

Module 4- Transformer



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Contents

- Construction
- Working Principle and types of single phase transformer
- Open circuit and short circuit tests: Losses and efficiency, all-day efficiency and regulation
- Autotransformer, Three phase transformer construction and connections

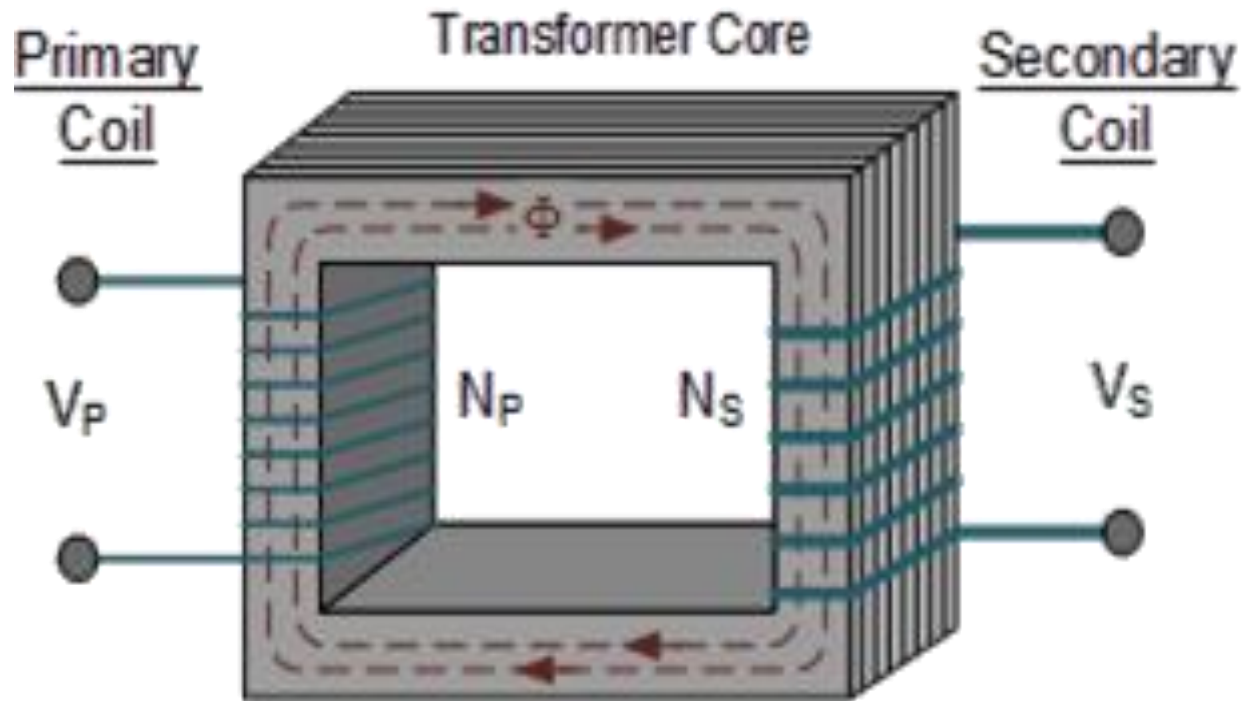
Transformer

- A static device
- Transfers electrical energy from one circuit to another with change in voltage level without a change of frequency
- Faraday's Law of electromagnetic induction.
- The two electric circuits are in mutual inductive influence of each other.
- Step up and Step Down Transformer

Transformer

- Static Electro-magnetization
- Voltage levels (230V, 400 V, 3.3 kV, 11 kV, 132 kV)
- Generation, Transmission and Distribution
- Changing current and voltage levels
- Highly efficient device
- Heart of Power System
- KVA Ratings

Transformer



Types of Transformer

A) Based on voltage level:

- 1) Step up transformer: Voltage increases (with subsequent decrease in current) at secondary.
- 2) Step down transformer: Voltage decreases (with subsequent increase in current) at secondary.

B) Based on type of supply:

- 1) Single phase transformer
- 2) Three phase transformer

C) Based on construction:

- 1) Core type
- 2) Shell type

D) Based on winding:

- 1) Single winding (Auto) transformer
- 2) Two winding transformer
- 3) Three winding transformer

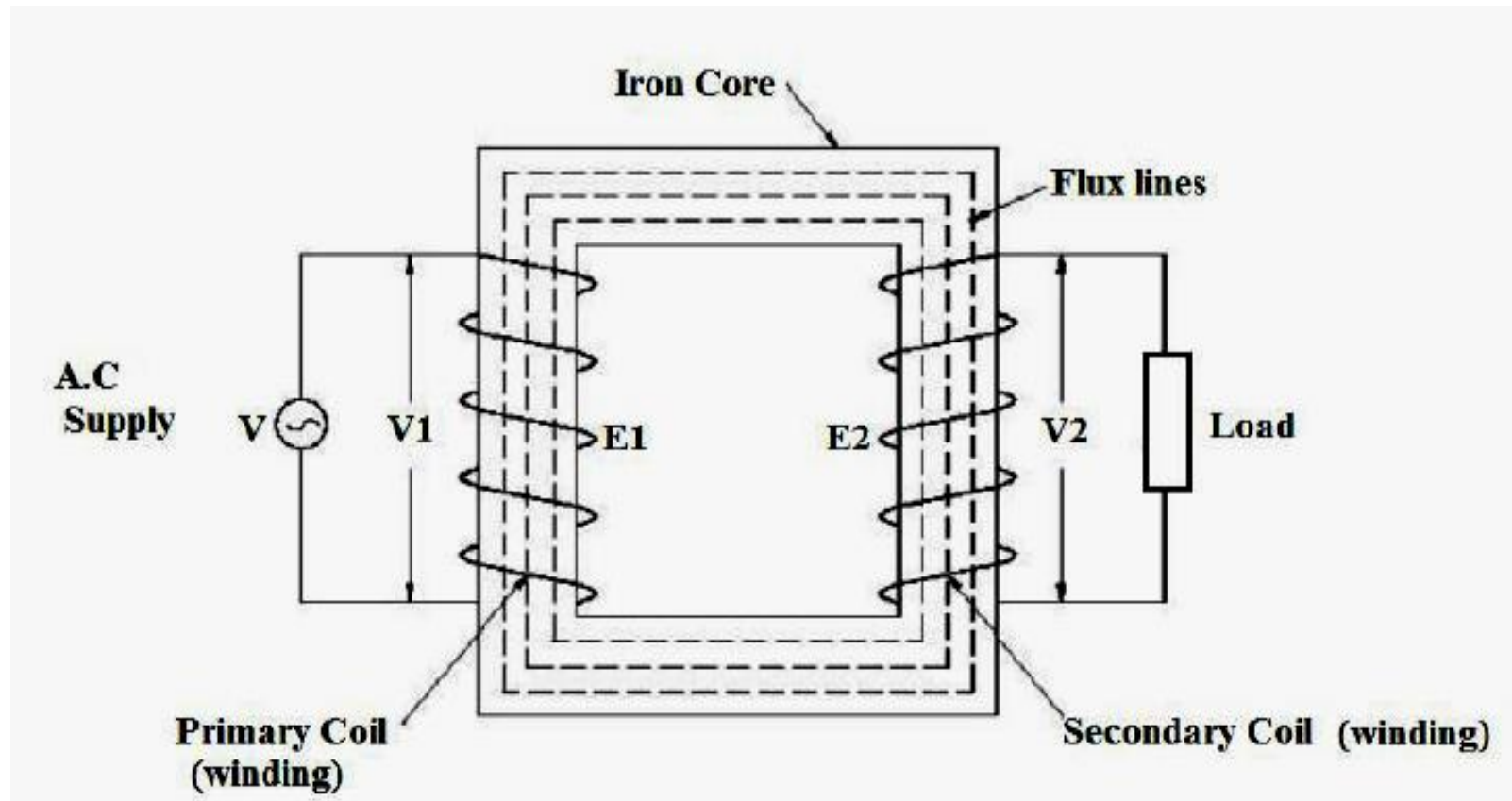
E) Based on cooling method used:

- 1) Natural air cooled transformer
- 2) Oil cooled transformer
- 3) Forced air cooled transformer
- 4) Water cooled transformer

F) Based on their use:

- 1) Power transformer: Used in transmission network, high rating
- 2) Distribution transformer: Used in distribution network, comparatively lower rating than that of power transformers.
- 3) Instrument transformer: Used in relay and protection purpose in different instruments in industries
 - a) Current transformer (CT)
 - b) Potential transformer (PT)

Construction of transformer



Construction of transformer

- A silicon steel core and two windings placed on it.
- The winding are insulated both from core and each other.
- The core is built up with thin soft iron silicon steel laminations to provide path of low reluctance to the magnetic flux.
- Copper or aluminum is used as winding material for Primary and Secondary Winding

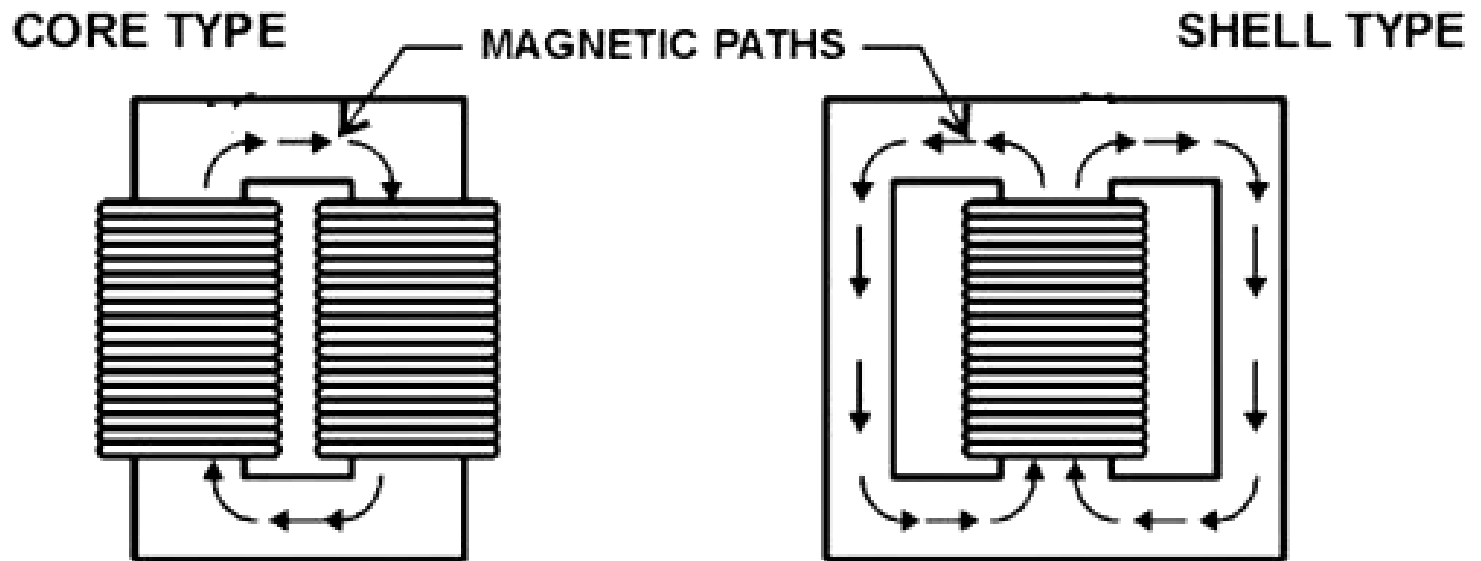
Principle of Operation

- Works on **Faraday's Law** of electromagnetic induction principle
- Alternating current flowing through primary –
-Alternating EMF - Alternating flux in core.
- Self induced EMF: E_1
- Alternating flux links to the secondary winding
- Alternating EMF is induced in secondary winding by principle of **mutual induction**.
- Mutual induced EMF: E_2
- The energy transferred to load by secondary is taken from primary via flux set in the core.

