find a.
- (42) The lengths of the legs of a right triangle are 7" and 24". The hypotenuse length is "
- (43) Evaluate $16(xy)^{\frac{1}{2}}$ if x = 4 and y = 9.
- (44) $5^7 \div 9$ has a remainder of _____
- $(45) (234_6)(5_6) = ____6$
- (46) Find x, x < 0, if |3x 5| = 7.
- (47) $(i)^{14} = a\sqrt{b}$, where $a,b \in \{-1,1\}$. Find a. _____
- (48) A ribbon 2 yards 2 feet 9 inches long is cut into 3 equal pieces. How long is each piece? _____ "
- $(49) 1 + 3 + 5 + 7 + ... + 19 + 21 = \underline{\hspace{1cm}}$
- *(50) 14 × 21 × 28 × 35 =
- (51) If ${}_{8}C_{n}$ = 56, then the largest value of n is _____
- (52) The roots of $2x^3 9x^2 + 10x 3 = 0$ are d, e, and f. Find (d + e)(e + f)(f + d).
- (53) $\log_2(16) = \log_8($ ______)
- (55) $8 \times \frac{13}{15} =$ (mixed number)
- (56) Given: 2,5,10,17,26,37,k,65,... . k = _____
- (57) The probability of losing is 48%. The odds of winning is ______ (improper fraction)

- (58) Find the sum of the reciprocals of the first eight triangular numbers.
- (59) $555 \times \frac{6}{37} =$
- *(60) $\left(\frac{\sqrt{5}+1}{2}\right) \times 10^3 =$ _____
- (61) How many ways can 5 people be seated in a circle of 6 chairs?
- (62) If A = $\begin{bmatrix} 3 & 5 \end{bmatrix}$ and B = $\begin{bmatrix} 5 \\ 3 \end{bmatrix}$ then AB = [x]. x =_____
- (63) $\frac{1}{3} + \frac{1}{9} + \frac{1}{27} + \frac{1}{81} + \dots = \underline{\hspace{2cm}}$
- (64) If $\sin(38^\circ) = \cos(A)$ and A is in QI then $A = \underline{\hspace{1cm}}^\circ$
- (65) Let $15^5 \div 5 = (3^x)(5^y)$. Find y x = _____
- (66) 40° C = _____° F
- (67) If 5 men can do a job in 5 days working together, then how long would it take 1 man to do the same job? ______ day(s)
- (68) Change $\frac{7}{16}$ to a base 4 decimal. _____ base 4
- (69) The harmonic mean of the roots of $2x^3 9x^2 + 10x 3 = 0 \text{ is}$
- *(70) (24)⁴ = _____
- (71) Find $x, 0 \le x \le 4$, if $2x 4 \equiv 6 \pmod{8}$.
- (72) How many positive 2-digit numbers end in 2? ____
- (73) If $31_b = 19$ then $13_b =$ _____
- (74) Let $f(x) = x^3 2x^2 3x + 4$. Find f''(5).
- $\lim_{x \to \infty} \frac{7x}{x 7} = \underline{\hspace{1cm}}$
- $(76) \int_{-2}^{2} (x^4) dx = \underline{\hspace{1cm}}$
- (77) 0.0303... base 5 = _____ base 5 (fraction)
- (78) $6^2 5^2 + 4^2 3^2 + 2^2 1 =$
- (79) 347 × 16 = _____
- *(80) 444 ÷ 555 × 666 = _____

University Interscholastic League - Number Sense Answer Key HS ● Invitation A ● 2019

*number) x - y means an integer between x and y inclusive

NOTE: If an answer is of the type like $\frac{2}{3}$ it cannot be written as a repeating decimal

