# Mapping Management and Expressive Ontologies in Ontology-Based Data Access

3. Theoretical Foundations of OBDA

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#### Outline

- Query rewriting wrt an OWL 2 QL ontology
- Saturation and optimization of the mapping
- Query reformulation



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### Query answering via query rewriting

#### Query answering can be done via query rewriting

Given a (U)CQ q and an ontology  $\mathcal{O} = \langle \mathcal{T}, \mathcal{A} \rangle$ :

- **1** Compute the perfect rewriting of q w.r.t.  $\mathcal{T}$ , which is a FOL query.
- **2** Evaluate the perfect rewriting over A. (We are ignoring the mapping.)



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Given a (U)CQ q and an ontology  $\mathcal{O} = \langle \mathcal{T}, \mathcal{A} \rangle$ :

- **Outpute** Solution q of q w.r.t. T, which is a FOL query.
- ullet Evaluate the perfect rewriting over  ${\cal A}$ . (We are ignoring the mapping.)

I briefly describe *PerfectRef* , a simple algorithm for Step 1 that requires to iterate over:

- rewriting steps that involve inclusion assertions, and
- unification steps.



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I briefly describe *PerfectRef* , a simple algorithm for Step 1 that requires to iterate over:

- rewriting steps that involve inclusion assertions, and
- unification steps.

*Note:* disjointness assertions and functionalities play a role in ontology satisfiability, but can be ignored during query rewriting (i.e., we have **separability**).



# Query rewriting step: Basic idea

Intuition: an inclusion assertion corresponds to a logic programming rule.

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When an atom in the query unifies with the **head** of the rule, generate a new query by substituting the atom with the **body** of the rule.

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The inclusion assertion  $\mathsf{M}$  corresponds to the logic programming rule

Consider the query  $q(x) \leftarrow Actor(x)$ .

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When an atom in the query unifies with the **head** of the rule, generate a new query by substituting the atom with the **body** of the rule.

We say that the inclusion assertion applies to the atom.

#### Example

The inclusion assertion corresponds to the logic programming rule  $Actor(z) \leftarrow MovieActor(z)$ .

MovieActor 

☐ Actor

Consider the query  $q(x) \leftarrow Actor(x)$ .

By applying the inclusion assertion to the atom Actor(x), we generate:  $g(x) \leftarrow MovieActor(x)$ .

This query is added to the input query, and contributes to the perfect rewriting.

# Query rewriting (cont'd)

#### Example

 $\text{Consider the query} \qquad \mathsf{q}(x) \ \leftarrow \ \mathsf{playsIn}(x,y), \mathsf{Movie}(y)$ 

and the inclusion assertion  $\exists \mathsf{playsln}^- \sqsubseteq \mathsf{Movie}$  as a logic programming rule:  $\mathsf{Movie}(z_2) \leftarrow \mathsf{playsln}(z_1, z_2)$ .

The inclusion applies to  $\mathsf{Movie}(y)$ , and we add to the rewriting the query

$$q(x) \leftarrow \mathsf{playsIn}(x, y), \mathsf{playsIn}(z_1, y).$$



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#### Example

Consider now the query  $q(x) \leftarrow playsln(x, y)$ 

and the inclusion assertion MovieActor  $\sqsubseteq \exists \mathsf{playsIn}$  as a logic programming rule:  $\mathsf{playsIn}(z, f(z)) \leftarrow \mathsf{MovieActor}(z)$ .

The inclusion applies to playsln(x, y), and we add to the rewriting the query

$$q(x) \leftarrow MovieActor(x)$$
.

D. Calvanese, B. Cogrel, G. Xiao (unibz)

### Query rewriting – Constants

#### Example

```
Conversely, for the query q(x) \leftarrow playsln(x, matrix)
```

and the same inclusion assertion as before as a logic programming rule:

$$\begin{array}{l} \mathsf{MovieActor} \sqsubseteq \exists \mathsf{playsIn} \\ \mathsf{playsIn}(z, f(z)) \leftarrow \ \mathsf{MovieActor}(z) \end{array}$$

 $\operatorname{playsln}(x,\operatorname{matrix})$  does not unify with  $\operatorname{playsln}(z,f(z))$ , since the **skolem term** f(z) in the head of the rule **does not unify** with the constant  $\operatorname{matrix}$ . Remember: We adopt the **unique name assumption**.



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#### Example

The same holds for the following query, where y is distinguished, since unifying f(z) with y would correspond to returning a skolem term as answer to the query:

$$q(x, y) \leftarrow playsln(x, y)$$
.

### Query rewriting – Join variables

An analogous behavior to the one with constants and with distinguished variables holds when the atom contains **join variables** that would have to be unified with skolem terms.

