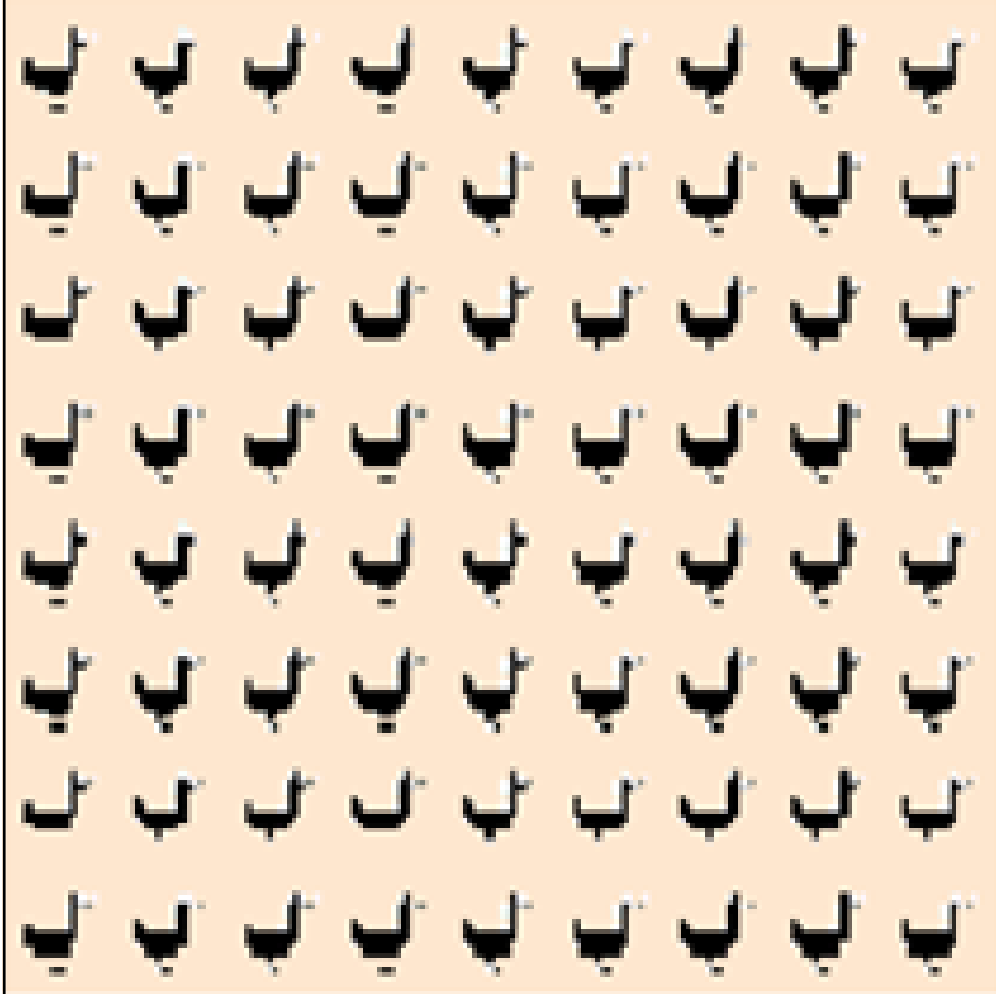
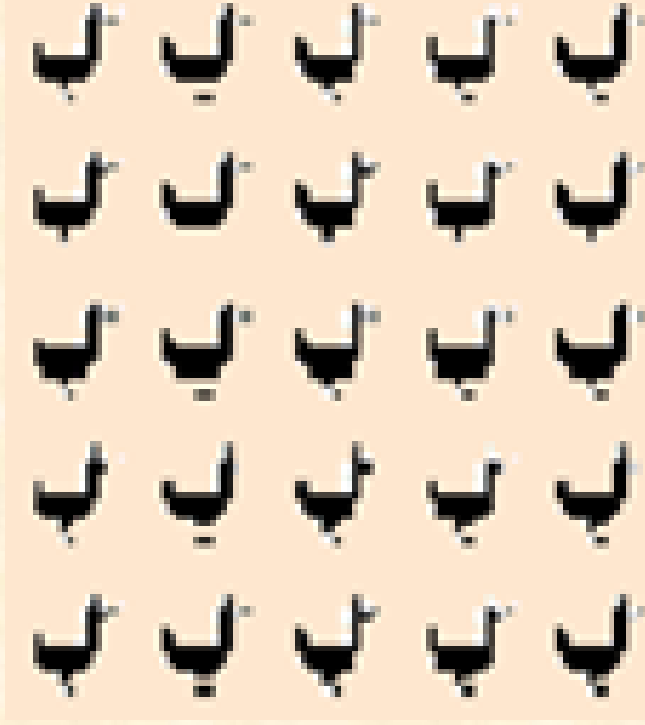
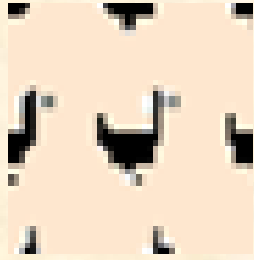
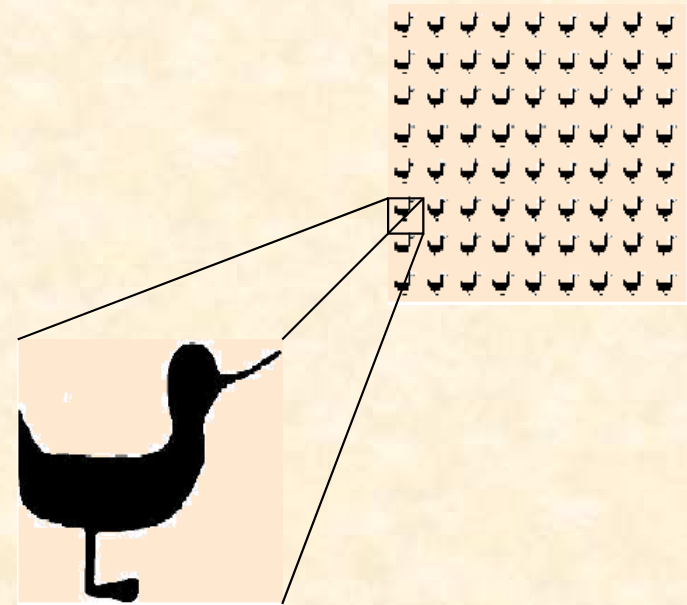


# TEXTURE ANALYSIS USING GABOR FILTERS

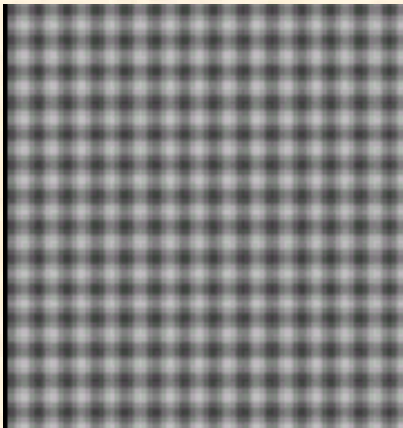


# Texture Types

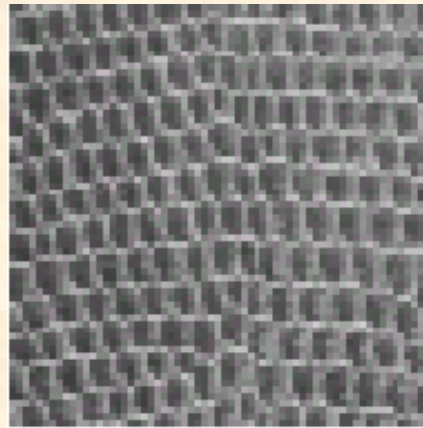
- Definition of Texture



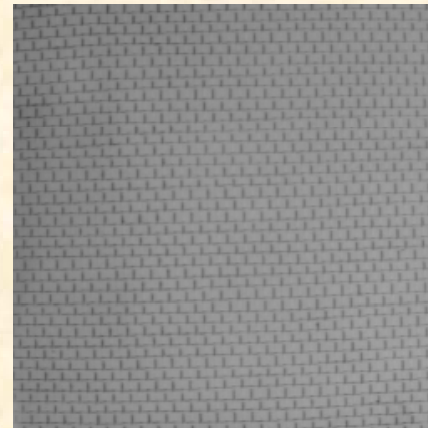
- Texture types



Synthetic



Natural

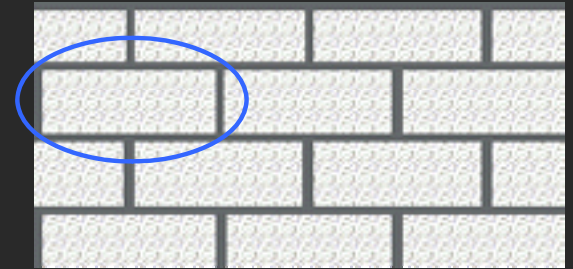


Stochastic



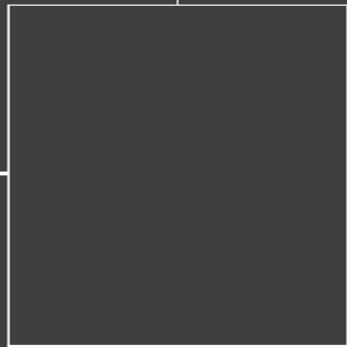
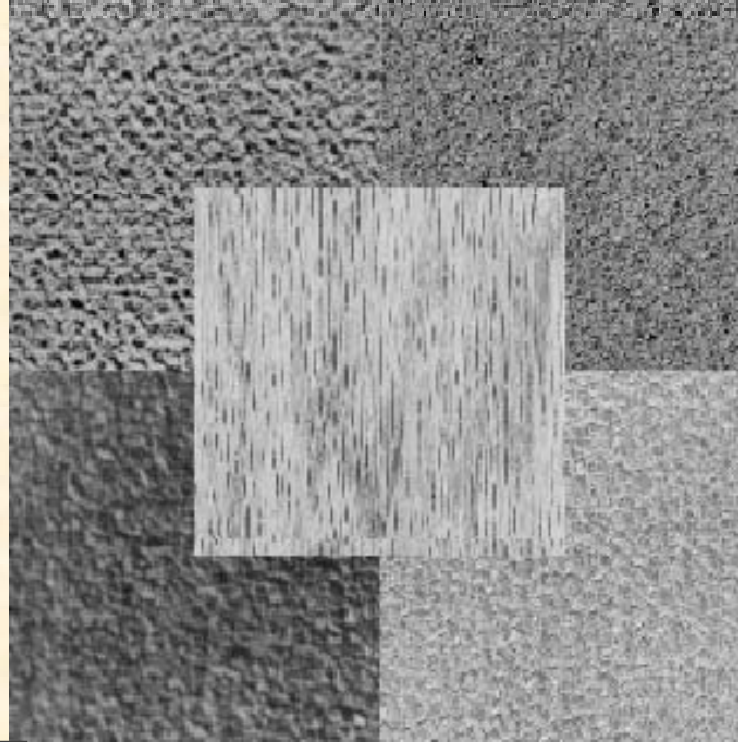
# Texture Definition

**Texture:** the regular repetition of an element or pattern on a surface.

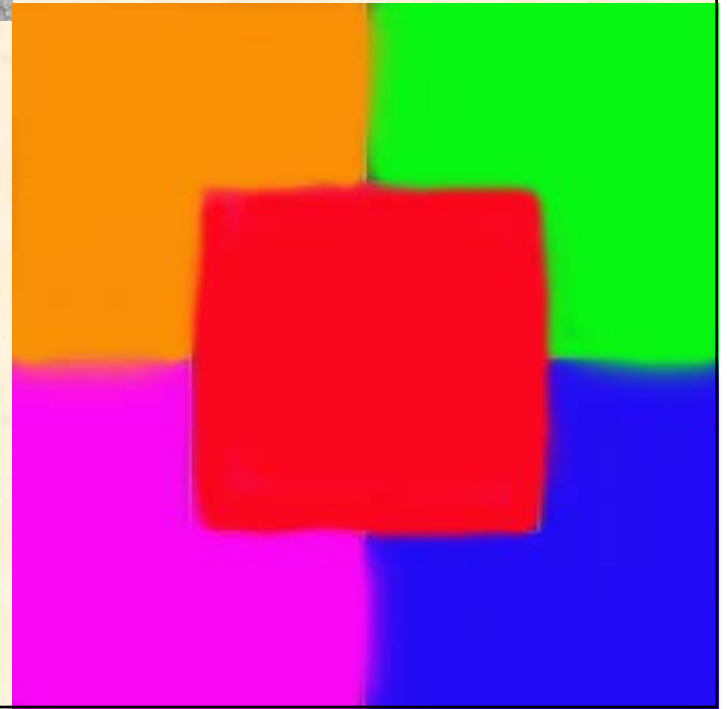


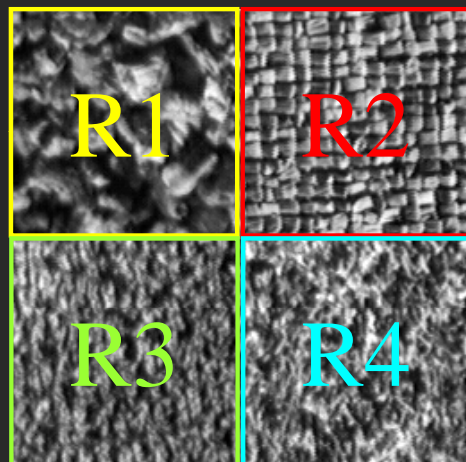
- Purpose of texture analysis:
  - To identify different textured and non-textured regions in an image.
  - *To classify/segment different texture regions in an image.*
  - *To extract boundaries between major texture regions.*
  - To describe the texel unit.
  - 3-D shape from texture

