

# Package ‘temStaR’

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**Title** Tempered Stable Distribution

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**Description** This package provides useful tools to use the multivariate normal tempered stable distribution and process

**License** `use\_mit\_license()`

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**Imports** functional,  
nloptr,  
pracma,  
spatstat,  
Matrix

**Suggests** functional,  
nloptr,  
pracma,  
spatstat,  
Matrix

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chf_NTS	<i>chf_NTS</i>
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## Description

chf\_NTS calculates Ch.F of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If a time parameter value is given, it calculates Ch.F of the NTS process  $\phi(u) = E[\exp(iu(X(t+s) - X(s)))] = \exp(t \log(E[\exp(iuX(1))]))$ , where X is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

## Usage

```
chf_NTS(u, param)
```

## Arguments

u	An array of u
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ .

## Value

Characteristic function of the NTS distribution

## Examples

```
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_NTS(u, ntsparm)
```

```
#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
```

```
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_NTS(u, ntsparam)
```

---

chf\_stdNTS

*chf\_stdNTS*

---

## Description

chf\_stdNTS calculates Ch.F of the standard NTS distribution with parameters  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates Ch.F of the standard NTS process  $\phi(u) = E[\exp(iu(X(t+s) - X(s))) = \exp(t \log(E[\exp(iuX(1))]))$ , where X is the standard NTS process generated by the standard NTS distribution with parameters  $(\alpha, \theta, \beta)$ .

## Usage

```
chf_stdNTS(u, param)
```

## Arguments

u	An array of u
ntsparam	A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ . For the standard NTS process case it is a vector of parameters $(\alpha, \theta, \beta, t)$ .

## Value

Characteristic function of the standard NTS distribution

## Examples

```
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_stdNTS(u, ntsparam)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
u <- seq(from = -2*pi, to = 2*pi, length.out = 101)
phi <- chf_stdNTS(u, ntsparam)
```

cvarnts

*cvarnts***Description**

cvarnts calculates Conditional Value at Risk (CVaR, or expected shortfall ES) of the NTS market model with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates CVaR of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$

**Usage**

```
cvarnts(eps, ntsparm)
```

**Arguments**

ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .
u	Real value between 0 and 1

**Value**

CVaR of the NTS distribution.

**References**

Y. S. Kim, S. T. Rachev, M. L. Bianchi, and F. J. Fabozzi (2010), Computing VaR and AVaR in infinitely divisible distributions, *Probability and Mathematical Statistics*, 30 (2), 223-245.

S. T. Rachev, Y. S. Kim, M. L. Bianchi, and F. J. Fabozzi (2011), *Financial Models with Levy Processes and Volatility Clustering*, John Wiley & Sons

**Examples**

```
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
u <- c(0.01, 0.05)
q <- cvarnts(u, ntsparm)

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
u <- c(0.01, 0.05)
q <- cvarnts(u, ntsparm)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
```

```

gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
u <- c(0.01, 0.05)
q <- cvarnts(u, ntsparm)

```

dnts

*dnts*

## Description

dnts calculates pdf of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates pdf of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates pdf of the NTS process  $f(x)dx = d(P((X(t+s) - X(s)) < x))$ , where  $X$  is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

## Usage

```
dnts(xdata, ntsparm)
```

## Arguments

xdata	An array of x
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . For the NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

## Value

Density of NTS distribution

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```

alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
x <- seq(from = -6, to = 6, length.out = 101)
d <- dnts(x, ntsparm)
plot(x, d, type = 'l')

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3

```

```

mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
x <- seq(from = -2, to = 2, by = 0.01)
d <- dnts(x, ntsparam)
plot(x,d,type = 'l')

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
x <- seq(from = -0.02, to = 0.02, length.out = 101)
d <- dnts(x, ntsparam)
plot(x,d,type = 'l')

```

---

fitmnts

*fitmnts*


---

## Description

fitmnts fit parameters of the n-dimensional NTS distribution.

$$r = \mu + \text{diag}(\sigma)X$$

where

$X$  follows  $\text{stdNTS}_n(\alpha, \theta, \beta, \Sigma)$

## Usage

