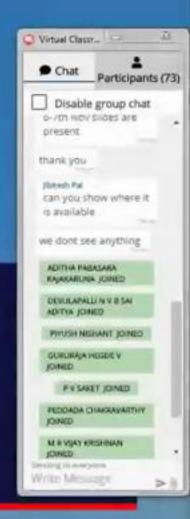






BITS Pilani

Mathematical Foundations for Data Science

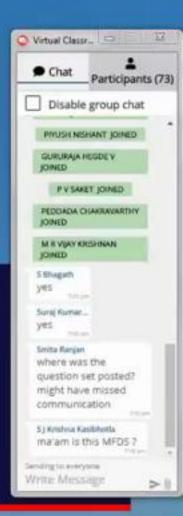






Mathematical Foundations for Data Science

BITS Pilani

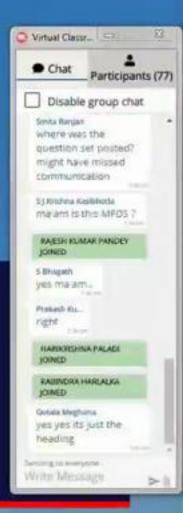






Mathematical Foundations for Data Science

BITS Pilani

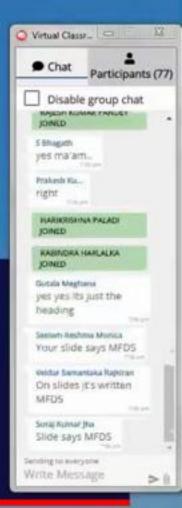






Mathematical Foundations for Data Science

Pilani Campus





The slide shows MFDS

Semiling musery soor

Write Musiage

INTRODUCTION TO STATISTICAL METHODS

WEBINAR 4:07.12.2021



Surat Komat...

Sampling or a warry pos-

Write Message

GALBIAY ANAND JOINED

INTRODUCTION TO STATISTICAL METHODS

WEBINAR 4:07.12.2021

- Random Variables
- Joint Distribution
- Family of Random Variables



- movemen
- Virtual Classr_
 - Chat Participants (82)

 Disable group chat
 - Siriq Kumar Jha Slide says MFDS

NEERAL SABHNANI JOINED

- Gunmeturan # The slide shows MFDS
- ***
- Suraj Kumar... yes
- GAURAY ANAND JOINED
- URELLA JAGADEESHWAR JOINED
- B CHEMANTH KUMAR JOINED SATHER KUMAR CV
- JOINED SUMAN CV
- DATTATRAYA UDAPIRAO KULKARNI JOINED
- MARISWARAN V JOINED
 ASHWIN RAY JOINED
- Sending to everyone
- Write Message

- Random Variables
- Joint Distribution
- Family of Random Variables

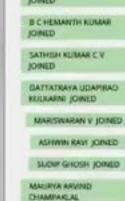
- mnovete
- O Virtual Classr
 - Disable group chat
 The side shows MFDS

 Sural Kumar...
 yes

 GAURAV ANAND JOINED

 ERILLA JAGADEESHWAR
 JOINED

- Random Variables
- Joint Distribution
- Family of Random Variables



SACHANADEVI JOINED

Write Message

- or consister.
- Virtual Classr_
 - Participants (85)
 - Suraj Kumar... Ves
 - URELLA JAGADEESHWAR

GAURAY ANAND JOINED

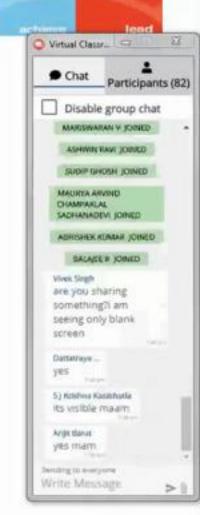
- B C HEMANTH KUMAR JONED
- SATHISH KUMAR CV KONED
- DATTATRAYA UDAPIRAO KUUKAKNI JOINED
- MARISWARAN V JOINED
 - ASHWIN RAVI JOINED
- SLOW GHOSH JOINED
- MADRYA ARVIND CHAMPAKLAL SADHANADEVI JONED
- AZHISHEK KUMAR JONED
- SALAREA JONED
- Write Message

- Random Variables
- Joint Distribution
- Family of Random Variables

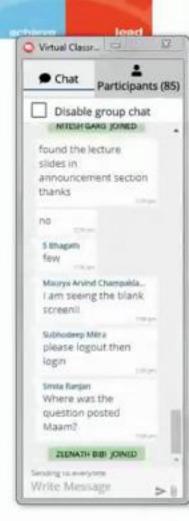
- Random Variables
- Joint Distribution
- Family of Random Variables



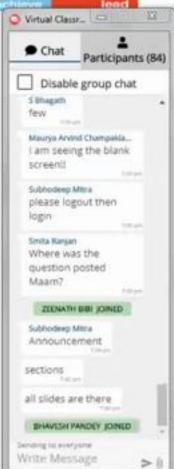
- Random Variables
- Joint Distribution
- Family of Random Variables



- Random Variables
- Joint Distribution
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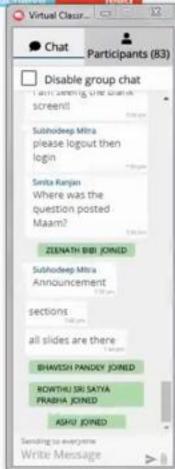


- Random Variables $f:S \to R$
- Joint Distribution
- Family of Random Variables

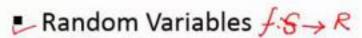




- Joint Distribution
- Family of Random Variables









- Joint Distribution
- Family of Random Variables





1. Check whether the following can serve as probability distributions:

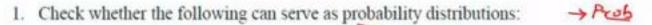
a.
$$f(x) = \frac{x-2}{2}$$
; $x=1,2,3,4$

b.
$$f(x) = \begin{cases} 2e^{-2x}; & x \ge 0 \\ 0 & \text{otherwise} \end{cases}$$



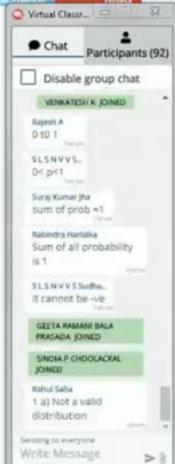
- Check whether the following can serve as probability distributions:
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- b. $f(x) = \begin{cases} 2e^{-2x}; & x \ge 0 \\ 0 & \text{otherwise} \end{cases}$





$$f(x) = \frac{x-2}{2}$$
; $x=1,2,3,4$

b
$$f(x) = \frac{x-2}{2}$$
; $x=1,2,3,4$
b $f(x) = \begin{cases} 2e^{-2x} : x \ge 0 \\ 0 & \text{otherwise} \end{cases}$





Check whether the following can serve as probability distributions: → Pcob

$$f(x) = \frac{x-2}{2}$$
; $x = 1,2,3,4$ Not valid Prob $x = 1$, $f(x) = -\frac{1}{2}$ (-ve)

$$f(x) = \begin{cases} 2e^{-2x}; & x \ge 0 \\ 0 & \text{otherwise} \end{cases}$$
1. $f(x) \ge 0$ for every $x \ge 0$