# Texture Regions & Edges



< Prev





Textured image

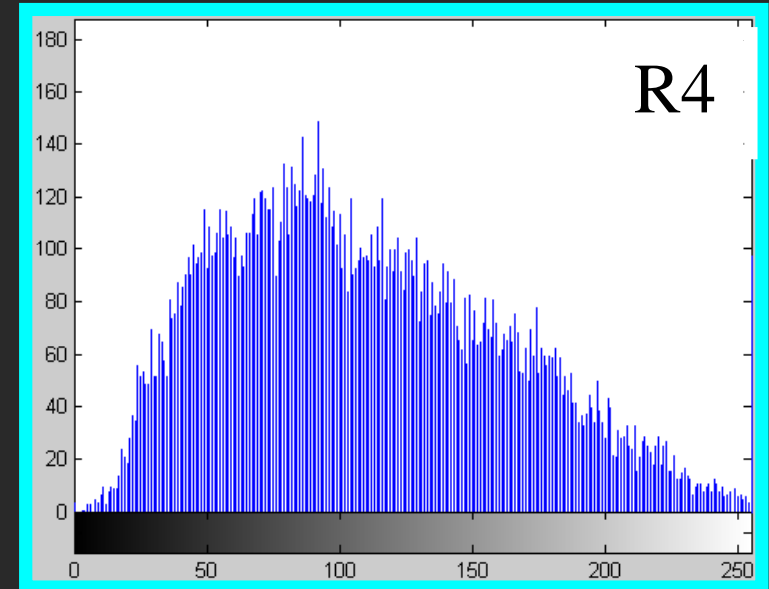
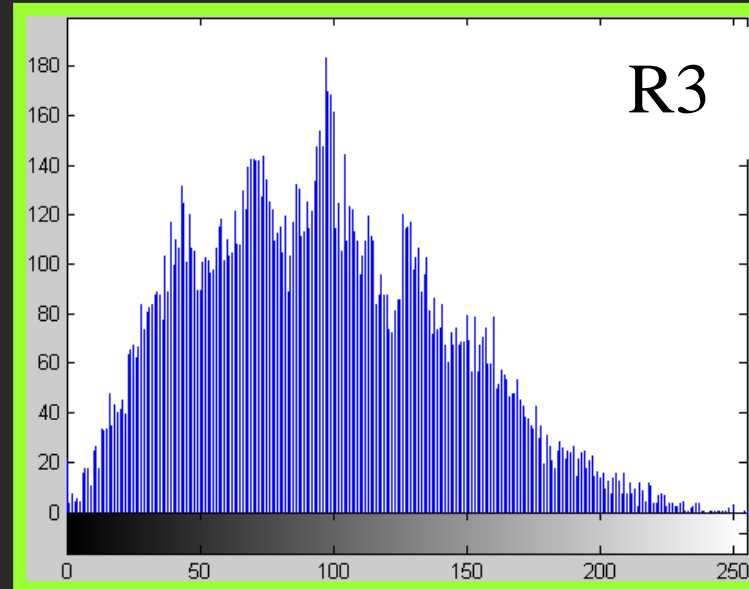
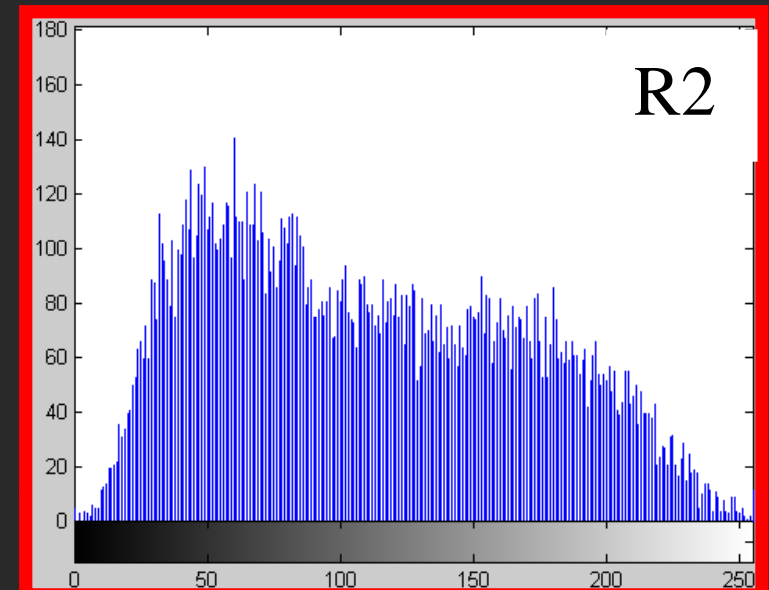
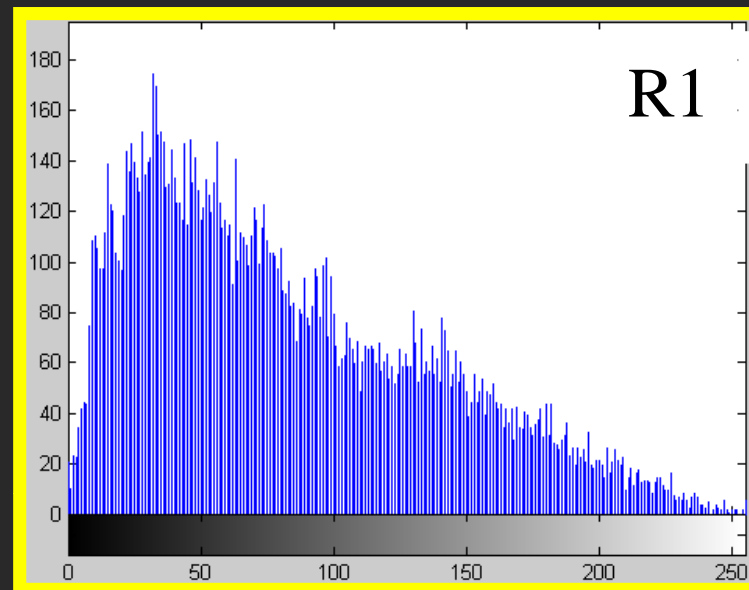
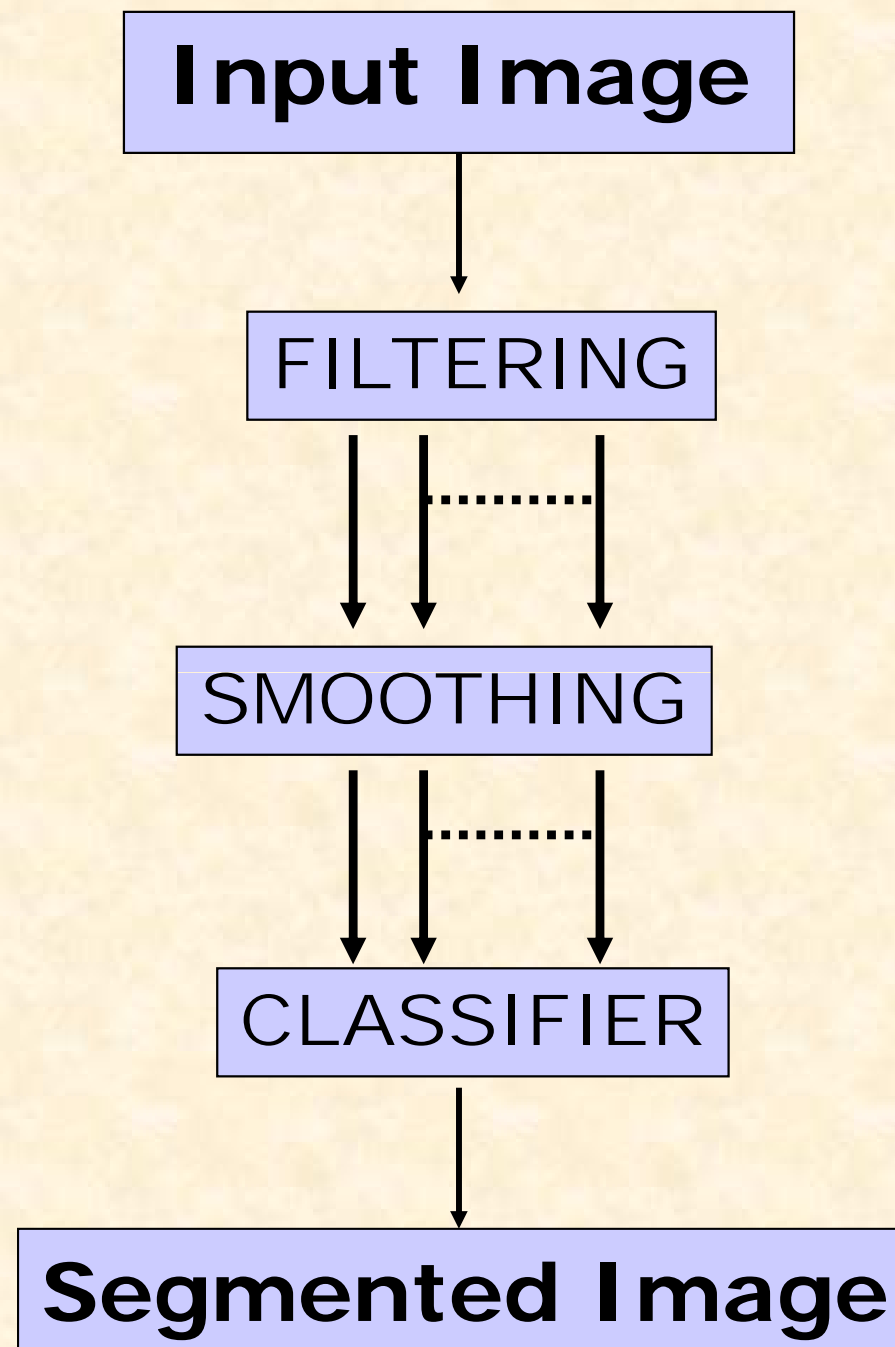
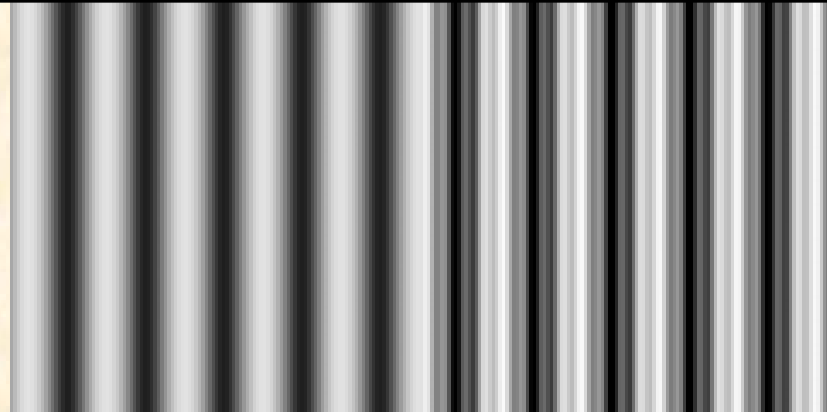