```

\code{res <- fitmnts(returndata, n)}
\code{res <- fitmnts(returndata, n, alphaNtheta = c(alpha, theta))}
\code{res <- fitmnts(returndata, n, stdflag = TRUE )}
\code{res <- fitmnts(returndata, n, alphaNtheta = c(alpha, theta), stdflag = TRUE)}

```

## Arguments

returndata	Raw data to fit the parameters. The data must be given as a matrix form. Each column of the matrix contains a sequence of asset returns. The number of row of the matrix is the number of assets.
n	Dimension of the data. That is the number of assets.
alphaNtheta	If $\alpha$ and $\theta$ are given, then put those numbers in this parameter. The function fixes those parameters and fits other remaining parameters. If you set <code>alphaNtheta = NaN</code> , then the function fits all parameters including $\alpha$ and $\theta$ .
stdflag	If you want only standard NTS parameter fit, set this value be TRUE.

## Value

Structure of parameters for the n-dimensional NTS distribution.

res\$mu :  $\mu$  mean vector (column vector) of the input data.

res\$sigma :  $\sigma$  standard deviation vector (column vector) of the input data.

res\$alpha :  $\alpha$  of the std NTS distribution (X).

res\$theta :  $\theta$  of the std NTS distribution (X).

res\$beta :  $\beta$  vector (column vector) of the std NTS distribution (X).

res\$Rho :  $\Sigma$  ( $\rho$ ) matrix of the std NTS distribution (X).

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
library(functional)
library(nloptr)
library(pracma)
library(spatstat)
library(Matrix)
library(quantmod)

getSymbols("^GSPC", src="yahoo", from = "2016-1-1", to = "2020-12-31")
pr1 <- as.numeric(GSPC$GSPC.Adjusted)
getSymbols("^DJI", src="yahoo", from = "2016-1-1", to = "2020-12-31")
pr2 <- as.numeric(DJI$DJI.Adjusted)

returndata <- matrix(data = c(diff(log(pr1)),diff(log(pr2))),
                     ncol = 2, nrow = (length(pr1)-1))
res <- fitmnts( returndata = returndata, n=2 )

#Fix alpha and theta.
#Estimate alpha dna theta from DJIA and use those parameter for IBM, INTL parameter fit.
getSymbols("^DJI", src="yahoo", from = "2020-8-25", to = "2020-12-31")
prDJ <- as.numeric(DJI$DJI.Adjusted)
ret <- diff(log(prDJ))
ntsparam <- fitnts(ret)
getSymbols("IBM", src="yahoo", from = "2016-1-1", to = "2020-12-31")
pr1 <- as.numeric(IBM$IBM.Adjusted)
getSymbols("INTL", src="yahoo", from = "2016-1-1", to = "2020-12-31")
pr2 <- as.numeric(INTL$INTL.Adjusted)

returndata <- matrix(data = c(diff(log(pr1)),diff(log(pr2))),
                     ncol = 2, nrow = (length(pr1)-1))
res <- fitmnts( returndata = returndata,
               n = 2,
               alphaNtheta = c(ntsparam["alpha"], ntsparam["theta"]) )
```

fitnts

*fitnts***Description**

fitnts fit parameters  $(\alpha, \theta, \beta, \gamma, \mu)$  of the NTS distribution. This function using the curvefit method between the empirical cdf and the NTS cdf.

**Usage**

```
\code{fitnts(rawdat)}
\code{fitnts(rawdat), ksdensityflag = 1}
\code{fitnts(rawdat, initialparam = c(alpha, theta, beta, gamma, mu))}
\code{fitnts(rawdat, initialparam = c(alpha, theta, beta, gamma, mu), ksdensityflag = 1)}
\code{fitnts(rawdat, initialparam = c(alpha, theta, beta, gamma, mu), maxeval = 100, ksdensityflag
```

**Arguments**

rawdat	Raw data to fit the parameters.
initialparam	A vector of initial NTS parameters. This function uses the nloptr package. If it has a good initial parameter then estimation performs better. If users do not know a good initial parameters, then just set it as initialparam=NaN, that is default. The function cffitnts() may be helpful to find the initial parameters.
maxeval	Maximum evaluation number for nloptr. The iteration stops on this many function evaluations.
ksdensityflag	This function fit the parameters using the curvefit method between the empirical cdf and the NTS cdf. If ksdensityflag = 1 (default), then the empirical cdf is calculated by the kernel density estimation. If ksdensityflag = 0, then the empirical cdf is calculated by the empirical cdf.

