



Announements

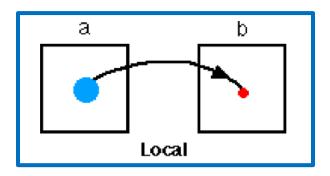
- TAs
 - Meher Shashwat Nigam
 - Soumyasis Gun
 - Adithya Arun
 - Surendra Gopireddy



Announcements

- Mini Quiz 2 today
- Tutorial Slot: 5pm, Saturday

▶ Neighborhood to Point

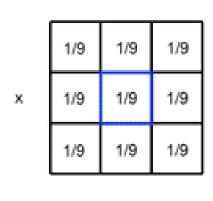


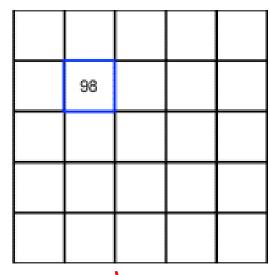
Spatial Domain Filtering



Mean/Average Filter (Smoothing)

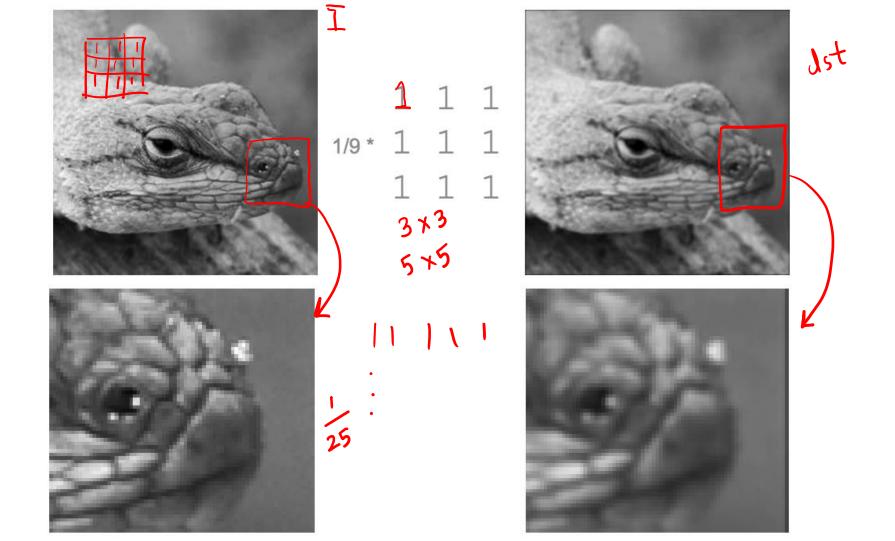
120	190	140	150	200
17	21	30	8	27
89	123	150	73	56
10	178	140	150	18
190	14	76	69	87



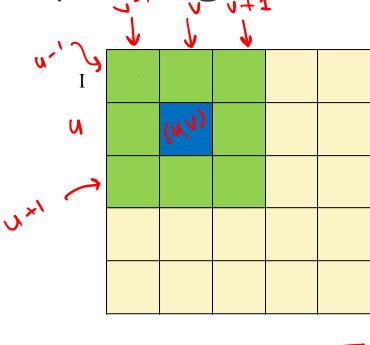


I

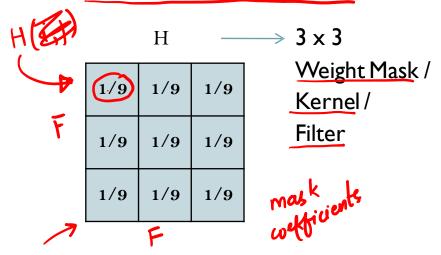
924



Mean/Average Filter



Note: Coefficients sum to 1



$$I'(u,v) \leftarrow \frac{1}{9} \cdot \sum_{j=-1}^{1} \sum_{i=-1}^{1} I(u+i,v+j)$$

$$I'(u,v) \leftarrow \sum_{j=-1}^{1} \sum_{i=-1}^{1} I(u+i,v+j) \bullet H(i,j)$$

Effect of Mask Size

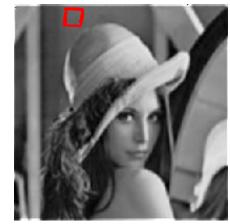
Original Image



[3x3]



