

## HUBS & AUTHORITIES

HUBS :-

→ A HUB is a page with many out-links

→ The page serves as organizer of information about a particular topic and points to many good authority pages on the topic.

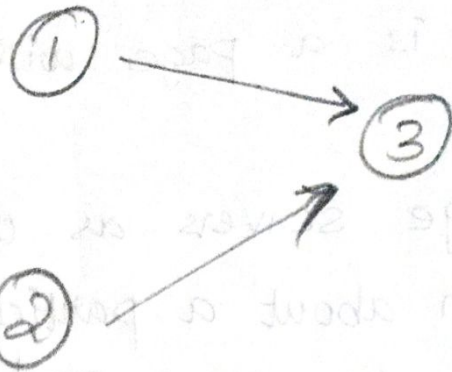
AUTHORITIES :-

→ Authority is a page with many in-links

→ The idea is that the page may have good or authoritative content on some topic and thus many people trust it and link to it.

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# HITS ALGORITHM:



Step 1:

Find the adjacency matrix of the graph.

(i.e.)

$$A = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$$

Step 2:

Find Matrix transpose

$$A^t = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix}$$



Assume the initial  
hub weight vector is  $u = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$

step: 3

Compute the authority weight vector

$$v = A^t \cdot u$$

$$v = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 1 & 0 \end{bmatrix} \cdot \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix}$$

step: 4

Then update hub weight:

(i, e)

$$u = A \cdot v$$

NOTE :- This is A  
not  $A^t$

$$u = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \\ 0 \end{bmatrix}$$

Results:-

Hub weights

$$\begin{bmatrix} 2 \\ 2 \\ 0 \end{bmatrix}$$

authority weights

$$\begin{bmatrix} 0 \\ 0 \\ 2 \end{bmatrix}$$

Node 1 is a hub since  $2 > 0$

Node 2 is a hub since  $2 > 0$

Node 3 is the Most authoritative since  $0 < 2$