- When current in the primary coil changes being alternating in nature, a changing magnetic field is produced.
- This changing magnetic field gets associated with the secondary through the soft iron core.
- Magnetic flux linked with the secondary coil changes.
- It induces EMF in the secondary.
- If the secondary winding is closed circuit, then mutually induced current flows through it, and hence the electrical energy is transferred from one circuit (primary) to another circuit (secondary).

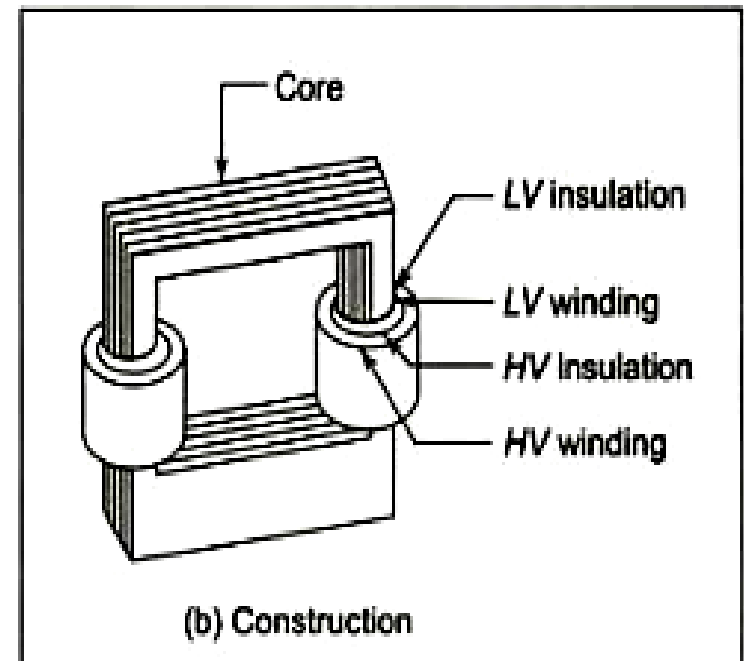
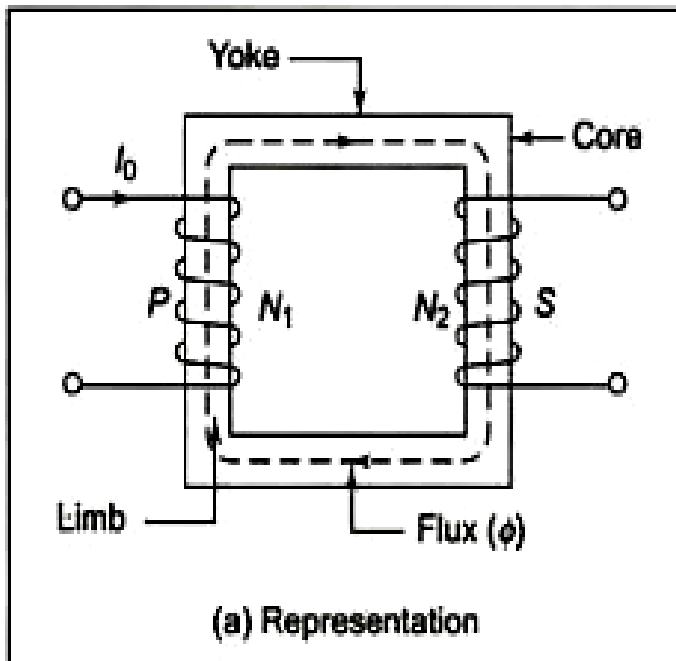
Types based on construction

- Core type transformer
- Shell type transformer



Core Type Transformer

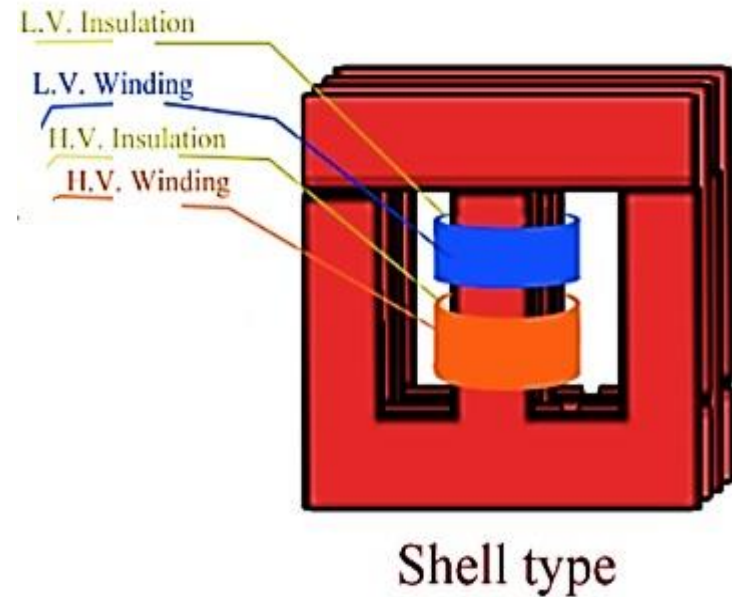
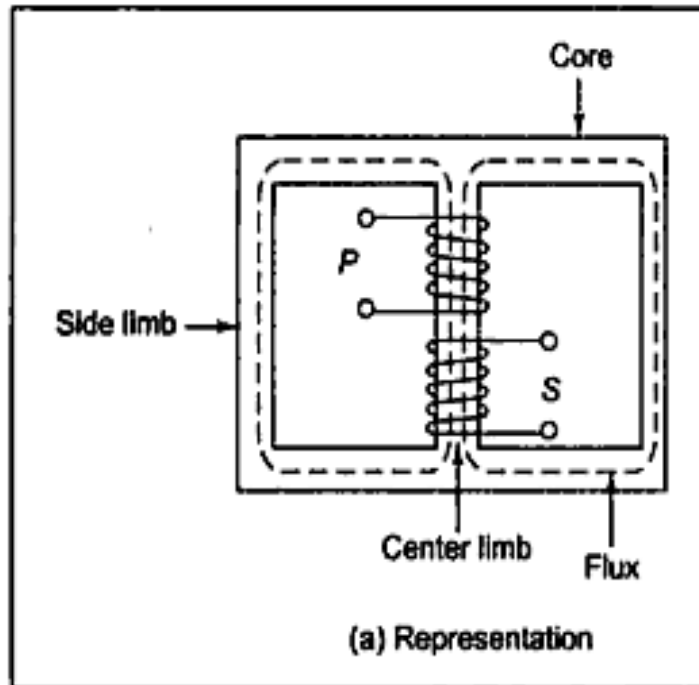
- Single magnetic circuit
- Core will be rectangular in shape and the coils used are cylindrical.
- Windings are uniformly distributed on two limbs of the core
- Winding encircles the core
- The cylindrical coils have different layers and each layer is insulated from each other. Materials like paper, cloth or mica can be used for insulation.
- Low voltage coil is placed inside near the core while high voltage coil surrounds the low voltage coil.
- Core with large number of thin laminations.



Shell Type Transformer

- Double magnetic circuit
- Core has three limbs and windings are placed on the central limb.
- Multilayer disc type or sandwich coils
- Core having large number of thin laminations.
- Better mechanical protection for winding

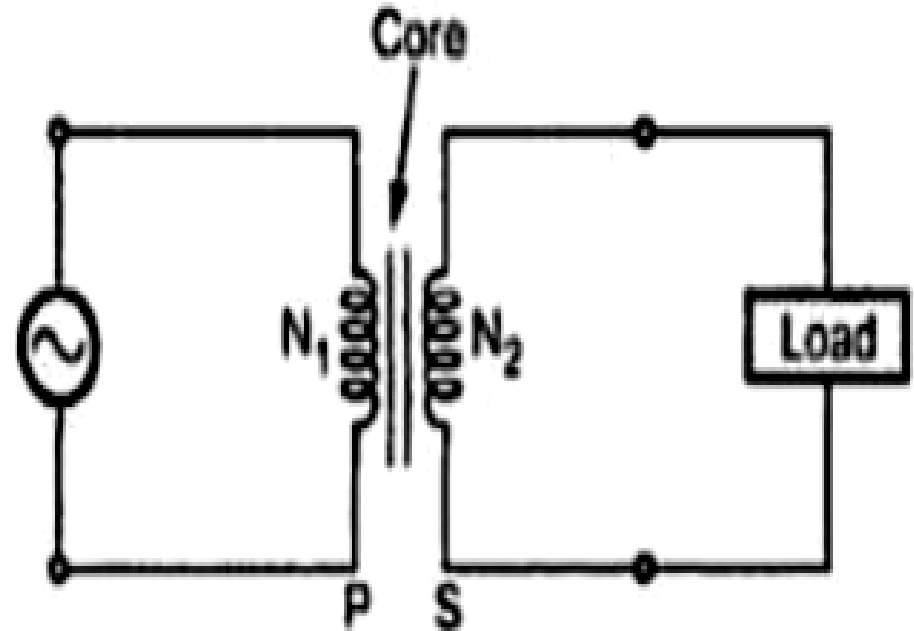
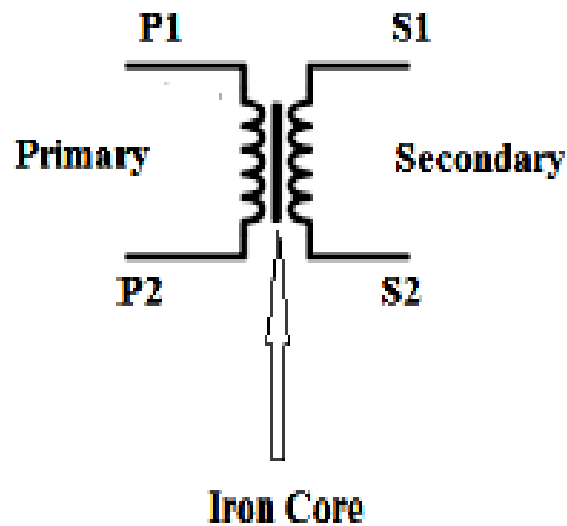
Shell Transformer



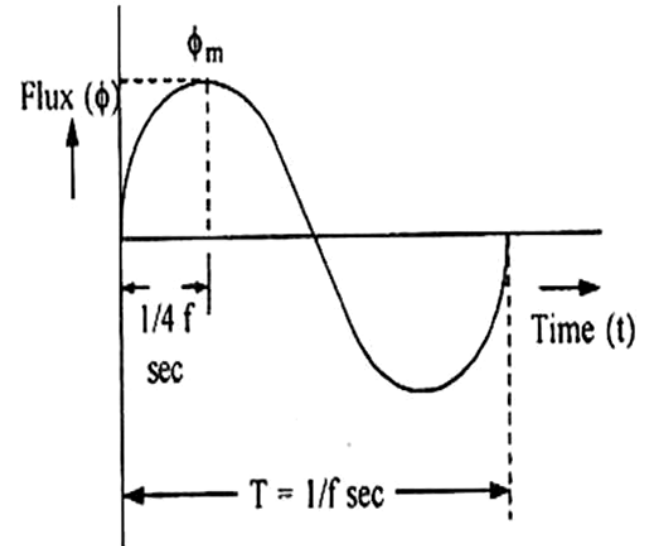
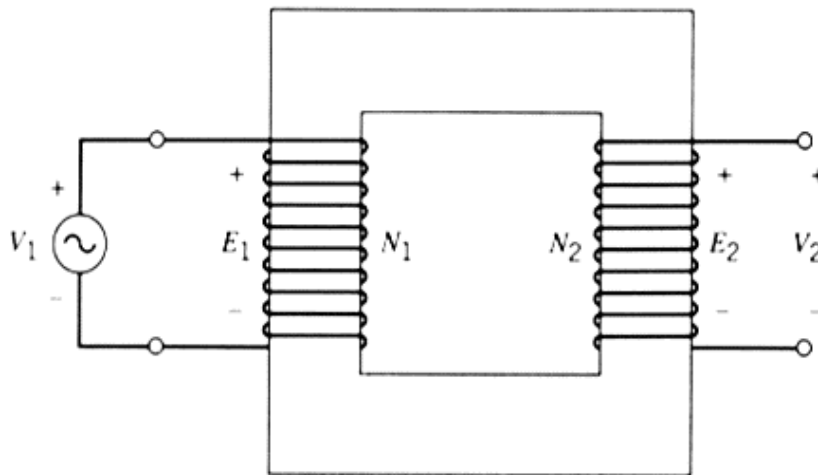
Comparison