[5x5]

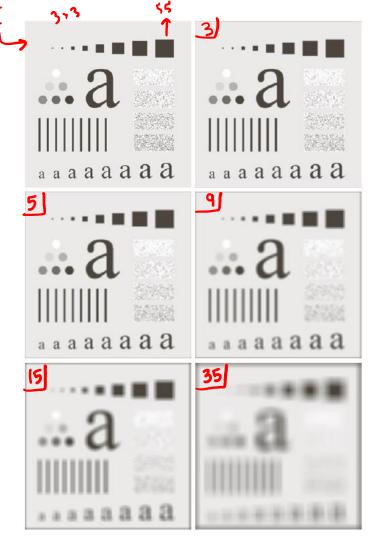


[7x7]



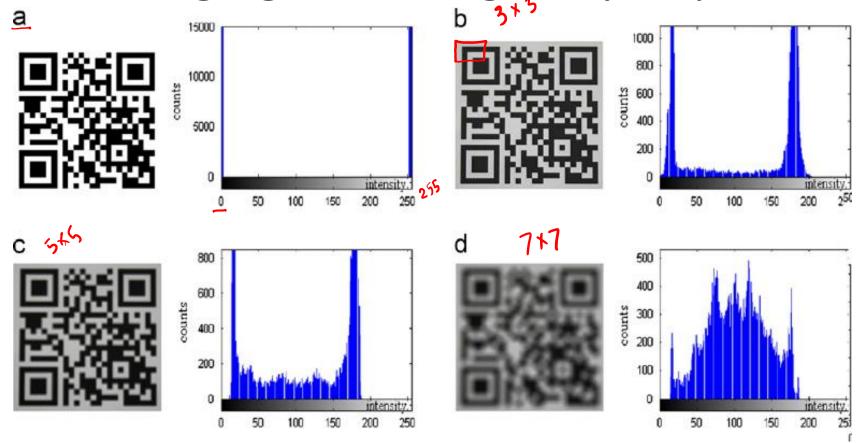
Square averaging filter

FIGURE 3.33 (a) Original image, of size 500×500 pixels. (b)–(f) Results of smoothing with square averaging filter masks of sizes m = 3, 5, 9, 15, and 35, respectively.' squares at the top are of sizes 3, 5, 9, 15, 25, 35, 45, and 55 pixels, respectively; their borders are 25 pixels apart. The letters at the bottom range in size from 10 to 24 points, in increments of 2 points; the large letter at the top is 60 points. The vertical bars are 5 pixels wide and 100 pixels high; their separation is 20 pixels. The diameter of the circles is 25 pixels, and their borders are 15 pixels apart; their intensity levels range from 0% to 100% black in increments of 20%. The background of the image is 10% black. The noisy rectangles are of size 50×120 pixels.



