Python Lecture Notes for CCPS 109

These lecture notes go through the important things about the core Python programming language and using that language to solve problems, as taught by <u>Ilkka Kokkarinen</u> for the course **CCPS 109 Computer Science I** for the Chang School of Continuing Education, Ryerson University, Toronto. This version of the document was released **March 7, 2021**.

These bullet points should cover all of the important ideas and all of the minor issues that we encounter during the course. However, the example programs in the GitHub repository ikokkari/PythonExamples are at least of equal importance to these notes, and absolutely necessary to see how all these theoretical concepts work out in practice.

This document and all our example programs use Python 3 throughout, and are not compatible with the older Python 2. These notes and example programs can be freely used and modified, with proper attribution, by other computer science instructors and students who find them useful. All this teaching material, including both the notes and the example programs, is released under GNU Public Licence v3 to ensure that all can freely do so without copyright restrictions.

Week 1: Python as scriptable calculator

1.1. Expressions

- When used in the **interactive mode**, the Python interpreter reads in **expressions** that the user enters one at the time, and prints out the results of evaluating these expressions. This makes Python handy for small scale experimentation and trying out things.
- Expressions can be built up from **constant literals**, **arithmetic operators** and **function calls**. Some expressions are "Hello" + 'world!', 2 + 2, 5 / 2, 5 // 2, 2 ** 3 or 5 > 8, these respectively evaluating to "Helloworld!", 4, 2.5, 2, 8 and False.
- Some functions and expressions can have **side effects** that produce output or change the data stored in the memory in a way that can affect the evaluation of later expressions.
- For no rhyme or reason, the character % has nothing to do with percentages, but denotes the **remainder** operator of integer division. For example, 10 % 3 equals 1.
- In most programming languages, the sign of the remainder is always the same as the sign of the first operand, regardless of the sign of the second operand. In Python, the remainder operator works in a different way that is technically speaking mathematically incorrect, but has one giant advantage in practical programming.

- The **precedence** and **associativity** of mathematical operators behave as you learned in basic mathematics, and can be bypassed with parentheses.
- Python can even handle **complex numbers** and their arithmetic operations directly built in the language, with the **imaginary part** denoted with the capital J after the number. For example, the expression (1 + 2J) * (1 1J) equals 3 + 1J.
- Every expression in Python evaluates to some **object**, although this result can also be the special value **None** denoting the absence of an object. In this special case, the interactive Python environment does not print out anything.
- Expressions can be arbitrarily long and complicated, since they can be **nested** to arbitrary depths. However, instead of trying to write a complicated computation as a **one-liner**, it is in many ways better to break it down into a series of simpler expressions executed in sequence.
- Python internally stores integers using a flexible encoding that makes life more convenient for programmers when the magnitude of integers is limited only by the memory available for the Python interpreter. Even behemoths such as 1234**5678 are a breeze to evaluate in a blink of an eye.
- (The fact that Python integers actually do work the way that we expect integers to mathematically work is never news to genuine beginners. It is news only to the lost souls from a more primitive era who were gaslit and browbeaten their entire lives to believe in the absurdity that in the hall of funhouse mirrors inside every computer, one billion is a large number, but three times that is something negative.)

1.2. Scripts

- When given an entire **script** to execute as a **program**, Python does not automatically print out the results of the individual expressions, since you certainly don't want your screen flooded with the results of possibly billions of evaluated expressions.
- Inside a script, the intermediate results are visible for the user only when the expression contains a call to the special print function that outputs its argument as characters.
- A Python script file absolutely must consist of **raw text**, with only the actual Python source code characters inside it. Any type of **rich text document** (for example, Microsoft Word or Google Docs documents) that contains formatting instructions such as font or paragraph styles embedded in the document itself cannot be executed as Python.
- As a rule, if opening the script file directly into a **raw text editor** such as Notepad or TextEdit shows any weird characters, your script file is not legal Python.
- When displaying such a raw text Python script, all modern text editors use **syntax highlighting** with colour and font effects to make the structure of the code easier to discern for the human eye. However, all these visual effects are dynamically generated by the editor for its display, and are not encoded inside the actual raw text script file.