S.R	Core Type Transformer	Shell type transformer
1	The core has only one magnetic circuit.	It has two magnetic circuits.
2	Core has two limbs.	Core has three limbs.
3	Cylindrical windings are used	Sandwich type windings are used
4	The winding is encloses considerable part of core.	Core encloses part of winding of transformer.
5	It has less mechanical protection to coil.	It has better mechanical protection to coil.
6	Natural cooling is provided.	Natural cooling cannot provide
7	It has better natural cooling since more surface is exposed to atmosphere.	Cooling is not very effective.
8	This transformer is easy to repair & maintenance.	This transformer is not easy to repair & maintenance.
9	Preferred for high voltage (less output)	Preferred for low voltage (high output)
10	Losses are more hence efficiency is less as compare to shell type	Losses are less hence efficiency is more as compare to core type

Symbol of Transformer



EMF Equation of transformer



EMF Equation of transformer

Φ = Flux

Φ_m = Maximum value of flux = $B_m * A$

N_1 = Number of primary winding turns

N_2 = Number of secondary winding turns

f = Frequency of the supply voltage (Hz)

E_1 = R.M.S. value of the primary induced EMF in volts

E_2 = R.M.S. value of the secondary induced EMF in volts

A = Cross-sectional area of core in m^2

- As shown in figure above, the core flux increases from its zero value to maximum value Φ_m in one quarter of the cycle, that is in $1/4$ frequency second. Therefore, average rate of change of flux = $\Phi_m / 1/4 f = 4f \Phi_m$ Wb/s
- Now, rate of change of flux per turn means induced emf in volts. Therefore,
average emf induced/turn = $4f \Phi_m$ Volt
- If flux Φ varies sinusoidally, then r.m.s value of induced e.m.f is obtained by multiplying the average value with form factor.
- Form Factor = r.m.s. value/average value = 1.11

- Therefore,
r.m.s value of e.m.f./turn = $1.11 \times 4f \phi_{\max} = 4.44f \phi_{\max}$
- Now, r.m.s value of induced e.m.f in the whole of primary winding
= (induced e.m.f./turn) \times Number of primary turns
- Therefore,
 $E_1 = 4.44 f N_1 \phi_m = 4.44 f N_1 B_m A$
- Similarly, r.m.s value of induced e.m.f in secondary is
 $E_2 = 4.44 f N_2 \phi_m = 4.44 f N_2 B_m A$
- In an ideal transformer on no load,
 $V_1 = E_1$ and $V_2 = E_2$, where V_2 is the terminal voltage

Voltage Transformation Ratio (K)

- From the above equations we get

$$E_2 / E_1 = V_2 / V_1 = N_2 / N_1 = K$$

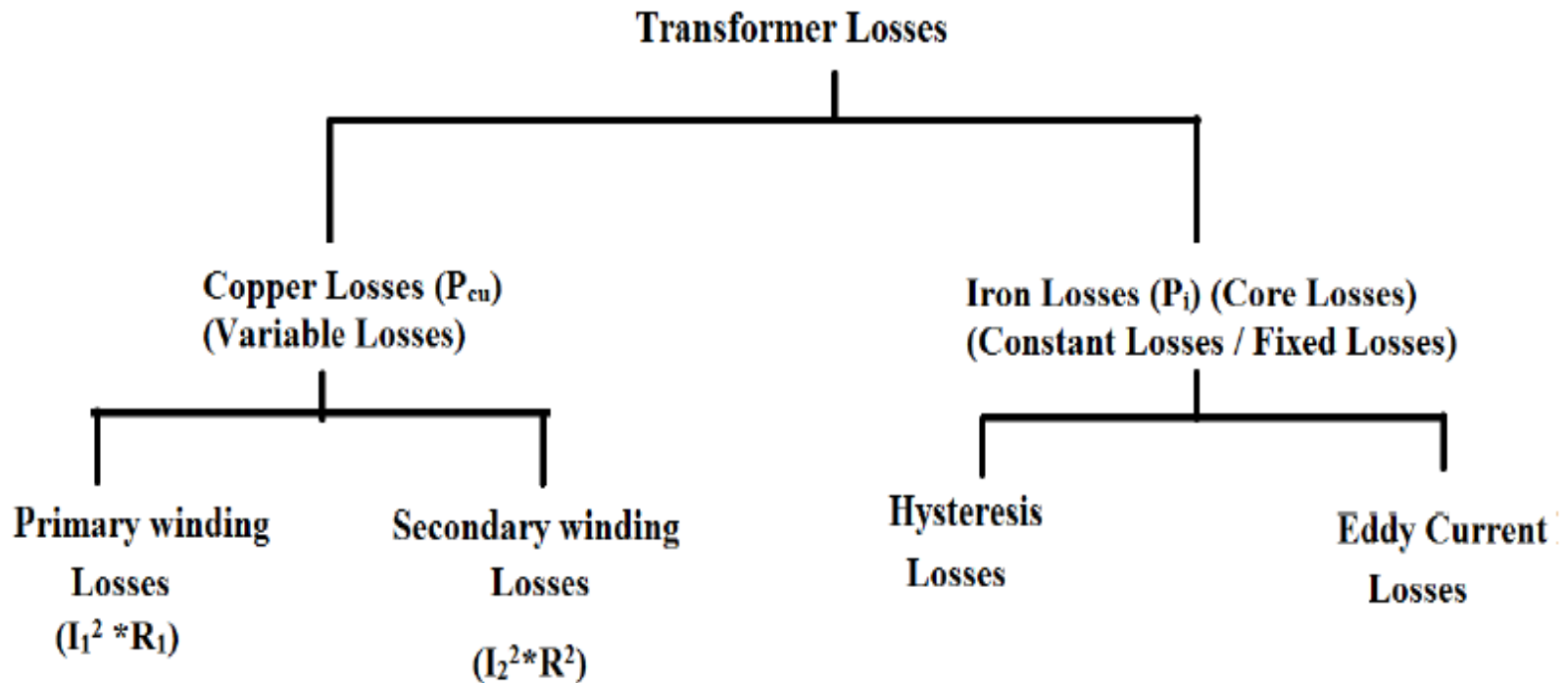
- (1) If $N_2 > N_1$, that is $K > 1$, then transformer is called step-up transformer.
- (2) If $N_2 < N_1$, that is $K < 1$, then transformer is known as step-down transformer.

- Again for an ideal transformer,

$$V_1 I_1 = V_2 I_2 \quad (\text{Constant power})$$

$$I_2 / I_1 = V_1 / V_2 = 1/K$$

Losses in Transformer



Copper Losses

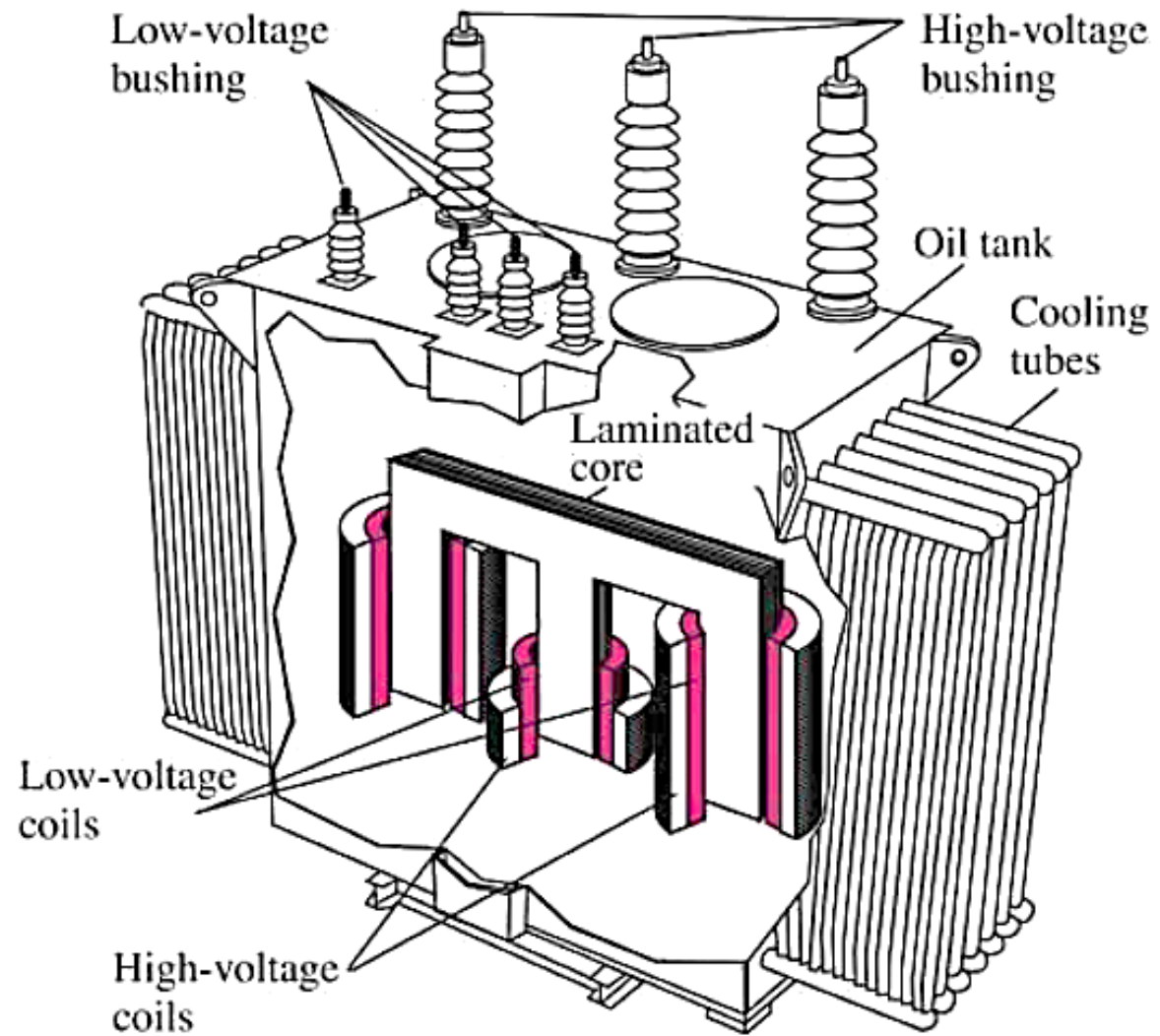
- Power wasted in the form of I^2R loss
- Resistances of the primary and secondary windings
- Copper losses are called variable losses as it changes as load changes.

