

# Chapter 5: Mining Frequent Patterns, Association and Correlations

**Dong-Kyu Chae**

**PI of the Data Intelligence Lab @HYU  
Department of Computer Science & Data Science  
Hanyang University**

# Challenges of Frequent Pattern Mining

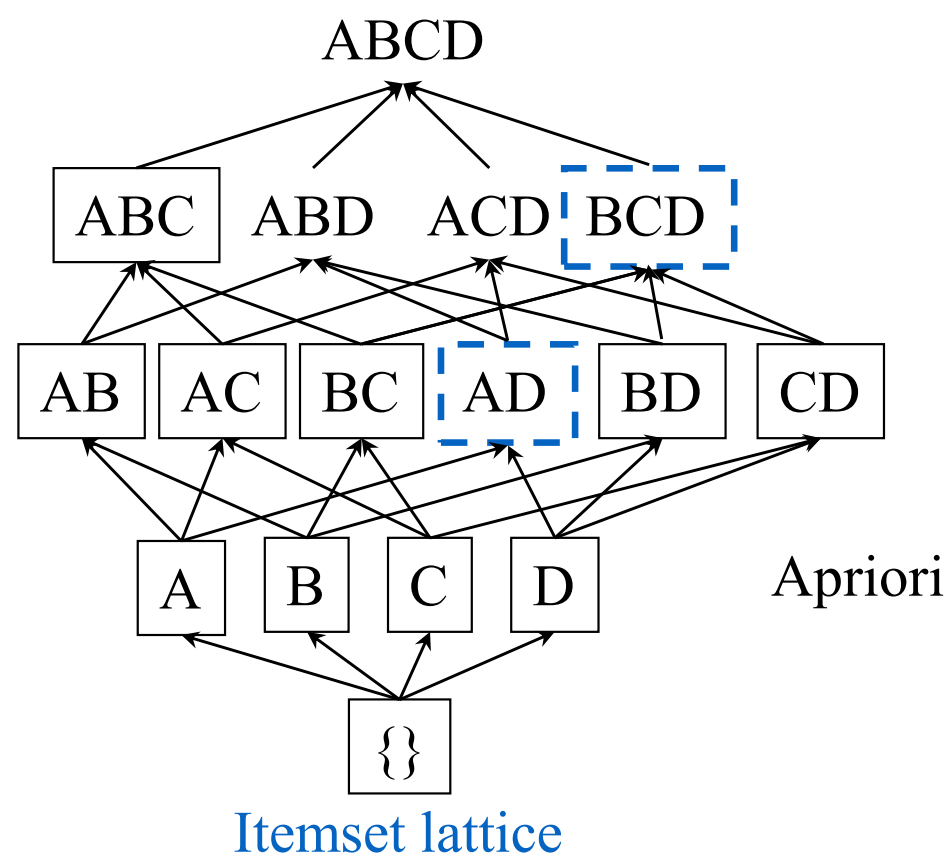
## □ Challenges

- Multiple scans of DB ( $k$  times): too much costly
- Huge number of candidates
  - To find frequent itemset  $i_1 i_2 \dots i_{100}$
  - # of scans: 100
  - # of Candidates =  $2^{100}-1 = 1.27*10^{30}!$
- Tedious workload of the candidate-generation-and-test process
  - support counting for candidates

## □ Improving Apriori: general ideas

- Reduce the number of DB scans
- Reduce the number of candidates
- Improve the candidate counting approaches

