

# Solar Radiation on a Horizontal Plane

## Fundamentals of PV Engineering

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Motivation

Data Sources

Quality Control

**Motivation**

Data Sources

Quality Control

- ▶ Extraterrestrial solar radiation is a deterministic process (it depends on latitude, day of year, and time of day).
- ▶ However, global radiation is a stochastic (random) process because of the interaction with the atmosphere:
  - ▶ Time variability
  - ▶ Spatial variability

# Long-term Estimations

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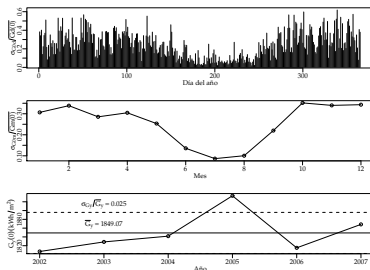
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- ▶ We are interested in **long-term estimations** of the performance of PV systems in a definite location.
- ▶ Solar radiation data sources must **capture the long-term behaviour** (interannual variability) and be **representative of the specified location** (spatial variability).

# Time Variability



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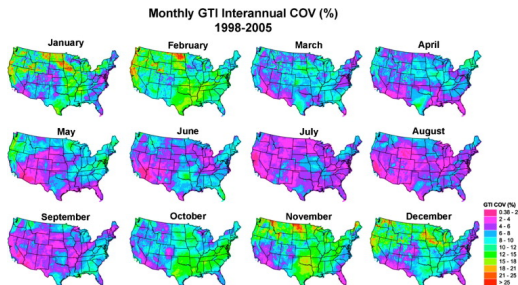
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## Key concepts

- ▶ Time variability **increases with time resolution** (higher for daily values than for monthly averages).
- ▶ Fluctuations are **higher in winter than in summer**.
- ▶ Reproducing **long-term trends** requires **long time series** (about 10 years length).

# Spatial Variability



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## Key concepts

- ▶ Spatial variability depends on the **local climatology**.
- ▶ Spatial variability is **higher in winter than in summer** (for a same location).
- ▶ Measurements are representative of nearby locations for a **limited distance** (about 10 kms.)

# Summary: Measurements requirements

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- ▶ Reliable and representative long-term estimations of PV performance require:
  - ▶ **Nearby measurements:**  $\leq 10$  km
  - ▶ **Long time series:**  $\simeq 10$  years

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# Meteorological stations

- ▶ Long time series.
- ▶ High time resolution (1 min)
- ▶ Low spatial resolution (point measurements).
- ▶ Errors due to meter inaccuracy (no models required).

## Pyranometer



# Satellite imaging

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- ▶ Low time resolution (1 hour or 1 day).
- ▶ High spatial resolution (15 km).
- ▶ Global solar radiation is estimated by processing images of the satellite radiometers.
- ▶ Errors due model inaccuracy (radiation is estimated).

- ▶ Ground measurements merged with satellite estimations to increase spatial resolution.
- ▶ Spatial interpolation
  - ▶ **Inverse Distance Weighting (IDW)** ( $d$  is the distance between locations  $x_0$  and  $x_i$ )

$$\hat{G}_d(x_0) = \frac{\sum_{i=1}^N w_i G_d(x_i)}{\sum_{i=1}^N w_i}$$

$$w_i = 1/d^2(x_0, x_i)$$

- ▶ **Ordinary Kriging**
- ▶ **Kriging with External Drift (KED)**

# Data sources

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Wiki

<https://github.com/oscarperpinan/mds/wiki>

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## Meteorological Stations

[https:  
//github.com/oscarperpinan/mds/wiki/stations](https://github.com/oscarperpinan/mds/wiki/stations)

## Satellite Estimations

- ▶ NASA: <https://github.com/oscarperpinan/mds/wiki/nasa>
- ▶ CM SAF: <https://github.com/oscarperpinan/mds/wiki/cmsaf>
- ▶ LSA SAF: <https://github.com/oscarperpinan/mds/wiki/lsasaf>

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## Hybrid estimations

- ▶ PVGIS: <https://github.com/oscarperpinan/mds/wiki/pvgis>
- ▶ ADRASE: <https://github.com/oscarperpinan/mds/wiki/adrase>

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- ▶ Measurements must be filtered and corrected to remove erroneous data and outliers.
  - ▶ Physical limits
  - ▶ Spatial coherence
  - ▶ Statistical analysis of deviations

- Daily clearness index\* cannot exceed 1 (daily global irradiation cannot exceed extraterrestrial solar irradiation).

$$K_{dT} \leq 1$$

$$G_d(0) \leq B_{0d}(0)$$

- Clearness index must be higher than 0.03

$$K_t = \frac{G_d(0)}{B_{0d}(0)} \geq 0.03$$

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\*Clearness index is defined as the ratio  $K_{dT} = G_d(0)/B_{0d}(0)$ .

- ▶ Measurements from a station should be compared with **nearby stations** (for example, using spatial interpolation)
- ▶ Comparison must be established with **aggregated values** (daily or monthly averages).

# Statistical Analysis of Deviations

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- Statistical analysis of the deviations, **D**, between Observations, **O**, and a Model, **M** (or another set of observations):

$$\mathbf{O} = \{o_1 \dots o_n\}$$

$$\mathbf{M} = \{m_1 \dots m_n\}$$

$$\mathbf{D} = \mathbf{M} - \mathbf{O} = \{(m_1 - o_1) \dots (m_n - o_n)\} = \{d_1 \dots d_n\}$$

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- Mean Bias Difference (MBD):

$$MBE = \overline{\mathbf{D}} = \overline{\mathbf{M}} - \overline{\mathbf{O}} = \frac{1}{n} \sum_{i=1}^n (m_i - o_i)$$

- Root Mean Square Error (RMSE):

$$RMSE = \left( \frac{1}{n} \sum_{i=1}^n d_i^2 \right)^{1/2} = \left( \frac{1}{n} \sum_{i=1}^n (m_i - o_i)^2 \right)^{1/2}$$

- Mean Absolute Deviation (MAD):

$$MAD = \frac{1}{n} \sum_{i=1}^n |d_i| = \frac{1}{n} \sum_{i=1}^n |m_i - o_i|$$