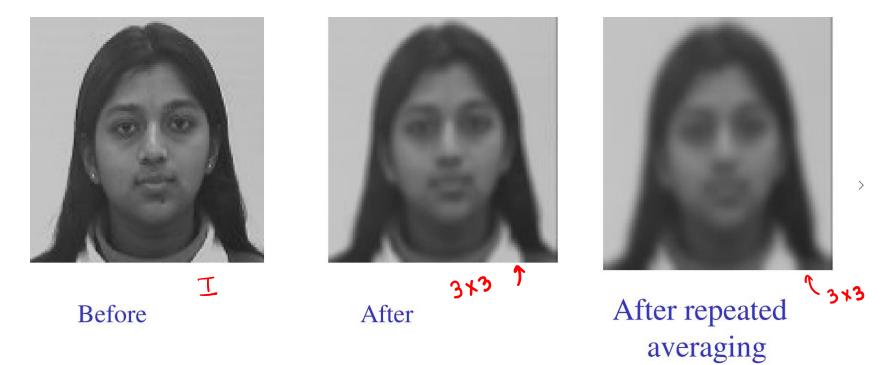
c d

Averaging – a histogram perspective



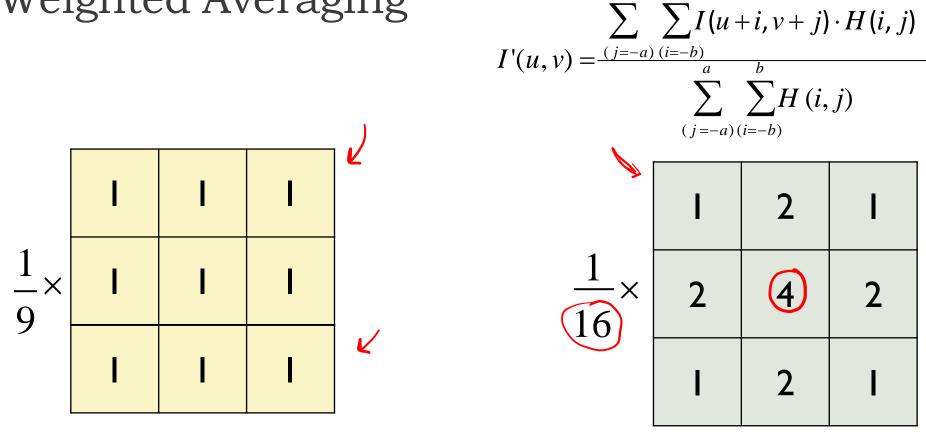
Repeated Averaging Using Same Filter





NOTE: Can get the effect of larger filters by smoothing repeatedly with smaller filters

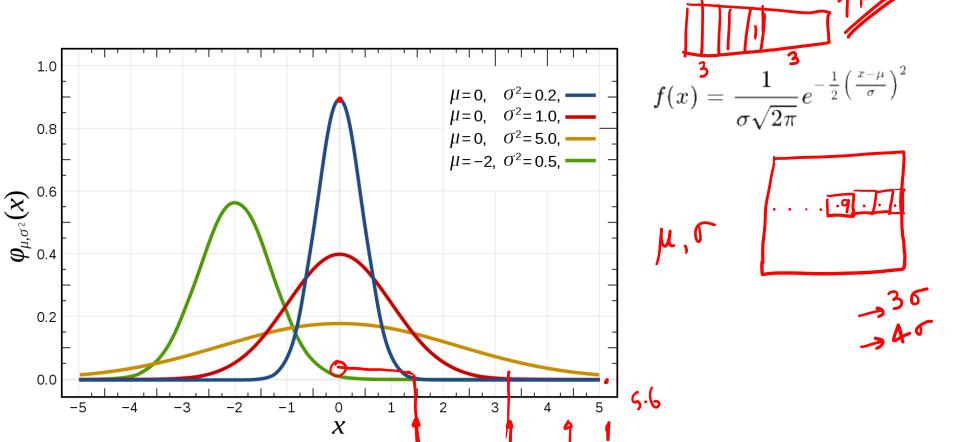
Weighted Averaging



Standard average

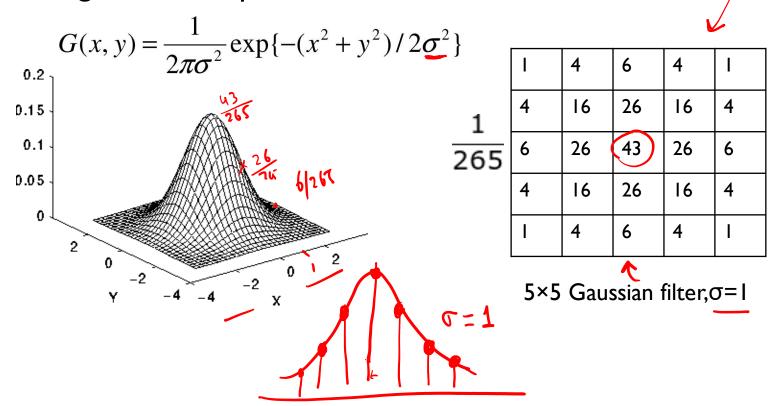
Weighted average

Gaussian Function (1-D)



