

Date: 02-02-2023

- i) Imagine that you have selected data from the all electronics data warehouse for analysis. The data set will be huge! The following data are a list of all electronics prices for commonly sold items (rounded to the nearest dollar). The numbers have been sorted 1, 1, 5, 5, 5, 5, 5, 8, 8, 10, 10, 10, 10, 12, 14, 14, 14, 15, 15, 15, 15, 15, 18, 18, 18, 18, 18, 19, 19, 20, 20, 20, 20, 20, 20, 20, 21, 21, 21, 21, 25, 25, 25, 25, 25, 28, 28, 30, 30, 30.
- (i) Partition the dataset using an equal-frequency partitioning method with bin equal to 3. (ii) apply data smoothing using bin means and bin boundary. (iii) Plot histogram for the above frequency division.

(ii) Partitioning using equal frequency

We divide the data set into 3 equal parts frequency bins, each containing the same number of observations. To calculate the bin boundaries, we count the number of observations the data set and divide that by the number of bins. In this case 3. Each bin will contain

$$\frac{40}{3} = 13 \text{ observations.}$$

The bin boundaries for equal-frequency partitioning method are:

$$\text{Bin 1: } 1-12$$

$$\text{Bin 2: } 12-21$$

$$\text{Bin 3: } 21-30$$

- (ii) Data smoothing using bin means and bin boundaries.

For data smoothing, we calculate the mean of the each bin and use that as the representative value for all observations in that bin.

$$\text{Bin 1: Mean} = (1+1+5+5+5+5+8+8+10+10+10+10)/13 = 6$$

$$\text{Bin 2: Mean} = (10+10+10+12+14+14+14+15+15+15+15+15)/13 = 15$$

$$\text{Bin 3: Mean} = (15+15+15+18+18+18+18+18+20+20+20+20+20+20+20+21+21+21+21+25+25+25+25+25+28+28+30+30+30)/13 = 24$$

The bin boundaries for smoothed data using bin means are

$$\text{Bin 1: } 6-12$$

$$\text{Bin 2: } 12-21$$

$$\text{Bin 3: } 21-30$$

(iii) Plotting Histogram

Using bin boundaries obtained from either equal frequency or data smoothing, we can plot a histogram by creating bars of the same width that span the bin boundaries, and the height of each bar is proportional to the frequency of observations in that bin. The x-axis represents the price of the item and the y-axis represents the frequency of observations.

R-program

Load the ggplot2 library
library(ggplot2)

Create a vector of the prices data

$$c(1, 1, 5, 5, 5, 5, 5, 8, 8, 10, 10, 10, 10, 12, 14, 14, 14, 15, 15, 15, 15, 15, 18, 18, 18, 18, 18, 19, 19, 20, 20, 20, 20, 20, 20, 20, 21, 21, 21, 21, 25, 25, 25, 25, 25, 28, 28, 30, 30, 30)$$

Partition the data using equal binned data

$$\text{binned} \leftarrow \text{data}(data, \text{breaks} = 3, \text{stat} = \text{P}("r", 19, "20-30", 10, 10) \text{ right} = \text{false})$$

Calculate the bin means

$$\text{bin-means} \leftarrow \text{tapply}(data, \text{binned_data}, \text{mean})$$

Calculate the bin boundaries

$$\text{bin-boundaries} \leftarrow c(-\text{Inf}, 19, 30, \text{Inf})$$

Apply data smoothing using bin means and bin boundaries
 $\text{smoothed_data} \leftarrow \text{cut}(data, \text{breaks} = \text{bin-boundaries}, \text{labels} = \text{bin-means}, \text{right} = \text{false})$

Plot the histogram

```
ggplot(data.frame(smoothed_data), aes(smoothed_data)) +
  geom_histogram(binwidth = 1, color = "black", fill = "white") +
  labs(x = "Price", y = "Frequency") + ggtitle("Histogram of the smoothed all electronics prices")
```

Show the plot

```
plot(ggplot(data.frame(smoothed_data), aes(smoothed_data)))
```

The following table could be plotted as (x, y) points with the first column being the x values as number of mobile phones sold and the second column being the y values as money. To use the scatter plot for how many mobile phones sold.

x	4	1	5	7	10	2	50	25	90	36
y	12	5	13	19	31	7	153	72	275	110

The scatter plot for the given table can be plotted as follows:

$(4, 12), (1, 5), (5, 13), (7, 19), (10, 31), (2, 7), (50, 153)$

$(85, 72), (90, 275), (36, 110)$