Image histograms

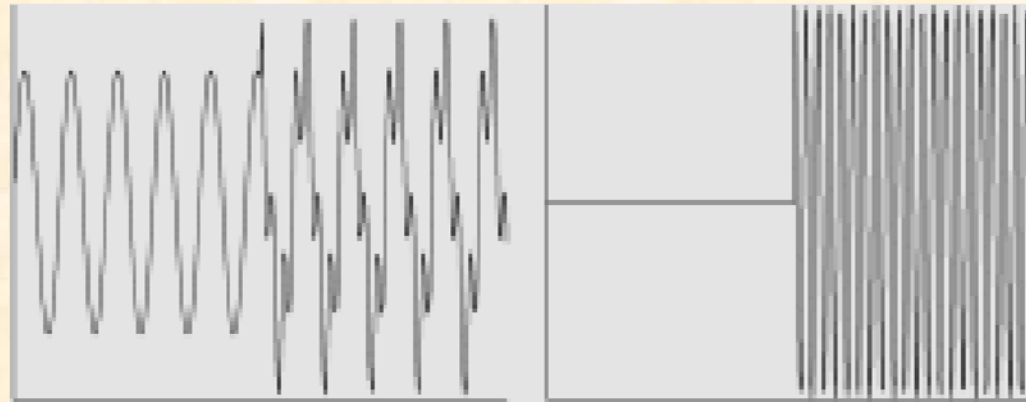


**Flow-chart of a typical method of texture classification**



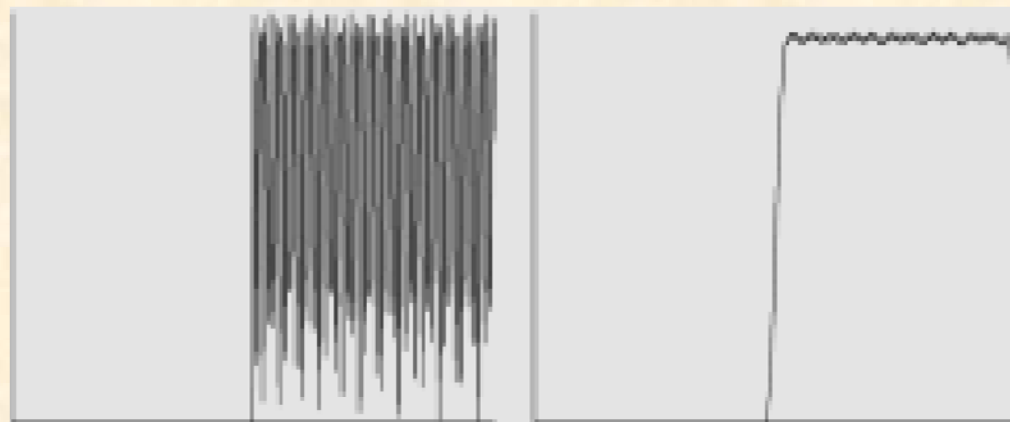
**Synthetic Texture  
Image**

**Horizontal  
intensity  
profile**

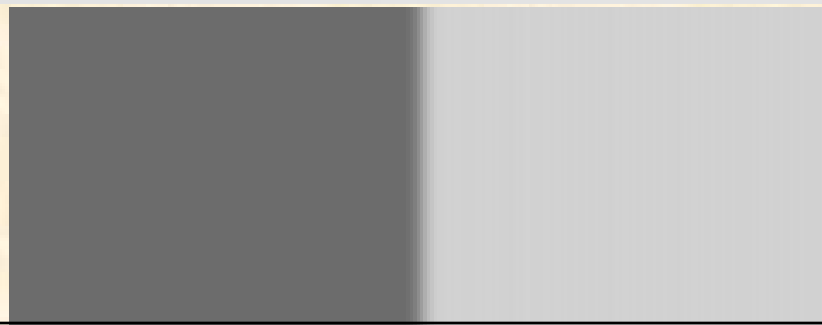


**Filtered  
output**

**Nonlinear  
transform**



**Smoothing**



**Segmented  
image**



# Processing of Texture-like Images

## 2-D Gabor Filter

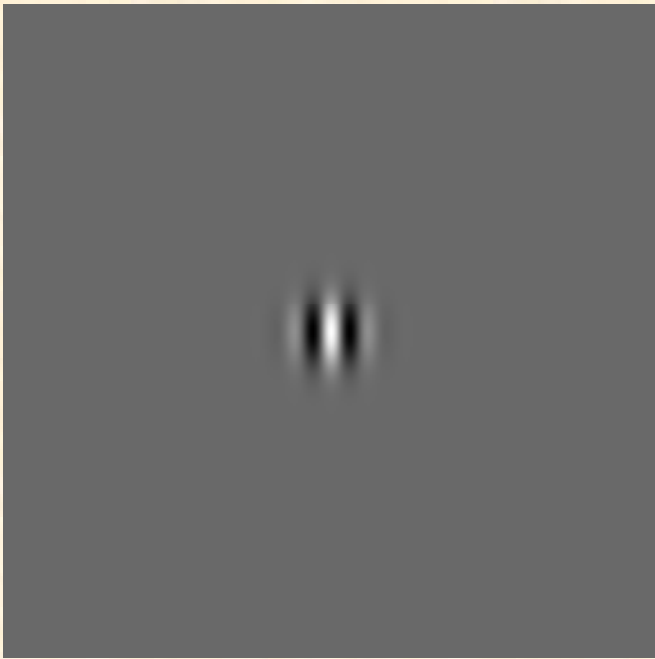
$$f(x, y, \omega, \theta, \sigma_x, \sigma_y) = \frac{1}{2\pi\sigma_x\sigma_y} \exp\left[\frac{-1}{2}\left(\left(\frac{x}{\sigma_x}\right)^2 + \left(\frac{y}{\sigma_y}\right)^2\right) + j\omega(x\cos\theta + y\sin\theta)\right]$$



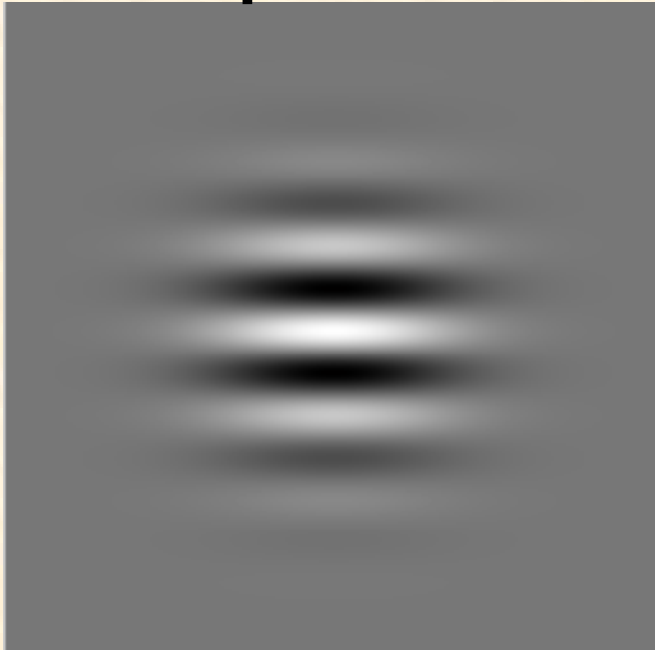
**A typical Gaussian filter with  $\sigma=30$**



**A typical Gabor filter with  $\sigma=30$ ,  $\omega=3.14$  and  $\theta=45^\circ$**



**Gabor filters with different combinations of spatial width  $\sigma$ , frequency  $\omega$  and orientation  $\theta$ .**



## 2-D Gabor filter:

$$f(x, y, \omega, \theta, \sigma_x, \sigma_y) = \frac{1}{2\pi\sigma_x\sigma_y} \exp\left[\frac{-1}{2}\left(\left(\frac{x}{\sigma_x}\right)^2 + \left(\frac{y}{\sigma_y}\right)^2\right) + j\omega(x\cos\theta + y\sin\theta)\right]$$

where

$\sigma$  is the spatial spread



$\omega$  is the frequency

$\theta$  is the orientation

## 1-D Gabor filter:

$$f(x, \omega, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(\frac{-x^2}{2\sigma^2} + j\omega x\right)$$

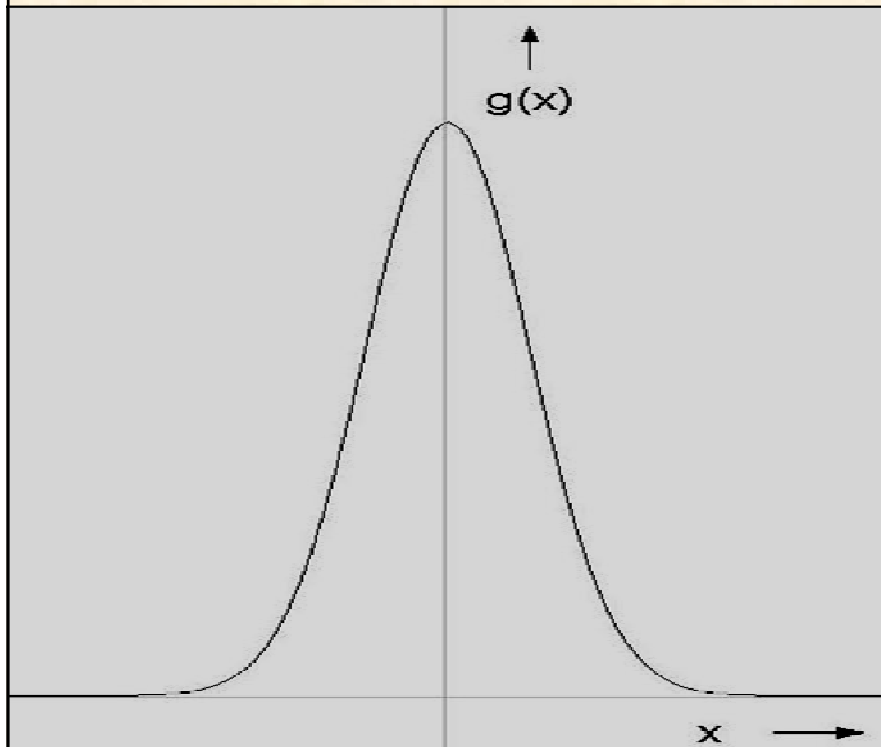
## 1-D Gaussian function:

$$g(x) = \frac{1}{\sqrt{2\pi}\sigma_1} \exp\left(\frac{-x^2}{2\sigma^2}\right)$$

# Processing of Texture-like Images

## 1-D Gaussian Filter

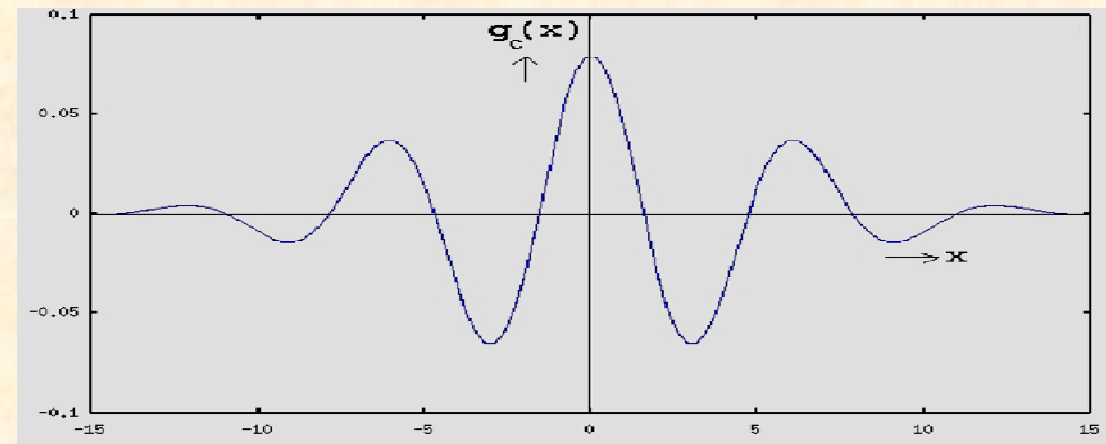
$$g(x) = \frac{1}{\sqrt{2\pi}\sigma_1} \exp\left(\frac{-x^2}{2\sigma^2}\right)$$



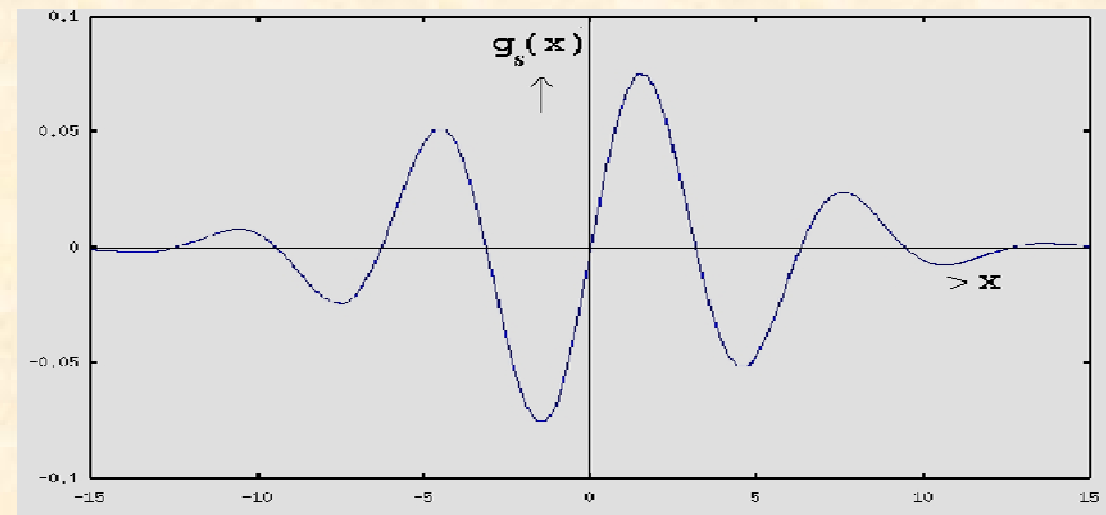
## 1-D Gabor Filter

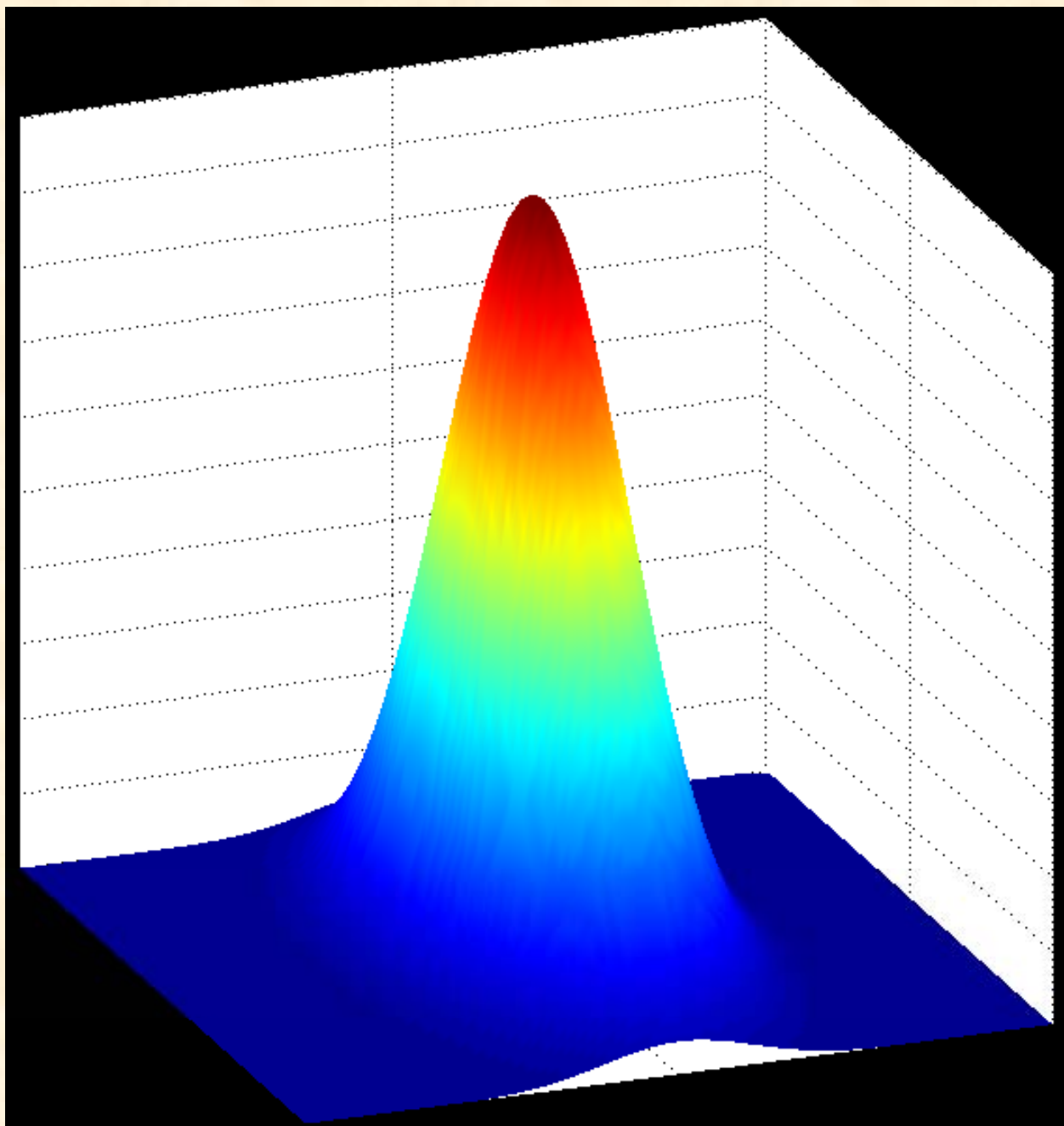
$$f(x, \omega, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(\frac{-x^2}{2\sigma^2} + j\omega x\right)$$