#### Example

```
Consider the query q(x) \leftarrow \mathsf{playsIn}(x,y), \mathsf{Movie}(y)
```

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and the inclusion assertion MovieActor \sqsubseteq \exists \mathsf{playsIn} as a logic programming rule: \mathsf{playsIn}(z, f(z)) \leftarrow \mathsf{MovieActor}(z).
```

The inclusion assertion above does **not** apply to the atom playsln(x, y).



# Query rewriting – Reduce step

#### Example

Consider now the query  $\begin{array}{ll} \mathsf{q}(x) \; \leftarrow \; \mathsf{playsln}(x,y), \mathsf{playsln}(z,y) \\ \mathsf{and} \; \mathsf{the} \; \mathsf{inclusion} \; \mathsf{assertion} \\ \mathsf{as} \; \mathsf{a} \; \mathsf{logic} \; \mathsf{rule:} \end{array} \qquad \begin{array}{ll} \mathsf{MovieActor} \; \sqsubseteq \; \exists \mathsf{playsln} \\ \mathsf{playsln}(z,f(z)) \leftarrow \; \mathsf{MovieActor}(z). \end{array}$ 

This inclusion assertion does not apply to  $\operatorname{playsIn}(x, \boldsymbol{y})$  or  $\operatorname{playsIn}(z, \boldsymbol{y})$ , since  $\boldsymbol{y}$  is in join, and we would again introduce the skolem term in the rewritten query.



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This inclusion assertion does not apply to  $\operatorname{playsln}(x, y)$  or  $\operatorname{playsln}(z, y)$ , since y is in join, and we would again introduce the skolem term in the rewritten query.

#### Example

However, we can transform the above query by unifying the atoms  $\mathsf{playsIn}(x,y)$  and  $\mathsf{playsIn}(z,y)$ . This rewriting step is called **reduce**, and produces the query

$$q(x) \leftarrow playsln(x, y)$$
.

Now, we can apply the inclusion above, and add to the rewriting the query

$$q(x) \leftarrow MovieActor(x)$$
.

# Query rewriting – Summary

To compute the perfect rewriting of a query q, start from q, iteratively get a CQ q' to be processed, and do one of the following:

• Apply to some atom of q' an inclusion assertion in  $\mathcal{T}$  as follows:

('\_' denotes a variable that appears only once)

ullet Choose two atoms of q' that unify, and apply the unifier to q'.

Each time, the result of the above step is added to the queries to be processed.



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The UCQ resulting from this process is the **perfect rewriting**  $r_{q,\mathcal{T}}$ .

# Query rewriting algorithm

```
Algorithm PerfectRef(Q, \mathcal{T}_P)
Input: union of conjunctive queries Q, set \mathcal{T}_P of DL-Lite inclusion assertions
Output: union of conjunctive gueries PR
PR := Q;
repeat
  PR' := PR;
  for each q \in PR' do
     for each q in q do
       for each inclusion assertion I in \mathcal{T}_P do
          if I is applicable to g then PR := PR \cup \{ ApplyPI(q, g, I) \};
     for each g_1, g_2 in q do
       if q_1 and q_2 unify then PR := PR \cup \{\tau(Reduce(q, q_1, q_2))\};
until PR' = PR:
return PR
```

#### Observations:

- Termination follows from having only finitely many different rewritings.
- Disjointness assertions and functionalities do not play any role in the rewriting of the query.



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```
TBox:

MovieActor \sqsubseteq Actor

Actor \sqsubseteq \exists playsIn

\exists playsIn^{-} \sqsubseteq Movie
```

```
Corresponding rules:
```

 $\mathsf{Query:}\ \mathsf{q}(x) \leftarrow \mathsf{playsIn}(x,y), \mathsf{Movie}(y)$ 



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$$q(x) \leftarrow \mathsf{playsIn}(x, y), \mathsf{Movie}(y)$$

$$\begin{array}{c} \mathsf{Perfect\ rewriting:}\ \mathsf{q}(x) \leftarrow \mathsf{playsIn}(x,y), \mathsf{Movie}(y) \\ \mathsf{q}(x) \leftarrow \mathsf{playsIn}(x,y), \mathsf{playsIn}(\_,y) \end{array}$$



 $g(x) \leftarrow \mathsf{plavsln}(x, \_)$ 



TBox:

# Query answering in *DL-Lite* – Example

```
\begin{array}{c} \mathsf{MovieActor} \sqsubseteq \mathsf{Actor} & \mathsf{Actor}(x) \leftarrow \mathsf{MovieActor}(x) \\ \mathsf{Actor} \sqsubseteq \exists \mathsf{playsIn} & \exists y(\mathsf{playsIn}(x,y)) \leftarrow \mathsf{Actor}(x) \\ \exists \mathsf{playsIn}^- \sqsubseteq \mathsf{Movie} & \mathsf{Movie}(x) \leftarrow \mathsf{playsIn}(y,x) \\ \mathsf{Query:} \ \mathsf{q}(x) \leftarrow \mathsf{playsIn}(x,y), \mathsf{Movie}(y) \\ \mathsf{Perfect rewriting:} \ \mathsf{q}(x) \leftarrow \mathsf{playsIn}(x,y), \mathsf{Movie}(y) \\ \mathsf{q}(x) \leftarrow \mathsf{playsIn}(x,y), \mathsf{playsIn}(-,y) \\ \mathsf{q}(x) \leftarrow \mathsf{playsIn}(x,-) \\ \mathsf{q}(x) \leftarrow \mathsf{Actor}(x) \end{array}
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```

Corresponding rules:



 $q(x) \leftarrow \mathsf{MovieActor}(x)$ 

Evaluating the perfect rewriting over the ABox (seen as a DB) produces as answer {keanu, sigourney, nicole}.



TBox: Person  $\sqsubseteq \exists$ hasFather

ABox: Person(john)

∃hasFather ⊑ Person

 $\textbf{Query: } \textbf{q}(x) \leftarrow \mathsf{Person}(x), \mathsf{hasFather}(x,y_1), \mathsf{hasFather}(y_1,y_2), \mathsf{hasFather}(y_2,y_3)$ 



TBox: Person □ ∃hasFather

ABox: Person(john)

 $\exists$ hasFather $^{-}$   $\sqsubseteq$  Person

Query:  $q(x) \leftarrow Person(x)$ , hasFather $(x, y_1)$ , hasFather $(y_1, y_2)$ , hasFather $(y_2, y_3)$ 

 $q(x) \leftarrow \mathsf{Person}(x), \mathsf{hasFather}(x, y_1), \mathsf{hasFather}(y_1, y_2), \mathsf{hasFather}(y_2, \bot)$ 



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TBox: Person \sqsubseteq \existshasFather \existshasFather \existshasFather \sqsubseteq Person

Query: q(x) \leftarrow Person(x), hasFather(x, y_1), hasFather(y_1, y_2), hasFather(y_2, y_3)

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```





```
TBox: Person \square \existshasFather
                                                     ABox: Person(john)
           ∃hasFather □ Person
Query: q(x) \leftarrow Person(x), hasFather(x, y_1), hasFather(y_1, y_2), hasFather(y_2, y_3)
  q(x) \leftarrow \mathsf{Person}(x), hasFather(x, y_1), hasFather(y_1, y_2), hasFather(y_2, ...)
                          \downarrow\downarrow Apply Person \sqsubseteq \existshasFather to the atom hasFather(y_2, \bot)
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  q(x) \leftarrow \mathsf{Person}(x), \mathsf{hasFather}(x, y_1), \mathsf{hasFather}(y_1, y_2), \mathsf{hasFather}(\_, y_2)
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  q(x) \leftarrow \mathsf{Person}(x)
```

# Complexity of query answering in *DL-Lite*

### Query answering for CQs and UCQs is:

- Efficiently tractable in the size of the TBox, i.e., PTIME.
- Very efficiently tractable in the size of the ABox, i.e.,  $AC^0$ .
- Exponential in the size of the query, more precisely NP-complete.
   In theory this is not bad, since this is precisely the complexity of evaluating CQs in plain relational DBs.



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#### Can we go beyond *DL-Lite*?

Essentially no! By adding essentially any additional constructor we lose these nice computational properties.



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- Saturation and optimization of the mapping
- Query reformulation



Saturation

# Querying the OBDA system

### OBDA system $\mathcal{K} = \langle \mathcal{T}, \mathcal{M}, \mathcal{D} \rangle$

- DL-Lite $_{\mathcal{R}}$  TBox  $\mathcal{T}$
- ullet RDF graph  ${\cal G}$  obtained from the mapping  ${\cal M}$  and the data sources  ${\cal D}$
- ullet  $\mathcal{G}$  can be viewed as the ABox





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### Query answering

• SPARQL query q over K



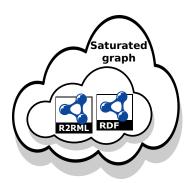
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### Saturated RDF graph $\mathcal{G}_{\mathsf{sat}}$

- ullet Saturation of  ${\mathcal G}$  w.r.t.  ${\mathcal T}$
- H-complete ABox



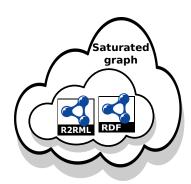
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### Query answering

- ullet SPARQL query  $oldsymbol{q}$  over  ${\mathcal K}$
- If there is no existential restriction  $B \sqsubseteq \exists R.C$  in  $\mathcal{T}$ , q can be directly evaluated over  $\mathcal{G}_{\mathsf{sat}}$



### Saturated RDF graph $\mathcal{G}_{sat}$

- ullet Saturation of  ${\mathcal G}$  w.r.t.  ${\mathcal T}$
- H-complete ABox



# How to handle the RDF graph $\mathcal{G}_{sat}$ in practice?

### By materializing it

- Materialization of G (ETL)
   + saturation
- Large volume
- Maintenance
- Typical profile: OWL 2 RL

### By keeping it virtual

- Query rewriting
- + No materialization required
- ullet Saturated mapping  $\mathcal{M}_{\mathsf{sat}}$
- Typical profile: OWL 2 QL



# H-complete ABox [RoKZ13; rweb-KontchakovZ14]

### ABox saturation

• H-complete ABox: contains all the inferable ABox assertions



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- Let K be a DL-LiteR knowledge base, and let K' be the result of saturating K. For every ABox assertion  $\alpha$ , we have:

$$\mathcal{K} \models \alpha \quad \text{iff} \quad \alpha \in \mathcal{K}'$$



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### Saturated mapping $\mathcal{M}_{sat}$ (also called T-mapping)

- $\bullet$  Composition of the mapping  ${\cal M}$  and the  $\textit{DL-Lite}_{\cal R}$  TBox  ${\cal T}$
- $\bullet \ \ \mathcal{M}_{\mathsf{sat}} + \mathcal{D} \to \mathcal{G}_{\mathsf{sat}} \ \mathsf{(H\text{-}complete ABox)}$



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- ullet Composition of the mapping  ${\mathcal M}$  and the  ${\it DL-Lite}_{\mathcal R}$  TBox  ${\mathcal T}$
- $\mathcal{M}_{\mathsf{sat}} + \mathcal{D} \to \mathcal{G}_{\mathsf{sat}}$  (H-complete ABox)
- Independent of the SPARQL query q (can be pre-computed)
- Can be optimized (query containment)