- Many built-in functions such as print are parameter polymorphic, that is, the same function can be applied to arguments of vastly different types, and the function still does the right thing in each case. For example, 2 + 2 equals 4, and 'hello' + 'world' equals 'helloworld', the operator + doing the right thing in both cases.
- Python is **case sensitive** everywhere, same way as most other programming languages. However, Python differs in style and spirit from most other programming languages in that it actively uses **whitespace** and **indentation** to denote the structure of the script.
- Almost all other major programming languages are designed to be insensitive to whitespace, and therefore need special parentheses, typically **curly braces**, to denote the program nested structure.
- Individual statements are separated by line breaks. However, if the statement is obviously **syntactically incomplete**, such as not yet having closed an earlier open parenthesis, the line break is treated as ordinary whitespace. This allows long statements to be broken into multiple lines for readability.
- A common oversimplification is to proclaim that Python language is not "compiled".
 More accurately, the programmer does not need to explicitly compile the Python source
 code script to a form executable by machine. Instead, the interpreter will compile the read
 in script into a more efficient internal representation before executing it, and while doing
 this transformation, check that all expressions in this script are syntactically legal.
- The result of this compilation is stored in a Python bytecode file with suffix .pyc for future use. Conventionally, Python source code files are named using suffix .py.
- So that other people (which includes all the near and far future versions of yourself) can understand what your code does, write **comments** to explain the purpose of the code. Python comments start with the octothorpe / pound sign / hashtag character (depending on the decade you grew up in) written as #, and continue to the end of the line.
- Always comment on the why, never on the what. Python code perfectly describes what it does already, so comments should talk about the reasoning that produced that code.
- If your code is so complex that it needs additional explanation of what it does, you should redesign that code to be less clever. (In programming lingo, calling something "clever" is sometimes done in a finger-quotes "ironic" fashion.)
- For those interested, originally written for Java and C++, the humorous document "<u>How to Write Unmaintainable Code</u>" applies just as well to Python programming.
- PEP 8 is the official style guide of Python. Many Python editors come with a built-in **linter**, a behind-the-scenes utility that looks for constructs that are legal in the language itself and can be executed as Python code, but go against the official uniform style and are occasionally symptoms of something being hinky in the underlying approach.

1.3. Naming things

- Every programming language needs the ability to create and give **names** (also called **variables**) to nameless data objects, so that later expressions can unambiguously talk about those objects. This is achieved with an **assignment** such as x=42.
- Names can consist of arbitrary **letters** (although in practice, you avoid a lot of trouble by using only the twenty-six letters of English), digits and underscore characters. However, a name may not begin with a digit.
- Python doesn't care one whit what these given names mean in our natural language, but of course you should aim to refer to your objects using names that are meaningful and informative for human readers.
- In the Python interactive environment, the special name _ that is merely a single underscore refers to the result of the most recently evaluated expression.
- Dan Bader's excellent Python tip page explains the <u>full rules for underscores in Python</u>.
- In general, your program needs to have a separate name for each separate piece of data that it deals with. When writing programs that need to deal with millions or even billions of items of data, we would rather not type in these names into the program code, but define a name that refers to an entire **sequence** of elements.
- Individual elements of a sequence are accessed based on their position counting from the beginning, analogous to how apartment numbers are used to identify the individual households inside the condo tower whose street address all these apartments share.
- Unlike in **statically typed languages**, names and their types don't need to be explicitly declared. Each name automatically comes into existence into your current **namespace** at the first assignment to it. The name will then refer to the object that was assigned to it. Trying to use a name that has not yet been created crashes the script with NameError.
- A **namespace** is a data structure internal to the Python virtual machine that keeps track of what names exist inside its **scope**, and which objects those names currently refer to.
- Unless otherwise specified, declared names appear in the **global namespace**.
- A name is a separate and qualitatively different thing from the data object that it points to. Any name can later be reassigned to point to some other object that does not need to be the same type as the original. The original object still continues to exist in memory, and might be simultaneously referred to by other names (aliasing).
- The relationship between names and objects is **unidirectional**: the name grants access to the object associated with it, but there is no automatic mechanism to go back from an object to all the names that point to that object.
- Names can be erased from the namespace with the del statement. If the object is still pointed to by some other name, it will continue to exist as before.

- Once an object becomes **unreachable** from the names that currently exist in your reachable namespaces, the **garbage collection** mechanism of Python interpreter releases its memory for future use. This way you never (or, well... perhaps more in tune with Gilbert and Sullivan, "hardly ever") need to worry about releasing these objects yourself.
- To find out what names exist in the current namespace or inside some object, use the
 function dir. Despite the name, this function has nothing to do with your local
 filesystem or disk access, but lists the names that exist in the current global namespace
 in memory inside the Python interpreter process (if called without an argument), or some
 particular object given as argument.
- Alternatively, the built-in function globals() returns the list of global variables.