Even Component



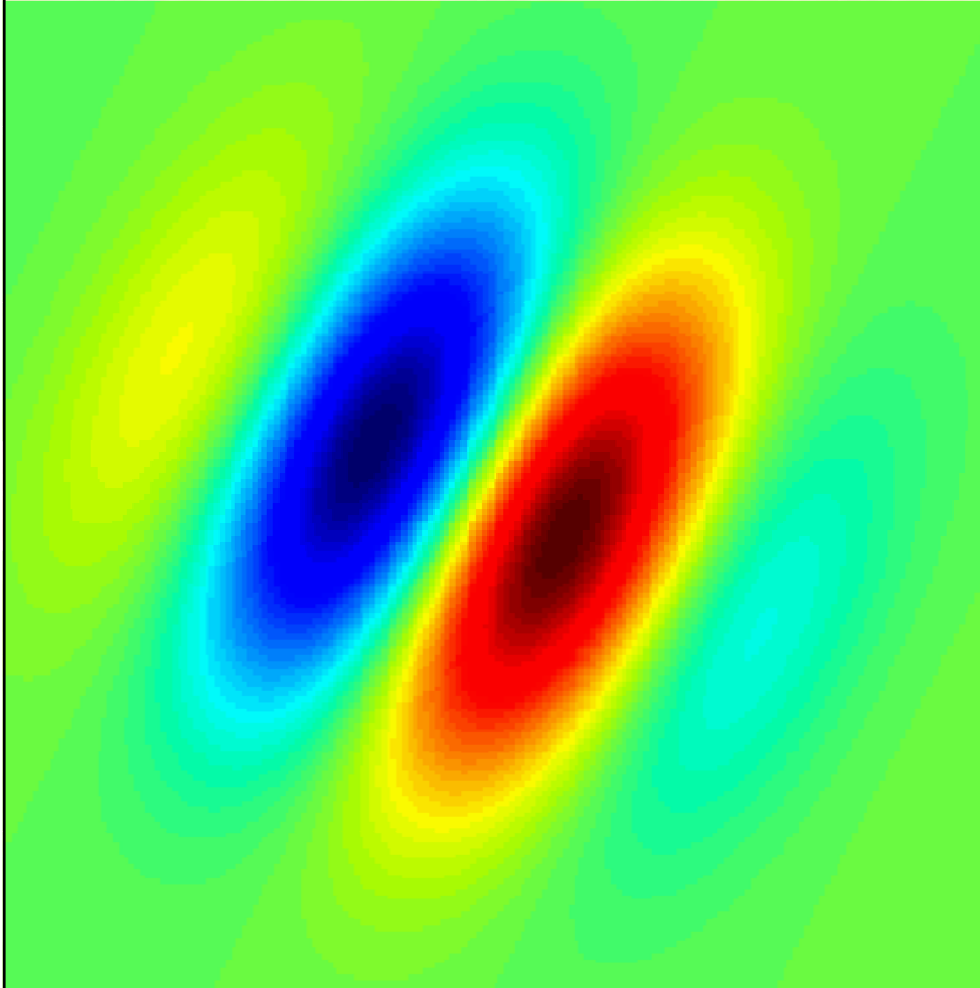
Odd Component






**Asymmetric 2-D Gaussian function**

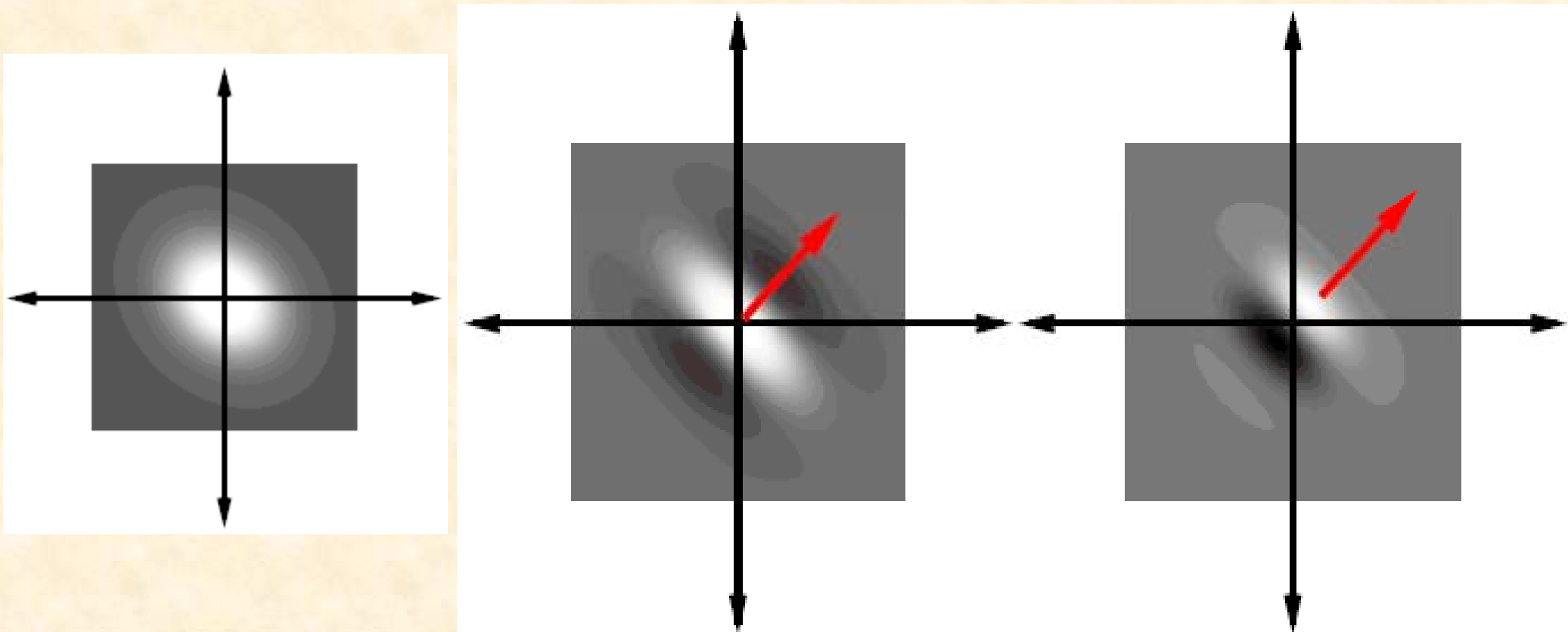
$$gab(x, y) = K \exp(-\pi(a^2(x - x_0)_\theta^2 + b^2(y - y_0)_\theta^2)) \exp(j(2\pi F_0(x \cos \omega_0 + y \sin \omega_0) + P))$$



- **K** : Scales the magnitude of the Gaussian envelop. 
- **(a, b)** : Scale the two axis of the Gaussian envelop.
- **θ** : (Rotation) angle of the Gaussian envelop.
- **(x<sub>0</sub>, y<sub>0</sub>)** : Location of the peak of the Gaussian envelop.
- **(u<sub>0</sub>, v<sub>0</sub>)** : Spatial frequencies of the sinusoidal carrier in Cartesian coordinates. It can also be expressed in polar coordinates as **(F<sub>0</sub>, ω<sub>0</sub>)**.
- **P** : Phase of the sinusoidal carrier.

$$gab(x, y) =$$

$$K \exp(-\pi(a^2(x - x_0)_\theta^2 + b^2(y - y_0)_\theta^2) + j(2\pi(u_0x + v_0y) + P))$$



**Asymmetrical Gaussian of  $128 \times 128$  pixels. The parameters are as follows:**

$$x_0 = y_0 = 0; a = 1/50 \text{ pixels}; b = 1/40 \text{ pixels}; \theta = -45 \text{ deg.}$$

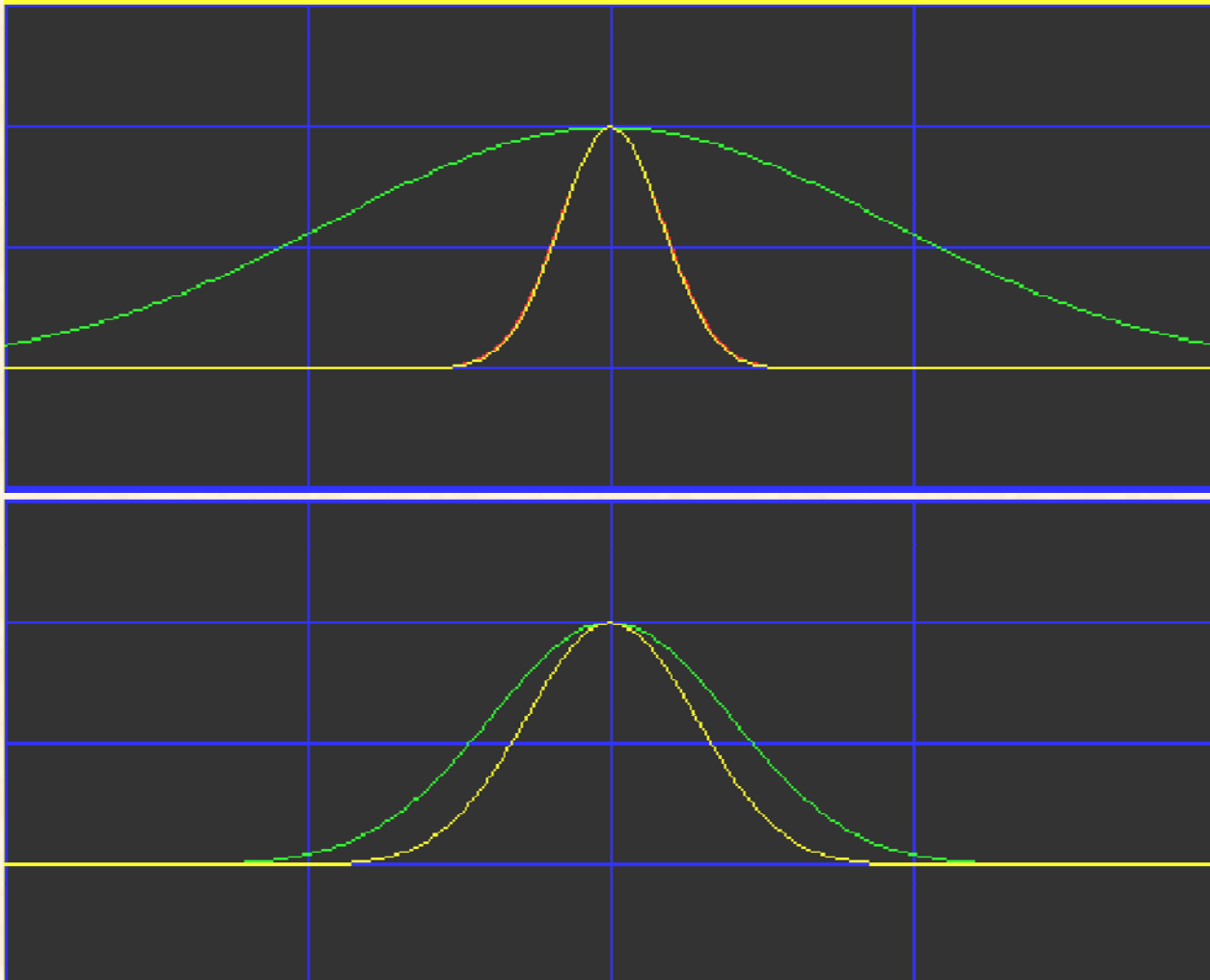
**The real and imaginary parts of a complex Gabor function in space domain, with**

$$F_0 = \sqrt{2}/80 \text{ cycles/pixel}, \omega_0 = 45 \text{ deg}, P = 0 \text{ deg.}$$

## Gaussian and its integral

$$\int_{-\infty}^{\infty} e^{-x^2} dx = \sqrt{\pi}$$

$$\int_{-\infty}^{\infty} a e^{-\frac{(x-b)^2}{2c^2}} dx = ac \cdot \sqrt{2\pi}.$$