```
Student \sqcup PostDoc \sqcup AssociateProfessor \sqcup \existsteaches \sqsubseteq Person
                        Student(URI_1(p)) \leftarrow uni1-student(p, f, l)
```

TBox, user-defined mapping assertions and foreign key

AssociateProfessor(URI<sub>2</sub>(a))  $\leftarrow$  uni1-academic(a, f, l, s), s = 2

FacultyMember(URI<sub>2</sub>(a))  $\leftarrow$  uni1-academic(a, f, l, s)

 $teaches(URI_2(a), URI_3(c)) \leftarrow uni1-teaching(c, a)$ 

FK:  $\exists y_1.\text{uni1-teaching}(y_1, x) \rightarrow \exists y_2 y_3 y_4.\text{uni1-academic}(x, y_2, y_3, y_4)$ 

(1)

(2)

(3)

(4)

(5)

 $\mathsf{PostDoc}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s), s = 9$ 

```
TBox, user-defined mapping assertions and foreign key
Student \sqcup PostDoc \sqcup AssociateProfessor \sqcup \existsteaches \sqsubseteq Person
                       Student(URI_1(p)) \leftarrow uni1-student(p, f, l)
                                                                                                   (1)
                      \mathsf{PostDoc}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s), s = 9
                                                                                                   (2)
         {\sf AssociateProfessor}(\mathrm{URI}_2(a)) \leftarrow \mathtt{uni1-academic}(a,f,l,s), s = 2
                                                                                                   (3)
             FacultyMember(URI<sub>2</sub>(a)) \leftarrow uni1-academic(a, f, l, s)
                                                                                                   (4)
           teaches(URI_2(a), URI_3(c)) \leftarrow uni1-teaching(c, a)
                                                                                                   (5)
FK: \exists y_1.uni1-teaching(y_1, x) \rightarrow \exists y_2y_3y_4.uni1-academic(x, y_2, y_3, y_4)
Non-optimized saturated mapping assertions for Person
```

 $Person(URI_1(p)) \leftarrow uni1-student(p, f, l)$ 

 $\mathsf{Person}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s)$ 

 $Person(URI_2(a)) \leftarrow uni1-teaching(c, a)$ 

 $Person(URI_2(a)) \leftarrow uni1-academic(a, f, l, s), s = 9$ 

 $\mathsf{Person}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s), s=2$ 

(6)

(7)

(8)

(9)

(10)