1.4. Assignment operator

- The assignment operator = evaluates its **right hand side**, which may be an arbitrary expression, and then makes the name on the **left hand side** refer to the object produced by the right hand side.
- Note what an utterly different thing it is to say a=b than to say b=a. Despite the unfortunate choice of the = character to denote assignment, assignment does not behave like equality in mathematics. This can be confusing to beginning programmers.
- Python is not a spreadsheet. At all times, every name only points to the associated object, but remembers no history about where that value came from.
- After assigning a=b, later reassignment of the name b to refer to something else does not change the value that a refers to.
- Names allow us to talk about objects in memory, since these objects themselves don't have any inherent names. Some programs could create millions of objects during their run, and you certainly don't want to think up and painstakingly type in a new distinct name for each and every one of these objects in your source code!
- The document "Facts and myths about Python names and values" by Ned Batchelder clarifies the distinction between names and the objects that those names refer to. This difference is not really important in everyday programming where we can oversimplify and blithely equate the object and the name that we have given to it (after all, that is how we basically deal with mathematical objects such as integers, and even with other people and their given names), but understanding this distinction is a way out of some otherwise confusing situations.
- To find out the **memory address identity** of a Python object, use the function id.
- The operator is checks if two names refer to the exact same object, as in the canonical example expression clark_kent is superman to illustrate a situation where the same object is (sometimes unknowingly) referred to with two separate names.

- The function input reads in a line of text input from the user. Since your program has zero control over the user and his sausage fingers, the characters that are entered can be anything, even if you explicitly ask the user to pretty please enter an integer. They might still type in 'Hello world' due to an accident or malice, or just to find out if your program is prepared for that possibility.
- As an aside, computer security 101: you cannot assume anything about data that is generated by and comes from the outside world. "Client is in the hands of the enemy!"
- Finally, this author's heartfelt plea: please don't ever use "input" as a verb. Doing so will always look stupid, especially in past tense where the word "inputted" sounds like something that would occur in a minigolf course. And you most certainly can't use the same verb "input" for both directions, as in the sentences "The program inputs a number" and "The user inputs a number".
- The correct and unambiguous verbs for passing data back and forth are "read" and "enter", as in "The program reads the input that the user enters."

1.5. Types

- Despite the fact that these types don't show up explicitly in the source code, Python is a **strongly typed** language; every object in memory has a **type** that determines how that object behaves and what operations are possible to do with it.
- Python typing is **implicit** in that the Python language itself does not talk about the types of objects that it performs computations on. Python will know the type of the resulting object after evaluating the expression that creates that object.
- For example, the expression 2 + 2 would produce a result that is an integer, whereas the expression 2 < 3 would produce a **boolean truth value**.
- In reality, the data in computer memory consists of **bytes**, little "boxes" that each contain a small integer number, but don't carry any additional inherent meaning about the type of the thing that they represent, or what these bytes are interpreted to semantically mean in aggregate.
- In principle, the exact same bytes in the memory can be treated as integers, text, machine code instructions, or whatever else. Bytes don't have any inherent semantics of their own other than being a place to store a small integer represented with eight **bits**.
- This is the grand idea of **von Neumann architecture** that all real computers follow: there exist only bytes, and the processor performs simple operations such as copying, comparison and arithmetic operations on those bytes. The operations are simple enough to be hardcoded into the electronics of the computer hardware.
- Any concepts above that level of primitive representation, such as "decimal numbers", "functions" or "conditions", is just as fictional as "hobbits" or "vampires". However, as long as everyone agrees on the properties of these fictional objects, these useful fictions