## Fourier transform of the **Gaussian**

$$g(x) = e^{-x^2/a}$$

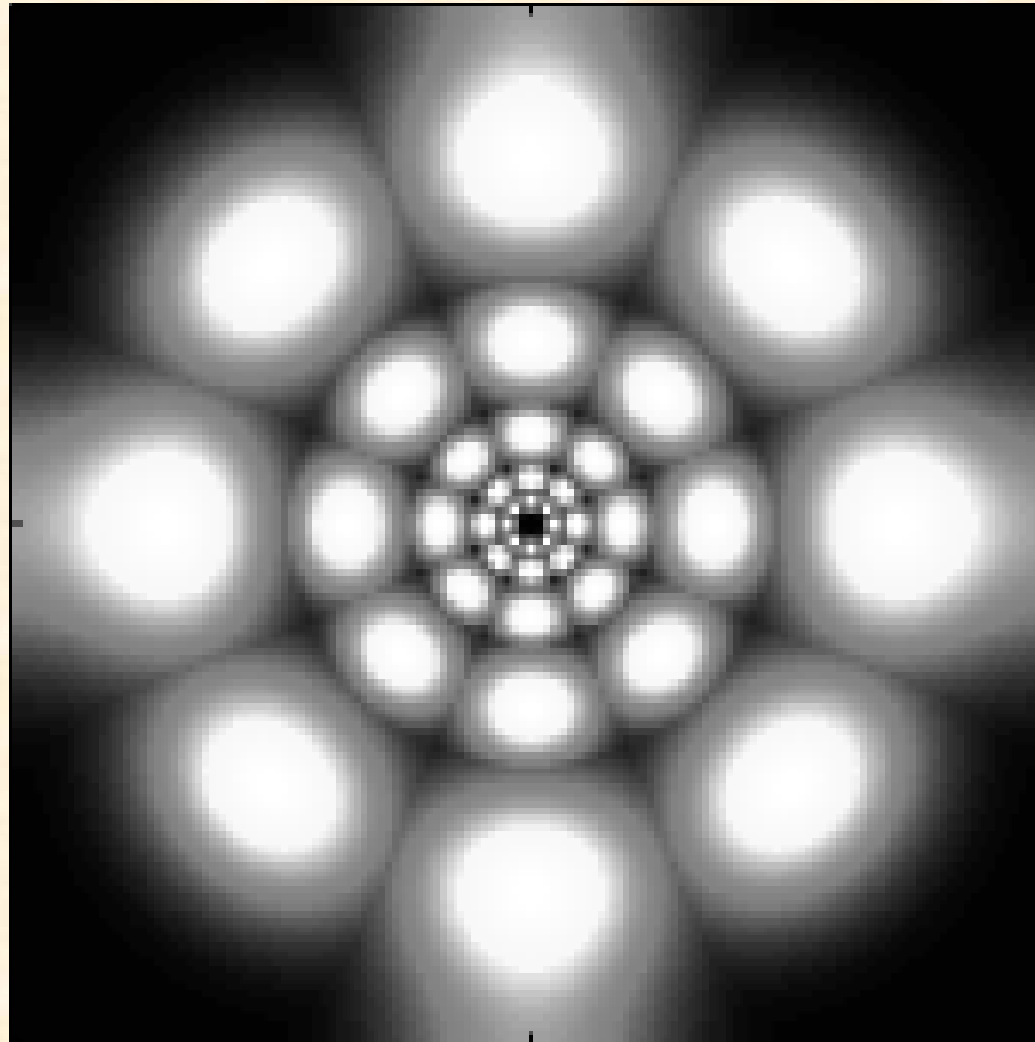
$$G(u) =$$

$$(\sqrt{a\pi}) e^{-au^2/4}$$

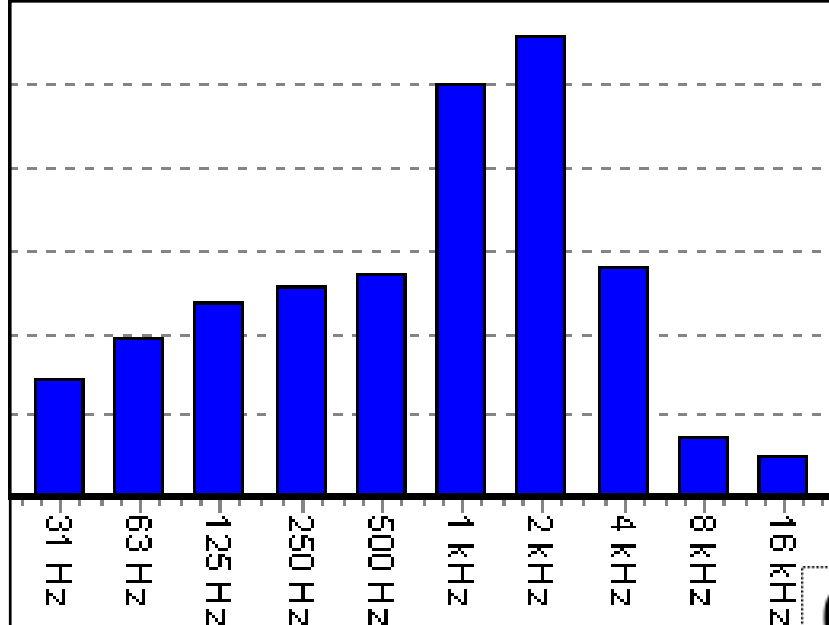
## Fourier transform of the **GABOR** ??

Green – Gaussian; Yellow – FT of Gaussian



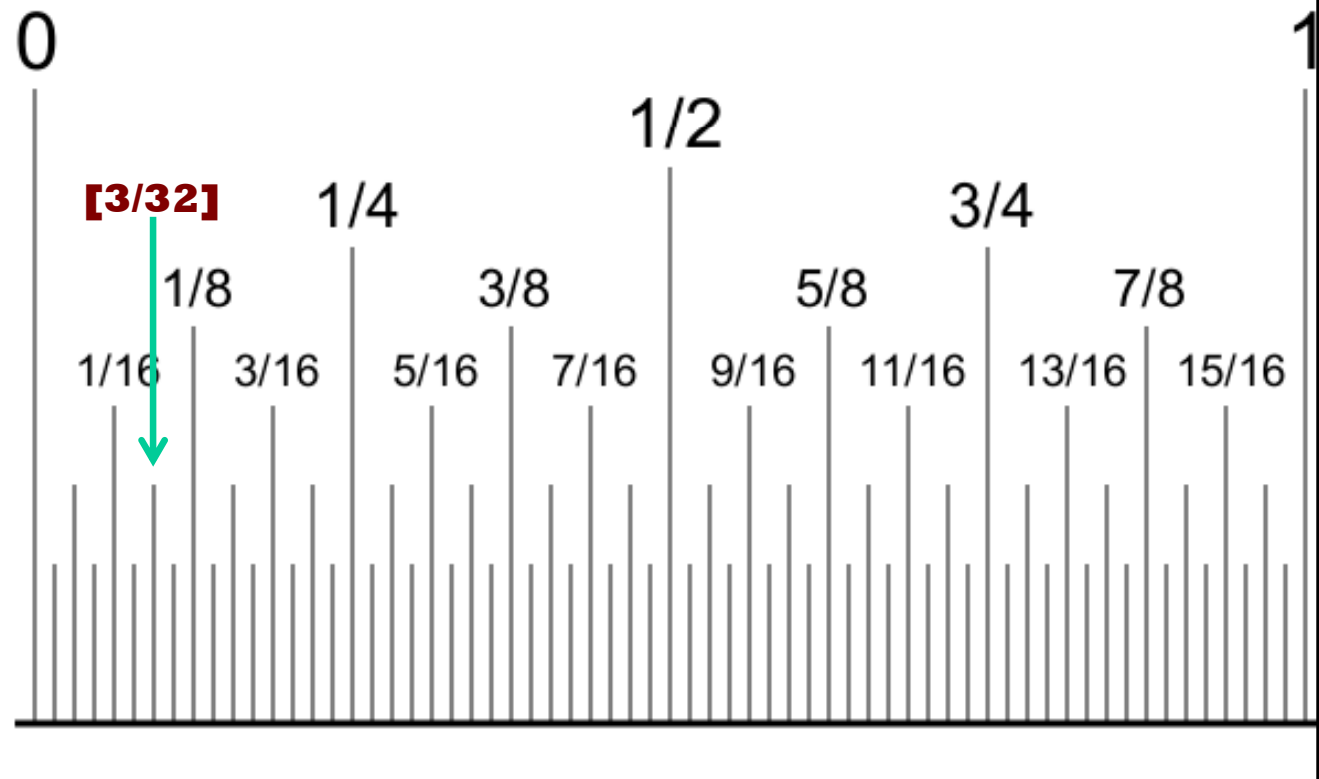


The frequency response of a typical *dyadic* bank of Gabor filters.  
One center-symmetric pair of lobes in the illustration  
represents each filter.



## Octave bands, due to Dyadic decomposition Filter bank


*Read more about –  
in wavelets, QMFB  
and Q-factor  
etc.*



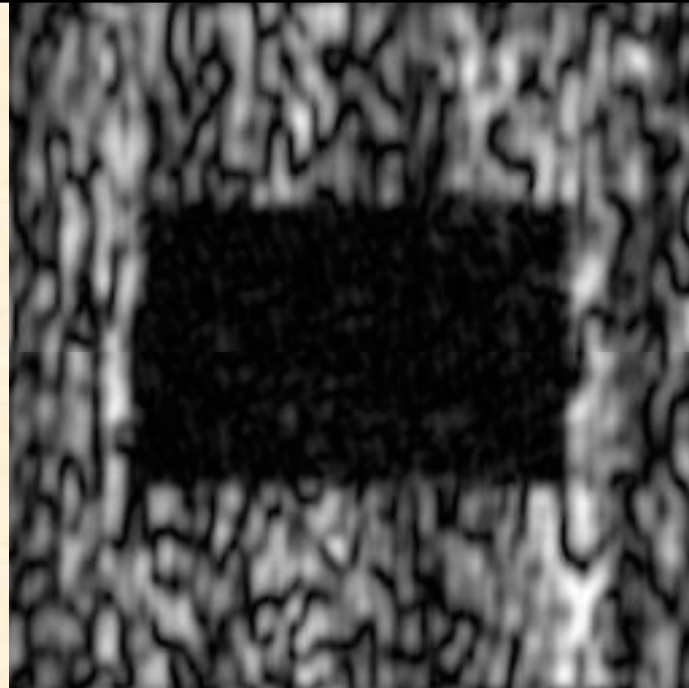
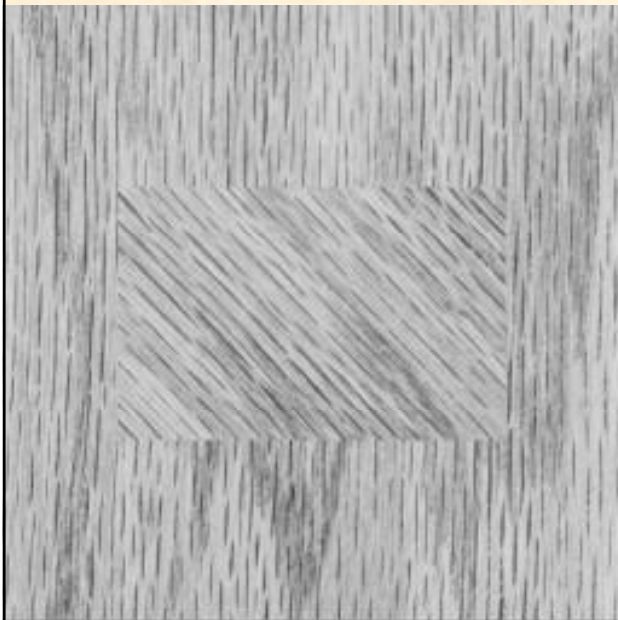
Octave bands:  $..(.., 0.0625); (0.0625, 0.125); (0.125, 0.25); (0.25, 0.5); (0.5, 1)$

Center frequencies: .... 0.0938 (3/32); 0.1875 (3/16); 0.375 (3/8); 0.75 (3/4).