Gaussian Smoothing

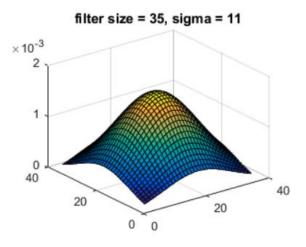
Mask weights are samples of a zero-mean 2-D Gaussian

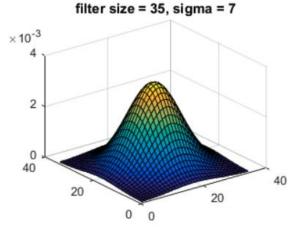


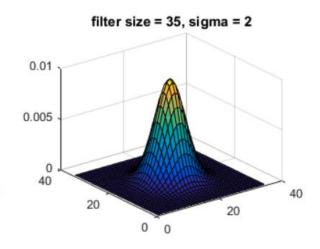
Gaussian Smoothing – Effect of sigma

$$G(x, y) = \frac{1}{2\pi\sigma^2} \exp\{-(x^2 + y^2)/2\sigma^2\}$$



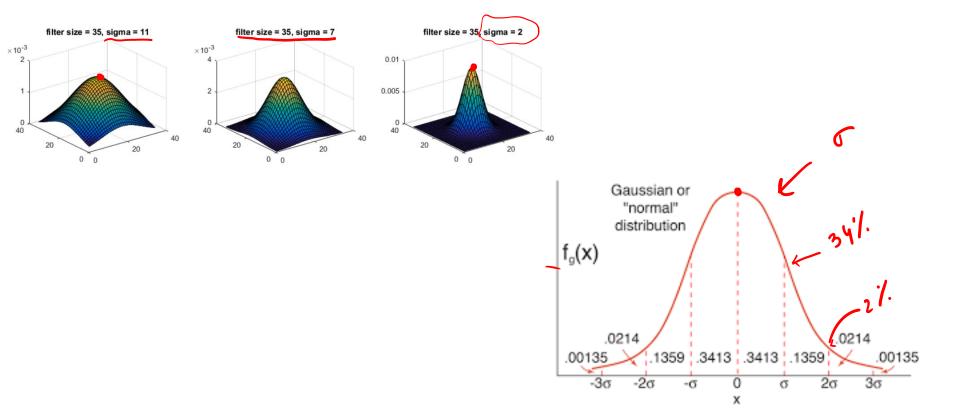






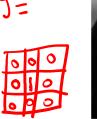
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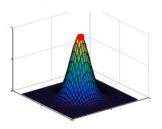


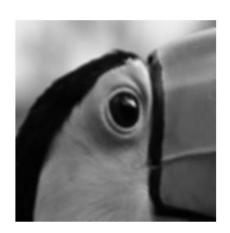


Original Image (Sigma 0)

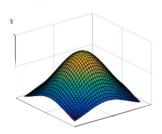


Gaussian Blur (Sigma 0.7)





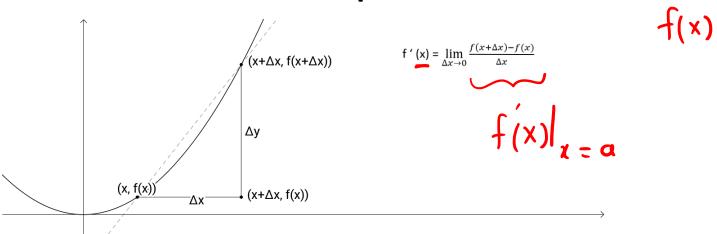
Gaussian Blur (Sigma 2.8)



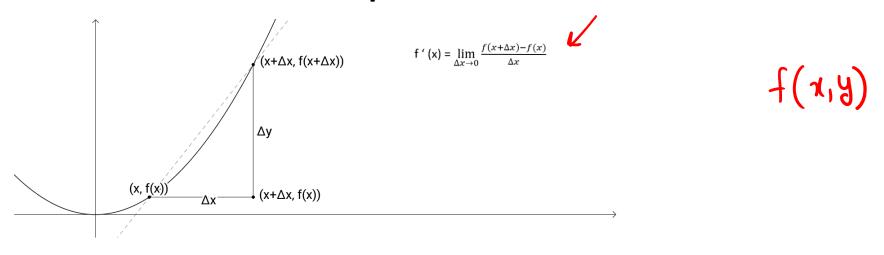


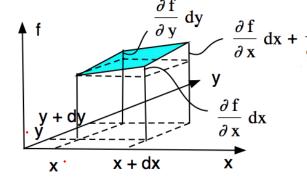
Averaging vs Gaussian filters 0 Smoother intensity transitions