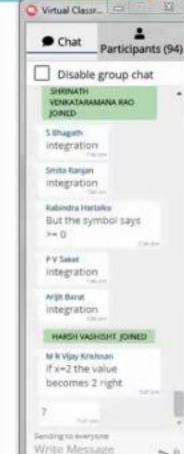
Ly Valid



Dismete - Sum Continuou - (



lead



- Check whether the following can serve as probability distributions: -> Prob
- $\int_{0}^{\infty} f(x) = \frac{x-2}{2}$; x=1,2,3,4 Not valid Prob x=1, $f(x)=-\frac{1}{2}$ (-ve)

f(x) > 0 for every

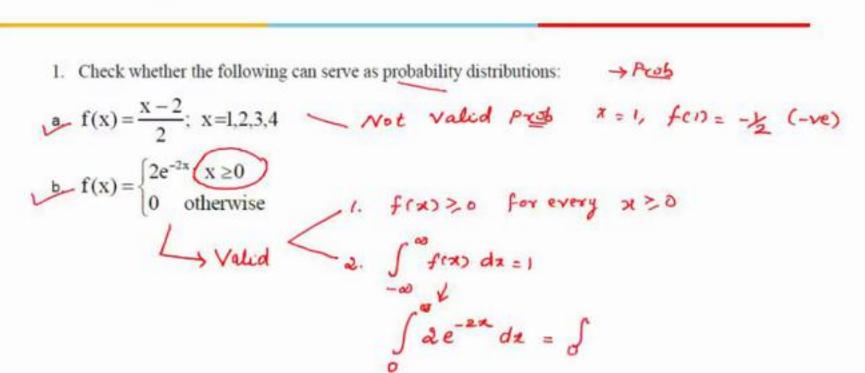
 $f(x) = \begin{cases} 2e^{-2x} & x \ge 0 \\ 0 & \text{otherwise} \end{cases}$

>11

Continuou - Sum



achtern lend





Dismete - Sum Continuou - (

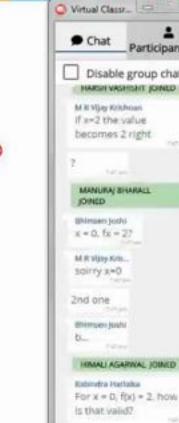




MANURA; BHARALL JOINED

Disable group chat HARSH VASHISHT JOINED

Participants (95)



 Check whether the following can serve as probability distributions: -> Prob

$$\int_{0}^{a} f(x) = \frac{x-2}{2}$$
; $x=1,2,3,4$ Not valid Prob $x=1$, $f(x)=-\frac{1}{2}$ (-ve)

$$f(x) = \begin{cases} 2e^{-2x} & x \ge 0 \\ 0 & \text{otherwise} \end{cases}$$

$$f(x) = \begin{cases} 2e^{-2x} & x \ge 0 \\ 0 & \text{otherwise} \end{cases}$$

$$f(x) \ge 0 \quad \text{for every}$$

$$\int \int de^{-2x} dz = \int de^{-3}$$

>1

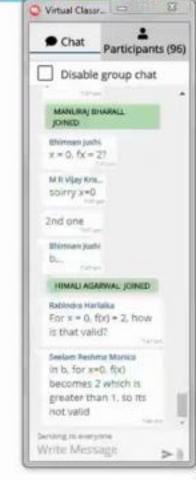
HIMALI ASARWAL JOINED

Sending to everyone Write Message

Continuou - Sum



lead

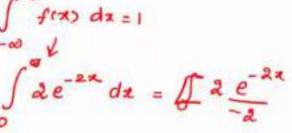


Check whether the following can serve as probability distributions: → Pcob

$$f(x) = \frac{x-2}{2}$$
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$$f(x) = \begin{cases} 2e^{-2x} & x \ge 0 \\ 0 & \text{otherwise} \end{cases}$$

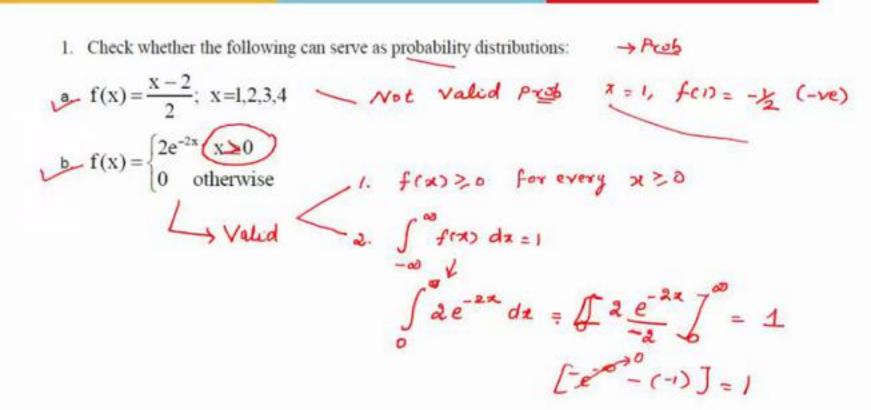
$$f(x) \ge 0 \quad \text{for every}$$



Continuou - Sum



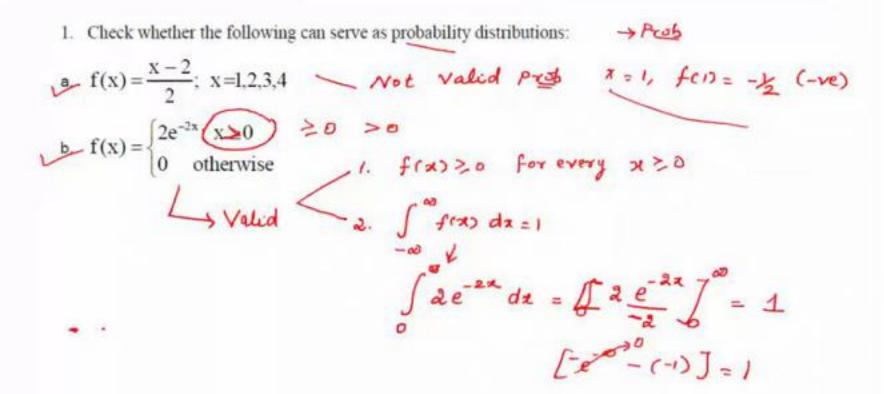
achieve lead

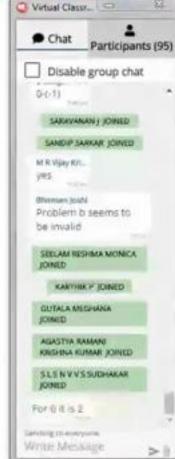




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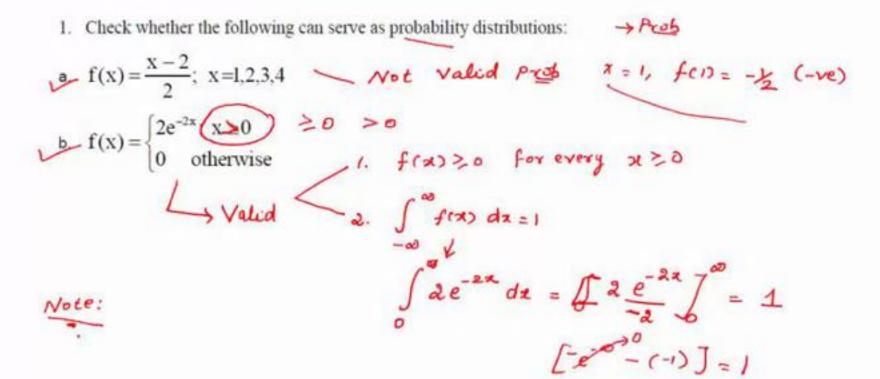