```
TBox, user-defined mapping assertions and foreign key
Student \sqcup PostDoc \sqcup AssociateProfessor \sqcup \existsteaches \sqsubseteq Person
                        Student(URI_1(p)) \leftarrow uni1-student(p, f, l)
                                                                                                       (1)
                       \mathsf{PostDoc}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s), s = 9
                                                                                                       (2)
          {\sf AssociateProfessor}(\mathrm{URI}_2(a)) \leftarrow \mathtt{uni1-academic}(a,f,l,s), s = 2
                                                                                                        (3)
              FacultyMember(URI<sub>2</sub>(a)) \leftarrow uni1-academic(a, f, l, s)
                                                                                                        (4)
            teaches(URI_2(a), URI_3(c)) \leftarrow uni1-teaching(c, a)
                                                                                                       (5)
FK: \exists y_1.uni1-teaching(y_1, x) \rightarrow \exists y_2y_3y_4.uni1-academic(x, y_2, y_3, y_4)
Non-optimized saturated mapping assertions for Person
                  Person(URI_1(p)) \leftarrow uni1-student(p, f, l)
                                                                                                        (6)
                  Person(URI_2(a)) \leftarrow uni1-academic(a, f, l, s), s = 9
                                                                                                        (7)
                  \mathsf{Person}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s), s=2
                                                                                                        (8)
                  \mathsf{Person}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s)
                                                                                                        (9)
```

(10)

(11)

(12)

 $Person(URI_2(a)) \leftarrow uni1-teaching(c, a)$ 

Mapping assertions for Person after optimization (query containment)

 $Person(URI_1(p)) \leftarrow uni1-student(p, f, l)$ 

 $\mathsf{Person}(\mathsf{URI}_2(p)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(p,f,l,s)$ 

### Outline

- Query rewriting wrt an OWL 2 QL ontology
- 2 Saturation and optimization of the mapping
- Query reformulation
  - Tree-witness rewriting
  - SQL query optimization



(17/27)

# Query reformulation

### Implemented by Ontop



| Step                      | Input                                    | Output                   |
|---------------------------|--|--------------------------|
| 1. Tree-witness rewriting | $q$ (SPARQL) and ${\cal T}$              | $q_{tw}$ (SPARQL)        |
| 2. Query unfolding        | $q_{\sf tw}$ and $\mathcal{M}_{\sf sat}$ | $q_{unf}$ (SQL)          |
| 3. Query optimization     | $q_{unf}$ , primary and foreign keys     | $q_{ m opt}$ (SQL) unibz |

### Example

Suppose that every graduate student is supervised by some professor, i.e.

 ${\tt GraduateStudent} \sqsubseteq \exists \ {\tt isSupervisedBy.Professor}$ 

and john is a graduate student:

GraduateStudent(john)



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Suppose that every graduate student is supervised by some professor, i.e.

 $\texttt{GraduateStudent} \sqsubseteq \exists \ \texttt{isSupervisedBy.Professor}$ 

and john is a graduate student:

GraduateStudent(john)

What is the answer to the following query?

SELECT ?x WHERE { ?x isSupervisedBy [ a Professor ] .}



### Example

Suppose that every graduate student is supervised by some professor, i.e.

 $\texttt{GraduateStudent} \sqsubseteq \exists \ \texttt{isSupervisedBy.Professor}$ 

and john is a graduate student:

GraduateStudent(john)

What is the answer to the following query?

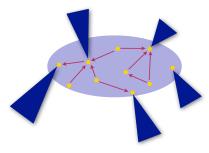
SELECT ?x WHERE { ?x isSupervisedBy [ a Professor ] .}

Yes. Even though we don't know who is john's supervisor.



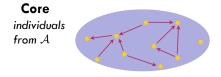
Reformulation

# Existential reasoning and tree-witness rewriting



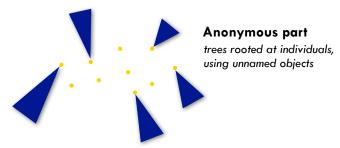


Fact: every consistent DL-Lite KB  $\mathcal{K}=(\mathcal{T},\mathcal{A})$  has a canonical model  $\mathcal{I}_{\mathcal{K}}$ , which gives the right answers to all CQs, i.e.,  $\operatorname{cert}(q,\mathcal{K})=\operatorname{ans}(q,\mathcal{I}_{\mathcal{K}})$ 



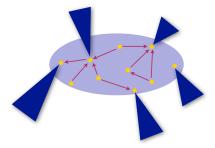
• The core part can be handled by the saturated mapping





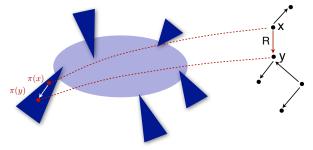
- The core part can be handled by the saturated mapping
- The anonymous part can be handled by Tree-witness rewriting





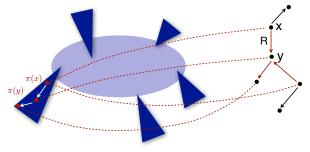
- The core part can be handled by the saturated mapping
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- The core part can be handled by the saturated mapping
- The anonymous part can be handled by Tree-witness rewriting





- The core part can be handled by the saturated mapping
- The anonymous part can be handled by Tree-witness rewriting



Using the tree witness rewriting algorithm, the query

```
SELECT ?x WHERE { ?x :isSupervisedBy [ a :Professor ] .}
```



```
Using the tree witness rewriting algorithm, the query
```

```
SELECT ?x WHERE { ?x :isSupervisedBy [ a :Professor ] .}
is rewritten to

SELECT ?x WHERE { ?x :isSupervisedBy [ a :Professor ] .}
UNION
SELECT ?x WHERE { ?x :GraduateStudent .}
```



Using the tree witness rewriting algorithm, the query

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SELECT ?x WHERE { ?x :isSupervisedBy [ a :Professor ] .}
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SELECT ?x WHERE { ?x :isSupervisedBy [ a :Professor ] .}

Therefore, john is computed as an answer.



### Using the tree witness rewriting algorithm, the query