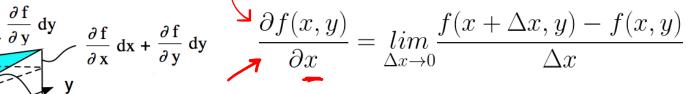
Recap: Derivatives



Recap: Derivatives





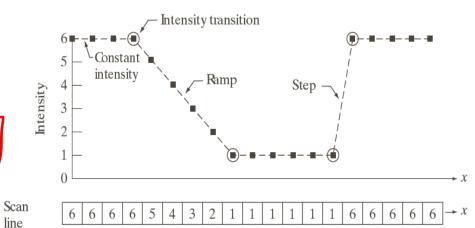


$$\frac{\partial f(x,y)}{\partial y} = \lim_{\Delta y \to 0} \frac{f(x,y+\Delta y) - f(x,y)}{\Delta y}$$

$$\frac{\partial f(x,y)}{\partial x} = \lim_{\Delta x \to 0} \frac{f(x+\underline{\Delta x},y) - f(x,y)}{\Delta x}$$

$$\frac{\partial f(x,y)}{\partial x} \sim f[x+\underline{1},y] - f[x,y]$$

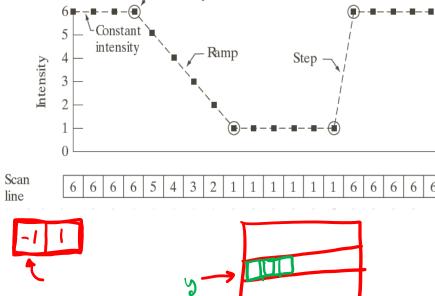
$$\frac{\partial f(x,y)}{\partial x} \sim f[x+1,y] - f[x,y]$$



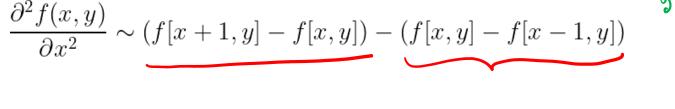
$$\frac{\partial f(x,y)}{\partial x} = \lim_{\Delta x \to 0} \frac{f(x+\Delta x,y) - f(x,y)}{\Delta x}$$

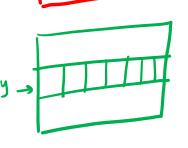
$$\frac{\partial f(x,y)}{\partial x} \sim \underline{f[x+1,y]} - \underline{f[x,y]}$$

Second Derivative (Digital Approximation)



Intensity transition

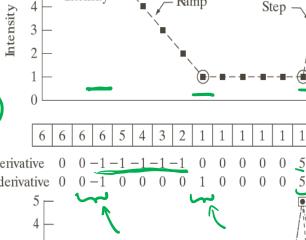




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Second Derivative (Digital Approximation)