(1) 121

(18) 5

(34) 3,016

 $(58) \frac{16}{9}, 1\frac{7}{9}$

(2) 983

(19) \$20.00

(35) 8

(59) 90

(3) 2,299

*(20) 425 — 469

(36) 9

*(60) 1,538 — 1,698

(4) 841

(21) 14,000

(37) 12

(61) 120

(5) 165

(22) 36

 $(38) \ 3\frac{1}{2}$

(62) 30

(6) 37.5

(23) - 2

(39) 2.5, $\frac{5}{2}$, $2\frac{1}{2}$

(63) $.5, \frac{1}{2}$

(7) 201

(24) 1

*(40) 18,729 — 20,699

(64) 52

(8) 27

(25) 4

(41) 2

(65) - 1

(9) 2,019

(26) 780

(42) 25

(66) 104

*(10) 11,528 — 12,740

(27) 50

(43) 96

(67) 25

(11) 48

(28) 7

(44) 5

(68) .13

(12) .028

(29) 64

(45) 2102

(69) .9, $\frac{9}{10}$

 $(13) 3\frac{3}{8}$

*(30) 317 — 350

(31) - 16

 $(46) - \frac{2}{3}$

*(70) 315,188 — 348,364

(14) 13

(32) 31

(47) - 1

(71) 1

(15) 41

(33) 90

(72) 9

(16) - 120

(49) 121

(48) 35

(73) 9

(17) 53

*(50) 273,714 — 302,526

(74) 26

(51) 5

(75) 7

(52) 21

(76) 12.8, $\frac{64}{5}$, $12\frac{4}{5}$

(53) 4,096

 $(77) \frac{1}{13}$

(54) 10011101

(78) 21

(55) $6\frac{14}{15}$

(79) 5,552

*(80) 507 - 559

(56) 50

 $(57) \frac{13}{12}$

The University Interscholastic League Number Sense Test ◆ HS B ◆ 2019

Final _____

Contestant's Number			2nd	
Read directions carefully before beginning test		UNFOLD THIS SHEET TOLD TO BEGIN	1st In	itials
Directions: Do not turn this page until 80 problems. Solve accurately and quic SOLVED MENTALLY. Make no caeach problem. Problems marked with a five percent of the exact answer will be The person conducting this contest s	kly as many as you can in alculations with paper and a (*) require approxima scored correct; all other	the order in which they appear d pencil. Write only the answ te integral answers; any answ problems require exact answer	ar. ALL PROBLEMS ARE TO lear in the space provided at the enderer to a starred problem that is with	BE d of
The person conducting this contest s	-	WAIT FOR SIGNAL!		
(1) 215 + 316 + 19 =		(19) \$2.40 is	% tax on \$3	0.00
(2) 2019 — 1516 — 3 =		*(20) 316 × 215 =		
(3) 15 × 16 + 19 =		$(21) 1691 \times 9 + 81 = $		
(4) 1516201 ÷ 9 has a remainder of		(22) 0.4666 =	(proper fract	ion)
(5) $\frac{5}{8} = $	% (decimal)	(23) 151 ₆ =		_ 10
$(6) \ \frac{5}{14} + \frac{3}{7} - 1 = \underline{\hspace{1cm}}$			nterest on \$3200.00 at 5.25% f	
$(7) 17 + 21 + 25 + 29 + 33 = \underline{\hspace{1cm}}$		$(25) \ 6\frac{1}{3} \times 9\frac{2}{3} = \underline{\hspace{1cm}}$	(mixed numb	er)
$(8) \ \ 3\frac{2}{9} - 1\frac{2}{3} = \underline{\hspace{1cm}}$	_ (mixed number)	(26) Let $n = \sqrt[3]{3375}$. F	Find n ²	
(9) The multiplicative inverse of 1.7	' is			
* (10) 2153 + 1620 + 1921 + 5316 = _		13 12	of_	
(11) The median of 2,1,5,3,1,2,0,1 and	19 is		more than $\frac{1}{2}$?	
$(12) 15 \times 16 + 19 \times 15 = \underline{\hspace{1cm}}$			2	
(13) The largest prime divisor of 352	is			
(14) 53 × 47 =		(31) Let $(2x + 3)(4x - 5)(4x + 5)(4x - 5)(4x$	$-1) = ax^2 + bx + c.$	
(15) 4 gallons -2 quarts -1 pint =	pints			
$(16) 15 - 16 \times 2^0 \div (1+9) = \underline{\hspace{1cm}}$			of $8x^2 + 10x - 3 = 0$ is	
(17) MDXVI =	(Arabic Numeral)		ents, set B has 8 elements, and	
(18) The smallest prime number large	er than 67 is	` ,	ents. $A \cup B$ has elem	

- (35) Find k, if $kx^2 x 12 = 0$ and the product of the roots is -2. k =
- (36) The angle complementary to 32° measures _____°
- (37) 1101₂ = ______4
- (38) The 4-digit number 215k is divisible by 8. k =____
- (39) The LCM of 12, 18 and 20 is _____
- * $(40) 16^3 =$ ______
- (41) If $4^x = 24$, then $4^{(x+1)} =$
- (42) If x + y = 8 and x y = 2, then xy =
- (43) The area of a circle is 24π in². The diameter of this circle is $a\sqrt{b}$ in., where a > 1. Find a + b.
- $(44) 74^2 66^2 = \underline{\hspace{1cm}}$
- (45) The coefficient of the x^2y^2 term in the expansion of $(3x-2y)^4$ is _____
- (46) 132 × 111 = ____
- (47) $(i)^{16} = a\sqrt{b}$, where $a,b \in \{-1,1\}$. Find b. _____
- $(48) \ \ (316_7) \div (4_7) = \underline{\hspace{1cm}} 7$
- $(49) \ \frac{3}{5} + \frac{3}{25} + \frac{3}{125} + \frac{3}{625} + \dots = \underline{\hspace{1cm}}$
- *(50) $\sqrt{1516} \times \sqrt{2019} =$ _____
- $(51) \log 4 \log 400 = \underline{\hspace{1cm}}$
- (52) The roots of $x^3 + x^2 2x = 0$ are d, e, and f. Find (d + e)(e + f)(f + d).
- (53) $\frac{4\pi}{5}$ radians = ______ degrees
- (54) The vertex of the parabola $x^2 6x 12$ is (h, k) and k =
- (55) If 3P = 4Q and 2Q = 5R then P = _____R
- (56) Given: 4,6,10,14,22,26,34,k,46,... . k = _____
- (57) $7 \times \frac{11}{13} =$ (mixed number)
- $(58) \ \frac{1}{3} + \frac{1}{6} + \frac{1}{10} + \frac{1}{15} + \dots \frac{1}{78} + \frac{1}{91} = \underline{\hspace{1cm}}$

