

# Visual-Odometric Localization and Mapping for Ground Vehicles Using SE(2)-XYZ Constraints

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## Objective and Motivation

- For ground vehicle SLAM, to estimate on-SE(2) ground vehicle poses without neglecting the out-of-SE(2) perturbation in real-world scenarios.

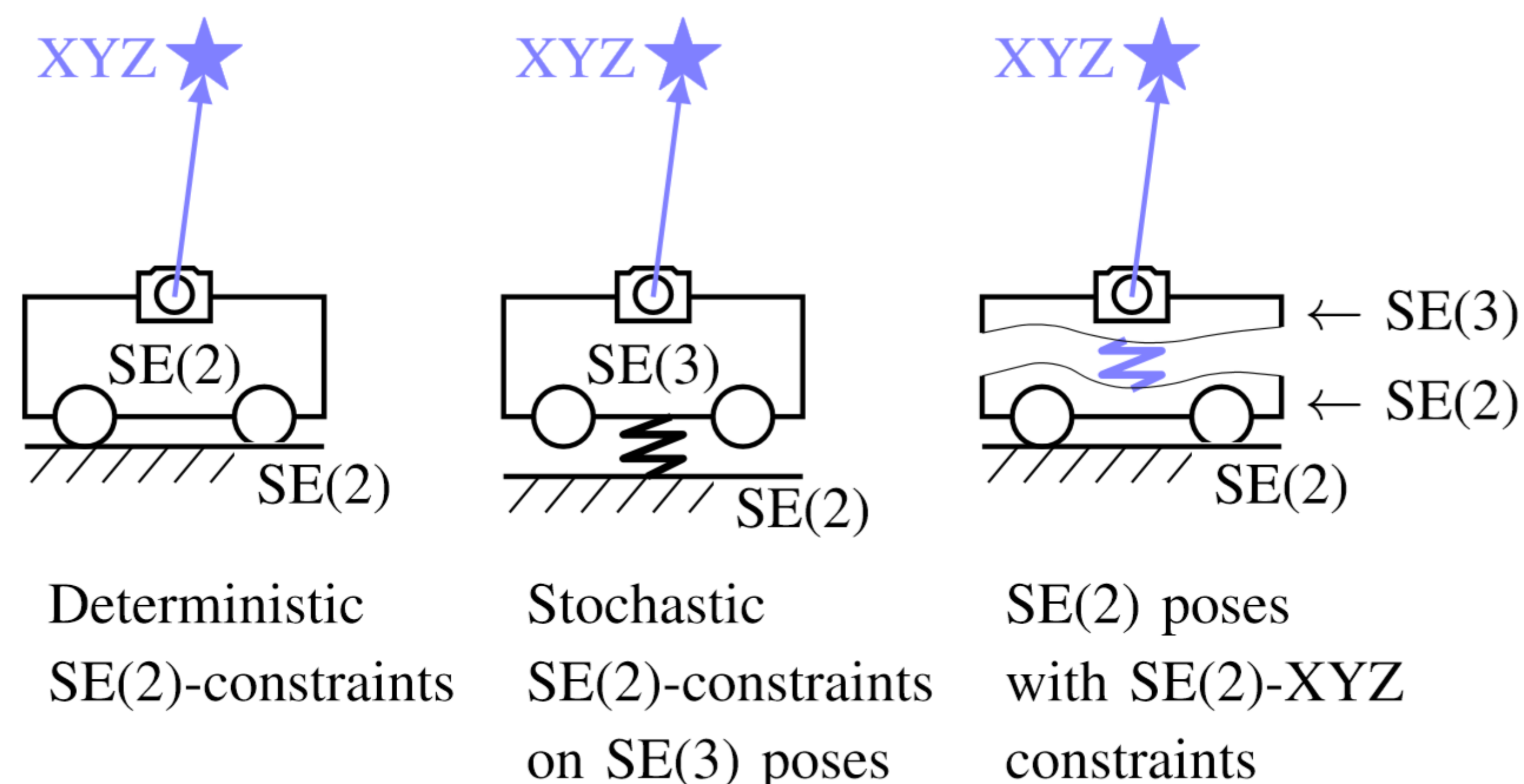


Fig 1. (a) Deterministic SE(2)-constraints are not accurate on rough terrains. (b) Stochastic SE(2)-constraints on SE(3) poses are accurate enough, but redundant. (c) SE(2)-XYZ constraints are compact and accurate