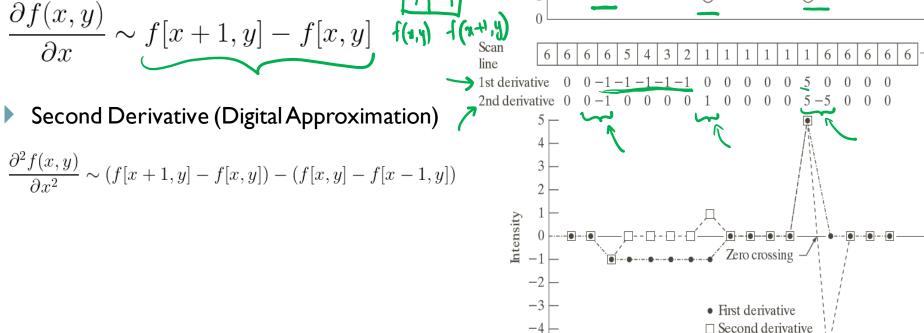


Intensity transition

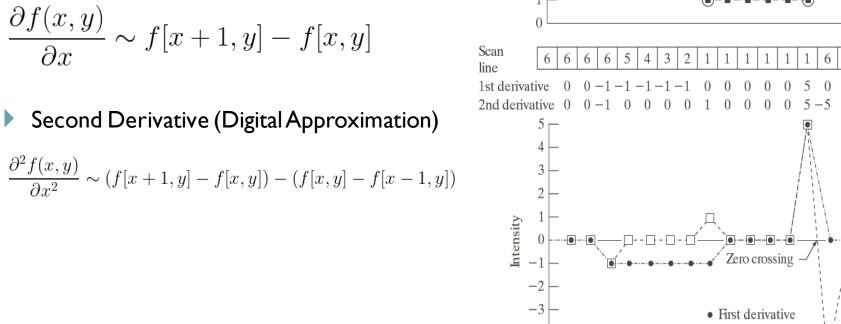
Ramp

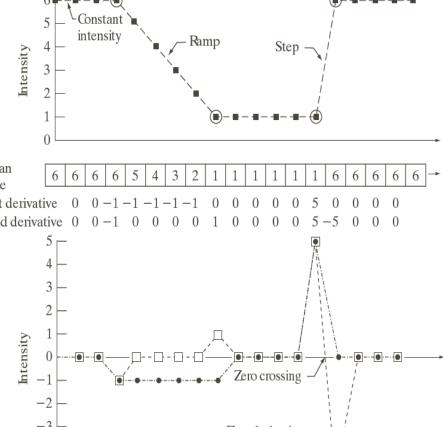
Constant

intensity



$$\frac{\partial f(x,y)}{\partial x} = \lim_{\Delta x \to 0} \frac{f(x + \Delta x, y) - f(x,y)}{\Delta x}$$





☐ Second derivative

Intensity transition

Alt: Derivative as symmetric Difference

$$f(x) = \begin{cases} f(x,y) - f(x,y) \\ f(x) = \begin{cases} f(x+h) - f(x-h) \\ h \to 0 \end{cases} \end{cases}$$

$$f(x) = \begin{cases} f(x+h) - f(x-h) \\ h \to 0 \end{cases}$$

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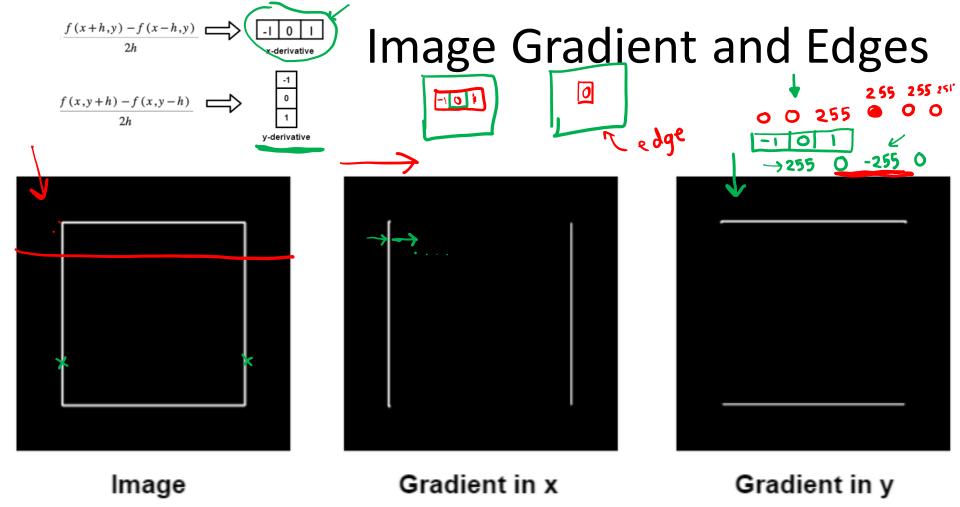
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Edge 'Image'