- (59) Let $(a 5i)^2 = -9 40i$. Find a.
- * $(60) (31)^6 \div (21)^5 =$
 - (61) How many ways can 4 people be seated in a circle of 6 chairs?
- $(62) 1234 \times 8 + 4 = \underline{\hspace{1cm}}$
- (63) The odds of passing the test is $\frac{13}{15}$. The probability of failing the test is _____ (proper fraction)
- (64) $\sin(\operatorname{Arcsin}(\frac{3}{5}) = \underline{\hspace{1cm}}$
- (65) The first four digits of the decimal for $\frac{13}{30}$ base 7 is 0.______ base 7
- (66) 95° F = _____° C
- (67) If 3 workers can do a job in 18 days, how many days would it take 5 workers working at the same rate? ______ days
- $(68) \ 50^2 48^2 + 46^2 44^2 = \underline{\hspace{1cm}}$
- (69) The sum of the product of the roots taken 3 at a time of $2x^4 13x^3 + 28x^2 23x + 6 = 0$ is ____
- *(70) 6 × 12 × 18 × 24 = _____
 - (71) Let $g(x) = x^2 9$. Find g(g(-3)).
 - (72) How many positive 3-digit numbers divisible by 5 exist?
 - (73) If $122_b = 50$ then $221_b =$ _____
 - (74) Let $f(x) = (3x + 4)^2$. Find f'(2).
 - (75) The horizontal asymptote of $y = 4^x$ is _____
- $| \begin{array}{c|c} -1 & 6 \\ 3 & -10 \end{array} | = \underline{ }$
- (77) If x > 0 and |3x + 16| = 20 then x =_____
- $(78) \ \frac{6 \times 5! 5 \times 4!}{3!} = \underline{\hspace{1cm}}$
- (79) 215 × 101 = _____
- *(80) 714.285 ÷ 14.2857 × 8.57142 =

University Interscholastic League - Number Sense Answer Key HS ● Invitation B ● 2019

*number) x - y means an integer between x and y inclusive

NOTE: If an answer is of the type like $\frac{2}{3}$ it cannot be written as a repeating decimal