## Methodology

### 1. GRAPH OPTIMIZATION WITH

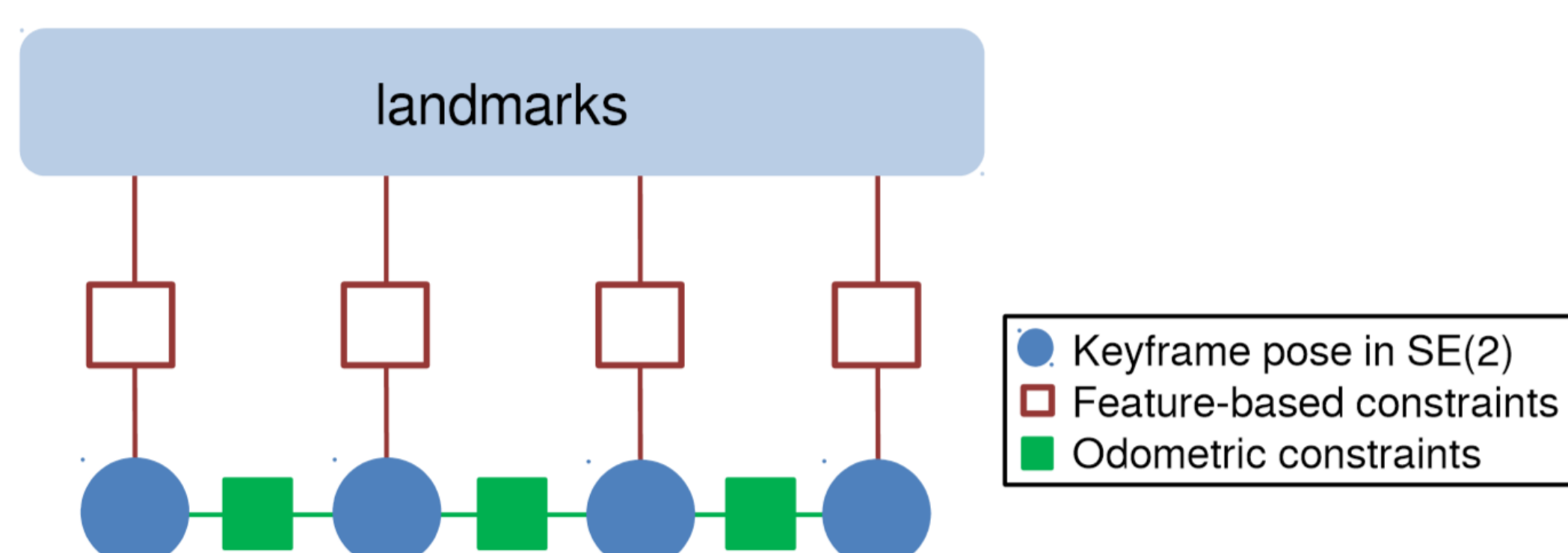


Fig 2. The graph structure for optimization.

#### 1) SE(2)-XYZ Constraints

Consider the perturbed SE(2) poses on SE(3):

$$\mathbf{R}_i \leftarrow \underbrace{\text{Exp}([\eta_{\theta_{xy}}^T \ 0]^T)}_{\eta_{\theta}} \mathbf{R}_i, \quad \mathbf{p}_i \leftarrow \mathbf{p}_i + \underbrace{[0 \ 0 \ \eta_z]^T}_{\eta_z}.$$

Then the linearized measurement model for the constraint:

$$\begin{aligned} \mathbf{u}(\nu_i, \mathbf{l}_\ell) &= \pi \left( {}^C \mathbf{R}_B \mathbf{R}_i^T \text{Exp}(-\eta_{\theta})(\mathbf{l}_\ell - \mathbf{p}_i - \eta_z) + {}^C \mathbf{p}_B \right) \\ &\quad + \eta_u \\ &\approx \pi({}^C \mathbf{l}_\ell) + \mathbf{J}_{\eta_{\theta}}^u \eta_{\theta} + \mathbf{J}_{\eta_z}^u \eta_z + \eta_u \end{aligned}$$