```
SELECT ?x WHERE { ?x :isSupervisedBy [ a :Professor ] .}
is rewritten to

SELECT ?x WHERE { ?x :isSupervisedBy [ a :Professor ] .}
UNION
SELECT ?x WHERE { ?x :GraduateStudent .}
```

Therefore, john is computed as an answer.

### Tree-witness rewriting option in *Ontop*

Note that if users want to enable existential reasoning, the option of tree-witness rewriting algorithm needs to be switched explicitly.

# Query reformulation

### Implemented by Ontop



| Step                      | Input                                | Output                   |
|---------------------------|--------------------------------------|--------------------------|
| 1. Tree-witness rewriting | $q$ (SPARQL) and ${\cal T}$          | $q_{tw}$ (SPARQL)        |
| 2. Query unfolding        | $q_{tw}$ and $\mathcal{M}_{sat}$     | $q_{unf}$ (SQL)          |
| 3. Query optimization     | $q_{unf}$ , primary and foreign keys | $q_{ m opt}$ (SQL) unibz |

### Objective: produce SQL queries that are ...

- similar to manually written ones
- $\bullet$  adapted to existing query planners



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### Structural optimization

- From join-of-unions to union-of-joins
- IRI decomposition to improve joining performance



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- Redundant join elimination
- Redundant union elimination
- Using functional constraints



### Objective: produce SQL queries that are ...

- similar to manually written ones
- adapted to existing query planners

### Structural optimization

- From join-of-unions to union-of-joins
- IRI decomposition to improve joining performance

### Semantic optimization

- Redundant join elimination
- Redundant union elimination
- Using functional constraints

### Integrity constraints

- Primary and foreign keys, unique constraints
- Sometimes implicit
- Vital for query reformulation!



# Reformulation example - 1. Unfolding

```
Saturated mappings
```

```
\begin{split} & \mathsf{firstName}(\mathsf{URI}_1(p),f) \leftarrow \mathsf{uni1}\text{-}\mathsf{student}(p,f,l) \\ & \mathsf{firstName}(\mathsf{URI}_2(a),f) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s) \\ & \mathsf{lastName}(\mathsf{URI}_1(p),l) \leftarrow \mathsf{uni1}\text{-}\mathsf{student}(p,f,l) \\ & \mathsf{lastName}(\mathsf{URI}_2(a),l) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s) \\ & \mathsf{Teacher}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a,f,l,s), s \in [1,8] \\ & \mathsf{Teacher}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{teaching}(c,a) \end{split}
```

#### Query

```
\begin{aligned} \textbf{\textit{q}}(x,y,z) &\leftarrow \mathsf{Teacher}(x), \mathsf{firstName}(x,y), \mathsf{lastName}(x,z) \\ \textbf{\textit{q}}_{\mathsf{tw}} &= \textbf{\textit{q}} \end{aligned}
```

# Reformulation example - 1. Unfolding

#### Saturated mappings

```
\begin{split} & \mathsf{firstName}(\mathsf{URI}_1(p), f) \leftarrow \mathsf{uni1}\text{-}\mathsf{student}(p, f, l) \\ & \mathsf{firstName}(\mathsf{URI}_2(a), f) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a, f, l, s) \\ & \mathsf{lastName}(\mathsf{URI}_1(p), l) \leftarrow \mathsf{uni1}\text{-}\mathsf{student}(p, f, l) \\ & \mathsf{lastName}(\mathsf{URI}_2(a), l) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a, f, l, s) \\ & \mathsf{Teacher}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{academic}(a, f, l, s), s \in [1, 8] \\ & \mathsf{Teacher}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{-}\mathsf{teaching}(c, a) \end{split}
```

### Query

$$\begin{aligned} q(x,y,z) &\leftarrow \mathsf{Teacher}(x), \mathsf{firstName}(x,y), \mathsf{lastName}(x,z) \\ q_{\mathsf{tw}} &= q \end{aligned}$$

#### Query unfolding

$$\begin{aligned} & \pmb{q}_{\text{unf1}}(x,y,z) \leftarrow \pmb{q}_{\text{unf1}}(x), \pmb{q}_{\text{unf2}}(x,y), \pmb{q}_{\text{unf3}}(x,z) \\ & \pmb{q}_{\text{unf1}}(\text{URI}_2(a)) \leftarrow \text{uni1-academic}(a,f,l,s), s \in [1,8] \\ & \pmb{q}_{\text{unf1}}(\text{URI}_2(a)) \leftarrow \text{uni1-teaching}(c,a) \\ & \pmb{q}_{\text{unf2}}(\text{URI}_1(p),f) \leftarrow \text{uni1-student}(p,f,l) \\ & \pmb{q}_{\text{unf2}}(\text{URI}_2(a),f) \leftarrow \text{uni1-academic}(a,f,l,s) \\ & \pmb{q}_{\text{unf3}}(\text{URI}_1(p),l) \leftarrow \text{uni1-student}(p,f,l) \\ & \pmb{q}_{\text{unf3}}(\text{URI}_2(a),l) \leftarrow \text{uni1-academic}(a,f,l,s) \end{aligned}$$

### Query unfolding

$$\begin{aligned} & q_{\mathsf{unf1}}(x,y,z) \leftarrow q_{\mathsf{unf1}}(x), q_{\mathsf{unf2}}(x,y), q_{\mathsf{unf3}}(x,z) \\ & q_{\mathsf{unf1}}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{--academic}(a,f,l,s), s \in [1,8] \\ & q_{\mathsf{unf1}}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1}\text{--teaching}(c,a) \\ & q_{\mathsf{unf2}}(\mathsf{URI}_1(p),f) \leftarrow \mathsf{uni1}\text{--student}(p,f,l) \\ & q_{\mathsf{unf2}}(\mathsf{URI}_2(a),f) \leftarrow \mathsf{uni1}\text{--academic}(a,f,l,s) \\ & q_{\mathsf{unf3}}(\mathsf{URI}_1(p),l) \leftarrow \mathsf{uni1}\text{--student}(p,f,l) \\ & q_{\mathsf{unf3}}(\mathsf{URI}_2(a),l) \leftarrow \mathsf{uni1}\text{--academic}(a,f,l,s) \end{aligned}$$

### Query unfolding