(1) 550

(19) 8

(35) 6

(59) 4

(2) 500

*(20) 64,543 — 71,337

(36) 58

*(60) 207 — 228

(3) 259

(21) 15,300

(37) 31

(61) 60

(4) 7

 $(22) \frac{7}{15}$

(38) 2

(62) 9,876

(5) 62.5

(23) 67

(39) 180

 $(63) \frac{15}{28}$

 $(6) - \frac{3}{14}$

(24) \$336.00

*(40) 3,892 — 4,300

 $(64) .6, \frac{3}{5}$

(7) 125

 $(25) 61\frac{2}{9}$

(41) 96

(65) 3222

(8) $1\frac{5}{9}$

(26) 225

(42) 15

(66) 35

 $(9) \frac{10}{17}$

 $(27) - \frac{25}{156}$

(43) 10

(67) 10.8, $\frac{54}{5}$, $10\frac{4}{5}$

*(10) 10,460 — 11,560

(28) 6

(44) 1,120

(68) 376

(11) 2

(29) 60

(45) 216

(46) 14,652

(69) $11.5, \frac{23}{2}, 11\frac{1}{2}$

(12) 525

*(30) 102 — 111

(47) 1

*(70) 29,549 — 32,659

(13) 11

(31) 15

(48) 55

(71) - 9

(14) 2,491

(32) .078125, $\frac{5}{64}$

(49) .75, $\frac{3}{4}$

(72) 180

(15) 27

 $(33) -1.5, -\frac{3}{2}, \\ -1\frac{1}{2}$

*(50) 1,663 — 1,836

(73) 85

(16) 13.4, $\frac{67}{5}$, 13 $\frac{2}{5}$

(34) 16

(51) - 2

(74) 60

(17) 1,516

(18) 71

(52) 2

(75) 0

(53) 144

(76) - 8

(54) - 21

 $(77) \frac{4}{3}, 1\frac{1}{3}$

 $(55) \frac{10}{3}, 3\frac{1}{3}$

(78) 100

(56) 38

(79) 21,715

(57) $5\frac{12}{13}$

*(80) 408 — 449

 $(58) \frac{6}{7}$

The University Interscholastic League Number Sense Test • HS District • 2019

•			Final
Contestant's Number			2nd
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Directions: Do not turn this page until the 80 problems. Solve accurately and quickle SOLVED MENTALLY. Make no calculate ach problem. Problems marked with a five percent of the exact answer will be some the person conducting this contest shape.	y as many as you can in culations with paper and (*) require approxima cored correct; all other p ould explain these dire	the order in which they appear. All pencil. Write only the answer in the integral answers; any answer to problems require exact answers.	LL PROBLEMS ARE TO BE a the space provided at the end of
(1) 329 + 330 + 2019 =		$(18) \ 3\frac{1}{2} + 6\frac{2}{3} =$	
(2) 16 × 75 =		2 3	\$
$(3) 910 + 203 - 923 = \underline{\hspace{1cm}}$			<u> </u>
(4) 32930 ÷ 9 has a remainder of			
(5) $79 \div 8 - 31 \div 8 =$			
(6) $\frac{4}{7} - \frac{7}{8} = $	(proper fraction)		base 7
$(7) 17 + 24 + 53 + 29 + 36 = \underline{\hspace{1cm}}$		(24) Find the simple intere	
(8) Which is larger, 0.59 or $\frac{9}{14} = $			A 41 6/25)
(9) The multiplicative inverse of 2.9 i	s		4 then f(25) =
10) $329 + 2019 + 9102 + 923 = $			(proper fraction)
11) CCCXXIX =((Arabic Numeral)	$(27) If f(x) = 3x^2 + 2x + 9$	then f(— 1) =
12) The LCM of 18 and 72 is		$(28) \ \frac{3^3}{(2^4)(5^2)} = \underline{\hspace{1cm}}$	(decimal
13) $4\frac{2}{3} - 1\frac{1}{12} = $	(mixed number)	(29) The largest root of 2x	$x^2 + 3x - 2 = 0$ is
14) 62 × 58 =		*(30) $\sqrt{329330} = $	
15) 10 is what percent of 8?		(31) If $(2x - 9)^2 = ax^2 + b$	ax + c then $a + b + c =$
16) The number of prime numbers les greater than 80 is		(32) Given: 2, 9, 11, 20, 31,	, p, q, r, 215, r =
		(33) 40% of 60 minus 80 =	
17) $33\frac{1}{3}\%$ of a yard =	inches	(34) If $ x + 18 = 4x$ and x	> 0 then x =

- (35) Set A has 14 elements, set B has 11 elements and A ∪ B has 15 elements. A ∩ B has _____ elements.
- (36) $\frac{1}{8}$ is _______ % more than $\frac{1}{10}$
- $(37) 10110₂ = _____4$
- (38) $8\frac{1}{6} \div 3\frac{1}{2} =$ _____ (mixed number)
- (39) The smallest root of $(3x 1)^2 = \frac{1}{9}$ is _____
- *(40) $\left(10\left(\frac{\sqrt{5}+1}{2}\right)\right)^3 =$ ______
- (41) If $2.5^x = 360$, then $2.5^{(x-1)} =$
- (42) If 2x + y = 8 and 2x y = 4, then xy =_____
- (43) The area of a circle is 32π in². The diameter of this circle is $a\sqrt{b}$ in., where a > 1. Find a + b.
- (44) 34 × 43 = _____
- $(45) \ 56^2 + 55^2 = \underline{\hspace{1cm}}$
- (46) 32 × 1111 = _____
- (47) (i)²² = $a\sqrt{b}$, where $a,b \in \{-1,1\}$. Find a. _____
- (48) A string 3 yards 2 feet long is cut into 3 equal pieces. How long is each piece? _____ inches
- $(49) 5 + 10 + 15 + 20 \dots + 70 + 75 = \underline{\hspace{1cm}}$
- *(50) 28 × 21 × 14 × 7 = _____
- (51) The integral sides of a right triangle are x, y & 25, where x < y < 25 and GCF(x,y) = 1. Find xy.
- (52) The roots of $x^3 6x^2 x + 1 = 0$ are d, e, and f. Find (d + e)(e + f)(f + d).
- (53) $\log_4(64) = \log_3($
- (54) The vertex of $3x^2 + 4x 5$ is (h, k). h =_____
- $(55) \ \ 2,442 \div 111 = \underline{\hspace{1cm}}$
- (56) Given: 0,2,5,9,14,20,k,35,44... . k = _____
- (57) The simplified coefficient of the x^3y^3 term in the expansion of $(x + 2y)^6$ is _____