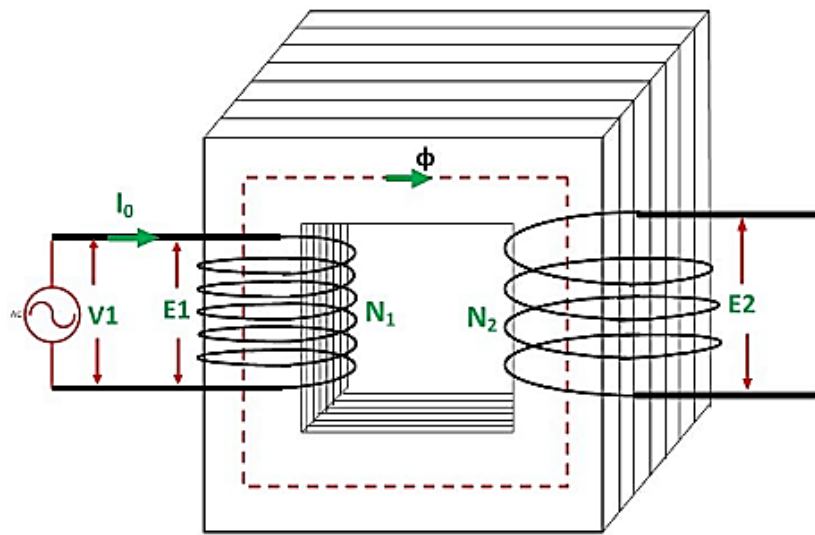
Core or Iron Losses

- Losses are proportional to flux density & supply frequency
- Independent of load current
- Constant losses
- Types of iron loss:
 1. Hysteresis Losses
 2. Eddy current Losses

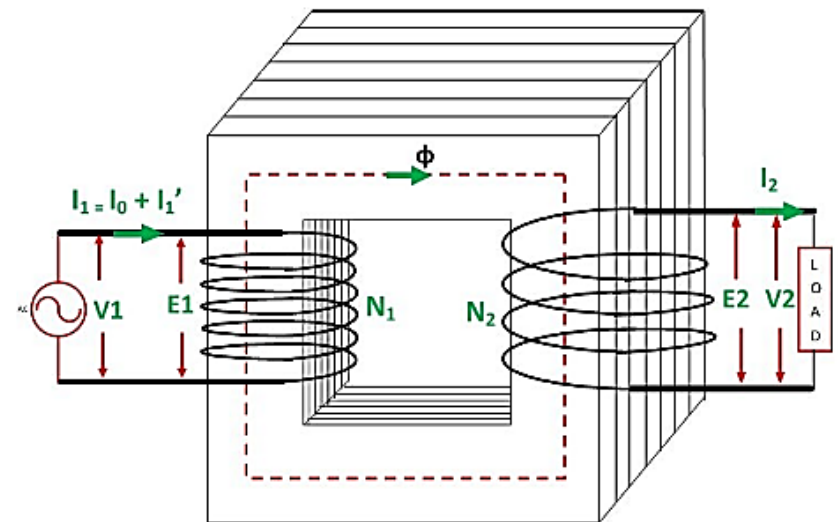
Rating of Transformer

- Power losses appear in the form of heat
- Output rating is the product of output voltage and output current.
- Copper loss in the transformer depends on the current through the winding.
- Iron or core loss depends on the voltage ($f = \text{const.}$)
- Losses don't depend on the power factor of the load.
- So transformer rating is in KVA





Transformer on no-load



Transformer on load

Transformer on No-Load

(Having No Winding Resistance and No Leakage Reactance)

- When an alternating source is applied in the primary, the source will supply the current for magnetizing the core of transformer. But this current is not the actual magnetizing current; it is a little bit greater than actual magnetizing current.
- Total current supplied from the source has two components, one is magnetizing current which is merely utilized for magnetizing the core, and another component of the source current is consumed for compensating the core losses in transformers.

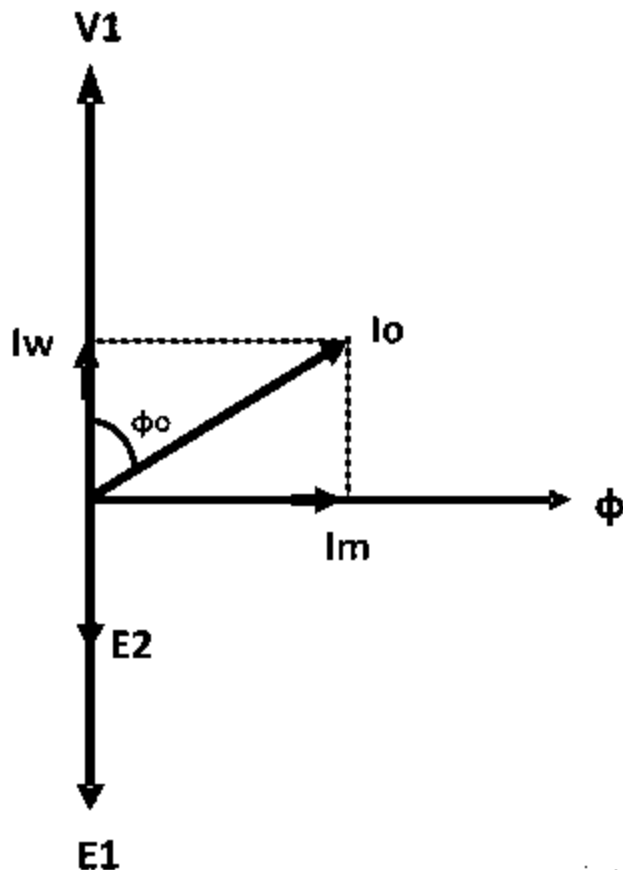
No load input current I_0 has two components:

1. A purely reactive component (I_m):

Magnetizing component to produce the flux.

2. An active component (I_w):

Power component which supplies core losses.



Working component $I_w = I_0 \cos \phi_0$

No load current $I_0 = \sqrt{I_w^2 + I_m^2}$

Magnetizing component $I_m = I_0 \sin \phi_0$

Power factor $\cos \phi_0 = \frac{I_w}{I_0}$

No load power input $P_0 = V_1 I_0 \cos \phi_0$

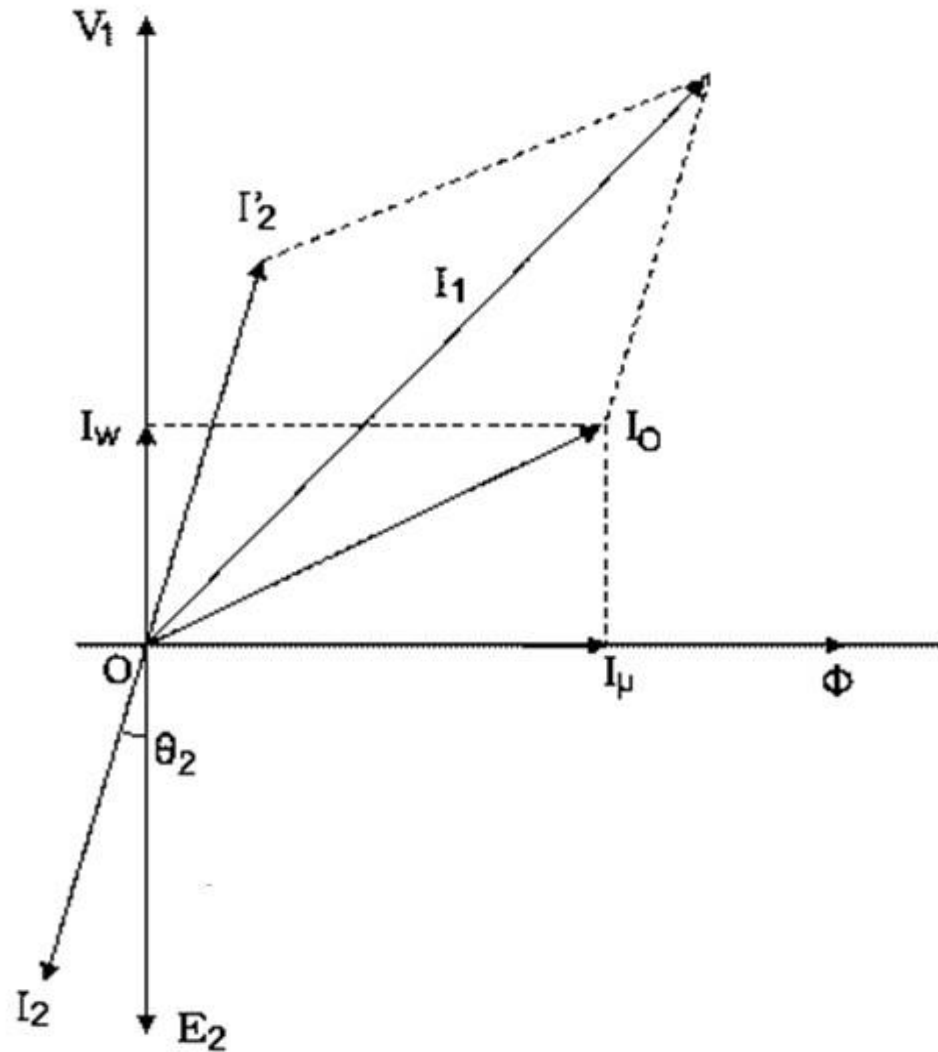
Transformer on Load

- Consider, a transformer having core loss but no copper loss and leakage reactance.
- When the load is connected to the secondary of the transformer, the I_2 current flows through their secondary winding. The secondary current induces the magnetomotive force $N_2 I_2$ on the secondary winding of the transformer. This force set up the flux ϕ_2 in the transformer core. The flux ϕ_2 oppose the flux ϕ , according to Lenz's law.
- As the flux ϕ_2 opposes the flux ϕ , the resultant flux of the transformer decreases and this flux reduces the induces EMF E_1 .