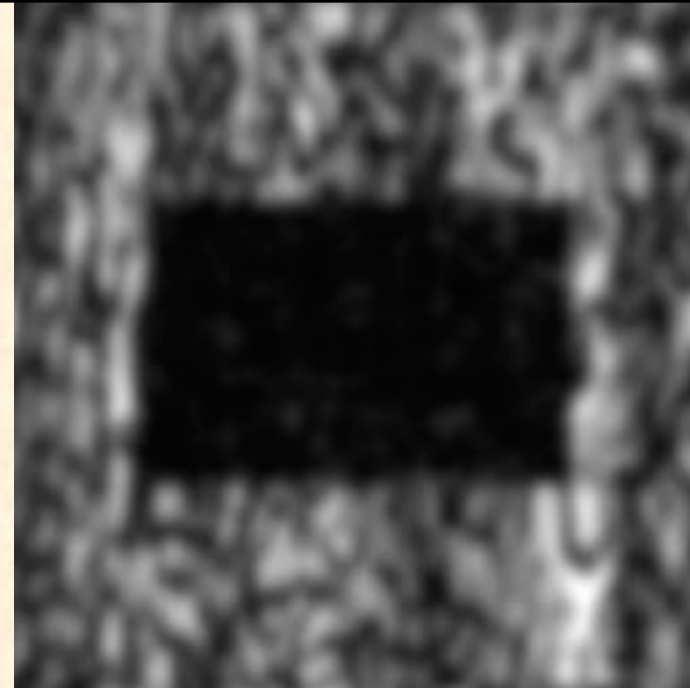
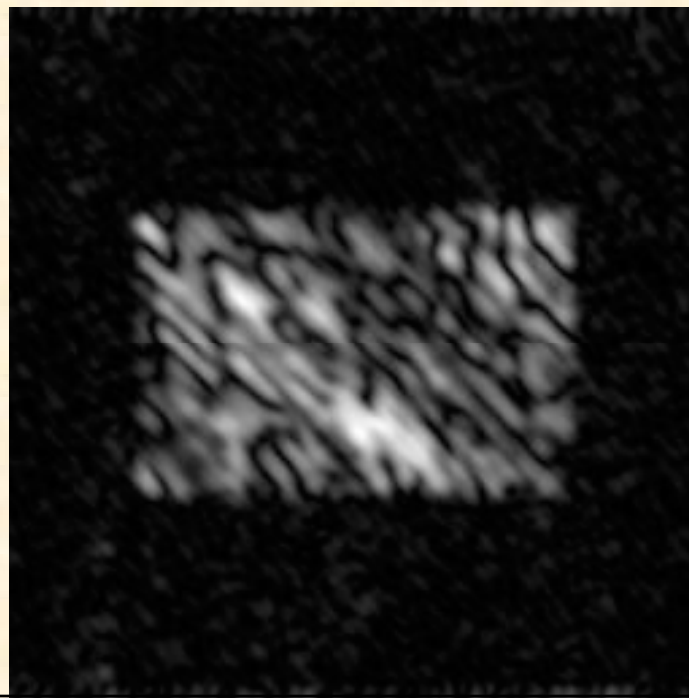
## **Some properties of Gabor filters:**

- **A tunable bandpass filter**
- **Similar to a STFT or windowed Fourier transform**
- **Satisfies the lower-most bound of the time-spectrum resolution (uncertainty principle)** 
- **It's a multi-scale, multi-resolution filter**
- **Has selectivity for orientation, spectral bandwidth and spatial extent.**
- **Has response similar to that of the Human visual cortex (first few layers of brain cells)**
- **Used in many applications – texture segmentation; iris, face and fingerprint recognition.**
- **Computational cost often high, due to the necessity of using a large bank of filters (or Gabor jet) in most applications**

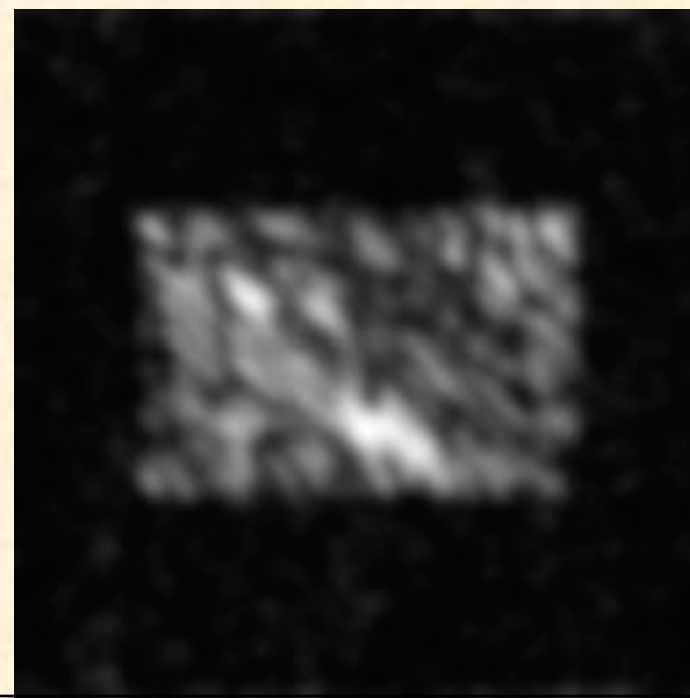
**Texture  
Image**



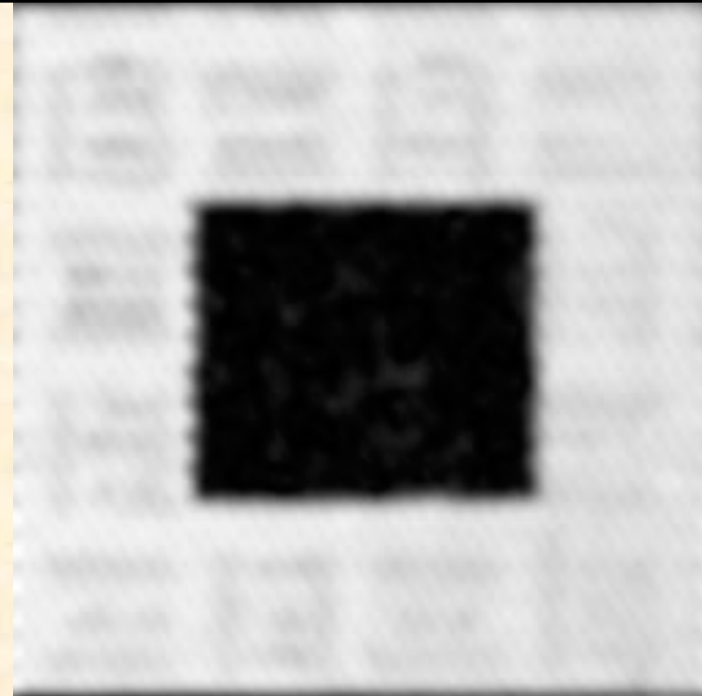
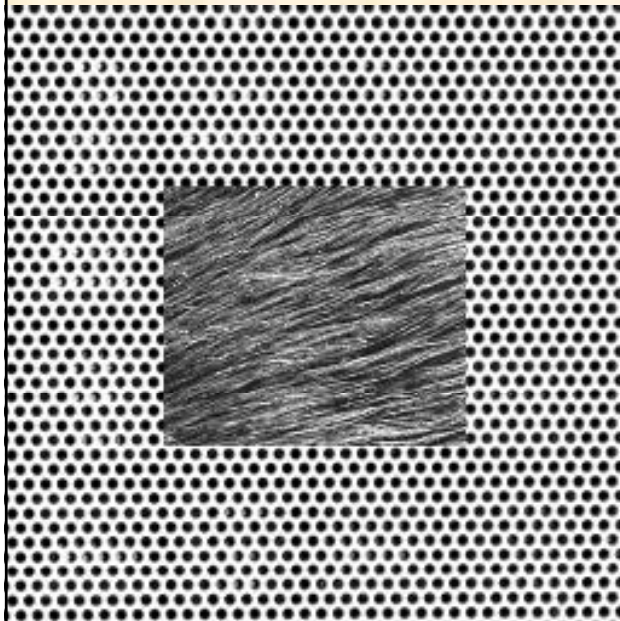
**Magnitude of the  
Gabor Responses**