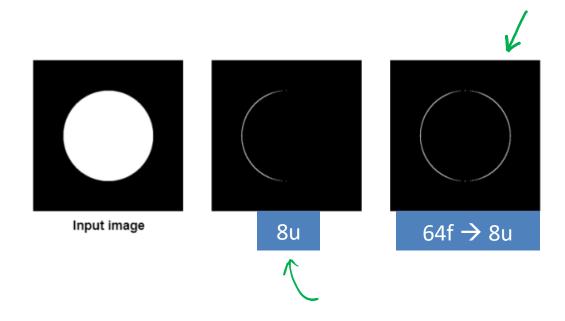


Image gradient

The gradient of an image:

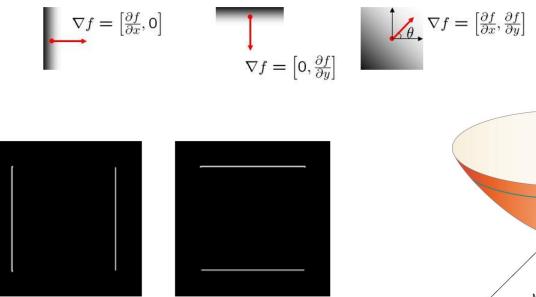
Gradient in x

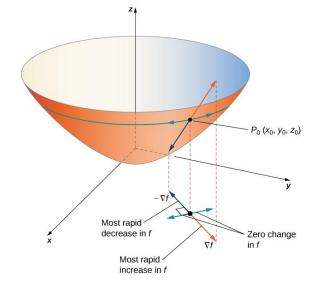
Image

$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right]$$

The gradient points in the direction of most rapid change in intensity

Gradient in y

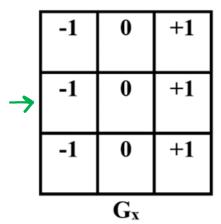




Dr. Prewitt

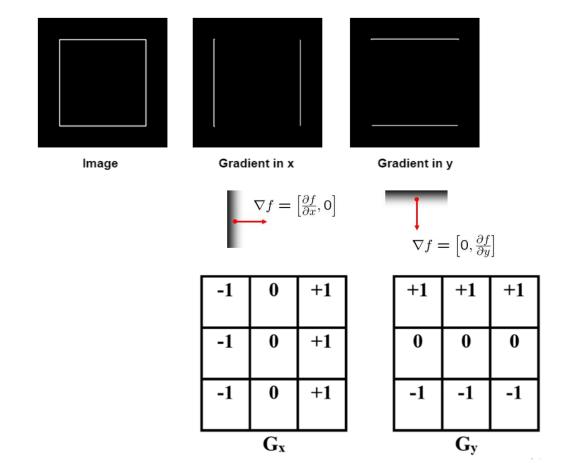
https://nihrecord.nih.gov/sites/recordNIH/files/pdf/1984/NIH-Record-1984-03-13.pdf

Prewitt Edge Filter

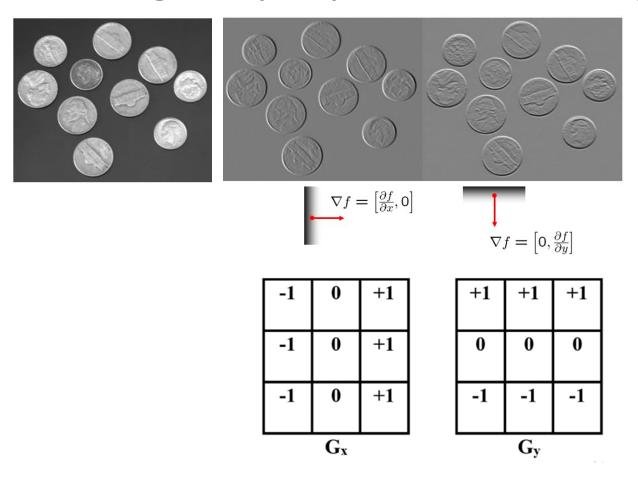


+1	+1	+1
0	0	0
-1	-1	-1
	Gy	

Edge is perpendicular to gradient



Edge is perpendicular to gradient



Scribe List