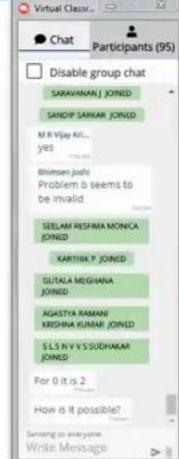


Continuou - Sum



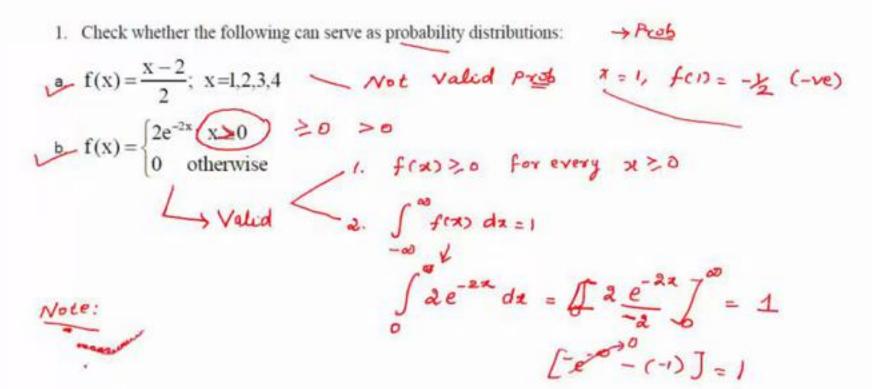
eve lend





Disrrete - Sum Continuou - S









2. A random variable X is having probability distribution function is given by

$$f(x) = \frac{e^{-k}k^x}{x!}$$
, x = 0,1,2,3...with k = 2

- a. Is it a valid distribution? Justify. If valid then find the following
- b. P(x > 2)
- c. $P(1 \le x \le 3)$





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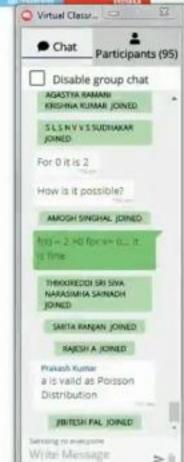




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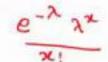
- a. Is it a valid distribution? Justify. If valid then find the following
- b. P(x > 2)
- c. P(1 < x < 3)





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$$f(x) = \frac{e^{-k}k^x}{x!}$$
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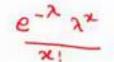
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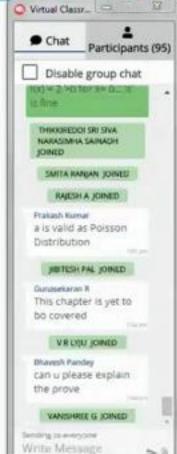
$$f(x) = \frac{e^{-k}k^x}{x!}$$
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a. Is it a valid distribution? Justify. If valid then find the following

- b. P(x > 2)
- c. P(1 < x < 3)

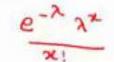
(i) frx) > 0
(ii) ge = 2 = e





2. A random variable X is having probability distribution function is given by

$$f(x) = \frac{e^{-k}k^x}{x!}$$
, $x = 0,1,2,3...$ with $k = 2$



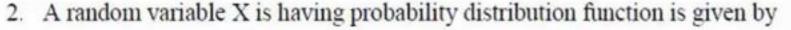
a. Is it a valid distribution? Justify. If valid then find the following

- b. P(x > 2)
- c. $P(1 \le x \le 3)$

(i) $\frac{g}{g} = \frac{g}{2} = \frac{g}{g} + \frac{g}{g}$

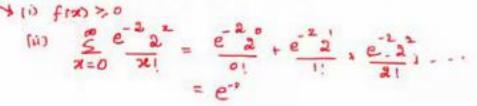






$$f(x) = \frac{e^{-k}k^x}{x!}$$
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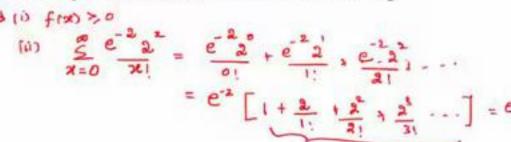




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$$f(x) = \frac{e^{-k}k^x}{x!}$$
, $x = 0,1,2,3...$ with $k = 2$

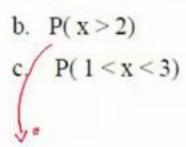
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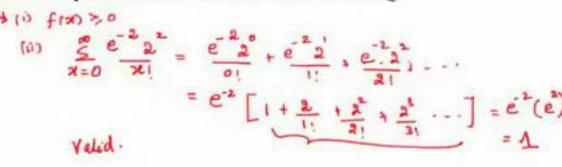


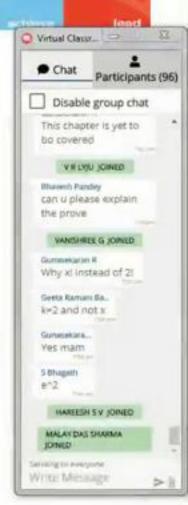




$$f(x) = \frac{e^{-k}k^x}{x!}$$
, $x = 0,1,2,3...$ with $k = 2$



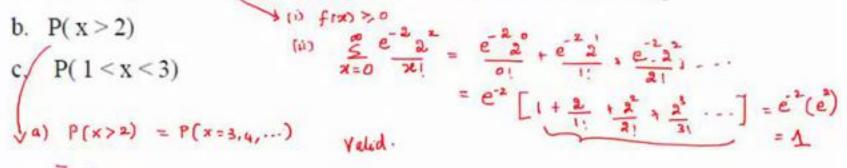






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$$f(x) = \frac{e^{-k}k^x}{x!}$$
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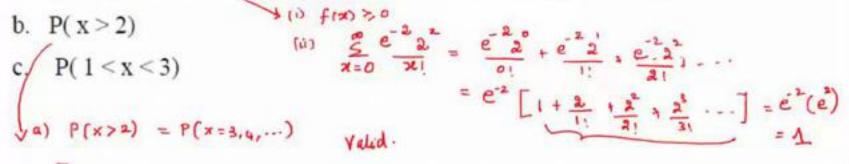