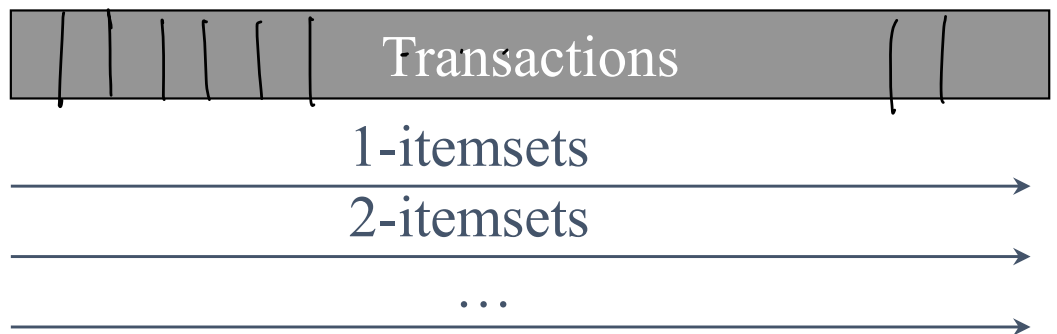
# DIC: Reduce Number of Scans



Apriori

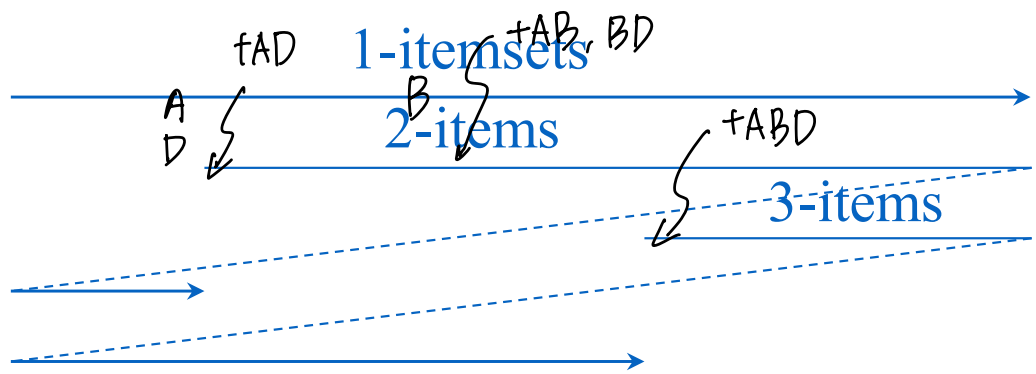
## DIC: Dynamic Itemset Counting

- Once both A and D are determined frequent, the counting of AD begins **at that time**
- Once all length-2 subsets of BCD are determined frequent, the counting of BCD begins at that time



VS

DIC



# Partition: Scan Database **Only Twice**

## □ Approach

- Divide a DB into k pieces (local databases called *partition*)

$$k=4$$

P1	P2	P3	P4
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$$m.s = 40$$

$$l.m.s = 40/4 = 10$$

- Each partition should reside in main memory
- Find *local frequent patterns* in each partition (scan 1)
  - localMinSup is set as  $(minSup / k)$  *partition size*
  - Local frequent patterns have their localSup larger than localMinSup in any local database

- Consolidate global frequent patterns (scan 2)

$\{A, B, C\} : \underline{11}(P1), 3(P2), 4(P3), 10(P4) \Rightarrow \text{Total frequency: } 28 (< m.s) \rightarrow \text{Not frequent pattern}$

# Partition: Scan Database Only Twice

- It guarantees that frequent patterns are never missed
- Any itemset globally frequent in DB must be frequent in *at least one partition* of DB

P1	P2	P3	P4
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$$\begin{aligned} \{A\ B\} &: 41 \\ q\ q\ q\ q &= 36 \\ (14)\ q\ q\ q &= 41 \end{aligned}$$

- A global frequent pattern must be a local frequent pattern
- But, a local frequent pattern may not be a global frequent pattern. This must be confirmed by scanning the entire DB (2<sup>nd</sup> scan)

# Sampling

- ❑ Randomly select a sample of an original database, mine frequent patterns within the sample (SDB) using Apriori (in the same way as before)



Sampling =>



sampled DB (SDB)

- ❑ Use a smaller value of the minimum support for SDB  
(say,  $\text{min\_sup} * (\text{size of SDB}) / (\text{size of DB})$ )
- ❑ Problems with the simple sampling
  - ❑ Some of frequent patterns found in SDB are not really frequent in the original database (similar with the local frequent patterns in Partition)
  - ❑ Some of true frequent patterns could be missed if they are not included in SDB (different with Partition)

# Sampling

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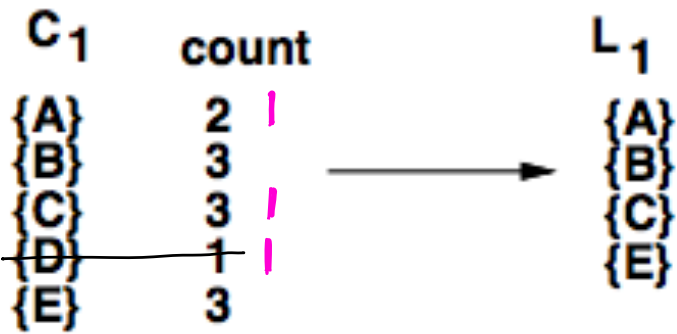
- ❑ **Solutions: two more scanning for verification**
- ❑ **1. Scan the whole database once, applying the original minimum support**
  - ❑ Verify the frequent itemsets (**S**) found in SDB, and its **negative borders** (**NB: not in S, but all its subsets are in S + single items**)
    - $S = \{a\}, \{b\}, \{c\}, \{f\}, \{a,b\}, \{a,c\}, \{a,f\}, \{c,f\}, \{a,c,f\}, \dots$
    - $NB = \{b,c\}, \{b,f\}, \{d\}, \{e\}, \dots$
- ❑ **2. Scan the whole database again**
  - ❑ Find missed frequent patterns (due to the success of NBs)
  - ❑ For example,  **$\{a,b,c\}$**  due to the success of  $\{a,b\}$ ,  $\{a,c\}$ , and  $\{b,c\}$