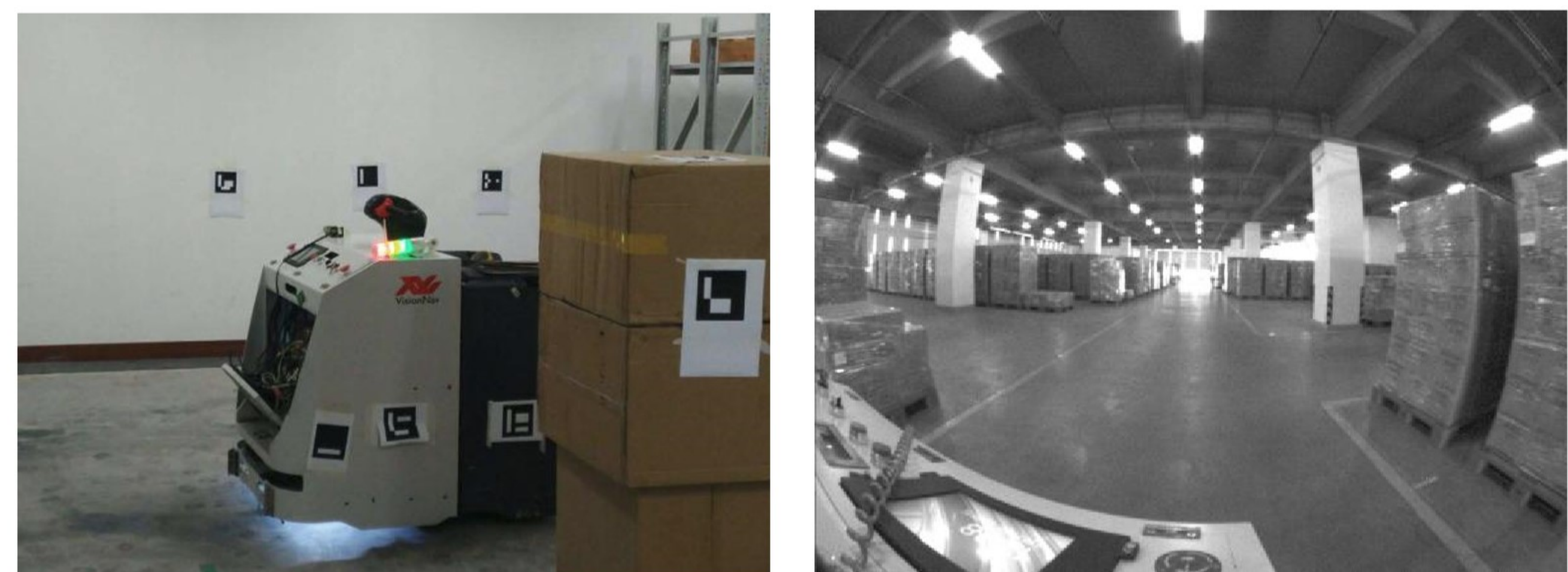
#### 2) On-SE(2) Preintegrated Odometric Constraints

Similar to preintegration for VINS, but on SE(2):

$$\begin{aligned} {}^i \phi_j &= \sum_{k=i}^{j-1} (\tilde{\phi}_k - \eta_{\phi k}) = \sum_{k=i}^{j-1} \tilde{\phi}_k - \sum_{k=i}^{j-1} \eta_{\phi k} \\ {}^i \mathbf{r}_j &\approx \sum_{k=i}^{j-1} \Phi({}^i \tilde{\phi}_k) \tilde{\mathbf{r}}_k - \sum_{k=i}^{j-1} \Phi({}^i \tilde{\phi}_k) (\eta_{rk} + \delta^i \phi_k^{\times} \tilde{\mathbf{r}}_k) \end{aligned}$$

### 2. PARALLEL TRACKING, MAPPING, LOOP CLOSING

## Results



(a) AGV for experiments.

(b) Dataset Warehouse environment.

Fig 3. The AGV and one testing field, by VisionNav Robotics Ltd.