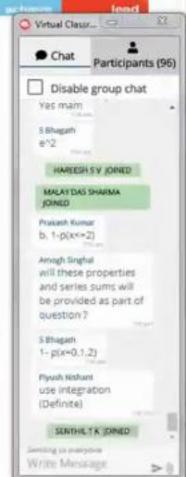




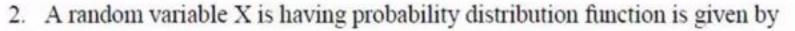


$$f(x) = \frac{e^{-k}k^x}{x!}, x = 0,1,2,3....$$
 with $k = 2$

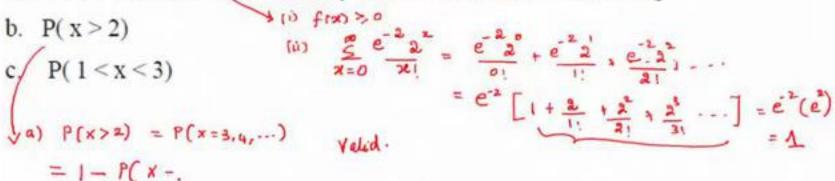


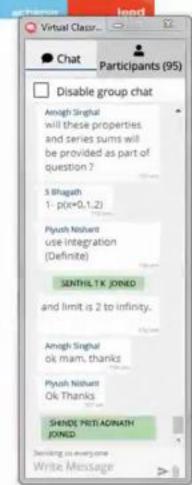






$$f(x) = \frac{e^{-k}k^x}{x!}, x = 0,1,2,3....$$
 with $k = 2$

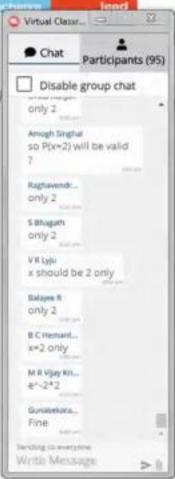


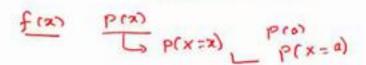


 An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows

$$P(a) = \begin{cases} 0 & x = 1 \\ 50 & 1 \le x \le 3 \\ 40 & 2 \le x \le 4 \\ 46 & 4 \le a = 6 \\ 50 & 0 \le x \le 12 \\ 1 & 12 \le x \end{cases}$$

- a. What is the PMF of X?
- b. Compute P(3≤ X ≤6)
- c. Obtain E(x) and Variance of X.



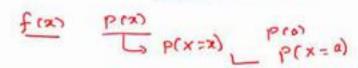


 An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows

$$F(x) = \begin{cases} 0 & x < 1 \\ .30 & 1 \le x < 3 \\ .40 & 3 \le x < 4 \\ .45 & 4 \le x < 6 \\ .60 & 6 \le x < 12 \\ 1 & 12 \le x \end{cases}$$

- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.





3. An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows
F(x) = P[x ≤ x]

$$F(x) = \begin{cases} 0 & x < 1 \\ 30 & 1 \le x < 3 \\ 40 & 3 \le x < 4 \\ 45 & 4 \le x < 6 \\ 60 & 6 \le x < 12 \\ 1 & 12 \le x \end{cases}$$

- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.

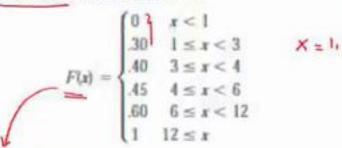
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PM F - discrete
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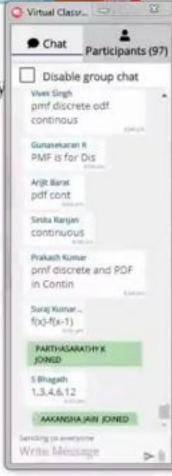
f(x) P(x=x) P(x=a)

cumulative + till

3. An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows
\[
\begin{align*}
\text{F(x)} = P[x \leq x]
\end{align*}
\]

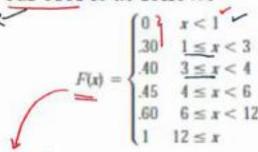


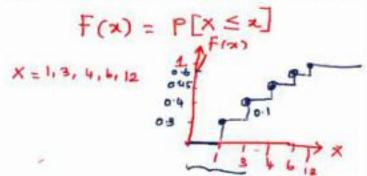
- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.



f(x) P(x=x) P(x=a)

3. An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows
F(x) = P[x ≤ x]



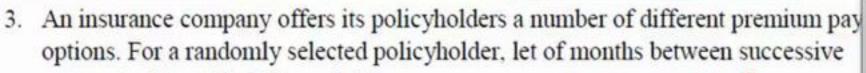


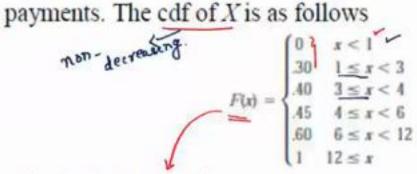
- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.

PMF - Continuous

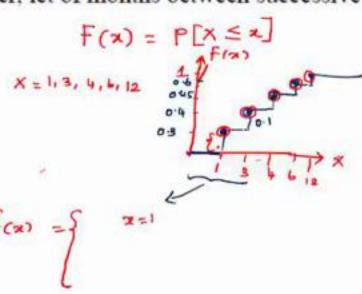


f(x) P(x=x) P(x=a)





- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.



O Virtual Classr_

Projects Woman

in Contin

Soraj Kumar... f(x)-f(x-1)

5 Bhagath 1.3,4,6,12

Disable group chat

omf discrete and PDF

SALKUMAR K.C. (DINED

RAKESH'T JOINED

HAJASEKAR O JOINED

DASADINA VEINVOEEP

SWAPNA KJOSEPH

0.3

Senang to everyone Writte Message

Participants (95)

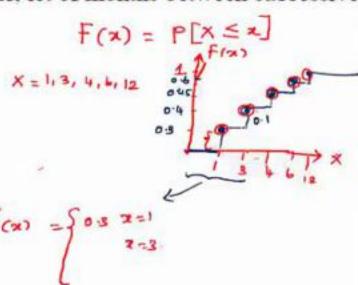
Chat

f(x) P(x=x) P(x=a)

3. An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows $F(x) = P[x \le x]$

$$F(x) = \begin{cases} 0 & x < 1 \\ 30 & 1 \le x < 3 \\ 40 & 3 \le x < 4 \\ 45 & 4 \le x < 6 \\ 60 & 6 \le x < 12 \\ 1 & 12 \le x \end{cases}$$

- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.



O Virtual Classr.

Disable group chat

Participants (95)

Chat

in Contin

5.8hagath 1.3.4,6.12

Surjej Kumar... f(x3-f(x-1)

PARTHASARATHY K

SALKERMAR'S C JOINES

MANISHBHAL JOINED

HAIASEKAR D KOINED

SWAPNA K JOSEPH

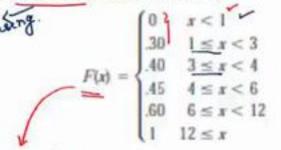
0.3

0.1

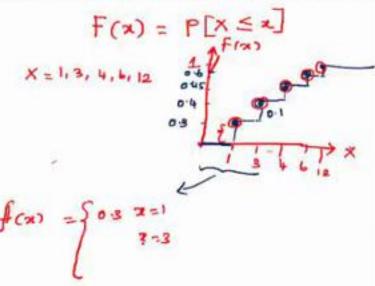
Write Message

f(x) P(x=x) P(x=a)

 An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows



- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.