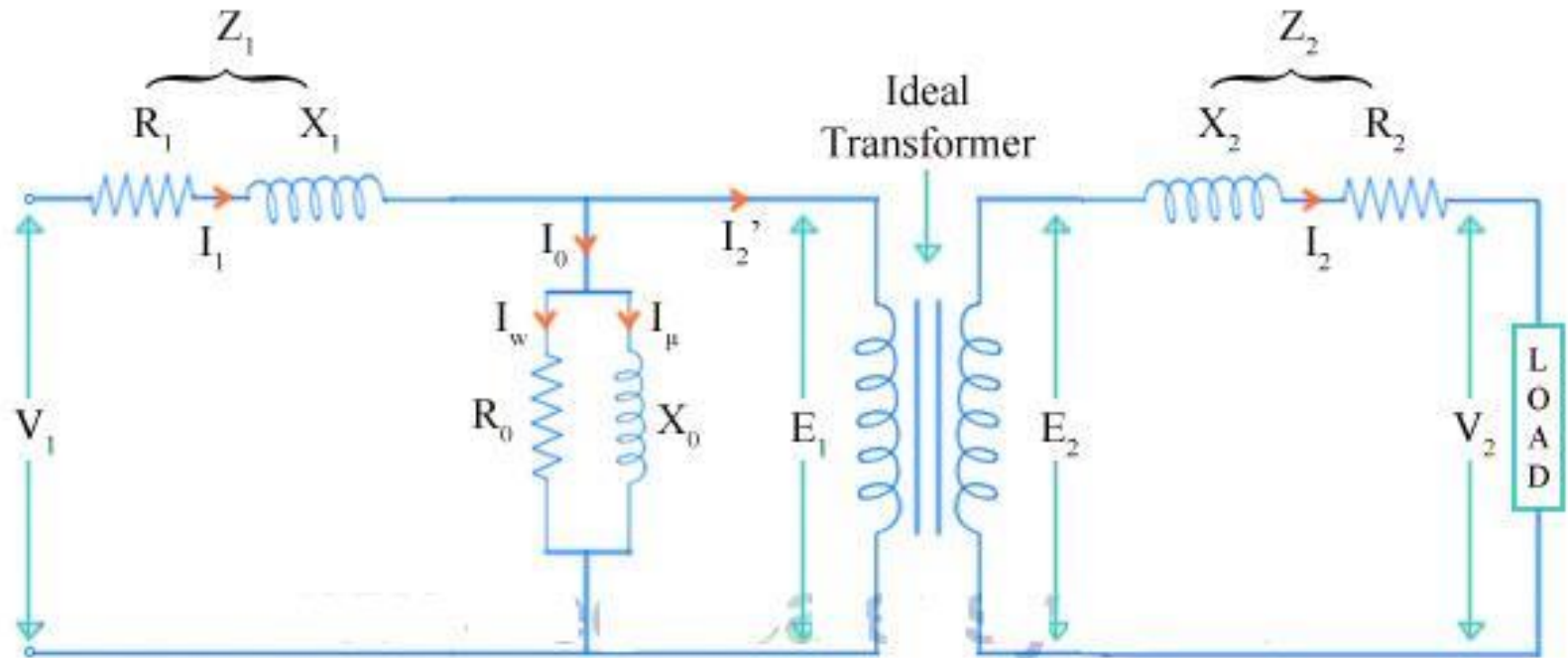
- Thus, the strength of the V_1 is more than E_1 and an additional primary current I'_1 drawn from the main supply. The additional current is used for restoring the original value of the flux in the core of the transformer so that the $V_1 = E_1$.
- So total current, this transformer draws from source can be divided into two components.
 - 1) First one is utilized for magnetizing the core and compensating the core loss, i.e., I_0 . It is the no-load component of the primary current.
 - 2) The second one is utilized for compensating the counter flux of the secondary winding. It is known as load component of the primary current.

$$I_1 = I_0 + I'_2$$

On-load Phasor diagram



Equivalent circuit of Transformer



Efficiency of a Transformer

- Power input = Power output + Total losses
= Power output + P_i + P_{Cu}
- The efficiency of any device is defined as the ratio of the power output to power input.

$$\eta = \frac{\text{output power}}{\text{input power}} = \frac{\text{output power}}{\text{output power} + \text{losses}}$$

$$\eta = \frac{\text{output power}}{\text{output power} + \text{iron losses} + \text{copper losses}}$$

$$\eta = \frac{V_2 I_2 \cos \phi_2}{V_2 I_2 \cos \phi_2 + P_i + P_c}$$

$$\eta_x = \frac{x \times \text{output}}{x \times \text{output} + P_i + x^2 P_c} = \frac{x V_2 I_2 \cos \phi_2}{x V_2 I_2 \cos \phi_2 + P_i + x^2 I_2^2 R_{es}}$$

All day efficiency of a transformer

- Distribution transformer serves residential and commercial loads which fluctuate throughout the day. For example, the distribution transformers are energized for 24 hours, but they deliver very light loads for the major portion of the day, and they do not supply rated or full load.
- There are various losses in the transformer such as iron and copper loss. The iron or core loss occurs for the whole day in the distribution transformer. The second type of loss known as copper loss occurs only when the transformers are in the loaded condition.

- Hence, the performance of such transformers cannot be judged by the commercial or ordinary efficiency, but the efficiency is calculated or judged by All Day Efficiency also known as operational efficiency or energy efficiency which is computed by energy consumed during 24 hours.
- The maximum efficiency in such transformers occurs at about 60-70 % of the full load.

$$\text{All day efficiency, } \eta_{\text{all day}} = \frac{\text{output in kWh}}{\text{input in kWh}} \quad (\text{for 24 hours})$$

Voltage Regulation of Transformer

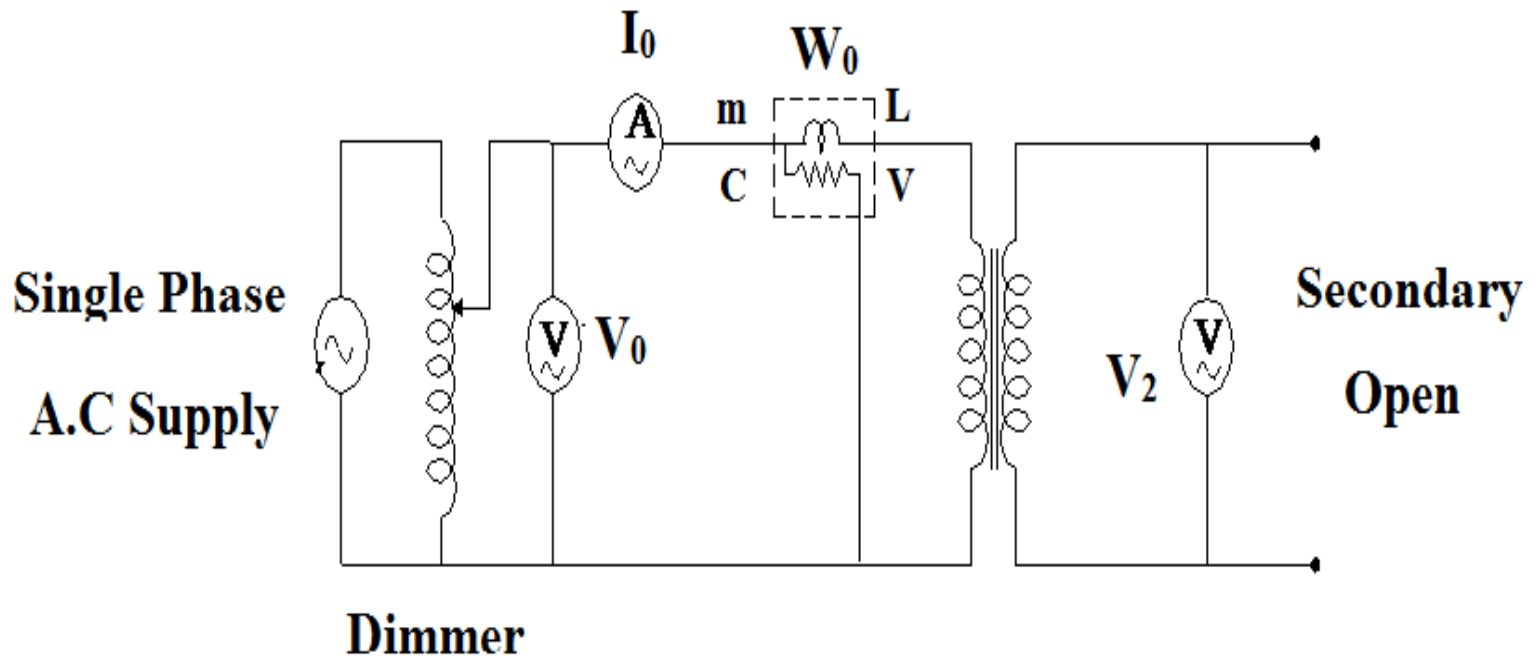
- The voltage regulation is the percentage of voltage difference between no load and full load voltages of a transformer with respect to its full load voltage.
- Suppose, electrical power transformer is open circuited, means load is not connected with secondary terminals. In this situation, the secondary terminal voltage of the transformer will be its secondary induced emf E_2 . Whenever full load is connected to the secondary terminals of the transformer, rated current I_2 flows through the secondary circuit and voltage drop comes into picture. At this situation, primary winding will also draw equivalent full load current from source.

- The voltage drop in the secondary is $I_2 Z_2$ where Z_2 is the secondary impedance of transformer.
- Now at this loading condition, voltage V_2 will be present across load terminals which is obviously less than no load secondary voltage E_2 and this is because of $I_2 Z_2$ voltage drop in the transformer.

$$\text{Voltage regulation}(\%) = \frac{E_2 - V_2}{V_2} \times 100\%$$

Open Circuit(O.C.) Test:

- Experimental setup:



Note : Usually H.V winding is Kept open

Primary winding is connected to a.c supply through dimmer. Voltmeter, Ammeter & wattmeter are connected to primary side to measure primary voltage, current & power (V_{oc} , I_{oc} , W_{oc}).

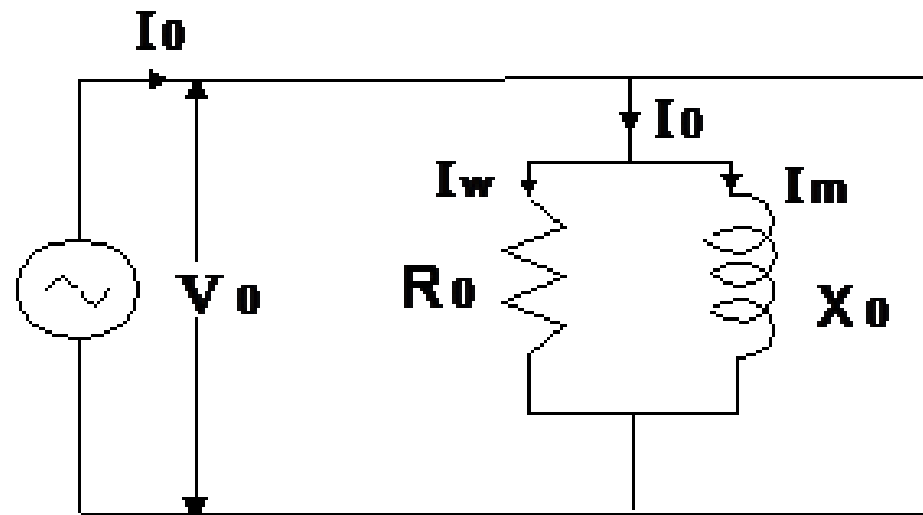
One voltmeter is connected at secondary side to measure no load voltage at secondary side ($V_2 = E_2$).

