

$$I. \{ \emptyset, \{a\}, \{a, a\} \} = P_{\{a, \{a\}\}}$$

$$II. \{ \emptyset, \{a\}, \{a, a\}, \{ \emptyset, a, \{a\} \} \} = P_{\{ \emptyset, a, \{a\} \}}$$

$$III. P_{\{1, 2, 3, 4\}} = \{ \emptyset, \{1\}, \{2\}, \{3\}, \{4\}, \{1, 2\}, \{1, 3\}, \{1, 4\}, \{2, 3\}, \{2, 4\}, \{3, 4\}, \{1, 2, 3\}, \{1, 2, 4\}, \{1, 3, 4\}, \{2, 3, 4\} \}$$

$$II. A \times B = \{ \langle 0, 1 \rangle, \langle 1, 2 \rangle, \langle 0, 2 \rangle, \langle 1, 1 \rangle \}$$

$$A^2 \times B = \{ \langle 0, 0, 1 \rangle, \langle 0, 1, 1 \rangle, \langle 1, 0, 1 \rangle, \langle 0, 0, 2 \rangle, \langle 0, 1, 2 \rangle, \langle 1, 0, 2 \rangle, \langle 1, 1, 2 \rangle \}$$

$$B \times A = \{ \langle 1, 0 \rangle, \langle 1, 1 \rangle, \langle 2, 0 \rangle, \langle 2, 1 \rangle \}$$

III. 1. II: 中正确 B 中包含 {A} 元素. 且为 C 的子集, 故 $A \in C$.
 2. (4): 3. 正确 B 为 A 的子集, B 为 C 中的一个元素. $\therefore A$ 为 C 中的一个元素.

$$IV. \text{中 } A \cap (B - C) \Rightarrow \{x \mid x \in A \cap (x \in B \cap x \notin C)\} \Rightarrow \{x \mid (x \in A \cap x \in B) \cap (x \in A \cap x \notin C)\}$$

$$\Rightarrow (A \cap B) - (A \cap C)$$

$\therefore A$ 正确.

$\therefore QED$

$$V. (A - B) - C = A - (B \cup C).$$

$$(A - B) - C \equiv A - B \cap C \equiv A - B \cup C \equiv A \cap \overline{B} \cup C \equiv \overline{A} \cup B \cup C \equiv A - (B \cup C)$$