O Virtual Classr.

Participants (94)

Disable group chat

Chat

f0x(-f0x-T)

58hagath 1.3.4.6.12

PARTHALAHATHY K

RAKESH T JOINED

RAJASEKAR D JOINED

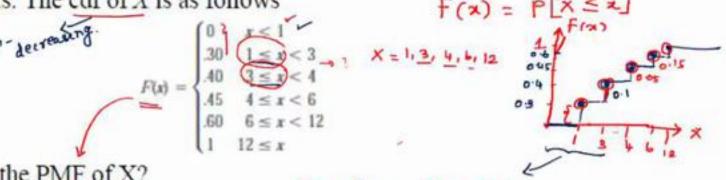
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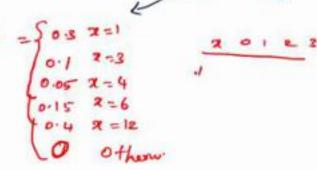
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x=2, or cumulative till f(x) p(x) p(x=a) p(x=a)

3. An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows
F(x) = P[x ≤ x]



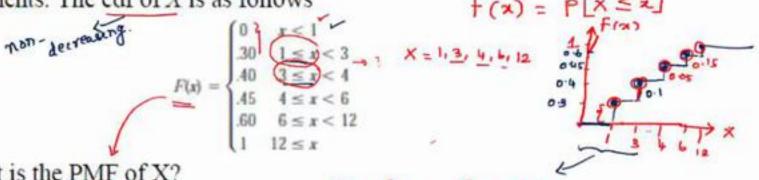
- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.



X - 2 , 0 fix

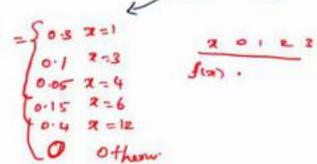
cumulative + till

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- a. What is the PMF of X?
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- 0.3

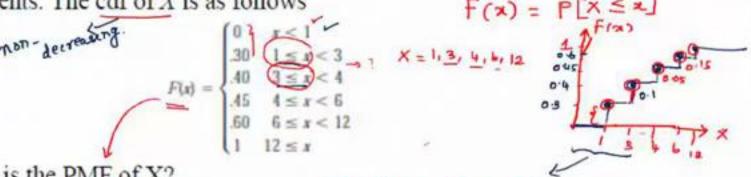


f(x) P(x=x) P(x=a)

cumulative - till

3. An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows
F(x) = P[x ≤ x]

X = 2 , 0



- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
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P[x = 3, 4, b] = 0.1+0.05+0.1

- 0.3

= 503 7=1 0.1 7=3 0.05 7=4 0.15 2=6 0.4 7=12

2 = 12

1 - 1 2 3 1 - 1 2 3 1(x) 0.10.40 0.5 F(x) 0.105051

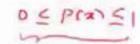
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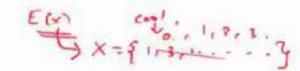
 An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows

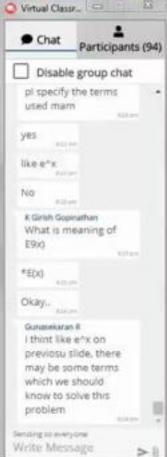
$$F(x) = \begin{cases} 0 & x < 1 \\ .30 & 1 \le x < 3 \\ .40 & 3 \le x < 4 \\ .45 & 4 \le x < 6 \\ .60 & 6 \le x < 12 \\ 1 & 12 \le x \end{cases}$$

- a. What is the PMF of X?
- b. Compute $P(3 \le X \le 6)$
- c. Obtain E(x) and Variance of X.









An insurance company offers its policyholders a number of different premium pay options. For a randomly selected policyholder, let of months between successive payments. The cdf of X is as follows

$$F(x) = \begin{cases} 0 & x < 1 \\ 30 & 1 \le x < 3 \\ 40 & 3 \le x < 4 \end{cases} \qquad P(x) \quad 0 \cdot 3 \quad 0 \cdot 1 \quad 0 \cdot 05 \quad 0 \cdot 15 \quad 0 \cdot 9 \\ 45 & 4 \le x < 6 \\ 60 & 6 \le x < 12 \\ 1 & 12 \le x \end{cases} \qquad x \quad P(x) \quad 0 \cdot 3 \quad 0 \cdot 3 \quad 0 \cdot 3 \quad 0 \cdot 3 \quad 0 \cdot 4 \quad 0 \cdot 9 \quad 4 \cdot 8$$

- a. What is the PMF of X?
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- c. Obtain E(x) and Variance of X.

Participants (94)

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Chat

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Okay...

Gunanekaran R I thint like e'x on previosu slide, there may be some terms. which we should know to solve this

problem Sensing to everyone Write Message

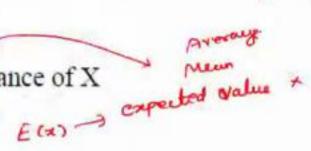
K Girish Goolnathan

What is meaning of

Cupumon 0 < 3 < 0

4. Let X denote the temperature at which a certain chemical reaction takes place that X has pdf con tinuous

$$\alpha = \begin{cases} \frac{1}{9}(4-x^2) & -1 \le x \le 2 \end{cases}$$







Obtain E(x) and Variance of X J' P(OCXCI)

$$= \frac{1}{4} \left[\frac{42 - \frac{2^{3}}{3}}{2} \right]_{0} = \frac{11}{27}$$

$$= \frac{1}{4} \left[\frac{42 - \frac{2^{3}}{3}}{2} \right]_{0} = \frac{11}{27}$$

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5. A service station has both self-service and full-service islands. On each island, there is a single regular unleaded pump with two hoses. Let X denote the number of hoses being used on the self-service island at a particular time and let Y denote the number of hoses on the full-service island in use at that time. The joint probability mass function of X and Y

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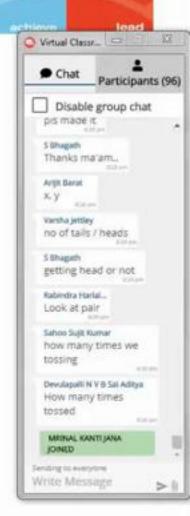
v	Y					
Λ	0	1	2			
0	0.10	0.04	0.02			
1	0.08	0.20	0.06			
2	0.06	0.14	0.30			

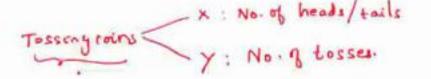
- a. Find the marginal probability mass function of X and Y
- b. Give the verbal description the event (X≠0 and Y≠0) and compute the probability of this
 event.
- c. Find P(X=1|Y=2) and P(Y=2|X=1)



v		Y					
Λ	0	1	2				
0	0.10	0.04	0.02				
1	0.08	0.20	0.06				
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- a. Find the marginal probability mass function of X and Y
- b. Give the verbal description the event (X≠0 and Y≠0) and compute the probability of this event.
- c. Find P(X=1/Y=2) and P(Y=2|X=1)