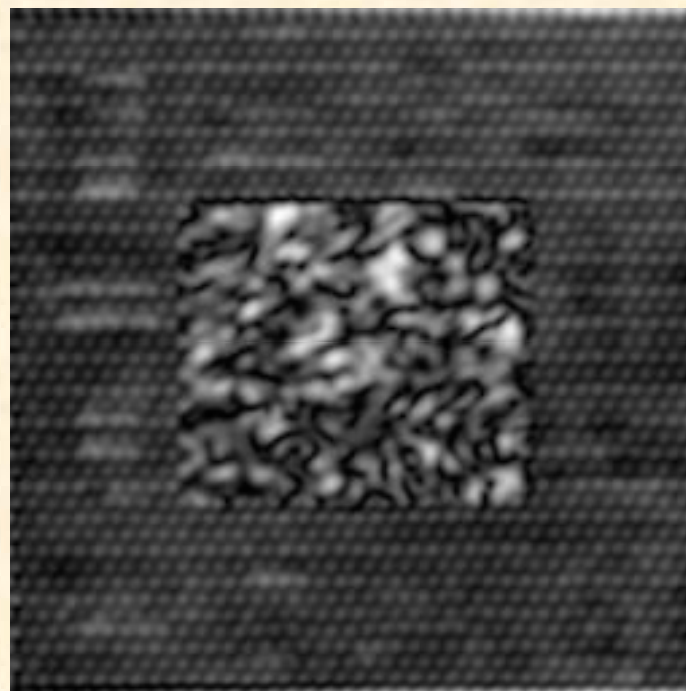
**Smoothed  
Features**



**Texture  
Image**



**Magnitude of the  
Gabor Responses**

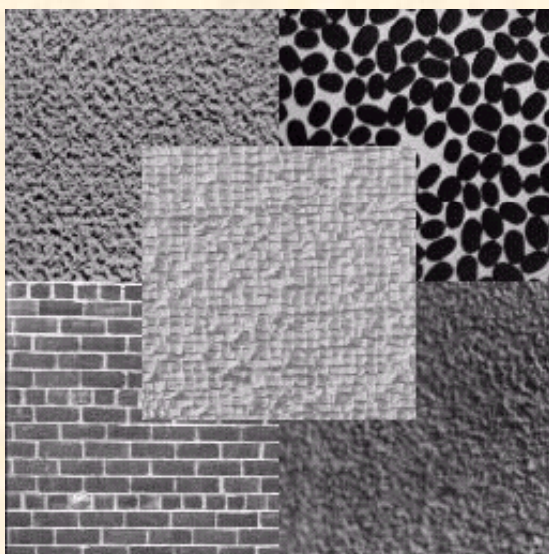


**Smoothed  
Features**

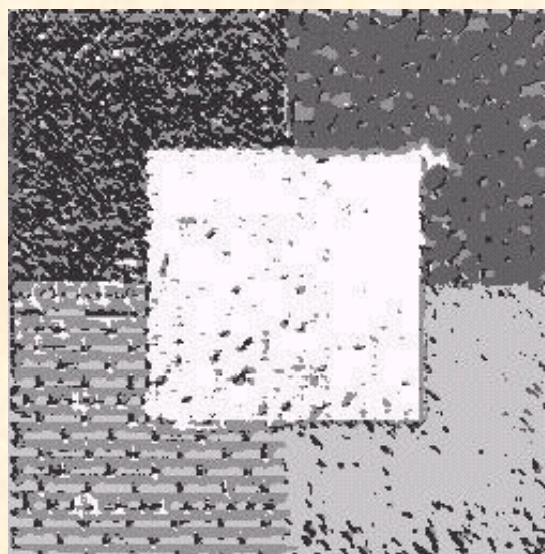




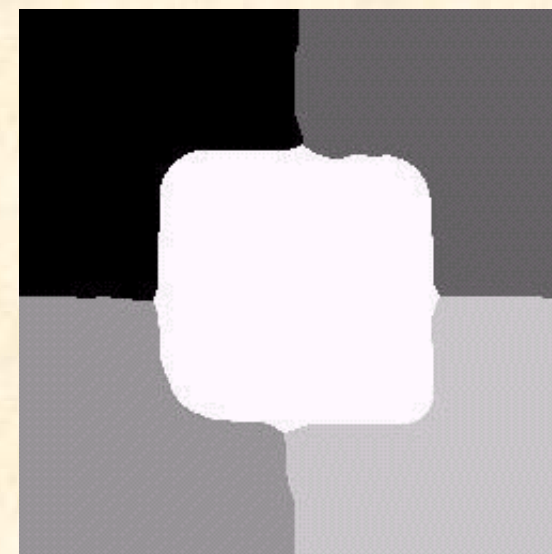
**Natural Textures**

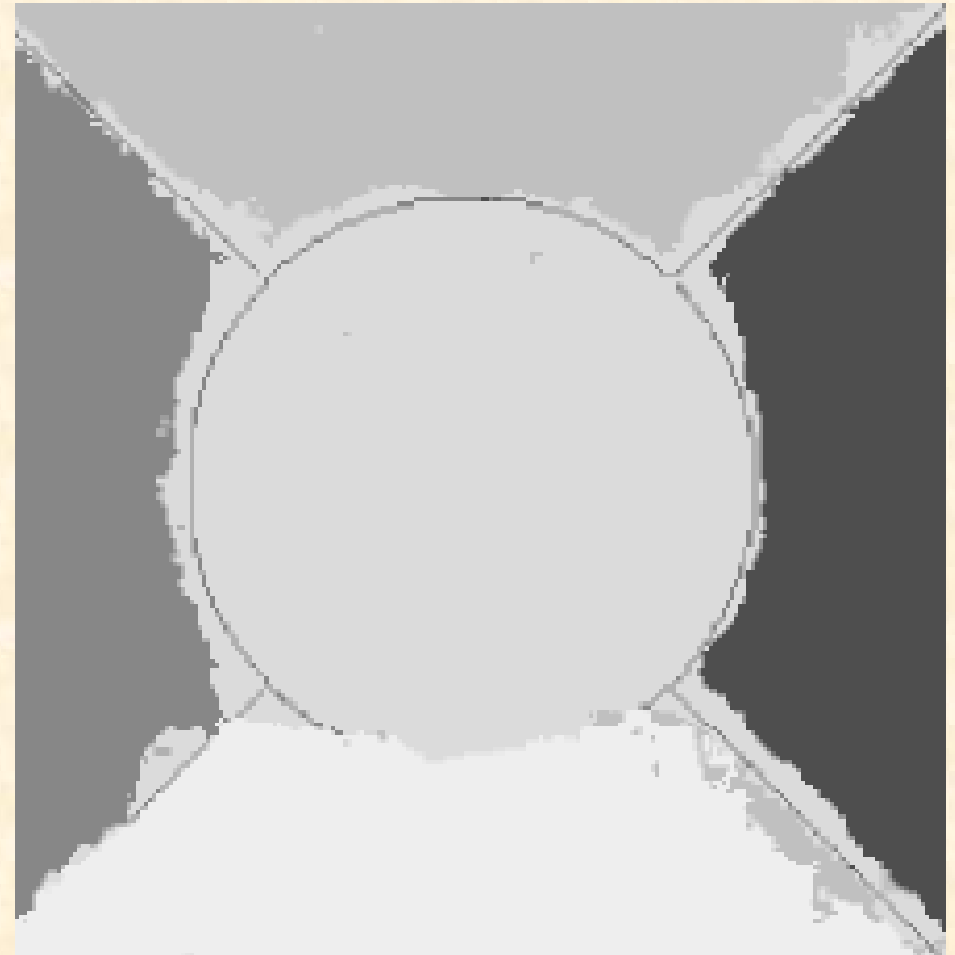
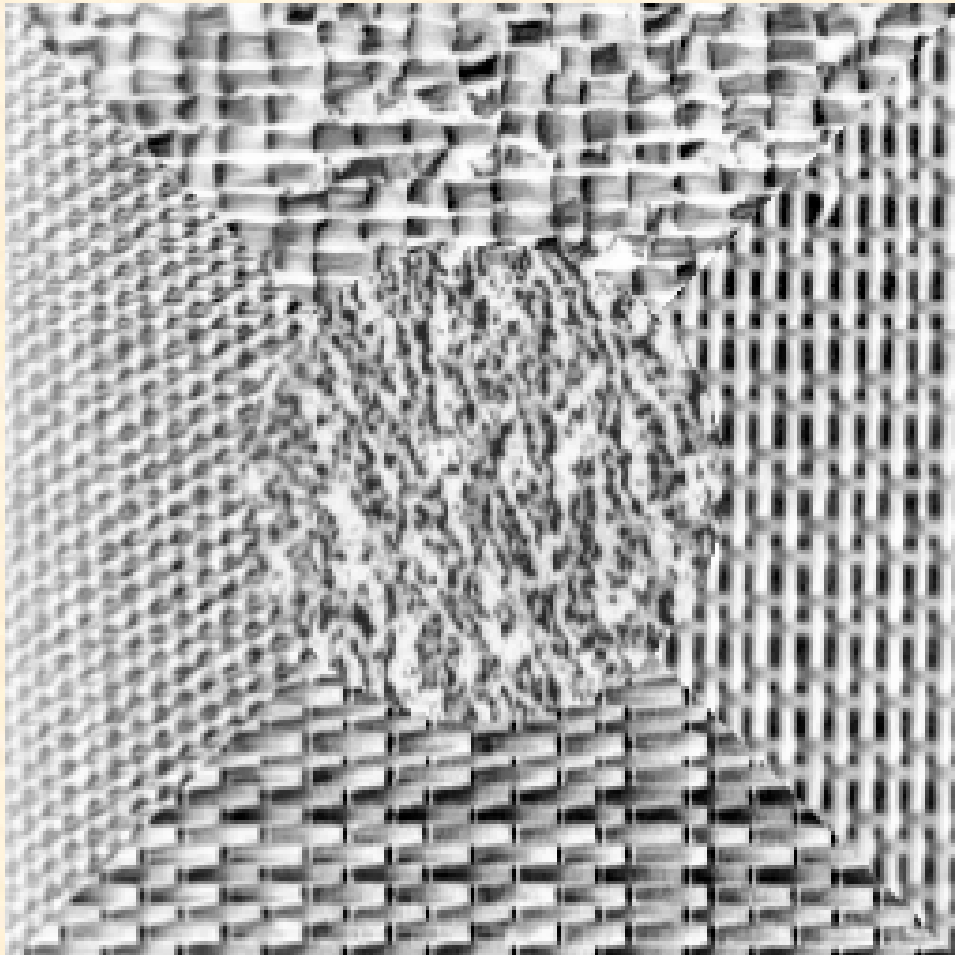


**Initial Classification**



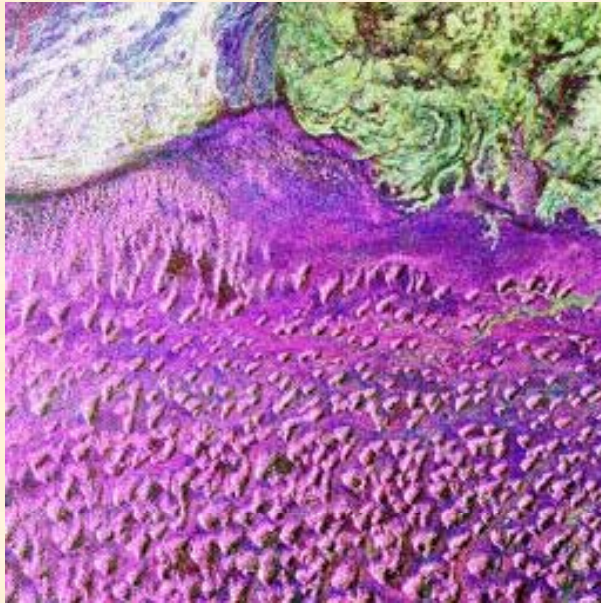
**Final Classification**



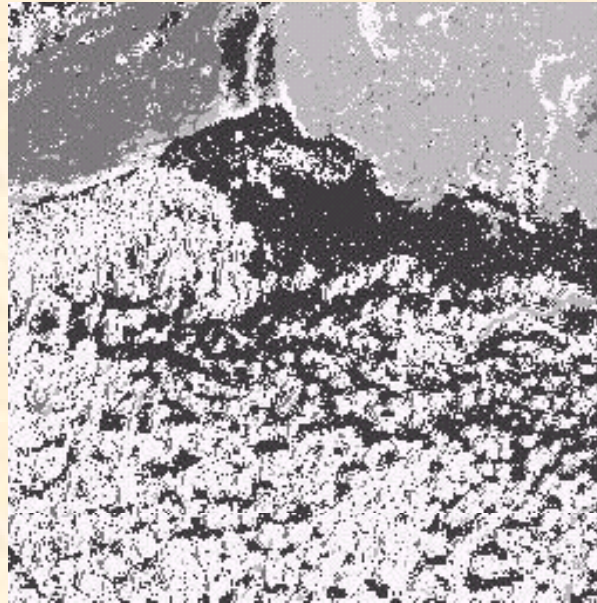


**Segmentation using Gabor based features of a texture image containing five regions.**

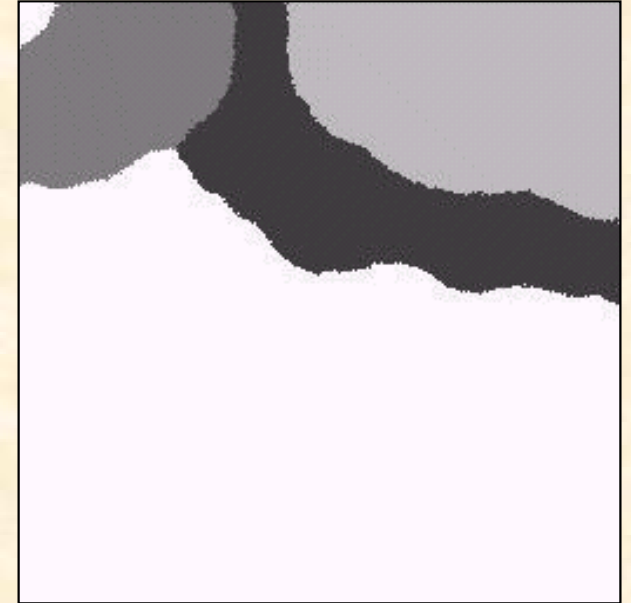
SIR-C/X-SAR image  
of Lost City of Ubar



Classification using  
multispectral information



Classification using  
multispectral and textural  
information





- **Filtering methods:**

- Discrete Wavelet Transform (DWT) (Daubechies 8-Taps)
- Gabor Filter (Bank of 8 Gabor filters)
- Discrete Cosine Transform (DCT) (9 filters) Ref: [Ng 92]
- Gaussian Markov random field models Ref: [Cesmeli 2001]
- Combination of DWT and Gabor filter Ref: [Rao 2004]
- Combination of DWT and MRF Ref: [Wang 99]

- **Non-linearity:**

- Magnitude ( $|\cdot|$ )

- **Smoothing:**

- Gaussian filter

- Combine Edge and region map using a CSNN

- **Feature vectors:**

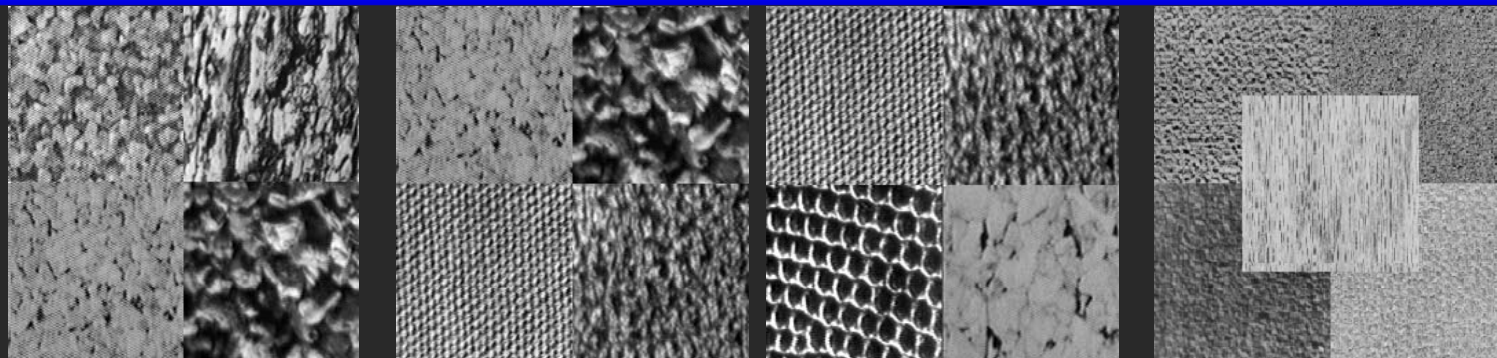
- Mean (computed in a local window around a pixel)

- **Classification:**

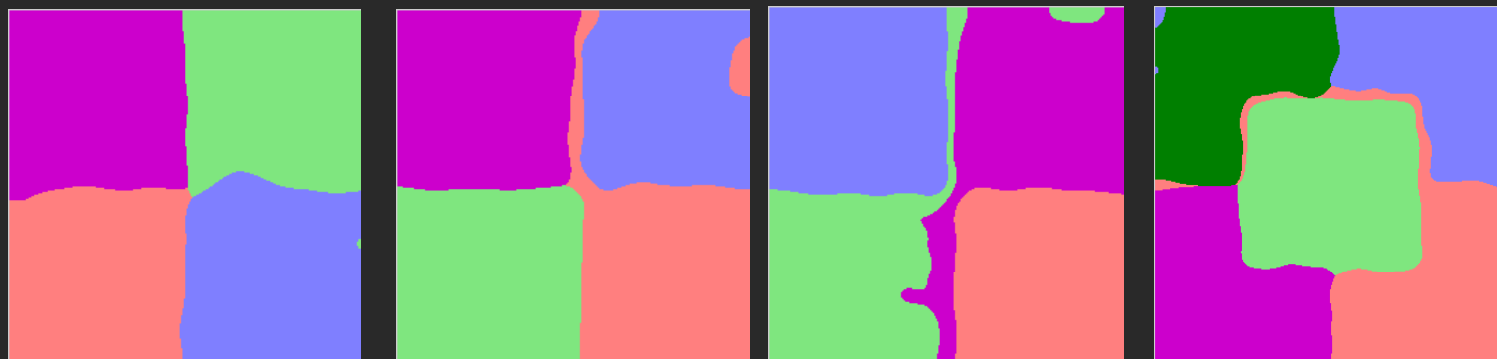
- Fuzzy-C Means (FCM) (unsupervised classifier)