- $(58) \ 1111001_2 = _____8$
- $(59) \ \ 222 \times \frac{5}{37} = \underline{\hspace{1cm}}$
- * $(60) (28)^5 \div (14)^3 =$ ______
- (61) How many ways can 3 people be seated in a row of 5 chairs?
- (62) $12345 \times 8 + 5 =$
- $(63) 4\sin(\frac{\pi}{3})\cos(\frac{\pi}{6}) = \underline{\hspace{1cm}}$
- (64) The first four digits of the decimal for $\frac{21}{40}$ base 5 is 0. ______ base 5
- (65) Let $18^9 \div 9 = (2^x)(9^y)$. Find x y =
- (67) If 4 workers can do a job in 12 days, how many can do it in 8 days working at the same rate?
- (68) $\begin{bmatrix} 1 & 2 \\ -4 & -3 \end{bmatrix} \times \begin{bmatrix} 3 & 4 \\ -2 & -1 \end{bmatrix} = \begin{bmatrix} a & c \\ b & d \end{bmatrix}. bd = \underline{\qquad}$
- (69) The harmonice mean of the roots of $3x^2 14x + 8 = 0$ is _____
- *(70) $4167 \div 0.0833 \times \frac{1}{2} =$
- (71) Let g(x) = 5x 1. Find g(g(1)).
- (72) Find $x, 0 \le x \le 6$, if $x + 5 \equiv 4 \pmod{7}$.
- (73) If $33_b = 24$ then $42_b =$ _____
- (74) Let $f(x) = (5x 7)^2$. Find f'(-3).
- (75) $\lim_{x \to 5} \frac{3x^2}{x+5} = \underline{\hspace{1cm}}$
- $| \begin{array}{c|c} -1 & 5 \\ -12 & -22 \end{array} | = \underline{ }$
- (77) 0.262626... base 8 = _____ base 8 (fraction)
- (78) $\int_{-1}^{1} (x-1) dx = \underline{\hspace{1cm}}$
- (79) 231 × 101 = _____
- *(80) 2222 × 333 ÷ 44 = _____

University Interscholastic League - Number Sense Answer Key HS • District • 2019 *number) x - y means an integer between x and y inclusive

NOTE: If an answer is of the type like $\frac{2}{3}$ it cannot be written as a repeating decimal

2,678

$$(18) \frac{61}{6}, 10\frac{1}{6}$$

$$(39) \frac{2}{9}$$

$$(6) - \frac{17}{56}$$

(35) 10

(36) 25

(37) 112

 $(38) 2\frac{1}{3}$

$$(8) \frac{9}{14}$$

(24) \$90.00

(9)
$$\frac{10}{29}$$

$$(26) \frac{2}{11}$$

(69)
$$\frac{8}{7}$$
, $1\frac{1}{7}$

$$(13) \ 3\frac{7}{12}$$

(29) .5,
$$\frac{1}{2}$$

*(30) 546 — 602

$$(47) - 1$$

$$(33) - 56$$

$$(74) - 220$$

(75) 7.5, $\frac{15}{2}$, $7\frac{1}{2}$

$$(54) - \frac{2}{3}$$

$$(77) \frac{26}{77}$$

$$(78) - 2$$

The University Interscholastic League Number Sense Test • HS Regional • 2019

			Final		
Contestant's Number	-		2nd		
			1st		
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Directions: Do not turn this page unt 80 problems. Solve accurately and qui SOLVED MENTALLY. Make no each problem. Problems marked with five percent of the exact answer will be	ickly as many as you can it calculations with paper an a a (*) require approxima	n the order in which they appear. ALI d pencil. Write only the answer in thate integral answers; any answer to a	PROBLEM he space pro	MS ARE vided at th	TO BE e end of
The person conducting this contest	should explain these dir	rections to the contestants.			
	STOP	WAIT FOR SIGNAL!			
(1) 301 + 412 + 413 =		(19) The number of prime n the month of April is			
(2) $3 \times 12 + 3 \times 13 =$		_			
(3) 301 ÷ 4 =	(mixed number)	*(20) 301412 ÷ 413 =			
(4) 2019 — 301 — 413 =		$(21) 2889 \times 11 + 121 = \underline{\hspace{1cm}}$			
$(5) \ 412 + 413 + 414 + 415 + 416 =$		(22) The average of 17, 31, a			
(6) 12 is what percent of 8?		(23) 413 base 10 is			_base 5
$(7) \ \frac{5}{9} - \frac{9}{10} = \underline{\hspace{1cm}}$		(24) 36 inches \times 12 feet \times 2	yards =	cub	ic yards
, <u>-</u> 0		(25) $(41 \times 24 - 13) \div 5$ has	a remaind	er of	
$(8) \ 81 \div 4\frac{1}{2} = \underline{\hspace{1cm}}$		$(26) \ (64)^{\frac{2}{3}} = \underline{\hspace{1cm}}$			
(9) $1,111,111 = 123456 \times 9 + k. k$	=	(27) 24% of 36 is 48% of			
*(10) 3014 + 1241 + 3201 + 9 =		(28) Find the smallest prime	number p	, where p	> 13
$(11) \ 3^4 \div (12 - 3) \times 14 = \underline{\hspace{1cm}}$		and 4p + 7 is a prime number.			
(12) The LCM of 36 and 84 is		(29) 35 ₇ =			9
$(13) \ 4\frac{1}{3} + 20\frac{1}{9} = \underline{\hspace{1cm}}$		*(30) 41 × 12 × 13 =			
(14) \$2.70 is 6.75% tax on \$		(31) Let $(18x - 13)(18x - 13)$ Find $a + b + c$.			
(15) The multiplicative inverse of —		(32) If $(4x + 1)^2 = ax^2 + bx$	+ c, then a	a — b — c	:=
$(16) \sqrt[3]{2197} = \underline{}$		(33) Two numbers have a su		_	
(17) 12 × 413 =		· · · · · · · · · · · · · · · · · · ·			
(18) The mode of 3, 0, 1, 4, 1, 2, 4, 1	, and 3 is	(34) If $ 4x - 13 = 2x$ and 0	< x < 6, t	then $x = $	