```
\begin{aligned} & \boldsymbol{q}_{\mathsf{unf1}}(x,y,z) \leftarrow \boldsymbol{q}_{\mathsf{unf1}}(x), \boldsymbol{q}_{\mathsf{unf2}}(x,y), \boldsymbol{q}_{\mathsf{unf3}}(x,z) \\ & \boldsymbol{q}_{\mathsf{unf1}}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1-academic}(a,f,l,s), s \in [1,8] \\ & \boldsymbol{q}_{\mathsf{unf1}}(\mathsf{URI}_2(a)) \leftarrow \mathsf{uni1-teaching}(c,a) \\ & \boldsymbol{q}_{\mathsf{unf2}}(\mathsf{URI}_1(p),f) \leftarrow \mathsf{uni1-student}(p,f,l) \\ & \boldsymbol{q}_{\mathsf{unf2}}(\mathsf{URI}_2(a),f) \leftarrow \mathsf{uni1-academic}(a,f,l,s) \\ & \boldsymbol{q}_{\mathsf{unf3}}(\mathsf{URI}_1(p),l) \leftarrow \mathsf{uni1-student}(p,f,l) \\ & \boldsymbol{q}_{\mathsf{unf3}}(\mathsf{URI}_2(a),l) \leftarrow \mathsf{uni1-academic}(a,f,l,s) \end{aligned}
```

### Normalization: explicit joining conditions

$$\begin{aligned} & \boldsymbol{q}_{\text{exp}}(x,y,z) \leftarrow \boldsymbol{q}_{\text{unf1}}(x), \boldsymbol{q}_{\text{unf2}}(x_1,y), \boldsymbol{q}_{\text{unf3}}(x_2,z), x = x_1, x = x_2 \\ & \boldsymbol{q}_{\text{unf1}}(\text{URI}_2(a)) \leftarrow \text{uni1-academic}(a,f,l,s), s \in [1,8] \\ & \boldsymbol{q}_{\text{unf1}}(\text{URI}_2(a)) \leftarrow \text{uni1-teaching}(c,a) \\ & \boldsymbol{q}_{\text{unf2}}(\text{URI}_1(p),f) \leftarrow \text{uni1-student}(p,f,l) \\ & \boldsymbol{q}_{\text{unf2}}(\text{URI}_2(a),f) \leftarrow \text{uni1-academic}(a,f,l,s) \\ & \boldsymbol{q}_{\text{unf3}}(\text{URI}_1(p),l) \leftarrow \text{uni1-student}(p,f,l) \\ & \boldsymbol{q}_{\text{unf3}}(\text{URI}_2(a),l) \leftarrow \text{uni1-academic}(a,f,l,s) \end{aligned}$$

```
Normalization: explicit joining conditions
       q_{\text{exp}}(x, y, z) \leftarrow q_{\text{unf}1}(x), q_{\text{unf}2}(x_1, y),
                         q_{unf3}(x_2,z),
                         x = x_1, x = x_2
  q_{unf1}(URI_2(a)) \leftarrow uni1-academic(a, f, l, s),
                         s \in [1, 8]
  q_{unf1}(URI_2(a)) \leftarrow uni1-teaching(c, a)
q_{unf2}(\mathrm{URI}_2(a), f) \leftarrow uni1-academic(a, f, l, s)
q_{unf3}(URI_1(p), l) \leftarrow uni1-student(p, f, l)
q_{unf3}(URI_2(a), l) \leftarrow uni1-academic(a, f, l, s)
```

```
Flattening (URI template lifting) - part 1/2
q_{\text{lift}}(\text{URI}_2(a), y, z) \leftarrow \text{uni1-academic}(a, f_1, l_1, s_1),
                           uni1-student(p, f_2, l_2),
                           uni1-student(p_1, f_3, l_3),
                           URI_2(a) = URI_1(p),
                           URI_2(a) = URI_1(p_1),
                           s_1 \in [1, 8]
q_{\text{lift}}(\text{URI}_2(a), y, z) \leftarrow \text{uni1-academic}(a, f_1, l_1, s_1),
                           uni1-student(p, f_2, l_2),
                           uni1-academic(a_2, f_3, z, s_3),
                           URI_2(a) = URI_1(p),
                           URI_2(a) = URI_2(a_2),...
      (One sub-query ignored)
q_{\text{lift}}(\text{URI}_2(a), y, z) \leftarrow \text{uni1-academic}(a, f_1, l_1, s_1),
                           uni1-academic(a_1, y, l_2, s_2),
                           uni1-academic(a_2, f_3, z, s_3),
                           URI_2(a) = URI_2(a_1),
                           URI_2(a) = URI_2(a_2),
```

 $s_1 \in [1, 8]$ 