# Results

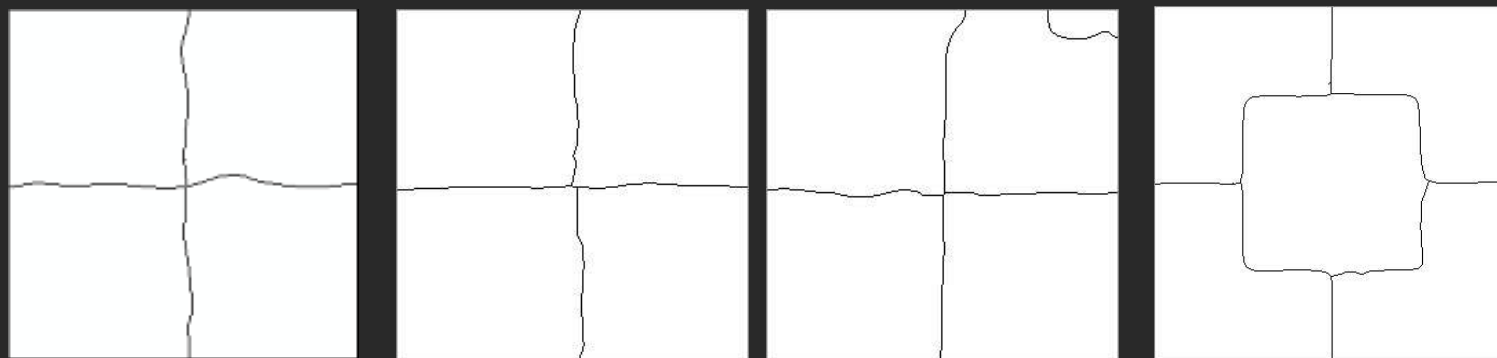
Input Image



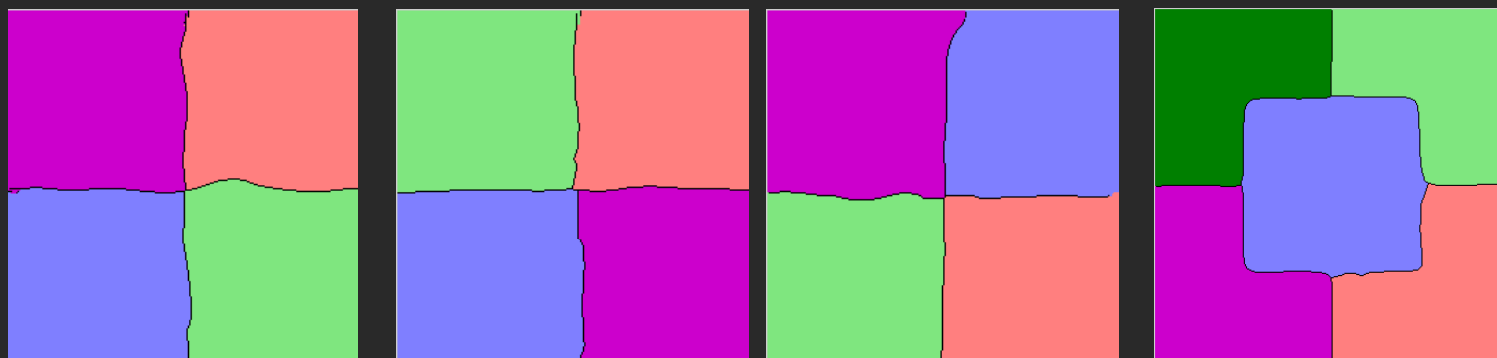
Segmented map  
before integration



Edge map before  
integration

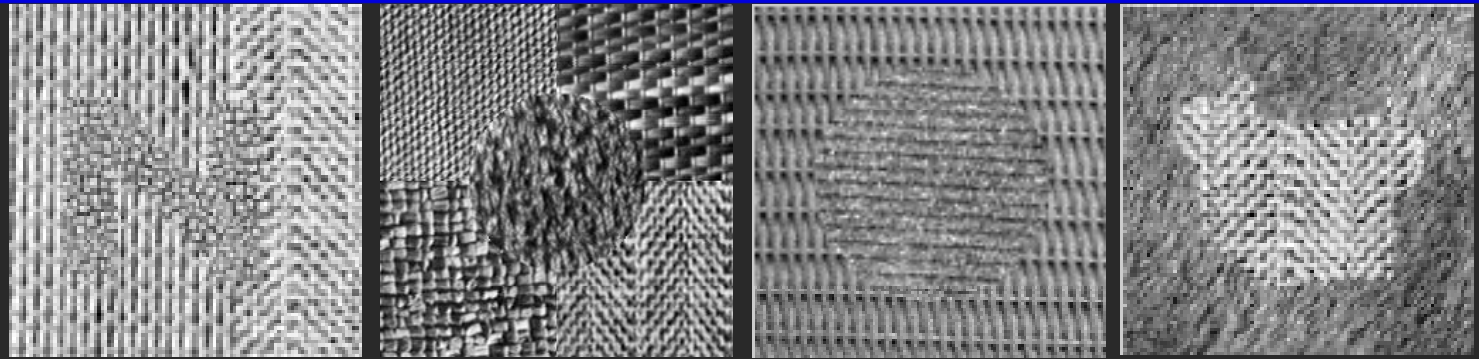


Segmented map  
and Edge map  
after integration

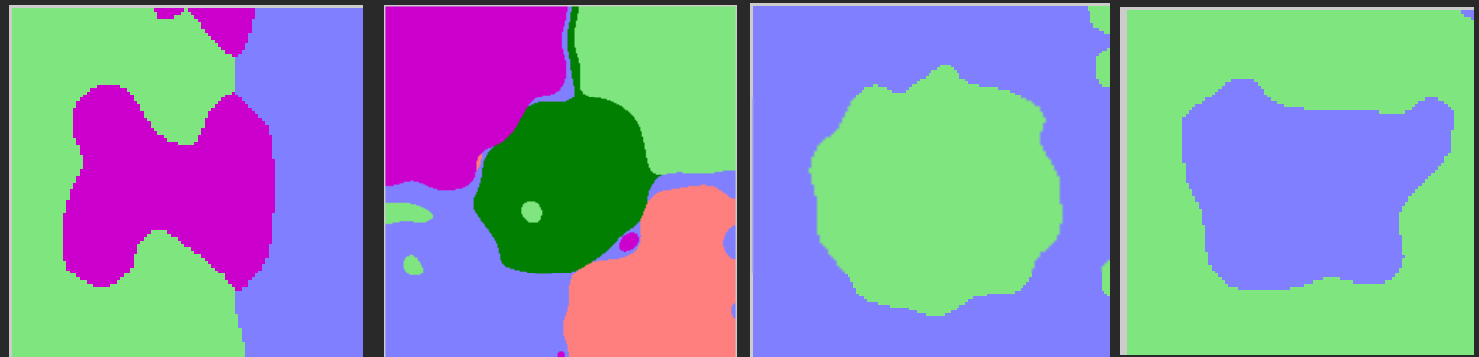


# Results

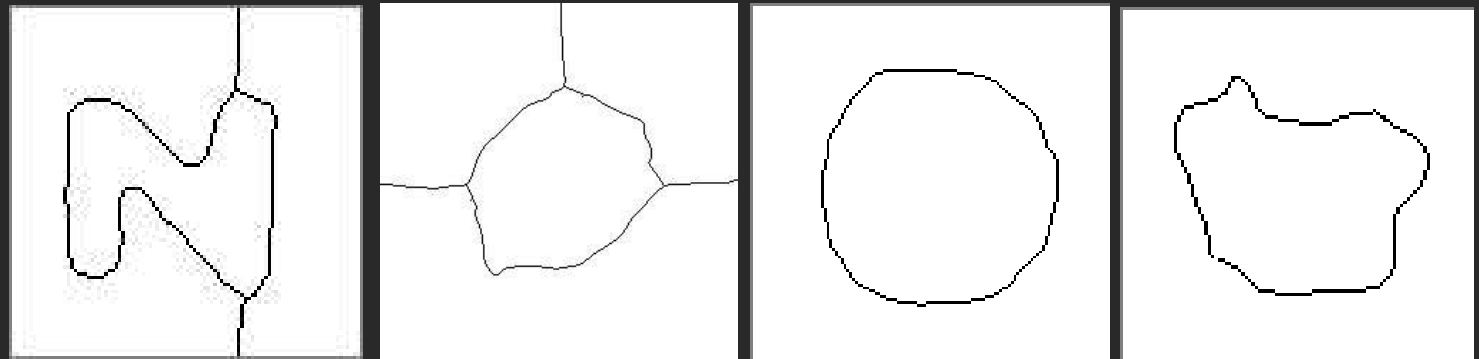
Input Image



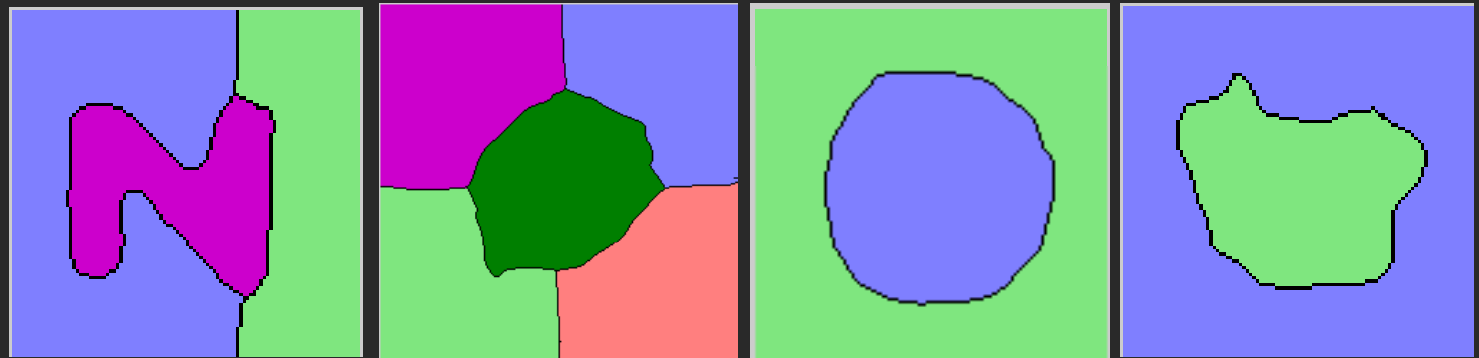
Segmented map  
before integration



Edge map before  
integration



Segmented map  
and Edge map  
after integration



## GLCM based texture feature (statistical)

The Grey Level Co-occurrence Matrix, GLCM  
(also called the **Grey Tone Spatial Dependency Matrix**)

The GLCM is a tabulation of how often different combinations of pixel brightness values (grey levels) occur in an image.

The GLCM is usually defined for a series of "second order" texture calculations.

**Second order** means they consider the relationship between groups of two pixels in the original image.

**First order** texture measures are statistics calculated from the original image values, like variance, and do not consider pixel relationships. **Third and higher order** textures (considering the relationships among three or more pixels) are theoretically possible but not implemented due to calculation time and interpretation difficulty.

0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

*A small image neighborhood*

<u>NPV &gt;</u>				
RPV	0	1	2	3
0				
1				
2				
3				

Spatial relationship  
between two pixels:

Neighbor/Reference Pixel Value

GLCM texture considers the relation between two pixels at a time, called the reference and the neighbour pixel. Let, the neighbour pixel is chosen to be the one to the **east (right)** of each reference pixel. This can also be expressed as a **(1,0) relation**:  $(i, j) \rightarrow (i+1, j)$ .

Each pixel within the window becomes the reference pixel in turn, starting in the upper left corner and proceeding to the lower right.

0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

*A small image neighborhood*

**(-1,0) relation:**  $(i, j) \rightarrow (i-1, j)$ .

*EAST*  
*GLCM*

<u>NPV&gt;</u> <u>RPV</u>	0	1	2	3
0	2	2	1	0
1	0	2	0	0
2	0	0	3	1
3	0	0	0	1

*WEST GLCM (why transpose ?)*

**Symmetrical (1,0) GLCM**

<u>NPV&gt;</u> <u>RPV</u>	0	1	2	3
0	2	0	0	0
1	2	2	0	0
2	1	0	3	0
3	0	0	1	1

<u>NPV&gt;</u> <u>RPV</u>	0	1	2	3
0	4	2	1	0
1	2	4	0	0
2	1	0	6	1
3	0	0	1	2



## Expressing the GLCM as a probability:

This is the number of times this outcome occurs, divided by the total number of possible outcomes.

This process is called normalizing the matrix. Normalization involves dividing by the sum of values.

## Symmetrical (1,0) GLCM

<u>NPV&gt;</u> <u>RPV</u>	0	1	2	3
0	4	2	1	0
1	2	4	0	0
2	1	0	6	1
3	0	0	1	2

$$P_{i,j} = \frac{V_{i,j}}{\sum_{i,j=0}^{N-1} V_{i,j}}$$

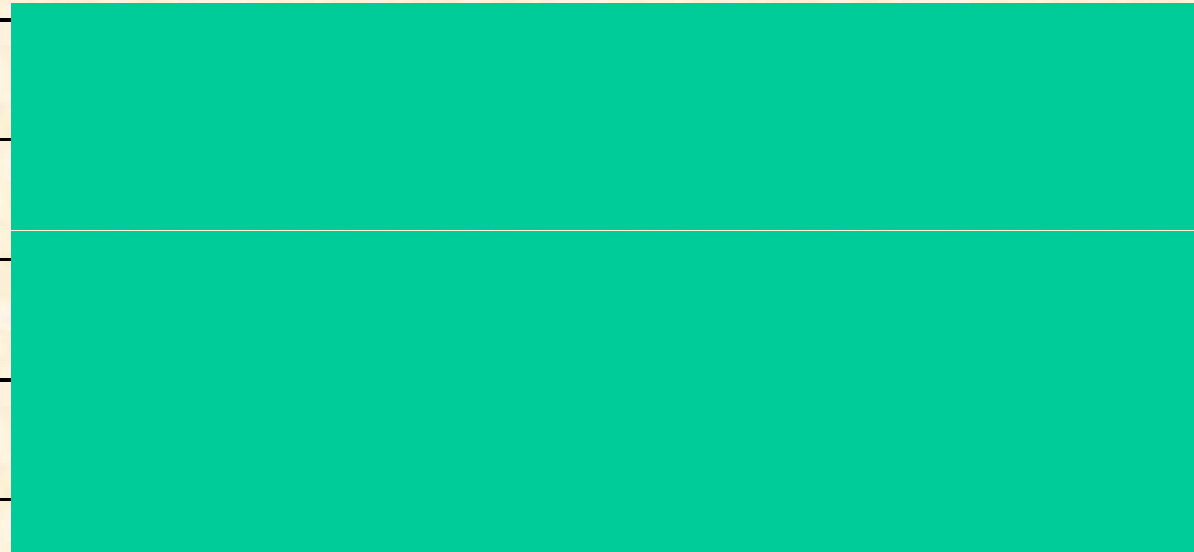
.166 (4/24)	.083 (2/24)	.042 (1/24)	0 (0/24)
.083	.166	0	0
.042	0	.25	.042
0	0	.042	.083

**Find,  
(1,0), South GLCM (solve it):**

*A small image  
neighborhood*

0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

3	0	2	0
0	2	2	0
0	0	1	2
0	0	0	0



**Normalized symmetrical  
vertical GLCM**

.250	0	.083	0
0	.166	.083	0
.083	.083	.083	.083
0	0	.083	0

*Any reason for  
Diagonal dominance ?*



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