Algebraic Topology Notes

Philip Warton

September 22, 2021

1 September 22

We start by defining Euclidean space, the unit ball and the unit sphere:

$$D^{n} = \{ x \in \mathbb{R}^{n} : ||x|| \le 1 \}$$
 (1)

$$S^{n-1} = \{ x \in \mathbb{R}^n : ||x|| = 1 \}$$
 (2)

Theorem 1.1 (Bauer Fixed Point). For all $n \ge 1$ every self-map of the unit n-ball D^n has a fixed point.