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v	Y					
-7	0	1	2			
0	0.10	0.04	0.02			
1	0.08	0.20	0.06			
2	0.06	0.14	0.30			

- Find the marginal probability mass function of X and Y
- b. Give the verbal description the event (X≠0 and Y≠0) and compute the probability of this event.
- c. Find P(X=1|Y=2) and P(Y=2|X=1)



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-		

9=2

	-v		Y			fx 127: 50.16 7 = 0
	A	0	1.	2	fx(x)	0.30 ME
5	0->	0.10	0.04	0.02	0.16	0.5 7.2 0 other
1	1	0.08	0.20	0.06	0.34	The state of the s
	2 fy(y)	0.06	0.14	0.30	0.5	fy 190 - Soize y=

Morganel PMF

9	Find the margina	probability mass	function of X and Y
ce.	I the the morethe	a probability mass	runction of a ging t

- Give the verbal description the event $(X\neq 0 \text{ and } Y\neq 0)$ and compute the probability of this event.
- Find P(X=1|Y=2) and P(Y=2|X=1)



$$P(x \neq 0 \text{ and } y \neq 0)$$
 $\Rightarrow P(A/B) = \frac{P(A \cap B)}{P(B)}$

Marceral DMT

P[x to and y to)	> P(A/B)=	P(B)
= 1- P(x=0 or y=0)		

					1.1 64 Acres	
	- v		Y			fx 127: 50.16 x = 0
		0	1	2	£x(x)	0.30 00=1
5	0->	0.10	0.04	0.02	0.16	0 5 7 - 2 0 other
1	1 -	0.08	0.20	0.06	0.34	
	fycu)	0.06	0.14	0.30	0.5	5y 150= 8 0.24 5= 0.38 4= 1
prob	ability ma	iss functi	on of X ar	ad Y		0'3P Y=
SCIII	tion the e	vent (X=	0 and Y = 0	() and cor	inpute the probability of this	y=1

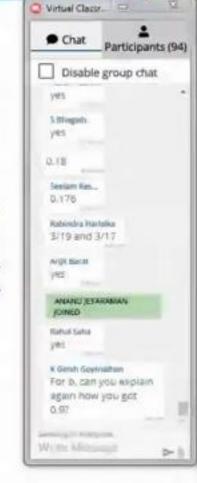
- Find the marginal
- Give the verbal description the event $(X\neq 0)$ and $Y\neq 0$ and compute the probability of this X=1.2
- Find P(X=1|Y=2) and P(Y=2|X=1)

event.

Find P(X=1|Y=2) and P(Y=2|X=1)

$$P(x = 1/y = 2) = \frac{P(x=1, Y=2)}{P(x=1, Y=2)} = \frac{0.06}{0.38} = 0.157 \approx 0.16$$

$$P(Y=2/x=1) = \frac{P(x=1, Y=2)}{P(x=1)} = \frac{0.06}{0.39} = 0.18$$



Midsem.

Consider the following Joint distribution of two random variables X and

X \ Y	1	2	3	4	5	
1 P(X)	0	0	2k	4k	4k	- 3
2	4k	4k	8k	8k	8k	
3	2k	2k	K	- k	0	
teres		1.	11.6	154	12 k	,

For what value(s) of k it is a valid distribution : 64 k = 1

Find Marginal Distribution of X and Y



c. Find $P(X \le 2)$

d. Find $P(X \le 2/Y = 2)$

e. Find $P(X \le 3/Y \le 2)$

























Write Message

>1



Consider the following Joint distribution of two random variables X and

X \ Y	1	2	3	4	5	6	fre
1 P(K)	0	0	2k	4k	4k	6k	16 K
2	4k	4k	8k	8k	8k	8k	40 K
3	2k	2k	k	- k	0	2k	8 k
1 y (2)	6K	6k	IIk	13k	12k	16k.	164K

c. Find $P(X \le 2)$

d. Find $P(X \le 2/Y = 2)$

e. Find $P(X \le 3/Y \le 2)$

For what value(s) of k it is a valid distribution : 64 k =)