- (35) Set A has 13 elements, $A \cap B$ has 4 elements, and $A \cup B$ has 20 elements. B has ______ elements
- (36) What number added to twelve gives the same result as the number times four?
- (37) 1213₄ = _______
- (38) How many integers between 8 and 88 are divisible by 8?
- (39) The units digit of 27⁽³⁷⁾ is _____
- *(40) $12^5 \div 6^3 \div 3^2 =$
- (41) The sum of the roots of $3x^2 + 13x 10 = 0$ is _____
- (42) If $7^{(x-1)} = 70$, then $7^{(x+1)} =$
- (43) Evaluate $8(xy)^{\frac{1}{3}}$ if x = 16 and y = 4.
- $(44) 78^2 82^2 = \underline{\hspace{1cm}}$
- $(45) \ 41_5 24_5 13_5 = \underline{\hspace{1cm}}_5$
- (46) 72 × 1111 = _____
- (47) $(i)^{19} = a\sqrt{b}$, where $a,b \in \{-1,1\}$. a-b=
- (48) A container holding 4 gallons 3 quarts 2 pints of liquid is divided into 5 equal containers. How many pints are in each of the smaller containers? _____
- $(49) \ 4_6 \times 1213_6 = \underline{\hspace{1cm}}_6$
- *(50) $\sqrt{31214} =$
 - $(51) \log 6 \log 6000 =$
 - (52) The roots of $x^3 + 2x^2 5x 6 = 0$ are d, e, and f. Find (d + e)(e + f)(f + d).
 - $(53) 214 \times 314 =$
- (54) $210^{\circ} = _{\pi}$ radians
- (55) $9 \times \frac{11}{16} =$ (mixed number)
- (56) Given: 3, 2, 4, 5, 8, 12, k, 30,... . k = ____
- $(57) \ \sqrt{63} \ \times \sqrt{112} = \underline{\hspace{1cm}}$
- (58) The simplified coefficient of the x^2y^3 term in the expansion of $(3x + 2y)^5$ is _____

- (59) Let $(a 7i)^2 = -24 70i$. Find a.
- *(60) $\left(100 \times \frac{\sqrt{5}-1}{2}\right)^3 =$ _____
- (61) The sum of the product of the roots taken 2 at a time of $2x^4 13x^3 + 28x^2 23x + 6 = 0$ is ____
- $(62) \ \frac{3}{4} + \frac{3}{16} + \frac{3}{64} + \frac{3}{256} + \dots = \underline{\hspace{2cm}}$
- (63) 95° F = _____° C
- $(64) \cos(\operatorname{Arcsin}(\frac{4}{5})) = \underline{\hspace{1cm}}$
- (65) Let $18^8 \div 36 = (2^x)(9^y)$. Find x + y =_____
- (66) $\cos(112^{\circ}) = \sin A$, $180^{\circ} < A < 270^{\circ}$. $A = _____{\circ}$
- (67) In how many ways can Peter, Paul, and Mary be seated in row of 5 chairs?
- (68) Change $\frac{9}{25}$ to a base 5 decimal. _____ base 5
- (69) If 6 men can do a job in 5 days, then 10 men working at the same rate can do it in _____ days
- *(70) The volume of a cone with a diameter of 12" and a height of 16" is ______ cu. in.
- (71) Let $f(x) = 4x^2 x 3$. Find f(f(-1)).
- (72) How many integers greater than 420 but less than 1357 exist?
- (73) If $314_b = 256$, then $412_b =$ _____
- (74) Let $f(x) = 5x^3 4x^2 3x + 2$. Find f''(-1).
- $\lim_{x \to \infty} \frac{x \cos(x)}{x} = \underline{\hspace{1cm}}$
- $(76) \begin{vmatrix} 4 & 13 \\ 20 & 19 \end{vmatrix} = \underline{\hspace{1cm}}$
- (77) 0.131313... base 4 = _____ base 4 (fraction)
- (78) $\int_{-1}^{3} (2x+1) \, dx = \underline{\hspace{1cm}}$
- (79) $1213 \times 14 =$
- *(80) 976.666 ÷ 58.333 × 41.666 =

University Interscholastic League - Number Sense Answer Key HS ● Regional ● 2019

*number) x - y means an integer between x and y inclusive

NOTE: If an answer is of the type like $\frac{2}{3}$ it cannot be written as a repeating decimal

