# CS 381 — Notes

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# 1 Elm

Trace for the evaluation of [1, 2] + +[5].

```
[1,2] ++ [5]

1::([2] ++ [5])

1::(2::[5])

1::[2,5]

[1,2,5]
```

For the function definition

```
(++) : List Int -> List Int -> List Int

11 ++ 12 = case 11 of

[] -> 12

x::xs -> x::(xs ++ 12)
```

First quiz is on Thursday in person, written on paper. We are allowed one sheet of notes, single sided. A function is a **parameterized expression**. Take something such as 3+5 and replace these with x+y and now it is a function on two variables. Notice how in "MAD LIBS" the parameters are given types that say what kind of argument should be placed into the function. A **function definition** is simply giving a name to a function. We make a simple sign function as follows

```
sign : Int \rightarrow Int sign x = if x==0 then 0 else x//abs x
```

Assume that a min function already exists that returns the smallest integer given two arguments. Then we can define min3 as

```
min3 : Int -> Int -> Int -> Int min3 x y z = min x (min y z)
```

We can also create a while loop recursively:

We must remember to keep in mind the mindshift about processing values. In programming with pattern matching

- A value v is a term built out of constructors
- A pattern p is a term build out of constructors and variables
- A rule  $p \rightarrow e$  consists of a patter p and an expression e
- Matching v agains p creates a set of variable bindings

• Evaluating a rule for v means to evaluate e in the context of bindings produced by matching v against p

For elm, the following syntax will give us pattern matching

General recursion template:

We practice this by constructing a recursive is Even function:

```
isEven : Int -> Bool
isEven x = case x of
    0 -> True
    1 -> False
    n -> isEven (n-2)
```

#### 1.1 Lists

Lists are built with two constructors, [] and v :: l. That is,

```
[] : List a
(::) : a -> List a -> List a
```

We have some accessors as well

```
isEmpty : List a -> Bool
head : List a -> Maybe a
tail : List a -> Maybe (List a)
```

If you apply head to an empty list then **Maybe** becomes important. You can raise a runtime error like Haskell does, or we can do it like elm. If head finds some element then it will return the value, otherwise some error will be thrown. We have a template for list processing using pattern matching:

### 1.2 Higher order functions and polymorphism

Every elm value has a type, as do functions, with some small exceptions ex. 3 (Number). If we recall our function 'length', it took a type of 'List a' to 'Int'. We are using a variable for the type. This is called parametric polymorphism instead of sub-type polymorphism. That is, 'a' is a type parameter that will work for any different type. Another example is our function 'Tuple.first' which maps a tuple  $(a,b) \to a$ . In this example we can have a tuple with two different type variables to the type variable of the first. If you see the same type variable name twice, they must inherit the same type. Often with these type parameters the type of a function dictates much of the implementation of that function. For example see this zip function that can be implemented in elm:

```
zip : List a -> List b -> List (a,b)
zip 11 12 = case 11 of
  [] -> []
  x::xs -> case 12 of
```

```
[] -> []
y::ys -> (x,y)::zip xs ys
```

The map function will apply a function to each element of a list. It is defined as

```
map : (a -> b) -> List a -> List b
map f l = case l of
    [] -> []
    x::xs -> f x::map f xs
```

One can notice that the type of the function almost entirely defines how we can possibly define the function.

```
andThen : Maybe a -> (a -> Maybe b) -> Maybe b
andThen m f = case m of
   Nothing -> Nothing
   Just x -> f x

reverse : List a -> List a
reverse l = case l of
   [] -> []
   x::xs -> reverse xs ++ [x]

last : List a -> Maybe a
last = head << reverse</pre>
```

We think of  $f \ll g$  as 'f composed with g'.

#### 2 Grammar

I am missing a lot of stuff on here to be honest.

### 2.1 Parse Trees

# 2.2 Abstract Syntax

All of the following were correct

- type Bin = A | B | Conc Bin Bin
- type Bin = Single Bool | Many Bool Bin
- type Bin = OnlyZero | OnlyOne | ZeroAnd Bin | OneAnd Bin
- type Bin = Seq Bool [Bool]

I am deceased.