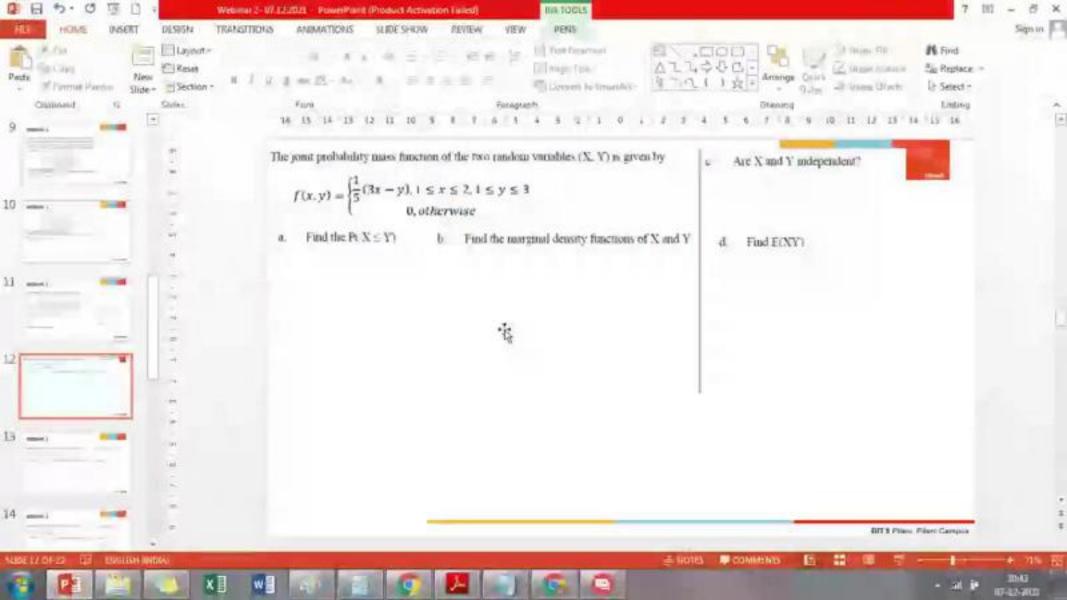
Find Marginal Distribution of X and Y

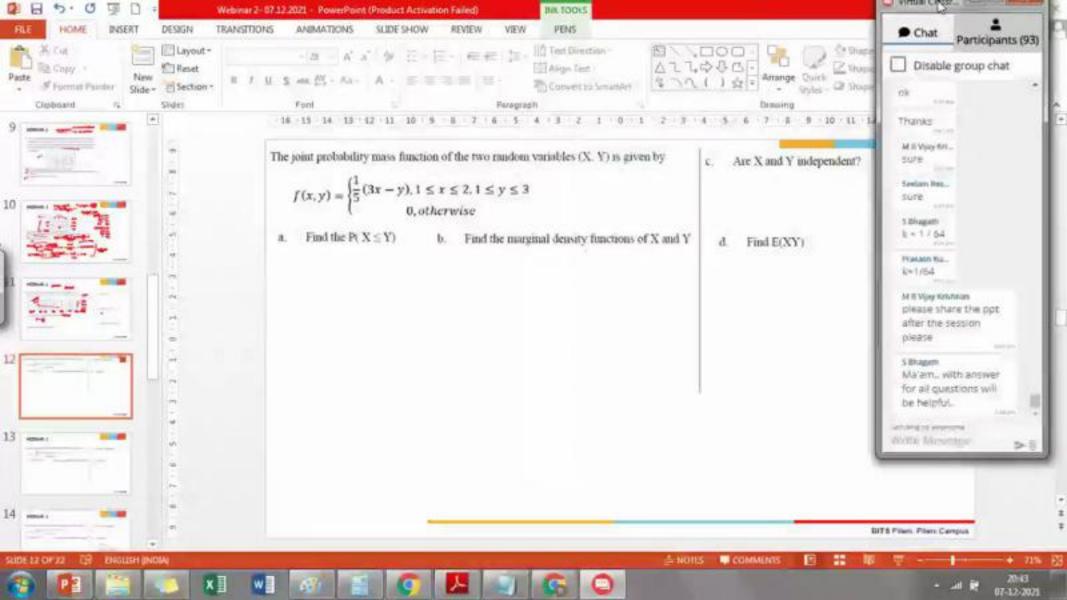
The joint probability mass function of the two random variables (X, Y) is given by

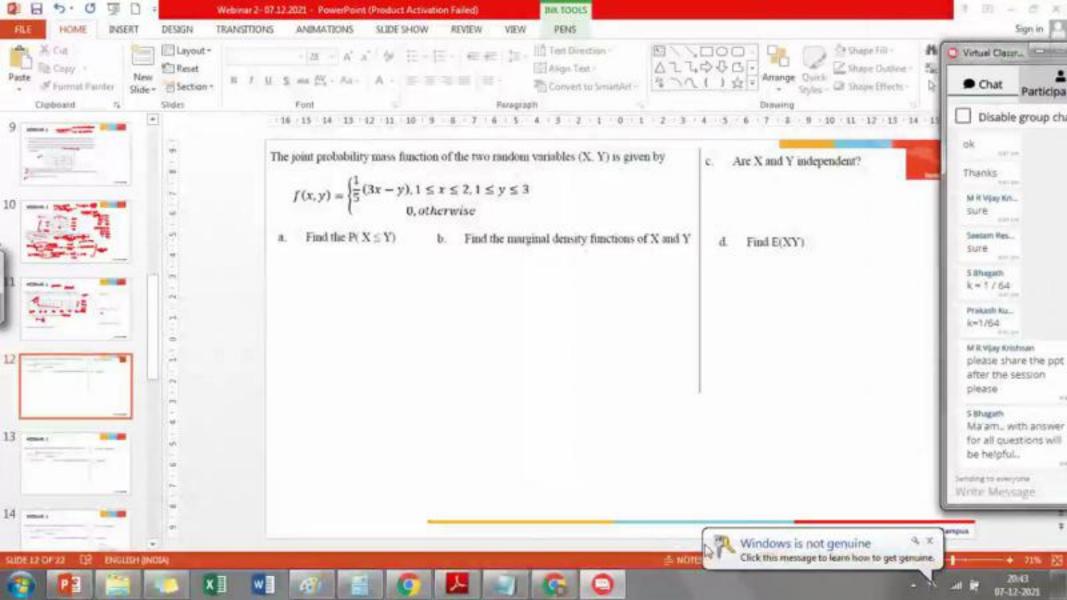
$$f(x,y) = \begin{cases} \frac{1}{5}(3x - y), 1 \le x \le 2, 1 \le y \le 3\\ 0, otherwise \end{cases}$$

- a. Find the $P(X \le Y)$
- b. Find the marginal density functions of X and Y
- d. Find E(XY)

Are X and Y independent?







The joint probability mass function of the two random variables (X, Y) is given by

$$f(x,y) = \begin{cases} \frac{1}{5}(3x - y), 1 \le x \le 2, 1 \le y \le 3\\ 0, otherwise \end{cases}$$

- a. Find the P($X \le Y$)
- Find the marginal density functions of X and Y

c. Are X and Y independent?

d. Find E(XY)



Midsem.

Consider the following Joint distribution of two random variables X and

X\Y	1	2	3	4	5	6	face
1 1/4	0	0	2k	4k	4k	6k	14K
2	4k	4k	8k	8k	8k	8k	40 K
3	2k	2k	k	- k	0	2k	8 k
{ y(2)	6K	6E	Hk	13k	12k	16k. 1	64 K

For what value(s) of k it is a valid distribution : 64 k =)

Find Marginal Distribution of X and Y

c. Find $P(X \le 2)$

d. Find $P(X \le 2/Y = 2)$

e. Find $P(X \le 3/Y \le 2)$

O Virtual Classr... Chat Disable group ch Thanks. M IE Vijay Kirk... Stitle. Seekam Res. sure 5 thugath k+1/64 Protesth ku... k=1/64 M R Vijay Krishnan please share the ppt after the session piease 5 Shagath Ma'am, with answer for all questions will be helpful... Senting to everyone Write Measure

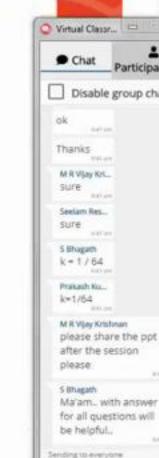
The joint probability mass function of the two random variables (X, Y) is given by

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- Find the P($X \le Y$)
- Find the marginal density functions of X and Y b.

Are X and Y independent?

Find E(XY)



Participa

Add on

Write Message

The joint probability mass function of the two random variables (X, Y) is given by

$$f(x,y) = \begin{cases} \frac{1}{5}(3x - y), 1 \le x \le 2, 1 \le y \le 3\\ 0, otherwise \end{cases}$$

- Find the P(X≤Y)
- b. Find the marginal density functions of X and Y

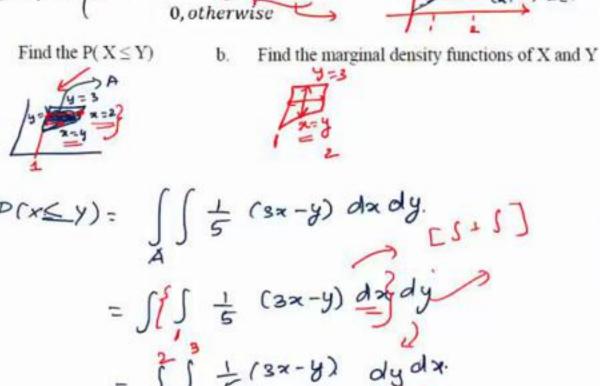
c. Are X and Y independent?

Find E(XY)



The joint probability mass function of the two random variables (X, Y) is given by

Find the P($X \le Y$)



Are X and Y independent?