- **Procedure:**

1. Connect circuit as per the circuit as shown.
2. Keep dimmer at its minimum position.
3. Switch on a.c supply & adjust dimmer to get rated primary voltage (230 V) as measured by voltmeter across primary winding.
4. Measure primary current & power (I_{oc} & W_{oc})

Two components of I_{oc} (no load current) are as ;

- $I_m = I_{oc} \sin \phi_o$
- $I_w = I_{oc} \cos \phi_o$



Equivalent Circuit Diagram for O.C. Test

Since no load power is given as

$$W_{oc} = V_{oc} I_{oc} \cos \phi_{oc}$$

Hence no load p.f is given as

$$\cos \phi_{oc} = W_{oc} / V_{oc} I_{oc}$$

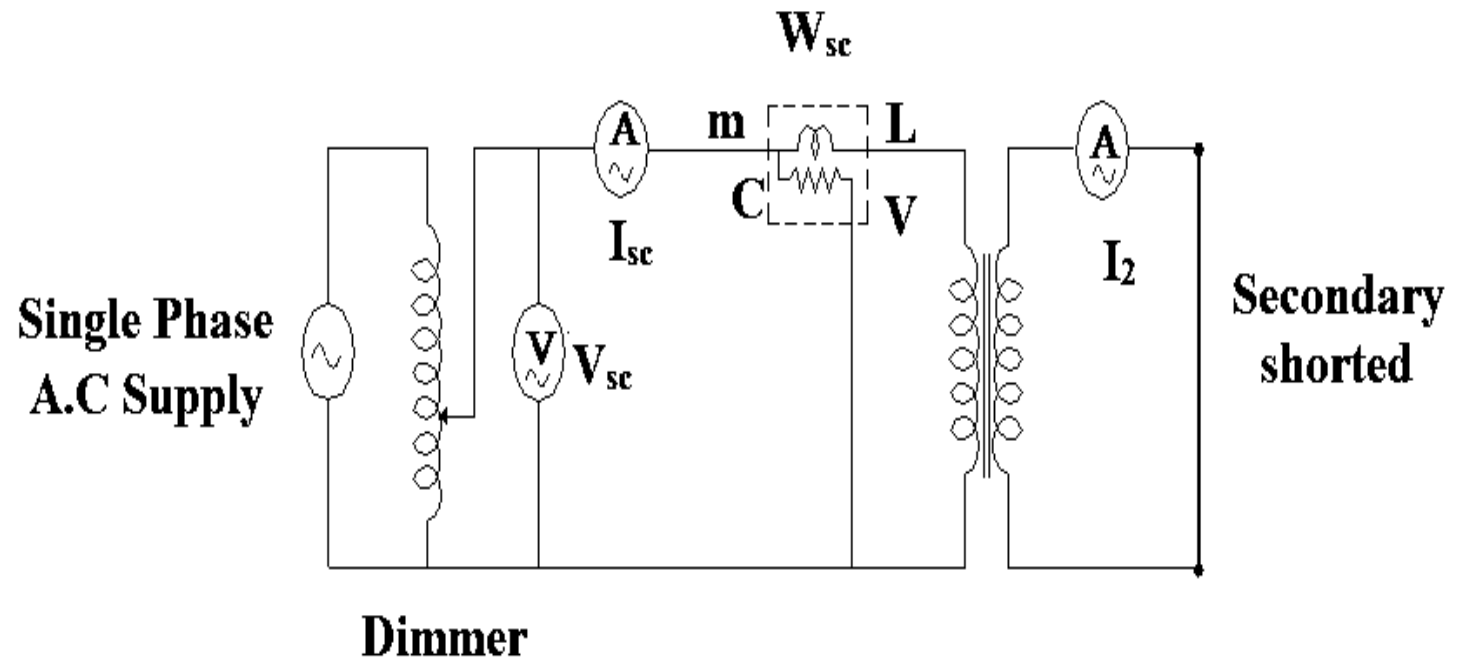
- I_{oc} is very small compared to full load current (about 3 % to 5% of full load) so primary copper losses are negligible and as $I_2 = 0$ therefore secondary losses = zero. Therefore total copper losses are very small hence assumed to be zero. Hence reading W_{oc} represents the Iron loss.

$$W_{oc} = P_i = \text{Iron Loss}$$

Calculations:

- $I_m = I_{oc} \sin \phi_{oc}$
- $I_w = I_{oc} \cos \phi_{oc}$
- $\cos \phi_{oc} = W_{oc} / V_{oc} I_{oc}$
- $R_0 = V_{oc} / I_w \text{ ohm}$
- $X_0 = V_{oc} / I_m \text{ ohm.}$

S.C. Test:



Note : Usually L.V winding is short circuited

Primary winding is connected to a.c supply through dimmer. Voltmeter, Ammeter & wattmeter are connected to primary side to measure primary voltage, current & power (V_{sc} , I_{sc} , W_{sc}). One Ammeter is connected at secondary side to measure short circuit current.

- **Procedure:**

1. Connect circuit as per the circuit as shown.
2. Keep dimmer at its minimum position.
3. Switch on a.c supply & adjust dimmer to get rated current I_{sc} as measured by ammeter connected in primary winding it will be obtained at a low voltage about 10% of its rated value.
(do not increase the primary voltage further)
4. Note down W_{sc} , V_{sc} , I_{sc}

At full load, Iron loss is very small. Hence they are neglected. Total loss is equal total copper loss at full load. Therefore wattmeter W_{sc} gives almost entirely the full load copper losses.

$$\mathbf{W_{sc} = \text{full load copper loss} = P_{cu}}$$

- Calculations-

$$W_{sc} = V_{sc} I_{sc} \cos \phi_{sc}$$

Hence full load p.f is given as

$$\cos \phi_{sc} = W_{sc} / V_{sc} I_{sc}$$

But W_{sc} indicates full load copper loss

Therefore: $W_{sc} = I_{sc}^2 R_1$

Therefore: $R_1 = W_{sc} / I_{sc}^2$

- $Z_1 = V_{sc} / I_{sc}$

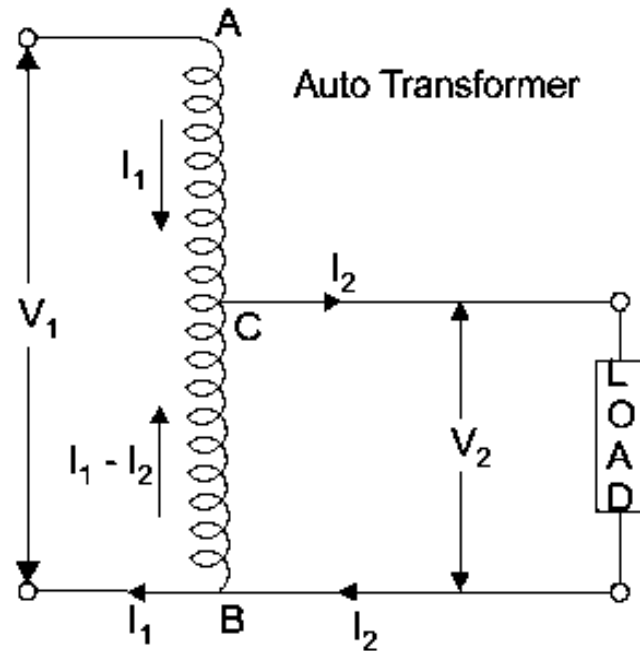
$$Z_1 = \sqrt{R_1^2 + X_1^2}$$

- Therefore:

$$X_1 = \sqrt{Z_1^2 - R_1^2}$$

Autotransformer

- Auto transformer is kind of electrical transformer where primary and secondary shares same common single winding. So basically it's a one winding transformer.
- In Auto Transformer, one single winding is used as primary winding as well as secondary winding. But in two windings transformer two different windings are used for primary and secondary purpose.



The winding AB of total turns N_1 is considered as primary winding. This winding is tapped from point 'C' and the portion BC is considered as secondary. Let's assume the number of turns in between points 'B' and 'C' is N_2 .

- If V_1 voltage is applied across the winding i.e. in between 'A' and 'C'.

So voltage per turn in this winding is $\frac{V_1}{N_1}$

- Hence, the voltage across the portion BC of the winding, will be,

$\frac{V_1}{N_1} \times N_2$ and from the figure above, this voltage is V_2

$$\text{Hence, } \frac{V_1}{N_1} \times N_2 = V_2$$

$$\Rightarrow \frac{V_2}{V_1} = \frac{N_2}{N_1} = \text{Constant} = K$$

- As BC portion of the winding is considered as secondary, it can easily be understood that value of constant 'K' is nothing but turns ratio or voltage ratio of that **auto transformer**. When load is connected between secondary terminals i.e. between 'B' and 'C', load current I_2 starts flowing. The current in the secondary winding or common winding is the difference of I_2 and I_1 .

Advantages of using Auto Transformers

- For transformation ratio = 2, the size of the **auto transformer** would be approximately 50% of the corresponding size of two winding transformer. Thus auto transformer is smaller in size and cheaper.
- An auto transformer has higher efficiency than two winding transformer. This is because of less copper loss and core loss due to reduction of transformer material.
- Auto transformer has better voltage regulation as voltage drop in resistance and reactance of the single winding is less.

Disadvantages of Using Auto Transformer

- The main disadvantage of an autotransformer is that it does not have the primary to secondary winding isolation of a conventional double wound transformer. Then an autotransformer can not safely be used for stepping down higher voltages to much lower voltages suitable for smaller loads.
- If the secondary side winding becomes open-circuited, load current stops flowing through the primary winding stopping the transformer action resulting in the full primary voltage being applied to the secondary terminals.
- If the secondary circuit suffers a short-circuit condition, the resulting primary current would be much larger than an equivalent double wound transformer due to the increased flux linkage damaging the autotransformer.
- Since the neutral connection is common to both the primary and secondary windings, earthing of the secondary winding automatically Earth's the primary as there is no isolation between the two windings. Double wound transformers are sometimes used to isolate equipment from earth

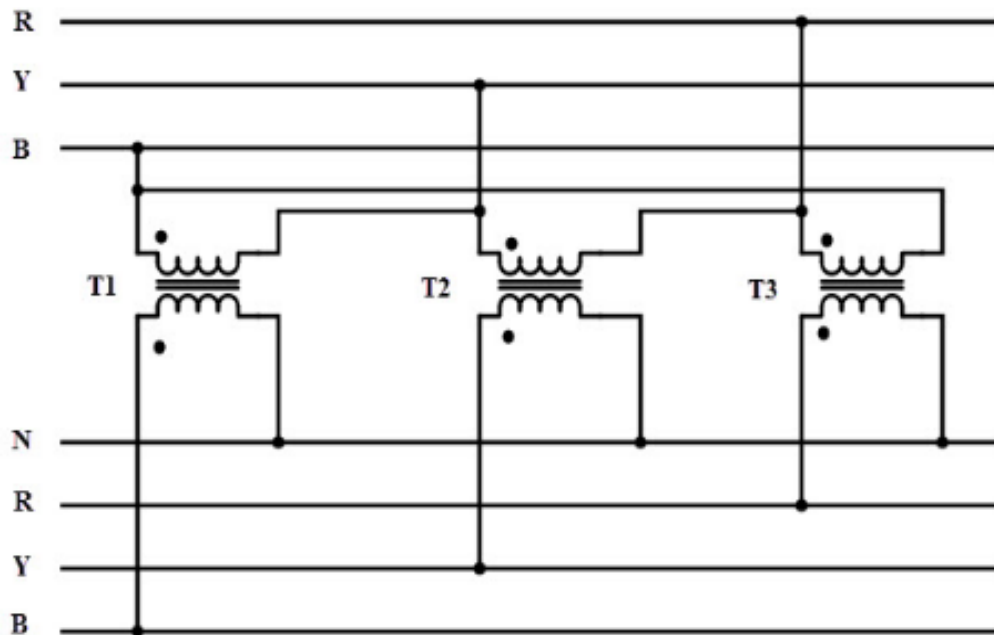
Applications of Auto-Transformers

- Compensating voltage drops by boosting supply voltage in distribution systems.
- Auto transformers with a number of tapping are used for starting induction and synchronous motors.
- Auto transformer is used as variac in laboratory or where continuous variable voltage over broad ranges are required

Three phase transformers

- Three phase transformers are used to step up(increase) or step-down(decrease) the high voltages in various stages of power transmission system.
- The power generated at various generating stations is in three phase nature and the voltages are in the range of 13.2KV or 22KV. In order to reduce the power loss to the distribution end, the power is transmitted at somewhat higher voltages like 132 or 400KV. Hence, for transmission of the power at higher voltages, three phase step-up transformer is used to increase the voltage.
- Also at the end of the transmission or distribution, these high voltages are step-down to levels of 6600, 400, 230 volts, etc. For this, a three phase step down transformer is used.

- A three phase transformer can be built in two ways; a bank of three single phase transformers or single unit of three phase transformer. The former one is built by suitably connecting three single phase transformers having same ratings and operating characteristics.
- A three phase bank can be constructed with a single three phase transformer consisting of six windings on a common multi-legged core.