(1) 1,126

(2) 75

(3) $75\frac{1}{4}$

(4) 1,305(5) 2,070

(6) 150

 $(7) - \frac{31}{90}$

(8) 18

(9) 7

*(10) 7,092 — 7,838

(11) 126

(12) 252

 $(13) \ \frac{220}{9}, 24\frac{4}{9}$

(14) \$40.00

 $(15) - \frac{10}{31}$

(16) 13

(17) 4,956

(18) 1

(19) 10

*(20) 694 — 766

(21) 31,900

(22) 60

(23) 3,123

(24) 8

(25) 1

(26) 16

(27) 18

(28) 19

(29) 28

*(30) 6,077 — 6,715

(31) 25

(32) 7

(33) 4

 $(34) \frac{13}{6}, 2\frac{1}{6}$

(35) 11

(36) 4

(37) 1100111

(38) 9(39) 7

*(40) 122 — 134

 $(41) - \frac{13}{3}, -4\frac{1}{3}$

(42) 3,430

(43) 32

(44) - 640

(45) - 1

(46) 79,992

(47) 0

(48) 8

(49) 5300

*(50) 168 — 185

(51) - 3

(52) 4

(53) 67,196

 $(54) \frac{7}{6}, 1\frac{1}{6}$

 $(55) 6\frac{3}{16}$

(56) 19

(57) 84

(58) 720

(59) 5

*(60) 224,265 — 247,871

(61) 14

(62) 1

(63) 35

(00) 00

(64) $.6, \frac{3}{5}$

(65) 13

(66) 202

(67) 60

(68) .14

(69) 3

*(70) 574 — 633

(71) 11

(72) 936

(73) 335

(74) - 38

(75) 1

(76) - 184

 $(77) \frac{13}{33}$

(78) 12

(79) 16,982

*(80) 663 — 732

The University Interscholastic League Number Sense Test • HS State • 2019

			Final	
Co	ontestant's Number		2nd	
			1st	
	ead directions carefully fore beginning test	DO NOT UNFOLD THIS SHEET UNTIL TOLD TO BEGIN	Sc	ore Initials
80 SC ea	prections: Do not turn this page until the person problems. Solve accurately and quickly as made of the many and pulled the person of the problems marked with a (*) recover percent of the exact answer will be scored of the problems.	any as you can in the order in which they app as with paper and pencil. Write only the ans- quire approximate integral answers; any answers	ear. ALL PROBLEMS wer in the space provide wer to a starred problem	ARE TO BE d at the end of
Th	ne person conducting this contest should ex	plain these directions to the contestants.		
		STOP WAIT FOR SIGNAL!		
(1) 5	503 + 350 + 530 =	(19) \$3.00 is 7.5% tax	k on \$	
(2) 5	504 + 450 - 45 =	*(20) 503 × 305 + 20	19 =	
(3) 1	$15 \times 24 \div 10 = \underline{\hspace{1cm}}$	$(21) 1881 \times 19 + 361$	l =	
(4) 2	25 × 7.2 =	$(22) 54^2 - 45^2 = \underline{\hspace{1cm}}$		
(5) 1	$103 \div 7 - 54 \div 7 = \underline{}$	(23) 503 base 10 is		base 7
(6) 1	8 is what percent of 12?	% (24) 48 inches × 6 fee	et × 2 yards =	cubic feet
(7) 1	12 + 34 + 56 + 78 =	(25) If A = -4, B = -	- 3, and C = 2, then A	$^{\prime}\mathbf{B}_{\mathbf{C}} = \underline{\qquad}$
(8) ($48 - 24) \times 12 \div 6 = \underline{\hspace{1cm}}$		(26) Find the smallest prime number p, where $p > 7$ and $4p + 7$ is a prime number	
(9) 5	$5.03 \times 10^2 - 53 =$	anu 4p + 7 is a p	orime number	
*(10) 5	503 + 201 + 930 + 504 =	(27) How many eleme subsets?	ents are in a set that h	
(11) I	f 1 gram = .04 oz., then 400 grams =	$02. (28) (2^4 + 6 \times 8) \div 5$	has a remainder of	
(12) 7	The median of 5,0,3,2,0,1,9,5,0, and 4 is _	$\frac{3}{4} \text{ is what percen}$	at more than $\frac{3}{5}$?	%
(13) 2	29 ² =		-	
	53 × 47 =	"(30) \$\sqrt{503} \times 1920 -		
	The multiplicative inverse of 5.4 is	(31) Let $(27x - 23)^2$	$= ax^2 + bx + c.$	
(16) 4	$4\frac{2}{3} \times 9\frac{3}{4} = \underline{\qquad} \text{ (mixed)}$	d number) (32) Let $(17x - 15)(1$ Find $a + b + c$.	$7x + 15$) = $ax^2 + bx$	
(17)	³ √2744 =			
(18) 7	The number of prime numbers greater t	han 50 and	20 20 40	_