Find E(XY)



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CONTRACTOR OF PARTY OF THE PART

The joint probability mass function of the two random variables (X. Y) is given by

$$f(x,y) = \begin{cases} \frac{1}{5}(3x - y), 1 \le x \le 2, 1 \le y \le 3\\ 0, otherwise \end{cases}$$

- Find the P(X≤Y)
- b. Find the marginal density functions of X and Y

c. Are X and Y independent?

Find E(XY)



It has been claimed that in 60% of all solar-heat installations the utility bill is reduced by at least one-third. Accordingly, what are the probabilities that the utility bill will be reduced by at least one-third in

- four of five installations:
- b. at least four of five installations
- atmost four of five installations?

Solution (a) Substituting x = 4, n = 5, and p = 0.60 into the formula for the binomial distribution, we get

$$b(4; 5, 0.60) = {5 \choose 4} (0.60)^3 (1 - 0.60)^{5-4}$$

= 0.259

(b) Substituting x = 5, u = 5 and p = 0.60 into the formula for the binomial distribution, we get

$$b(5; 5, 0.60) = {5 \choose 5} (0.60)^5 (1 - 0.60)^{5-5}$$

= 0.078

and the answer is b(4; 5, 0.60) + b(5; 5, 0.60) = 0.259 + 0.078 = 0.337



For health reasons, homes need to be inspected for radon gas which decays and produces alpha particles. One device counts the number of alpha particles that hit its detector. To a good approximation, in one area, the count for the next week follows a Poisson distribution with mean 1.3. Determine

- the probability of exactly one particle next week.
- the probability of one or more particles next week.
- the probability of at least two but no more than four particles next week.

Solution

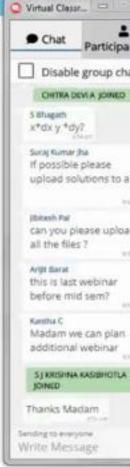
Unlike the binomial case, there is no choice of a fixed Bernoulli trial here because one can always work with smaller intervals.

(a)
$$P(\hat{X} = 1) = \frac{\lambda^{1} e^{-\lambda}}{1!} = \frac{1.3 e^{-1.3}}{1} = .3543$$

Alternatively, using Table 2W, F(1, 1.3) - F(0, 1.3) = 0.627 - 0.273 = 0.354

(b)
$$P(X \ge 1) = 1 - P(X = 0) = 1 - e^{-1.3} = 0.727$$

(c)
$$P(2 \le X \le 4) = F(4, 13) - F(1, 13) = 0.989 - 0.627 = 0.362$$



Virtual Classe...

Thanks

A computing system manager states that the rate of interruptions to the internet service is 0.2 per week. Use the Poisson distribution to find the probability of

- a. one intentiption in 3 weeks
- at least two interruptions in 5 weeks
- at most one interruption in 15 weeks.

Solution

Interruptions to the network occur randomly and the coaditions for the Poisson disinbutton initially appear reasonable. We have $\lambda \approx 0.2$ for the expected number of intecruptions in one week.

in terms of the cumulative probabilities,

(a) with
$$\lambda = (0, 2) \cdot 3 = 0.6$$
, we get

$$F(1; 0.6) - F(0; 0.6) = 0.878 - 0.549$$

= 0.329

(b) With
$$\lambda = (0.2) \cdot 5 = 1.0$$
, we get

$$1 - F(1, 10) = 1 - 0.736$$

= 0.264

(c) With
$$\lambda = (0.2) \cdot 15 = 3.0$$
 we get

$$F(1,3,0) = 0.199$$

The Poisson Approximation to the Binomial Distribution:

- 11. It is known that 5% of the books bound at a certain bindery have defective bindings. Find the probability that 2 of 100 books bound by this bindery will have defective bindings using
 - a. the formula for the binomial distribution;
 - the Poisson approximation to the binomial distribution

Solution

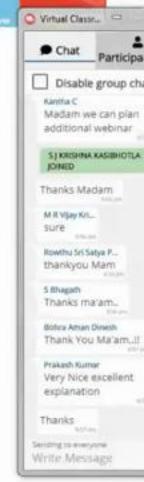
(a) Substituting x = 2, n = 100, and p = 0.05 into the formula for the binomial distribution, we get

$$b(2; 100, 0.05) = {100 \choose 2} (0.05)^2 (0.95)^{98} = 0.081$$

(b) Substituting x = 2 and λ = 100(0.05) = 5 into the formula for the Poisson distribution, we get

$$f(2;5) = \frac{5^2 \cdot e^{-5}}{2!} = 0.084$$

It is of interest to note that the difference between the two values we obtained (the error we would make by using the Poisson approximation) is only 0.003. [Had we used Table 2W instead of using a calculator to obtain e^{-5} , we would have obtained f(2; 5) = F(2; 5) - F(1; 5) = 0.125 - 0.040 = 0.085.]



Let X, the grade of a randomly selected student in a test of a ISM course, be a norn random variable. A professor is said to grade such a test on the curve if he finds the avera μ and the standard deviation σ of the grades and then assigns letter grades according to t following table.

Ratige of the grade	$X \ge \mu + \sigma$	$\mu \le X < \mu + \sigma$	$\mu - \sigma \le X < \mu$	$\mu - 2\sigma \le X < \mu - \sigma$	$X < \mu - 2\sigma$
Letter grade	Α	В	С	D	F

Suppose that the professor of the probability course grades the test on the curve. Determine the percentage of the students who will get A. B. C. D. and F. respectively.



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WEBINAR 2

Let X, the grade of a randomly selected student in a test of a ISM course, be a norn random variable. A professor is said to grade such a test on the curve if he finds the avera μ and the standard deviation σ of the grades and then assigns letter grades according to t following table.

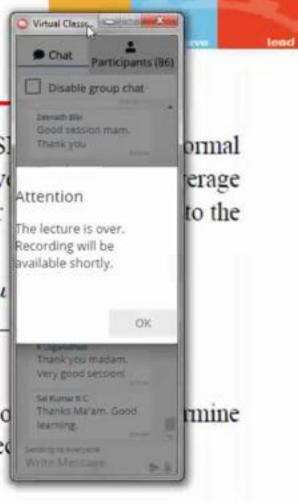
Range of the grade	$X \ge \mu + \sigma$	$\mu \leq X < \mu + \sigma$	$\mu - \sigma \leq X < \mu$	$\mu - 2\sigma \le X < \mu - \sigma$	$X < \mu - 2\sigma$
Letter grade	Α	В	С	D	F

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Letter	Α	В	С	D

Suppose that the professor of the probability course grades the test of the percentage of the students who will get A, B, C, D, and F, respec





























Range of the grade	$X \ge \mu + \sigma$	$\mu \leq X < \mu + \sigma$	$\mu - \sigma \leq X < \mu$	$\mu - 2\sigma \le X < \mu - \sigma$	$X < \mu - 2\sigma$
Letter grade	Α	В	С	D	F

Suppose that the professor of the probability course grades the test on the curve. Determine the percentage of the students who will get A, B, C, D, and F, respectively.