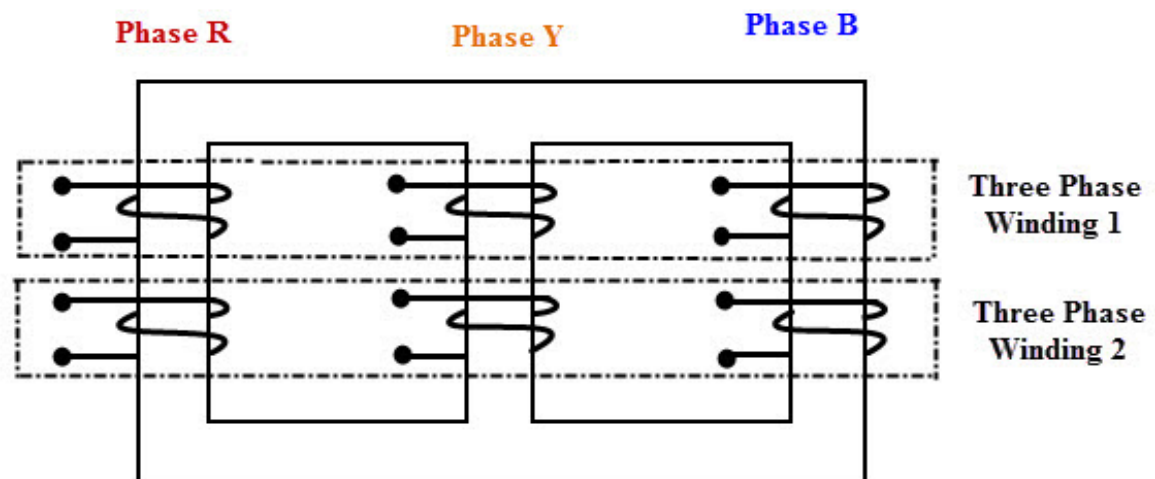


Three Phase Transformer

Construction

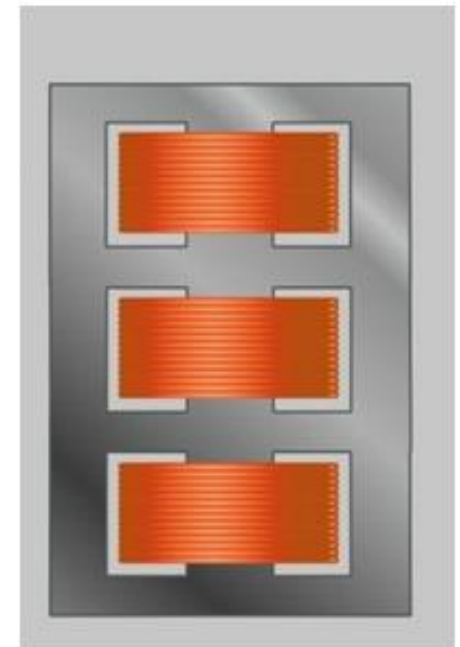
A) Core Type Construction

- In core type three phase transformer, core is made up of three limbs or legs and two yokes. The magnetic path is formed between these yokes and limbs. On each limb both primary and secondary windings are wound concentrically. Circular cylindrical coils are used as the windings for this type of transformer. The primary and secondary windings of one phase are wound on one leg.



B)Shell Type Construction

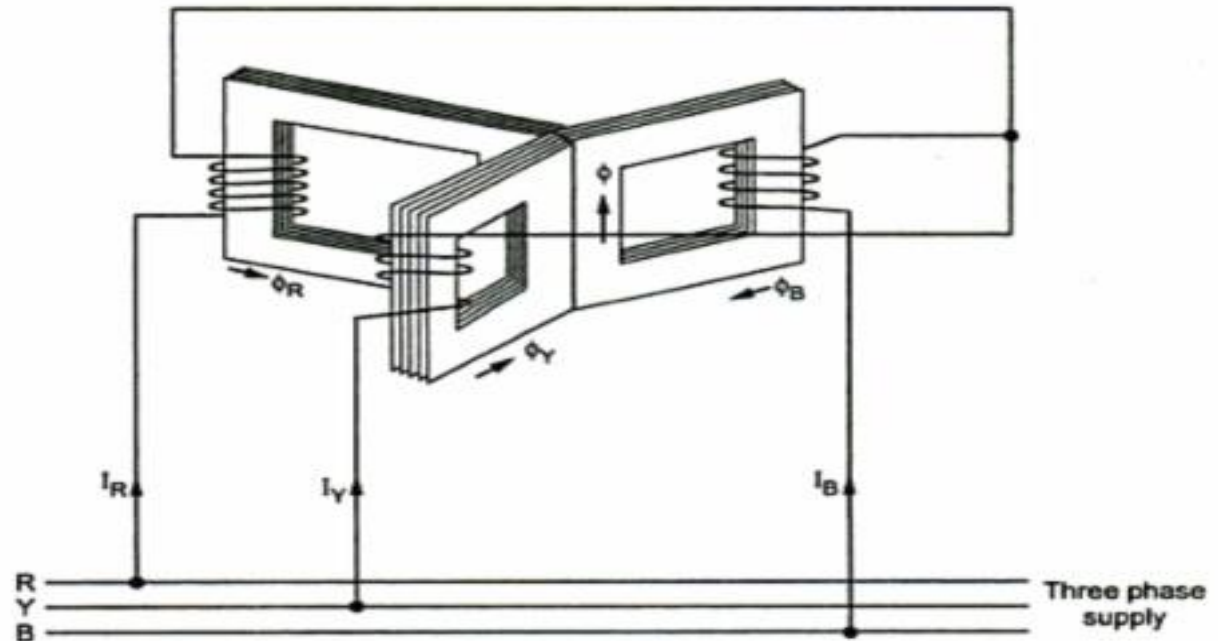
- In shell type, three phases are more independent because each phase has independent magnetic circuit compared with core type transformer.
- The construction is similar to the single phase shell type transformer built on top of another. The magnetic circuits of this type of transformer are in parallel. Shell type constructed transformers are rarely used in practice.



Shell Type

Working of Three Phase Transformers

- Consider the below figure in which the primary of the transformer is connected in star fashion on the cores. For simplicity, only primary winding is shown in the figure which is connected across the three phase AC supply.
- The three cores are arranged at an angle of 120 degrees to each other.



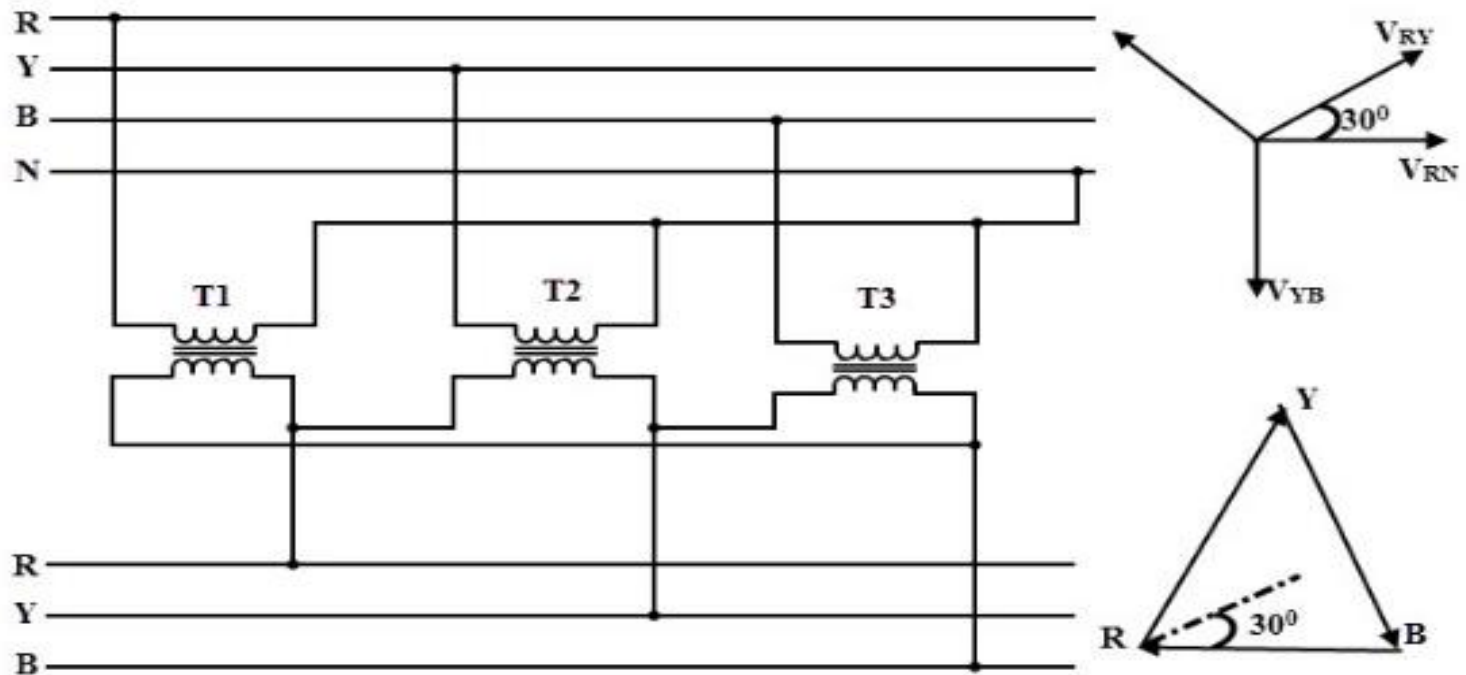
- When the primary is excited with the three phase supply source, the currents I_R , I_Y and I_B are starts flowing through individual phase windings. These currents produce the magnetic fluxes Φ_R , Φ_Y and Φ_B in the respective cores. Since the center leg is common for all the cores, the sum of all three fluxes are carried by it.
- These fluxes induce the secondary EMFs in respective phase such that they maintain their phase angle between them. These EMFs drives the currents in the secondary and hence to the load. Depends on the type of connection used and number of turns on each phase, the voltage induced will be varied for obtaining step-up or step-down of voltages.

Three Phase Transformer Connections

The primary and secondary windings are connected in different ways, such as in delta or star or combination of these two. The voltage and current ratings of the three phase transformer is depends on suitable connection. The most commonly used connections are