# DHP: Direct Hashing and Pruning

- When generating  $L_k$ , this algorithm also generates all the **size  $k+1$  itemsets for each transaction**, and **hashes** them to a hash table and keeps a count

Database

Tid	Items
100	A, C, D
200	B, C, E
300	A, B, C, E
400	B, E



minimum support,  $s = 2$

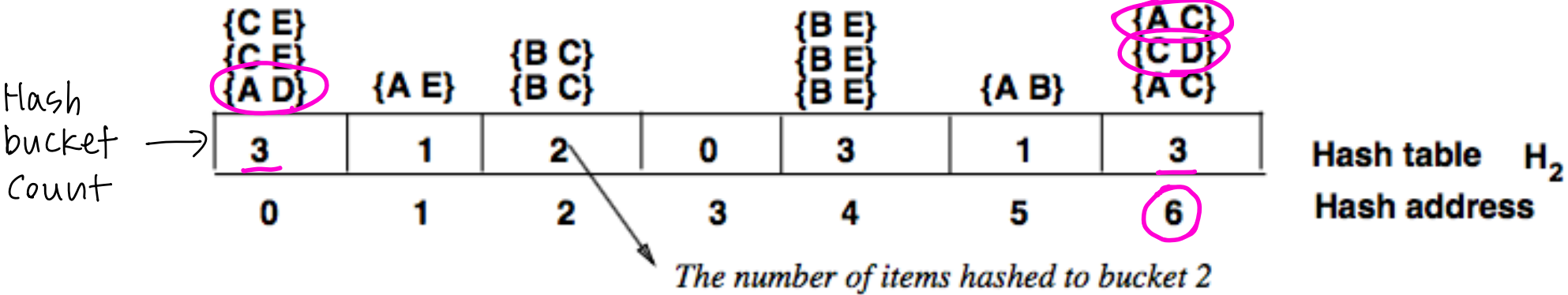
Making a hash table

100	{A C}, {A D}, {C D}
200	{B C}, {B E}, {C E}
300	{A B}, {A C}, {A E}, {B C}, {B E}, {C E}
400	{B E}

ex) predefined order  
: A1, B2, C3, D4, E5  
We can use any hash function

$h(\{x y\}) = ((\text{order of } x) \times 10 + (\text{order of } y)) \bmod 7;$

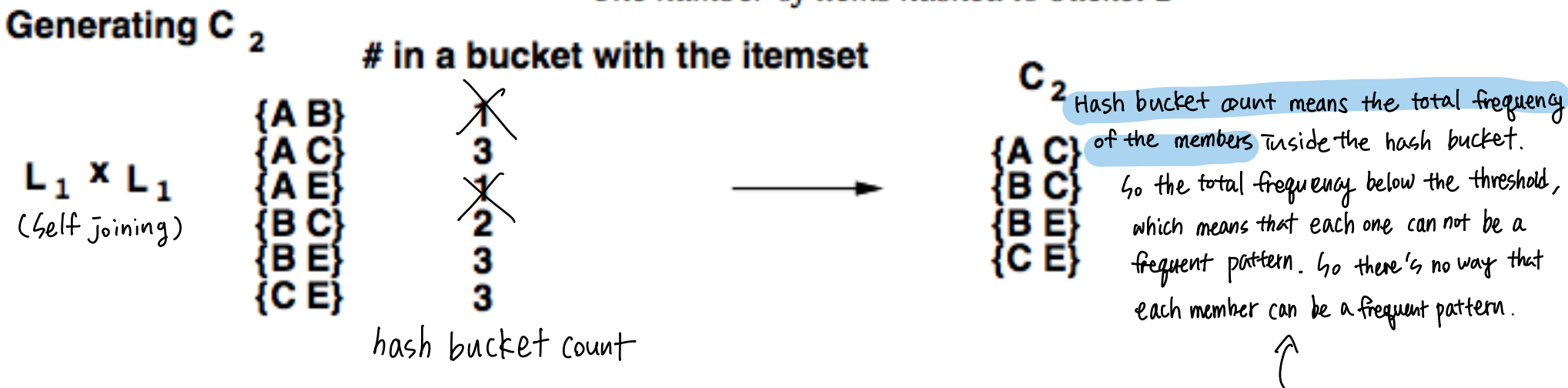
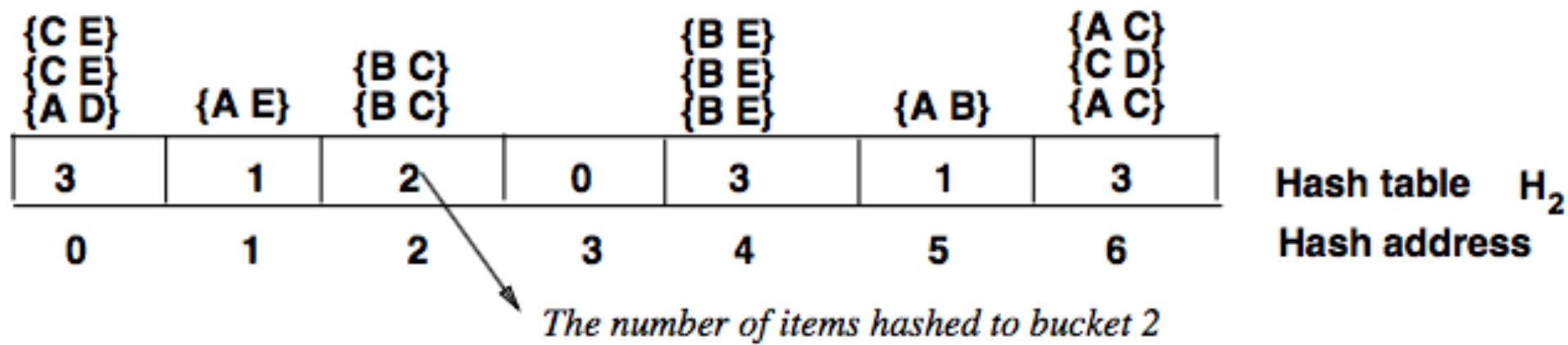
Example:  $h(\{A C\}) = (1 \times 10 + 3) \bmod 7 = 13 \bmod 7 = 6$





# DHP: Direct Hashing and Pruning

- While generating  $C_{k+1}$  via  $L_k$ , it first accesses to the hash table, looks at each candidate's **hash bucket count**.



- If the hash bucket count is below the  $min\_sup$ , it cannot be a candidate!
  - Effective in reducing # of candidates

# Original Apriori VS. DHP

$Sup_{min} = 2$

Tid	Items
10	A, C, D
20	B, C, E
30	A, B, C, E
40	B, E

$C_1$

Itemset	sup
{A}	2
{B}	3
{C}	3
{D}	1
{E}	3

$L_1$

Itemset	sup
{A}	2
{B}	3
{C}	3
{E}	3

