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**Algorithm 1** Multi-stage Reconstruction-based Membership Inference Attack

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1: Input: Private dataset  $D_i$  for each client, initialized model  $\omega$ , teacher model  
    $T$ , number of clients  $N$ , global rounds  $T$   
2: Output: Robust global model  
3: for  $t = 1, 2, \dots, T$  do  
4:   for  $i = 1, \dots, N$  in parallel do  
5:     Send global model  $\omega'$  to local client  $i$   
6:      $\omega' \leftarrow \text{LocalUpdate}(\omega')$   
7:   end for  
8:    $L(\omega) \leftarrow \sum_{i \in [N]} \frac{D_i}{\sum_{i \in [N]} D_i} L_i(\omega') \quad (3)$   
9: end for  
10: LocalUpdate( $\omega'$ )  
11: for each local epoch do  
12:   for each batch  $(x_i, y_i)$  of  $D_i$  do  
13:     /* Adversarial examples generation */  
14:      $x_i^{adv} \leftarrow x_i + \delta \quad (6)$   
15:     /* Clean examples augmentation */  
16:      $x_{ij} \leftarrow \lambda x_i + (1 - \lambda)x_j \quad (8)$   
17:     /* Adversarial examples augmentation */  
18:      $x_i^{adv} \leftarrow x_{ij} + \lambda(1 - \lambda)x_i^{adv} \quad (12)$   
19:     /* Vanilla mixture knowledge distillation */  
20:      $L_{VKD} \leftarrow KL(z_{ij}, z_{ij}^{adv}) + KL(z_{ij}, z_{isj}) \quad (11)$   
21:     /* Adversarial mixture knowledge distillation */  
22:      $L_{AKD} \leftarrow KL(z_i^{adv}, z_s^{adv}) + KL(z_{ij}^{adv}, z_s^{adv}) \quad (14)$   
23:     /* Consistency regularization */  
24:      $L_{ALG} \leftarrow \lambda_{adv} \|z_s^{adv} - z_g^{adv}\|^2 \quad (15)$   
25:     /* Overall local objective for each client */  
26:      $L \leftarrow \alpha L_{VKD} + (1 - \alpha)L_{AKD} + \lambda L_{ALG} \quad (16)$   
27:   end for  
28: end for  
29: return  $\omega_i$ 
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