- **Star-delta**
- **Delta-star**
- **Delta-delta**
- **Star-star**

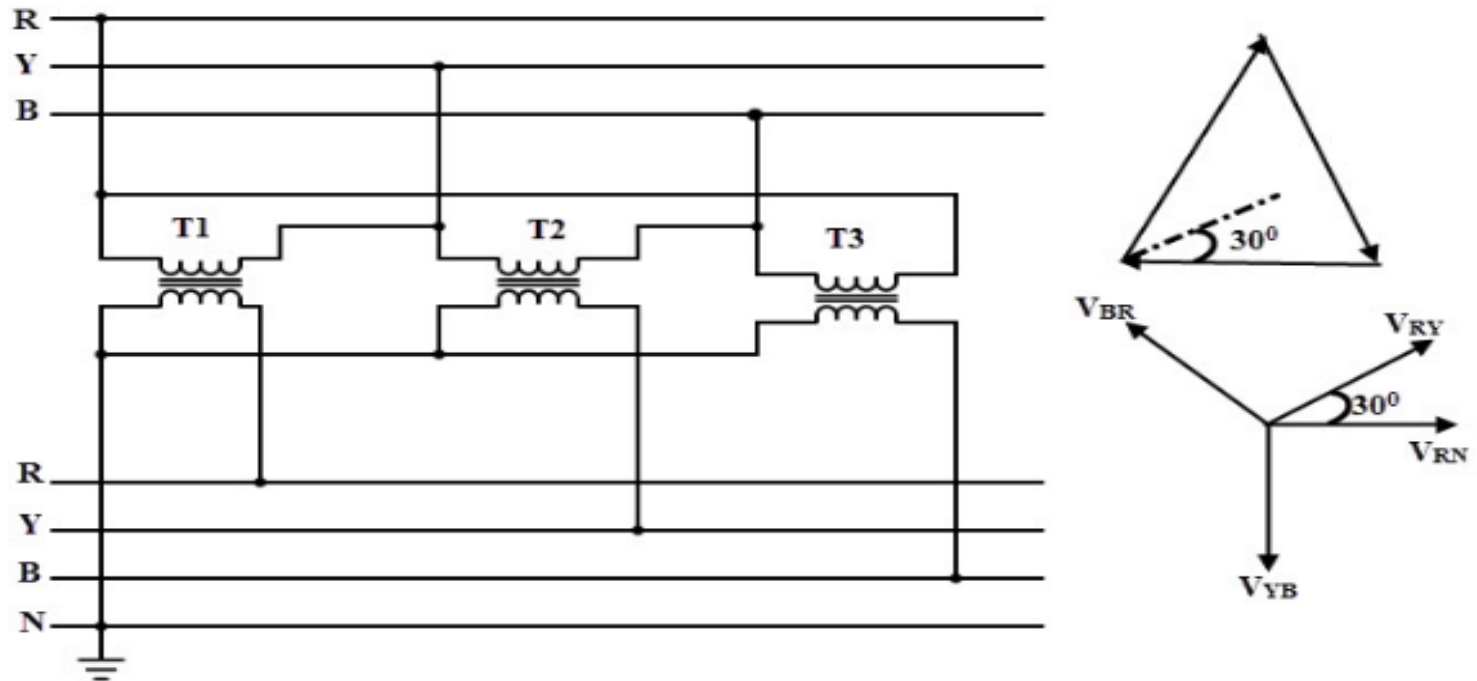
Star– Delta Connection



- This type of connection is commonly used to step-down the voltages to a lower value in transmission end substations. Utility companies use this connection to reduce the voltage levels for distribution systems.
- In this, the primary winding of the transformer is connected in star and secondary in delta connection.

- The neutral point on the primary or high voltage side can be grounded which is desirable in most of the cases.
- The line voltage ratio between secondary and primary is $1/\sqrt{3}$ times the transformation ratio of each transformer.
- There exists 30 degrees phase difference between primary and secondary line voltages.
- Since the actual primary coil voltage is 58% of the primary line voltage, the insulation requirements for HV windings is reduced by using this winding.
- In this connection balanced three phase voltage are obtained at the secondary or LV side, even when the unbalanced currents are flowing in the primary or HV side due to neutral wire. The neutral wire grounding also provides lightning surge protection.

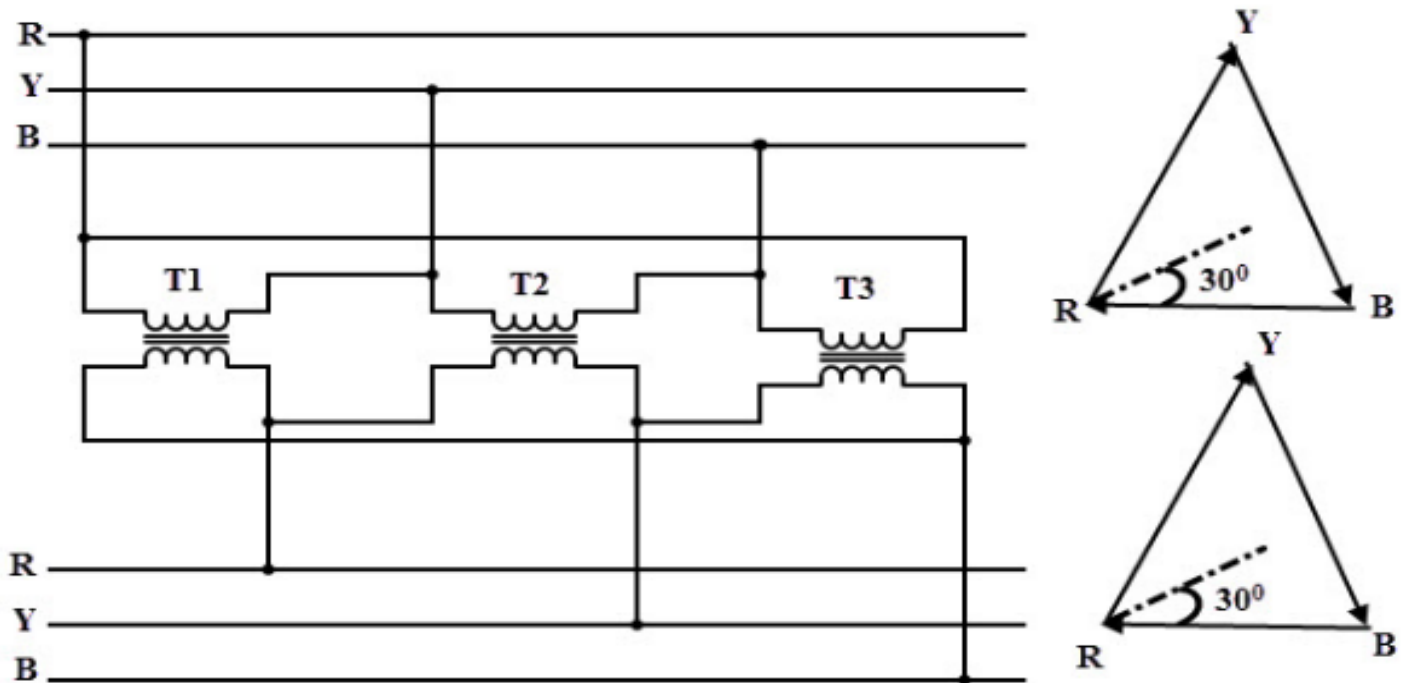
Delta – Star Connection




- This connection is used to step-up the voltage level and is commonly employed in sending end or starting of high voltage transmission system.
- In this, the primary is connected in delta fashion and secondary in star fashion so that three phase 4 wire system at secondary is possible.

- The secondary voltage to the load is $\sqrt{3}$ times the delta connected primary voltage. Also the load and secondary currents will be the same due to the same series circuit.
- Dual voltages are obtained delta-star connection. Low single phase voltages are obtained by wiring between any phase and ground. Higher single phase voltages are obtained by wiring between any two phases. And by connecting all three phases to the load, three phase voltage is obtained.
- The insulation requirement on high voltage side is lowered due to the star (less number of turns per phase) connected secondary.
- Similar to star-delta, this connection causes to create a 30 degrees phase difference between primary and secondary line voltages.
- By using this connection, it is not possible to connect it parallel with delta-delta and star-star transformers due to the primary and secondary voltage phase difference.

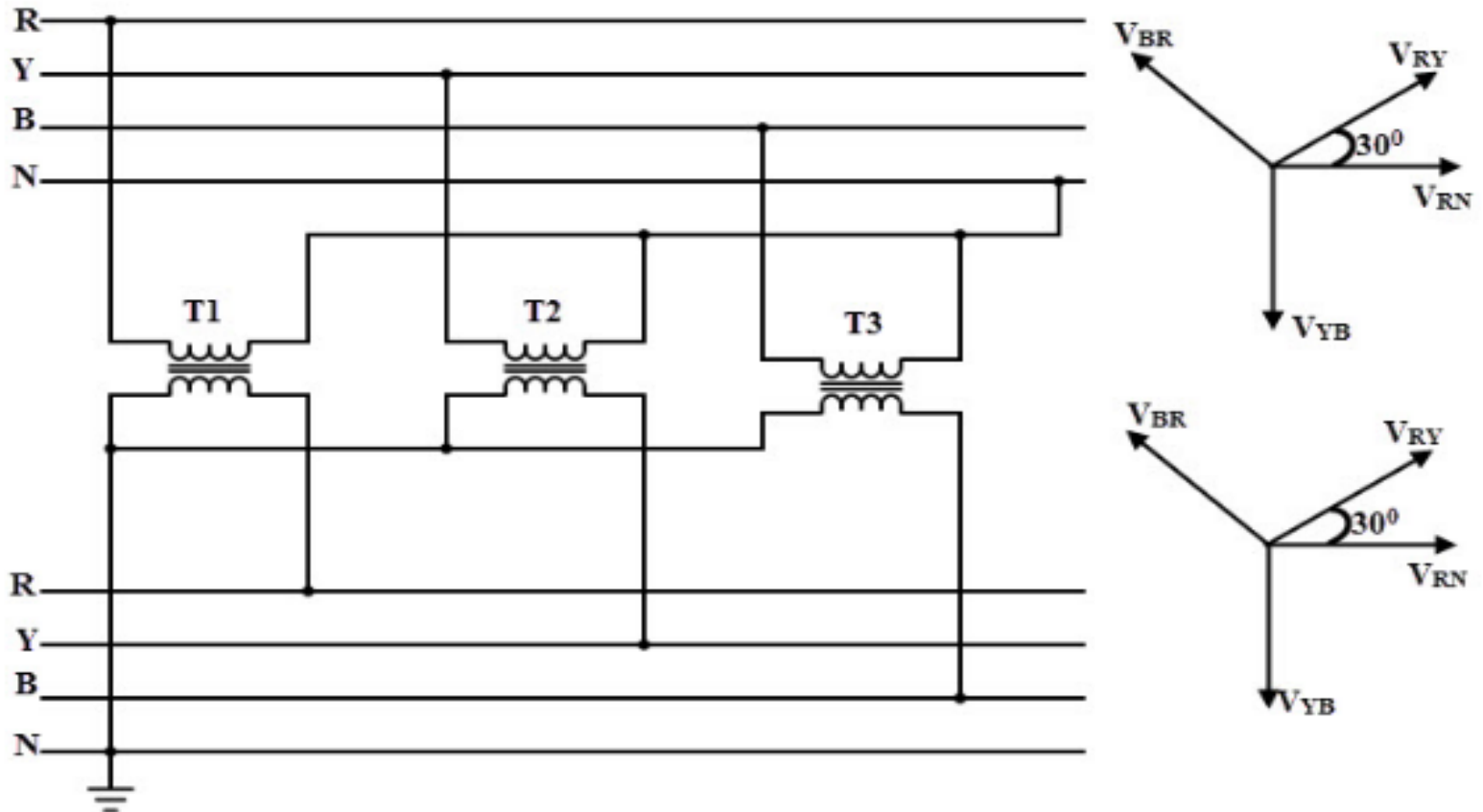
Delta-delta Connection




- This type of connection is used when the supply source is delta connected and the secondary load needs single voltage with high current. This is generally employed for three phase power loads (like three phase motor).
- In this, both primary and secondary windings are connected in delta fashion.

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- The voltage across the load is equal to the secondary voltage and voltage across the primary winding is equal to source voltage. In this, the current flow through the load will be 1.732 times the secondary current and the feeder current will equal to the 1.732 times current through the primary winding.
 - In this, there exists no phase difference between the primary and secondary voltages.
 - The main advantage of this connection is if the one transformer is defective or removed for service (open delta connection), then remaining two transformers continue to deliver three phase power at reduced load capacity.

Star-Star Connection



- In this, both primary and secondary windings are connected in star fashion and also there exist no phase difference between the primary and secondary voltages.

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- In this, current flowing through both primary and secondary windings are equal to the currents of the lines to which they are connected (supply source and load). And voltages between line phases on either end equal to 1.732 times respective winding voltages.
 - Due to neutral availability, it is well suited for three phase four wire system.
 - This connection considerably generates interference with communication lines and hence with this connection configuration, telephone lines cannot be run in parallel.
 - Star-Star connection is rarely used and not employed in practice.