**DHP**

<div><div>{CE}</div><div>{CE}</div><div>{AD}</div></div>	<div><div>{AE}</div></div>	<div><div>{BC}</div><div>{BC}</div></div>	<div><div>{BE}</div><div>{BE}</div><div>{BE}</div></div>	<div><div>{AC}</div><div>{CD}</div><div>{AC}</div></div>		
3	1	2	0	3	1	3
0	1	2	3	4	5	6

Remove before counting freq

DHP는 frequency 세기 전에 hash bucket count 에 기반하여 useless candidates 를 제거한다

$L_2$

Itemset	sup
{A, C}	2
{B, C}	2
{B, E}	3
{C, E}	2

$C_2$

Itemset	sup
{A, B}	1
{A, C}	2
{A, E}	1
{B, C}	2
{B, E}	3
{C, E}	2

**DHP**

more reduced size of candidates

아직 frequent pattern of Apriori Candidates

Itemset
{A, C}
{B, C}
{B, E}
{C, E}

Itemset
{A, B}
{A, C}
{A, E}
{B, C}
{B, E}
{C, E}

$C_2$



# Until now...

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- ❑ **We have learned DIC, Partition, Sampling, DHP**
  - ❑ Reduce DB scanning time: DIC, Partition, Sampling
  - ❑ Reduce # of candidates: DHP, Sampling
- ❑ **But, they still have limitations, and they are still very slow**
- ❑ **Can we **completely avoid** candidate generation?**
  - ❑ Yes, FP(frequent pattern)-Growth can do this!
- ❑ **Next class: FP-Growth**
  - ❑ Mining Frequent Patterns **Without Candidate Generation**

# Thank You



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