



A. 单选题 3

fn 函数题 1

2-1 Rod-cutting Problem: Given a rod of total length  $N$  inches and a table of selling prices  $P_L$  for lengths  $L = 1, 2, \dots, M$ . You are asked to find the maximum revenue  $R_N$  obtainable by cutting up the rod and selling the pieces. For example, based on the following table of prices, if we are to sell an 8-inch rod, the optimal solution is to cut it into two pieces of lengths 2 and 6, which produces revenue  $R_8 = P_2 + P_6 = 5 + 17 = 22$ . And if we are to sell a 3-inch rod, the best way is not to cut it at all.

Length $L$	1	2	3	4	5	6	7	8	9	10
Price $P_L$	1	5	8	9	10	17	17	20	23	28

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Which one of the following statements is FALSE? (2分)

- ☐ A. This problem can be solved by dynamic programming
- ☐ B. The time complexity of this algorithm is  $O(N^2)$
- ☐ C. If  $N \leq M$ , we have  $R_N = \max\{P_N, \max_{1 \leq i < N}\{R_i + R_{N-i}\}\}$
- ☒ D. If  $N > M$ , we have  $R_N = \max_{1 \leq i < N}\{R_i + R_{N-M}\}$

2-1 答案正确 (2 分) 创建提问

2-2 In dynamic programming, we derive a recurrence relation for the solution to one subproblem in terms of solutions to other subproblems. To turn this relation into a bottom up dynamic programming algorithm, we need an order to fill in the solution cells in a table, such that all needed subproblems are solved before solving a subproblem. Among the following relations, which one is impossible to be computed? (2分)

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- ☐ A.  $A(i, j) = \min(A(i - 1, j), A(i, j - 1), A(i - 1, j - 1))$
- ☐ B.  $A(i, j) = F(A(\min\{i, j\} - 1, \min\{i, j\} - 1), A(\max\{i, j\} - 1, \max\{i, j\} - 1))$
- ☐ C.  $A(i, j) = F(A(i, j - 1), A(i - 1, j - 1), A(i - 1, j + 1))$
- ☒ D.  $A(i, j) = F(A(i - 2, j - 2), A(i + 2, j + 2))$

2-2 答案正确 (2 分) 创建提问

2-3 Given a recurrence equation  $f_{i,j,k} = f_{i,j+1,k} + \min_{0 \leq l \leq k}\{f_{i-1,j,l} + w_{j,l}\}$ . To solve this equation in an iterative way, we cannot fill up a table as follows: (2分)

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- ☐ A. `for k in 0 to n: for i in 0 to n: for j in n to 0`
- ☒ B. `for i in 0 to n: for j in 0 to n: for k in 0 to n`
- ☐ C. `for i in 0 to n: for j in n to 0: for k in n to 0`
- ☐ D. `for i in 0 to n: for j in n to 0: for k in 0 to n`

2-3 答案正确 (2 分) 创建提问