Fast top-k frequent itemset mining under Local Differential Privacy*

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I. INTRODUCTION

Differential privacy(DP) [7] is the state-of-the-art approach that is used to protect individual privacy in the process of data collection, which has been named one of the world's top 10 breakthrough technologies in 2020 by the MIT technology review. It is a means in cryptography that aims to provide a way to maximize the accuracy of data queries when querying from statistical databases while minimizing the chances of identifying their records. As a mathematical technique, it can add noise to the data while quantifying the extent of the increase in privacy, thus making the process of adding "noise" more rigorous.

Due to its unique advantages, DP has been widely studied by the academia and industry. For example, Google, Microsoft, apple and other companies use this technology to protect users' privacy, and at the same time, mobile phones aggregate data, so as to improve service quality. And the U.S. government is to complete a census of 330 million U.S. residents by 2020, keeping their identities secret, in what would be the largest census ever.

There are two types of differential privacy - Centralized differential privacy(CDP) and Local differential privacy(LDP). Compared with CDP, the LDP does not require the assumptions of a trusted third party and provides stronger privacy guarantees. DP's research has involved many aspects, in recent years, the work in data mining(DM) has attracted the attention. A lot of work [3]–[6] has been done to solve DM problems in CDP. However, since the analyst holds the user's raw data in CDP setting, its main job is to add noise to the results to satisfy the DP definition.

The LDP setting, by contrast, has no reliance on third party assumptions. The main challenge with a DM task is that the data analyst does not hold the user's original sensitive information, so it is quite difficult to mine useful information with noise data.Qin et al. [1] proposed LDPMiner protocol

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for heavy hitter estimation over set-valued data and left data mining as an open problem. Wang et al. [2] solved the top-k frequent itemset mining(FIM) task for the first time with **padding-and-sampling-based frequency oracle**(PSFO). In [2], the Set-Value Item Mining(SVIM) protocol had been proposed to handles set values under the LDP setting, with the purpose of finding the k most frequent items and their frequencies. To mine frequent itemsets , a core technique is "Guessing Frequency(GF)". That is, the analyst first calculated the frequency of a given itemset X for all candidate itemsets by (1),

$$\varphi(X) = \prod_{x \in X} \mu(x), \mu(x) = \frac{0.9 \times \tilde{\theta}(x)}{\max_{x \in S'} \tilde{\theta}(x)}$$
(1)

where $\varphi(X)$ represents the speculative frequency of itemset X, S' and $\tilde{\theta}(x)$ are denoted separately the top-k frequent items set and the frequency of a given item x. Then 2k itemsets with highest guessing frequencies are selected to construct candidate set IS. Finally, reference [2] utilized SVIM protocol again with the domain IS to mine top-k itemsets.

In [2], the SVSM protocol first selected 2k itemsets with highest guessing frequencies to construct candidate set IS, then utilized SVIM protocol again with the domain IS to mine top-k itemsets. We observe that, the size of candidate set to construct IS increase significantly with k. As a result, it is computationally expensive when k is large(e.g., k=100).

TABLE I SAMPLE OF TRANSACTIONAL DATA.

TID	List of items
T01	a, f, c, g, p
T02	a,b,c,f,l,o
T03	b, f, h, o
T04	b, c, p
T05	f, a, c, l, p, n

Inspiringly, we propose minefp protocol, which aims at finding top - k itemsets under the LDP setting and provides similar accuracy while providing lower overhead than existing protocol(SVSM) within the same privacy constraints. First,

the SVIM protocol is used to estimate the k most frequent items and their frequencies. Second, users report the number of frequent items they have; the analyst estimates the distribution user reported and figure out the right M as the maximum iteration of the tree. Third, users interact with the analyst to build effectively the FP-tree [8]. Fourth, the analyst optimizes and mines the FP-tree(post-processing). Fifth, the analyst publishes top-k itemsets. Experimental results how that minefp outperforms SVSM in that it identifies quickly frequent itemsets as well as estimates the frequencies more accurately.

To summarize, the main contributions of this paper are:

- We study the application of fp-growth algorithm and design the FP-tree-based-mine(minefp) protocol to find frequent itemsets as well as their frequencies in the LDP setting. Experimental results on real-world datasets show the significant improvement over previous techniques.
- We investigate guessing frequency(GF) to construct candidate set and point out that it is beneficial to build hierarchically FP-tree.

Roadmap.

II. BACKGROUND

A. Local Differential Privacy(LDP)

In the local setting, there is no trusted third party and an aggregator wants to gather information from users. The privacy of the data contributor is protected by perturbing her/his original data at the data contributor's side; thus, the agregator cannot access the original data, but is still able to obtain population statistics.

Definition 1(Local Differential Privacy) A randomized algorithm \mathcal{A} satisfies ϵ -LDP, if and only if for (1) all pairs of input v_i and v_j , and (2) any output \mathcal{O} of \mathcal{A} , we have:

$$\frac{\Pr[\mathcal{A}(v_i) = \mathcal{O}]}{\Pr[\mathcal{A}(v_j) = \mathcal{O}]} \le e^{\epsilon}$$

where $\epsilon \leq 0$ is the privacy budget.—

B. FP-growth algorithm

Frequent pattern growth(FP-growth) [8] is an algorithm that mines the complete set of frequent patterns without a costly candidate generation process, which based on the frequent pattern tree(FP-tree) structure that is an extended prefix-tree structure for storing compressed, crucial information about frequent patterns. The FP-Tree is further divided into a set of Conditional FP-Trees for each frequent item so that they can be mined separately. An example of the FP-Tree that represents the frequent items is shown in Fig. 1, where the minimum support count is set to 3.

The FP-growth algorithm solves the problem of identifying long frequent itemsets by searching through smaller conditional FP-tree repeatedly. The conditional pattern base is a "sub-database" which consists of every prefix path in the FP-Tree that co-occurs with every frequent length-1 item. It is used to construct the conditional FP-tree and generate all the

frequent patterns related to every frequent length-1 item. In this way, the cost of searching for the frequent patterns is substantially reduced.

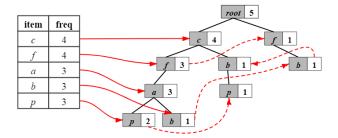


Fig. 1. Frequent pattern tree(FP-tree).

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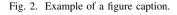


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