**Value**

Estimated parameters

**References**

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```
library("quantmod")
getSymbols("^GSPC", src="yahoo", from = "2010-1-1", to = "2020-12-31")
pr <- as.numeric(GSPC$GSPC.Adjusted)
ret <- diff(log(pr))
ntsparam <- fitnts(ret)

Femp = ecdf(ret)
x = seq(from=min(ret), to = max(ret), length.out = 100)
cemp = Femp(x)
ncdf = pnts(x, c(ntsparam))
```



```

plot(x,ncdf,type = 'l', col = "red")
points(x,cemp, type = 'l', col = "blue")
a = density(ret)
p = dnts(x,ntsparm)
plot(x,p,type = 'l', col = "red")
lines(a,type = 'l', col = "blue")

```

fitstdnts

*fitstdnts*

## Description

fitstdnts fit parameters  $(\alpha, \theta, \beta)$  of the standard NTS distribution. This function using the curvefit method between the empirical cdf and the standard NTS cdf.

## Usage

```

\code{fitstdnts(rawdat)}
\code{fitstdnts(rawdat), ksdensityflag = 1}
\code{fitstdnts(rawdat, initialparam = c(alpha, theta, beta))}
\code{fitstdnts(rawdat, initialparam = c(alpha, theta, beta)), ksdensityflag = 1}
\code{fitstdnts(rawdat, initialparam = c(alpha, theta, beta)), maxeval = 100, ksdensityflag = 1}

```

## Arguments

rawdat	Raw data to fit the parameters.
initialparam	A vector of initial standard NTS parameters. This function uses the nloptr package. If it has a good initial parameter then estimation performs better. If users do not know a good initial parameters, then just set it as initialparam=NaN, that is default.
maxeval	Maximum evaluation number for nloptr. The iteration stops on this many function evaluations.
ksdensityflag	This function fit the parameters using the curvefit method between the empirical cdf and the standard NTS cdf. If ksdensityflag = 1 (default), then the empirical cdf is calculated by the kernel density estimation. If ksdensityflag = 0, then the empirical cdf is calculated by the empirical cdf.

## Value

Estimated parameters

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```

library("quantmod")
getSymbols("^GSPC", src="yahoo", from = "2010-1-1", to = "2020-12-31")
pr <- as.numeric(GSPC$GSPC.Adjusted)
ret <- diff(log(pr))
stdret <- (ret-mean(ret))/sd(ret)
stdntsparam <- fitstdnts(stdret)

Femp = ecdf(stdret)
x = seq(from=min(stdret), to = max(stdret), length.out = 100)
cemp = Femp(x)
ncdf = pnts(x, c(stdntsparam))
plot(x,ncdf,type = 'l', col = "red")
lines(x,cemp, type = 'l', col = "blue")
a = density(stdret)
p = dnts(x,stdntsparam)
plot(x,p,type = 'l', col = "red", ylim = c(0, max(a$y, p)))
lines(a,type = 'l', col = "blue")

```

gensamplepathnts

*gensamplepathnts***Description**

gensamplepathnts generate sample paths of the NTS process with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it generate sample paths of the standard NTS process with parameters  $(\alpha, \theta, \beta)$ .

**Usage**

```
gensamplepathnts(npath, nimestep, ntsparm, dt)
```

**Arguments**

npath	Number of sample paths
nimestep	number of time step
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .
dt	the time length of one time step by the year fraction. "dt=1" means 1-year.

**Value**

Structure of the sample path. Matrix of sample path. Column index is time.

**Examples**

```

#standard NTS process sample path
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)

```

```

npath <- 5
ntimestep <- 250
dt <- 1/250
simulation <- gensamplepathnts(npath, ntimestep, ntsparm, dt)
matplot(colnames(simulation), t(simulation), type = 'l')

#NTS process sample path
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
npath <- 5
ntimestep <- 250
dt <- 1/250
simulation <- gensamplepathnts(npath, ntimestep, ntsparm, dt)
matplot(colnames(simulation), t(simulation), type = 'l')

```

ipnts

*ipnts*

## Description

ipnts calculates inverse cdf of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates inverse cdf of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$

## Usage

```
ipnts(u, ntsparm, maxmin = c(-10, 10), du = 0.01)
```

## Arguments

u	Real value between 0 and 1
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

## Value

Inverse cdf of the NTS distribution. It is the same as qnts function.

