Redox & Energetics Cheatsheet

Oxidation state

The following rules allow you to work out the oxidation states for elements with complex oxidation states.

- 1. Any atoms in elemental form have an oxidation state of 0 ex: O₂, N₂, S₀, Fe(s)
- 2. The more electronegative elements in a compound will have a negative oxidation state, while the less electronegative elements in a compound will have a positive oxidation state. As a result of their electronegativities, some elements will almost always have certain oxidation states.
- Alkali metals are always +1
- Alkaline earth metals are always +2
- Fluorine is always -1
- Hydrogen is almost always +1 (Exception: metal hydrides, ex: NaH, where H is -1 because Na is +1 and the compound is neutral.)
- Oxygen is almost always -2 (Exceptions: peroxides, ex H₂O₂, where O is -1 because H can only donate 1 electron and the compound is neutral; and F_2O , where O is +2 because F is the only thing more electronegative than O.
- 3. The sum of oxidation states in a species is equal to the net charge of the species.

Redox reactions

Half reactions

A generalized redox reaction $aA_{ox} + bB_{red} \longrightarrow cC_{red} + dD_{ox}$ can also be written as two half reactions.

- $\begin{array}{ccc} \bullet & aA_{ox} + ne^{-} \longrightarrow cC_{red} \\ \bullet & bB_{red} \longrightarrow dD_{ox} + ne^{-} \end{array}$

Rules for balancing redox reactions

The following is one possible approach for systematically balancing redox reactions.

- 1. Separate out the two half reactions
- 2. Balance all elements except H & O
- 3. Balance O with H₂O
- 4. Balance H with H⁺
- 5. Balance charge with e⁻ [check yourself here that the number of electrons transferred matches the change in oxidation state
- 6. Multiply half reactions so that the number of electrons match
- 7. Add half reactions together

Energetics

Consider the generalized redox reaction:

$$a \cdot A_{ox} + b \cdot B_{red} \longrightarrow c \cdot C_{red} + d \cdot D_{ox}$$

Gibbs free energy

The Gibbs free energy of reaction (ΔG_R) quantifies the potential thermodynamic energy of the reaction ($< 0 \rightarrow exothermic$, $> 0 \rightarrow endothermic, = 0 \rightarrow at\ equilibrium)$ and can be calculated with:

$$\Delta G_R = \Delta G_R^0 + RT \ln \frac{\left[\mathcal{C}_{\text{red}}\right]^c \left[\mathcal{D}_{\text{ox}}\right]^d}{\left[\mathcal{A}_{\text{ox}}\right]^a \left[\mathcal{B}_{\text{red}}\right]^b} = \Delta G_R^0 + RT \ln Q$$

The standard Gibbs free energy of the reaction ΔG_R^0 is:

$$\Delta G_R^0 = \left(\sum \Delta G_f\right)_{products} - \left(\sum \Delta G_f\right)_{reactants} = -RT \ln K_{eq}$$

Nernst potential

The redox potential (E) or electromotrive force is the electron-centric view of a redox reaction (as opposed to the reactant/product centric view inherent in the Gibbs free energy), the two are related as follows:

$$\Delta G_R = -n_{e^-} \cdot F \cdot E$$

$$\Delta G_R^0 = -n_{e^-} \cdot F \cdot E^0$$

Assuming the reaction is at 25C, plugging in the constants and switching from natural log to base 10 logarithm, this becomes:

$$E = E^{0} - \frac{RT}{n_{e^{-}}F} \ln Q = E^{0} - \frac{59.2 \,\text{mV}}{n_{e^{-}}} \log Q$$

Electron activity

The electron activity pe is a theoretical concept similar to pH (the proton activity) that can be calculated from the equilibrium constant (K_{eq}) and reaction quotient (Q) of a redox couple $A_{ox} + e^- \rightleftharpoons A_{red}$:

$$pe^{0} = \frac{1}{n_{e^{-}}} \log K$$
$$pe = pe^{0} - \frac{1}{n_{e^{-}}} \log Q$$

E and pe are related by $E = \frac{\ln 10RT}{F}$ pe = 59.2 mV · pe

Units

- Temperature (T): in degrees Kelvin (K) unless otherwise specified
- Gibbs free energy of reaction (ΔG_R): usually in kJ₁mol (sometimes J₁mol) where mol refers to one of the products or
- Gibbs free energy of formation (ΔG_f): same units as ΔG_R (kJ, mol)
- Equilibrium constant (K_{eq}) : dimensionless, technically based on activities instead of concentrations but concentrations are a reasonable approximation in dilute solutions
- Reaction quotient (Q): dimensionless ratio of products over reactions $\left(\prod (c_i^{n_i})_{prod} / \prod (c_i^{n_i})_{reac}\right)$, also technically based on activities
- Nernst potential aka redox potential, electromotive force (E): in volts (V) or milli volts (mV)
- Number of electrons (n_{e^-}) : dimensionless (usually an integer number)
- Electron Activity (pe): dimensionless

Constants

- The ideal gas constant (R): $8.314 \cdot 10^{-3} \frac{kJ}{K \cdot mol}$ The Farady constant (F): $96.49 \frac{kJ}{V \cdot mol \ e^-}$