less than 70 is

(34) If $f(x) = 25x^2 + 30x + 9$, then f(4) is _____

- (35) The slope of the line 5x 3y = 2 is (58) Find the sum of the reciprocals of the first nine (36) How many positive integers less than 60 are relatively prime to 60? $(37) 1001011₂ = _____4$ (38) Given: 2, 7, 9, 16, 25, 41, k, 107, 173, k = _____ (39) The smallest root of $(5x + 1)^2 = \frac{1}{16}$ is _____
- *(40) $16^5 \div 8^3 \times 4^2 =$
- (41) If $7^{(x-1)} = 50$, then $7^{(x+1)} =$
- (42) The sum of the roots minus the product of the roots of $15x^2 - 13x + 10 = 0$ is _____
- (43) The area of a circle is 45π in². The radius of this circle is $a\sqrt{b}$ in., where a > 1. Find a + b.
- $(44) (503_6)(4_6) =$
- (45) The coefficient of the x^4y^2 term in the expansion of $(2x + 3y)^6$ is _____
- $(46) 503 \times 1111 =$
- (47) $(i)^{53} = a\sqrt{b}$, where $a,b \in \{-1,1\}$. Find a + b.
- (48) If 5x + y = 3 and 2x 3y = 5, then $x = _____$
- (49) A container has 2 gallons 2 quarts 2 pints of water in it. How many pints are left in the container if 5 quarts 7 pints are poured out? _____ pints
- *(50) $17 \times 34 \times 51 \times 68 =$
 - (51) The integral sides of a right triangle are x, y & 13, where x < y < 13 and GCF(x,y) = 1. Find xy.
 - (52) The roots of $x^3 + 2x^2 15x = 0$ are d, e, and f. Find (d + e)(e + f)(f + d).
- $(53) (89)^2 (55)(144) =$
- (54) The vertex of the parabola $x^2 8x + 15$ is (h, k) and h + k = _____
- (55) The sum of the 5th triangular number and the third pentagonal number is
- (56) Given: 1,0,2,3,6,10,17,k,46,... . k = ____
- (57) The probability of winning is 76%. The odds of winning is _____ (improper fraction)

- triangular numbers.
- $(59) 534 \times 219 =$

*(60)
$$\left(\pi \times e \times \frac{\sqrt{5}+1}{2}\right)^3 = \underline{\hspace{1cm}}$$

- (61) In how many ways can 3 boys and 2 girls be seated in a row if a boy has to be in the first seat?
- $(62) \ _5P_3 _5C_3 = \underline{\hspace{1cm}}$
- (63) $\sin(\frac{\pi}{4})\cos(\frac{3\pi}{4})\tan(\frac{5\pi}{4}) =$ _____
- (64) Y varies inversely as X, and X = 5 when Y = 3. Find Y when X = 7. Y =
- (65) The first four digits of the decimal for $\frac{27}{34}$ base 8 is
- (66) $140^{\circ} \text{ F} = {}^{\circ} \text{ C}$

(67)
$$\begin{bmatrix} 5 & 0 \\ 3 & 4 \end{bmatrix} \times \begin{bmatrix} 2 & 1 \\ 0 & 9 \end{bmatrix} = \begin{bmatrix} a & c \\ b & d \end{bmatrix}. \quad ad = \underline{\qquad}$$

- (68) Change $\frac{11}{216}$ to a base 6 decimal. _____ base 6
- (69) The harmonic mean of the roots of $x^5 - 11x^4 + 47x^3 - 97x^2 + 96x - 36 = 0$ is
- *(70) The volume of a cone with a radius of 9" and a height of 21" is _____ cu. in.
- (71) Let $f(x) = 3x^2 5x 2$. Find f(-f(1)).
- (72) How many positive 2-digit numbers divisible by 3 exist?_____
- (73) If $113_b = 75$, then $34_b =$ _____
- (74) The remainder of $(3x^2 5x 2) \div (x 4)$ is ____
- (75) $\lim_{x \to 0} \frac{x^2 + 3x}{x} =$
- $(76) \int_{1}^{2} (3-4x) = \underline{\hspace{1cm}}$
- $(77) \ \frac{5! \times 0! 4! \times 1!}{3! \times 2!} = \underline{\hspace{1cm}}$
- (78) Let $f(x) = \frac{5x-4}{3} 2$. Find $f^{-1}(-1)$.
- $(79) 724 \times 17 =$
- *(80) 3333 × 222 ÷ 66 = ____

University Interscholastic League - Number Sense Answer Key HS • State • 2019 *number) x - y means an integer between x and y inclusive

NOTE: If an answer is of the type like $\frac{2}{3}$ it cannot be written as a repeating decimal

(1)	1.383
(1)	1,303

$$(12) \ \ 2.5, \frac{5}{2}, 2\frac{1}{2}$$

$$(15) \frac{5}{27}$$

$$(16) \ 45\frac{1}{2}$$

$$(25) - 36$$

$$(35) \frac{5}{3}, 1\frac{2}{3}$$

$$(39)$$
 $-.25, -\frac{1}{4}$

$$(42)$$
 .2, $\frac{1}{5}$

(48)
$$\frac{14}{17}$$

$$(51)$$
 60

$$(57) \frac{19}{6}$$

(58) 1.8,
$$\frac{9}{5}$$
, $1\frac{4}{5}$

$$*(60)$$
 2,507 — 2,770

$$(63)$$
 $-.5, -\frac{1}{2}$

$$(64) \ \frac{15}{7}, 2\frac{1}{7}$$

(69) 1.875,
$$\frac{15}{8}$$
, $1\frac{7}{8}$

$$(75)$$
 3

$$(76) -3$$

(78) 1.4,
$$\frac{7}{5}$$
, $1\frac{2}{5}$