```
\begin{aligned} & \text{Normalization: explicit joining conditions} \\ & q_{\text{exp}}(x,y,z) \leftarrow q_{\text{unf1}}(x), q_{\text{unf2}}(x_1,y), \\ & q_{\text{unf3}}(x_2,z), \\ & x = x_1, x = x_2 \\ & q_{\text{unf1}}(\text{URI}_2(a)) \leftarrow & \text{uni1-academic}(a,f,l,s), \\ & s \in [1,8] \\ & q_{\text{unf1}}(\text{URI}_2(a)) \leftarrow & \text{uni1-teaching}(c,a) \\ & q_{\text{unf2}}(\text{URI}_1(p),f) \leftarrow & \text{uni1-student}(p,f,l) \\ & q_{\text{unf2}}(\text{URI}_2(a),f) \leftarrow & \text{uni1-academic}(a,f,l,s) \\ & q_{\text{unf3}}(\text{URI}_1(p),l) \leftarrow & \text{uni1-student}(p,f,l) \end{aligned}
```

 $q_{unf3}(URI_2(a), l) \leftarrow uni1-academic(a, f, l, s)$ 

```
Flattening (URI template lifting) - part 2/2
q_{\text{lift}}(\text{URI}_2(a), y, z) \leftarrow \text{uni1-teaching}(c, a),
                          uni1-student(p, f_2, l_2),
                          uni1-student(p_1, f_3, l_3),
                          URI_2(a) = URI_1(p),
                           URI_2(a) = URI_1(p_1)
      (One sub-query ignored)
q_{\text{lift}}(\text{URI}_2(a), y, z) \leftarrow \text{uni1-teaching}(c, a),
                          uni1-academic(a_1, y, l_2, s_2),
                          uni1-student(p, f_3, l_3),
                           URI_2(a) = URI_2(a_1),
                          URI_2(a) = URI_1(p)
q_{\text{lift}}(\text{URI}_2(a), y, z) \leftarrow \text{uni1-teaching}(c, a),
                          uni1-academic(a_1, y, l_2, s_2),
                          uni1-academic(a_2, f_3, z, s_3),
                           URI_2(a) = URI_2(a_1),
                           URI_2(a) = URI_2(a_2)
```

### Simplification and implicit equality normalization

```
\begin{aligned} \boldsymbol{q}_{\mathsf{struct}}(\mathrm{URI}_2(a), y, z) \leftarrow & \mathsf{uni1}\text{-}\mathsf{academic}(a, f_1, l_1, s_1), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, y, l_2, s_2), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, f_3, z, s_3), s_1 \in [1, 8] \\ \boldsymbol{q}_{\mathsf{struct}}(\mathrm{URI}_2(a), y, z) \leftarrow & \mathsf{uni1}\text{-}\mathsf{teaching}(c, a), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, y, l_2, s_2), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, f_3, z, s_3) \end{aligned}
```

### Simplification and implicit equality normalization

```
\begin{aligned} \boldsymbol{q}_{\mathsf{struct}}(\mathrm{URI}_2(a), y, z) \leftarrow& \mathsf{uni1}\text{-}\mathsf{academic}(a, f_1, l_1, s_1), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, y, l_2, s_2), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, f_3, z, s_3), s_1 \in [1, 8] \\ \boldsymbol{q}_{\mathsf{struct}}(\mathrm{URI}_2(a), y, z) \leftarrow& \mathsf{uni1}\text{-}\mathsf{teaching}(c, a), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, y, l_2, s_2), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, f_3, z, s_3) \end{aligned}
```

### Remarks on the flattening step:

- Possible exponential blowup!
- Usually avoided thanks to incompatible URI templates.

### Reformulation example - 3. Semantic optimization

### Simplification and implicit equality normalization

$$\begin{aligned} \boldsymbol{q}_{\mathsf{struct}}(\mathrm{URI}_2(a), y, z) \leftarrow& \mathsf{uni1}\text{-}\mathsf{academic}(a, f_1, l_1, s_1), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, y, l_2, s_2), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, f_3, z, s_3), s_1 \in [1, 8] \\ \boldsymbol{q}_{\mathsf{struct}}(\mathrm{URI}_2(a), y, z) \leftarrow& \mathsf{uni1}\text{-}\mathsf{teaching}(c, a), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, y, l_2, s_2), \\ & \mathsf{uni1}\text{-}\mathsf{academic}(a, f_3, z, s_3) \end{aligned}$$

### Self-join elimination (semantic optimization)

$$\begin{split} \mathsf{PK:} \ \mathsf{uni1-academic}(a,b,c,d) \wedge \mathsf{uni1-academic}(a,b',c',d') \\ & \to (b=b') \wedge (c=c') \wedge (d=d') \\ & \boldsymbol{q_{\mathsf{opt}}}(\mathrm{URI}_2(a),y,z) \leftarrow \\ & \leftarrow \\ & \boldsymbol{q_{\mathsf{opt}}}(\mathrm{URI}_2(a),y,z) \leftarrow \\ & \leftarrow \\ & \leftarrow \\ & \boldsymbol{q_{\mathsf{opt}}}(\mathrm{URI}_2(a),y,z) \leftarrow \\ & \leftarrow \\ &$$



References I