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
u <- seq(from = 0.01, to = 0.99, length.out = 99)
q <- ipnts(u, ntsparam)
plot(u,q,type = 'l')
```

```
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
u <- seq(from = 0.01, to = 0.99, length.out = 99)
q <- ipnts(u, ntsparam)
plot(x,q,type = 'l')
```

```
#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
u <- seq(from = 0.01, to = 0.99, length.out = 99)
q <- ipnts(u, ntsparam)
plot(x,q,type = 'l')
```

---

moments\_NTS

---

*moments\_NTS*


---

**Description**

moments\_NTS calculates mean, variance, skewness, and excess kurtosis of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

**Usage**

```
moments_NTS(param)
```

**Arguments**

param                      A vector of the NTS parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

**Value**

First 4 moments (Mean, Variance, Skewness, Excess Kurtosis) of NTS distribution. The mean is always the same as the parameter  $\mu$ .

## References

Kim, Y.S, K-H Roh, R. Douady (2020) Tempered Stable Processes with Time Varying Exponential Tails <https://arxiv.org/pdf/2006.07669.pdf>

## Examples

```
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
moments_NTS(param = ntsparam)
```

---

moments\_stdNTS

*moments\_stdNTS*


---

## Description

moments\_stdNTS calculates mean, variance, skewness, and excess kurtosis of the standard NTS distribution with parameters  $(\alpha, \theta, \beta)$ .

## Usage

```
moments_stdNTS(param)
```

## Arguments

param                      A vector of the standard NTS parameters  $(\alpha, \theta, \beta)$ .

## Value

First 4 moments (Mean, Variance, Skewness, Excess Kurtosis) of NTS distribution. Of course, the mean and variance are always 0 and 1, respectively.

## References

Kim, Y.S, K-H Roh, R. Douady (2020) Tempered Stable Processes with Time Varying Exponential Tails <https://arxiv.org/pdf/2006.07669.pdf>

## Examples

```
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
moments_stdNTS(param = ntsparam)
```

pnts

*pnts***Description**

pnts calculates cdf of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates cdf of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates cdf of the process  $F(x) = P((X(t+s) - X(s)) < x)$ , where  $X$  is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

**Usage**

```
pnts(xdata, ntsparm, dz = 2^-8, m = 2^12)
```

**Arguments**

xdata	An array of x
ntsparm	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For the NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of the standard NTS parameters $(\alpha, \theta, \beta)$ .

**Value**

Cumulative probability of the NTS distribution

**References**

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

**Examples**

```
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparm <- c(alpha, theta, beta)
x <- seq(from = -6, to = 6, length.out = 101)
p <- pnts(x, ntsparm)
plot(x, p, type = 'l')
```

```
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
x <- seq(from = -2, to = 2, by = 0.01)
p <- pnts(x, ntsparm)
plot(x, p, type = 'l')
```

```
#Annual based parameters
alpha <- 1.2
```

```

theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparam <- c(alpha, theta, beta, gamma, mu, dt)
x <- seq(from = -0.02, to = 0.02, length.out = 101)
p <- qnts(x, ntsparam)
plot(x,p,type = 'l')

```

qnts

*qnts*

## Description

qnts calculates quantile of the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it calculates quantile of the standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it calculates quantile of NTS process. That is it finds  $x$  such that  $u = P((X(t+s) - X(s)) < x)$ , where  $X$  is the NTS process generated by the NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ .

## Usage

```
qnts(u, ntsparam)
```

## Arguments

ntsparam	A vector of the NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For the NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of standard NTS parameters $(\alpha, \theta, \beta)$ .
vector	of probabilities.

## Value

The quantile function of the NTS distribution

## Examples

```

alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
u <- c(0.01, 0.05, 0.25, 0.5, 0.75, 0.95, 0.99)
q <- qnts(u, ntsparam)

```

```

alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparam <- c(alpha, theta, beta, gamma, mu)
u <- c(0.01, 0.05, 0.25, 0.5, 0.75, 0.95, 0.99)

```

```

q <- qnts(u, ntsparm)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
u <- c(0.01,0.05,0.25,0.5, 0.75, 0.95, 0.99)
q <- qnts(u, ntsparm)

```

---

rmnts	<i>rmnts</i>
-------	--------------

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## Description

rmnts generates random vector following the n dimensional NTS distribution.

$$r = \mu + \text{diag}(\sigma)X,$$

where

$X$  follows  $\text{stdNTS}_n(\alpha, \theta, \beta, \Sigma)$

## Usage

```
rmnts(strPMNTS, numofsample, rW = NaN, rTau = NaN)
```

## Arguments

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). strPMNTS\$Rho : $\Sigma$ ( $\rho$ ) matrix of the std NTS distribution (X).
numofsample	number of samples.

## Value

Simulated NTS random vectors

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>



## Examples