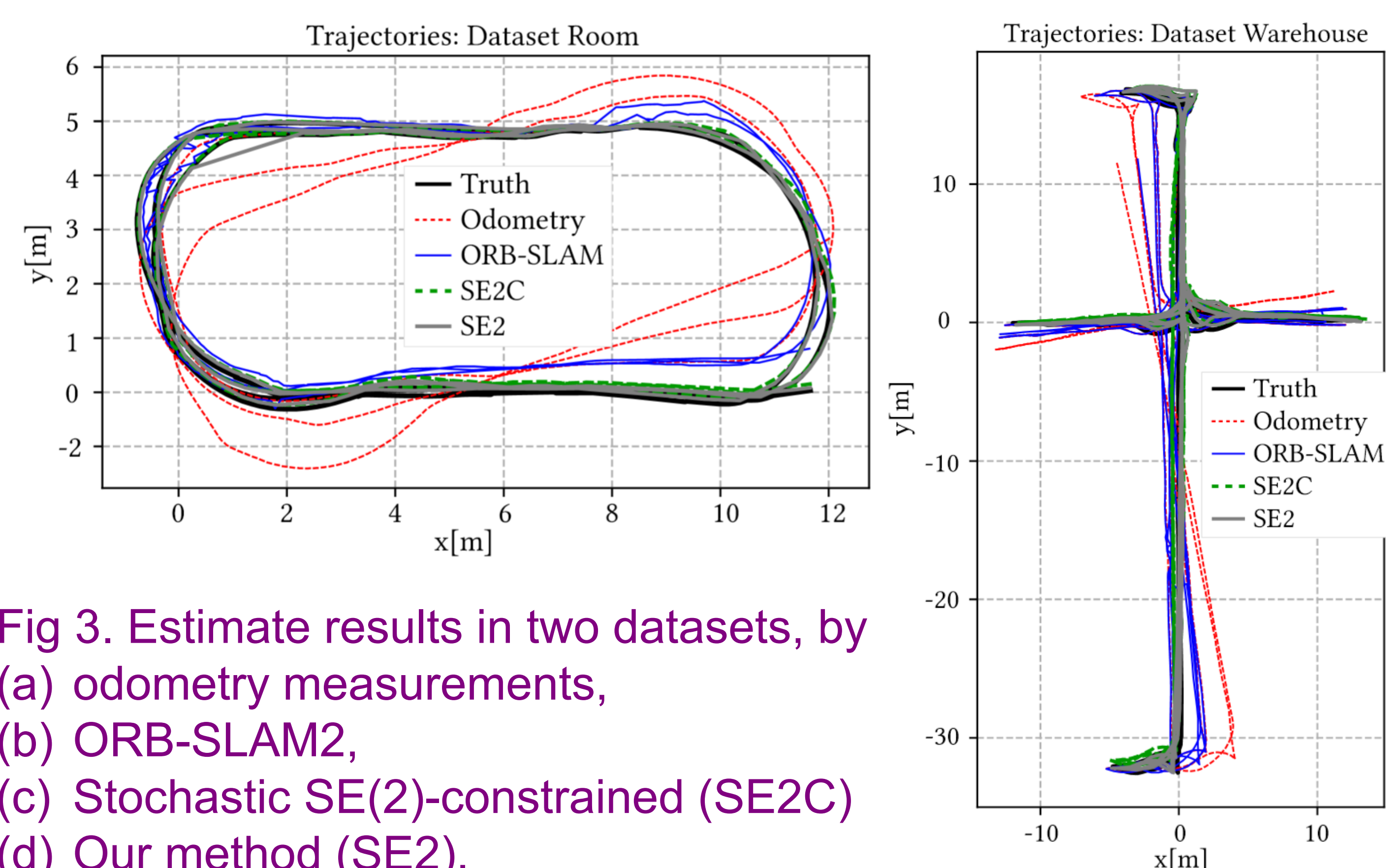


Fig 3. Estimate results in two datasets, by (a) odometry measurements, (b) ORB-SLAM2, (c) Stochastic SE(2)-constrained (SE2C) (d) Our method (SE2), (e) the ground truth

TABLE I  
ESTIMATION ERRORS STATISTICS (RMSE)

	Odom.	ORB-SLAM	SE2C	SE2
<b>DATASET ROOM</b>				
x err. (mm)	541.24	135.33	62.44	61.106
y err. (mm)	1028.83	371.01	93.15	59.021
$\phi$ err. (rad)	0.24835	0.12809	0.01567	0.01181
trans. err.(mm)	1162.51	394.93	112.15	84.956
accuracy*	4.469%	1.343%	0.381%	0.288%
<b>DATASET WAREHOUSE</b>				
x err. (mm)	1615.19	1038.66	304.22	171.129
y err. (mm)	460.90	507.13	393.87	279.766
$\phi$ err. (rad)	0.10062	0.17149	0.03924	0.04921
trans. err.(mm)	1679.67	1155.85	497.68	327.955
accuracy	1.142%	0.787%	0.339%	0.223%

\*Accuracy is calculated by the translation error over the travel distance in *one loop*.

## More Info

- Open source !

[github.com/izhengfan/se2lam](https://github.com/izhengfan/se2lam)

