



BITS Pilani
Pilani Campus

MACHINE LEARNING WEBINAR-2

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Linear Regression

Agenda



- Introduction
- Machine Learning approach
- Python Libraries
- Linear Regression
- Demo

Overview

Machine Learning problem has

- Target/Dependent variable
- Predictor/Independent variables
- Historical data – target and predictor variables

Overview

Machine learning pipeline consists of:

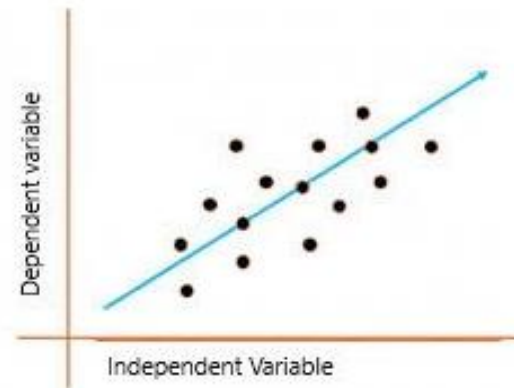
- Importing Data : csv, xls, json etc..
- Exploratory Data Analysis : Univariate and Multivariate
- Data Pre-processing
- Model building: Regression, Classification
- Model Evaluation

Python Libraries

- Pandas : Data Manipulations
- Numpy : Mathematical operations
- Scikit-learn : Scikit-learn is most popular for classical ML algorithms
- Matplotlib and Seaborn : Visualisations

Linear Regression

- Linear regression is a the simplest statistical regression method used for predictive analysis
- It shows the linear relationship between the independent(predictor) variable i.e. X-axis and the dependent(target) variable i.e. Y-axis
- Single input variable **X**(independent variable) : **Simple linear regression**



Linear Regression

To calculate best-fit line linear regression uses a linear equation :

$$Y = B_0 + B_1 * X$$

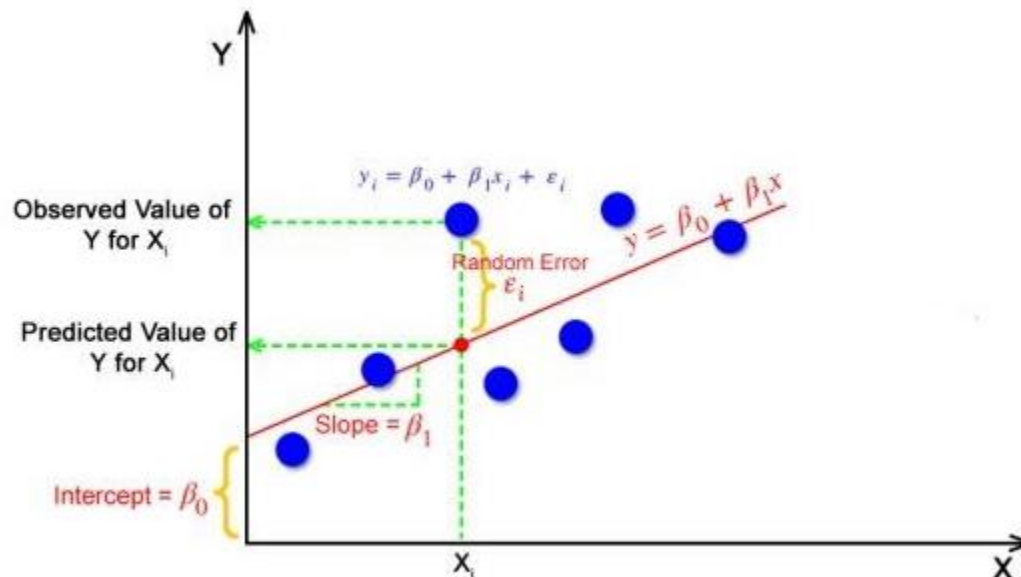
where Y = Dependent Variable

B_0 = intercept

B_1 = slope

X = Independent variable

To find best-fit line, get best values for B_0 , B_1



Cost Function : Linear regression

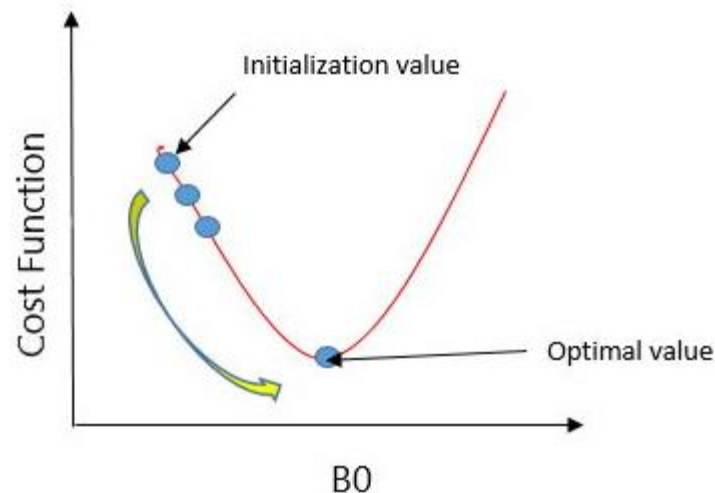
- Cost function helps to get the optimal values for B_0 and B_1
- Linear Regression, uses **Mean Squared Error (MSE)** cost function
 - average of squared error that occurred between the $\mathbf{y}_{\text{predicted}}$ and \mathbf{y}_i .
- We calculate MSE :

$$MSE = \frac{1}{N} \sum_{i=1}^n (y_i - (B_1 x_i + B_0))^2$$

- Values of B_0 and B_1 should be determined such that the MSE value settles at the minima
- This can be done using Gradient Descent method

Gradient Descent : Linear Regression

- Gradient Descent is an optimization algorithms that optimize the cost function to reach the optimal minimal solution
- Reduce the cost function(MSE) for all data points by updating the values of B_0 and B_1 iteratively until an optimal solution is obtained



Gradient Descent : Linear Regression

- To update B_0 and B_1 , we take gradients from the cost function
- To find these gradients, we take partial derivatives for B_0 and B_1 .

$$J = \frac{1}{n} \sum_{i=1}^n (B_0 + B_1 \cdot x_i - y_i)^2$$

$$\frac{\partial J}{\partial B_0} = \frac{2}{n} \sum_{i=1}^n (B_0 + B_1 \cdot x_i - y_i)$$

$$\frac{\partial J}{\partial B_1} = \frac{2}{n} \sum_{i=1}^n (B_0 + B_1 \cdot x_i - y_i) \cdot x_i$$

$$B_0 = B_0 - \alpha \cdot \frac{2}{n} \sum_{i=1}^n (pred_i - y_i)$$

$$B_1 = B_1 - \alpha \cdot \frac{2}{n} \sum_{i=1}^n (pred_i - y_i) \cdot x_i$$

Evaluation Metrics : Linear Regression

- Linear regression model can be assessed using various evaluation metrics
 - Root Mean Squared Error (RMSE)
specifies how close the observed data points are to the predicted values

$$RMSE = \sqrt{\frac{RSS}{n}} = \sqrt{\sum_{i=1}^n (y_i^{Actual} - y_i^{Predicted})^2 / n}$$

- Residual sum of Squares (RSS) is defined as the sum of squares of the residual for each data point