```
strPMNTS <- list(ndim = 2,
                 mu = c( 0.00011, 0.00048 ),
                 sigma = c( 0.0162, 0.0231 ),
                 alpha = 1.23,
                 theta = 3.607,
                 beta = c( -0.1209, 0.0905 ),
                 Rho = matrix( data = c(1.0, 0.55, 0.55, 1.0), nrow = 2, ncol = 2)
                 )
gensim <- rmnts( strPMNTS, 100 )
plot(gensim)
```

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<i>rnts</i>	<i>rnts</i>
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## Description

*rnts* generates random numbers following NTS distribution with parameters  $(\alpha, \theta, \beta, \gamma, \mu)$ . If only three parameters are given, it generates random numbers of standard NTS distribution with parameter  $(\alpha, \theta, \beta)$ . If a time parameter value is given, it generates random numbers of increments of NTS process for time interval  $t$ .

## Usage

```
rnts(n, ntsparam)
```

## Arguments

<i>n</i>	number of random numbers to be generated.
<i>ntsparam</i>	A vector of NTS parameters $(\alpha, \theta, \beta, \gamma, \mu)$ . For NTS process case it is a vector of parameters $(\alpha, \theta, \beta, \gamma, \mu, t)$ . A vector of standard NTS parameters $(\alpha, \theta, \beta)$ .

## Value

NTS random numbers

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
alpha <- 1.2
theta <- 1
beta <- -0.2
ntsparam <- c(alpha, theta, beta)
r <- rnts(100, ntsparam) #generate 100 NTS random numbers
plot(r)

alpha <- 1.2
theta <- 1
```

```

beta <- -0.2
gamma <- 0.3
mu <- 0.1
ntsparm <- c(alpha, theta, beta, gamma, mu)
r <- rnts(100, ntsparm) #generate 100 NTS random numbers
plot(r)

#Annual based parameters
alpha <- 1.2
theta <- 1
beta <- -0.2
gamma <- 0.3
mu <- 0.1
#scaling annual parameters to one day
dt <- 1/250 #one day
ntsparm <- c(alpha, theta, beta, gamma, mu, dt)
r <- rnts(100, ntsparm) #generate 100 NTS random numbers
plot(r)

```

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setPortfolioParam	<i>setPortfolioParam</i>
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## Description

Portfolio return with capital allocation weight is  $R_p = \langle w, r \rangle$ , which is a weighted sum of elements in the N-dimensional NTS random vector.  $R_p$  becomes an 1-dimensional NTS random variable. setPortfolioParam find the parameters of  $R_p$ .

## Usage

```
\code{res <- setPortfolioParam(strPMNTS,w)}
```

## Arguments

strPMNTS	Structure of parameters for the n-dimensional NTS distribution. strPMNTS\$ndim : dimension strPMNTS\$mu : $\mu$ mean vector (column vector) of the input data. strPMNTS\$sigma : $\sigma$ standard deviation vector (column vector) of the input data. strPMNTS\$alpha : $\alpha$ of the std NTS distribution (X). strPMNTS\$theta : $\theta$ of the std NTS distribution (X). strPMNTS\$beta : $\beta$ vector (column vector) of the std NTS distribution (X). strPMNTS\$Rho : $\Sigma$ matrix of the std NTS distribution (X).
w	Capital allocation weight vector.

## Value

The weighted sum follows 1-dimensional NTS.

$$R_p = \langle w, r \rangle = \mu + \text{diag}(\sigma)X,$$

where

$X$  follows  $stdNTS_1(\alpha, \theta, \beta, 1)$ .

Hence we obtain

res\$mu :  $\mu$  mean of  $R_p$ .

res\$sigma :  $\sigma$  standard deviation of  $R_p$ .

res\$alpha :  $\alpha$  of  $X$ .

res\$theta :  $\theta$  of  $X$ .

res\$beta :  $\beta$  of  $X$ .

## References

Kim, Y. S. (2020) Portfolio Optimization on the Dispersion Risk and the Asymmetric Tail Risk  
<https://arxiv.org/pdf/2007.13972.pdf>

## Examples

```
strPMNTS <- list(ndim = 2,
                 mu = c( 0.00011, 0.00048 ),
                 sigma = c( 0.0162, 0.0231 ),
                 alpha = 1.23,
                 theta = 3.607,
                 beta = c( -0.1209, 0.0905 ),
                 Rho = matrix( data = c(1.0, 0.55, 0.55, 1.0), nrow = 2, ncol = 2)
)
w <- c(0.3, 0.7)
res <- setPortfolioParam(strPMNTS,w)
```

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