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$$x_j: -10, -5, 0, 5, 10$$

$$h(x): 3, -5, -1, -5, 3$$

$$\begin{cases} p_0 = 1 \\ p_1 = x \\ p_2 = x^2 - 50 \end{cases} \quad \leftarrow \geq L 11.6$$

$$w_2^*(x) = \sum_{k=0}^n a_k f_k$$

$$a_k = \frac{\langle h, p_k \rangle}{\langle p_k, p_k \rangle}$$

$$a_0 = \frac{3 - 5 - 1 - 5 + 3}{5} = -1$$

$$a_1 = \frac{(3 \cdot (-10)) + ((-5) \cdot (-5)) + ((-5) \cdot 5) + (3 \cdot 10)}{(-10)^2 + (-5)^2 + 5^2 + 10^2} = 0$$

$$a_2 = \frac{(3 \cdot 50) + ((-5) \cdot (-25)) + 50 + ((-5) \cdot (-25)) + (3 \cdot 50)}{50^2 + (-25)^2 + (-50)^2 + (-25)^2 + 50^2} = \frac{12}{175}$$

$$w_2^* = (-1) \cdot 1 + 0 \cdot x + \frac{12}{175} (x^2 - 50) = \frac{12}{175} x^2 - \frac{17}{7}$$