- can be used as notational shorthands to express truths about phenomena that are very real!
- (Strictly speaking, even "bytes" and "processor" are useful fictions one level of abstraction below the previous one. In the actual reality, inside a computer there exist only cleverly arranged logic gates, through which electricity then ebbs and flows...)
- An object, once created, cannot change its type or memory address as long as that object exists in the memory. The contents of mutable objects can change without changing the identity of that object, though.
- To find out the type of some object, use the built-in function type. The result of this function is an object (in Python 3, everything is an object)... but what is the type of this type object itself? Try it out!
- To test whether some object is of some particular type, use the operator isinstance.
- Python has many built-in functions to convert an object to a different type. For example, if the name num contains some integer expressed as a string of digits, such as "42", the expression int(num) extracts this number.
- What about **semantically nonsensical** expressions such as **int("Hello")**? When an expression cannot have any meaningful possible result, Python **raises an error** instead.
- Python allows optional **type annotations** that can never affect the compilation or execution of the code itself, but make it possible for outside tools such as <u>mypy</u> to perform additional **static code analysis** and other computations.
- Type annotations also make it clear to the human readers that, for example, some function is supposed to receive a text string as an argument, but never an integer or a dictionary. This could be written as a comment, but a type annotation is harder to miss or to be interpreted incorrectly.
- Type annotations go against the Pythonic spirit of flexible **duck typing** in which the formal type of the object should never be important, but the **capabilities** of an object fully determine how you can use that object in your functions. If it "walks like a duck" and all that, that object can be given to any function that expects a duck, since that object is "enough of a duck" so that treating it as if it really were one will never lead anybody astray.

1.6. Importing functionality from modules

- As exclaimed in its old slogan, Python famously comes with "batteries included". In actual programming you don't want to be constantly reinventing the endless wheels spinning inside larger wheels, but **import** as much of existing stuff as possible.
- The import statement is used to execute the script (whose name is given without the filename extension .py) so that the names created in the script are stored in a new namespace that becomes a module object in your current namespace.

- To access a name inside some module object, use the form module.name. The same syntax can be used to access a name inside any object. Modules are also objects inside Python, the exact same way that integers, strings and files are objects.
- Python is in fact even more flexible than that, in that **every user-defined object contains an internal namespace** in which new names can be freely added and removed. Objects and their properties can be modified during runtime in near complete anarchy, so that "do what thou wilt" shall be the whole of the law here.
- If some statically typed language weenie vehemently insists that all computational structures should be set in stone at compilation to shave down a few microseconds from the computation time and let him sleep more soundly at night not fearing any runtime type errors ever crashing his program, just respond "Types, schmypes!"
- (As you can see, the author's jokes tend to come from a culturally different milieu. The current young and hip generation can instead apply their own ultimate pragmatist retort "ha ha virtual machine goes brrrr".)
- For example, complex number objects have internal names real and imag that allow you to access the real and imaginary parts of the complex number.
- Sometimes these internal names inside objects refer directly to the value itself, and sometimes to a function object that computes the value on command. In the latter case, make sure to actually call the function with its arguments between parentheses.
- Python does not offer any kind of proper **encapsulation mechanism** to force some names to be **private** so that they can't be accessed from outside the object. Almost every other programming language from the last three decades offers such encapsulation, but Pythonistas tend to take a more jovial attitude of being friends and consenting adults.
- For names defined inside module objects and other objects, the naming convention of **starting a name with an underscore** informs the reader that the name is an internal implementation detail that should not be accessed from the outside, at least not without a good reason. The outside entity that makes the choice to access such a name then takes the responsibility of whatever side effects and future incompatibilities this shortcut may cause and what kind of **technical debt** it will accumulate down the line.
- Using a **double underscore** is even more common, as this makes the name to behave properly in **class inheritance** that we will talk about in the last lecture. In fact, you can use a double underscore to denote a name that is intended to be an implementation detail, passing the buck of responsibility for all the consequences of accessing that name on the shoulders of whoever voluntarily chooses to do so.
- If you need only some particular function from a given script, you can use the alternative form from Foo import bar, where Foo is the name of the script, and bar is the name that you wish to import. The script is still executed first in a separate namespace, but afterwards, the name bar is created to your current namespace and set to point to the same object that the name points to inside the module namespace.

- The wildcard version from Foo import * imports all names defined by the script. However, you should use this form only if you are certain that none of the names of the module clash with the names that you already use, since all the names inside that module are flooded into your current namespace. In practice, this form is only ever used in the REPL, never in scripts, and modern IDE's will even mark it as a style violation.
- The import mechanism keeps track of the previously imported modules. If some module is imported the second time, the mechanism simply uses the previously generated namespace. (This discipline ensures that any internal initialization logic essential to the proper working of that module is executed only once.)

1.7. Dealing with floating point numbers

- Important library modules such as math provide functions needed in many programs. (For complex numbers, there is an equivalent library cmath.)
- Python stores decimal numbers internally using **floating point** in 64 bits per number. The floating point is an excellent way to **approximate** a wide range of decimal values with dynamic precision that gets less granular the further away you get from zero.
- When performing arithmetic calculations, the floating point arithmetic will always produce the representable result that is closest to the true result. This error is so small that it does not matter when the result is rounded to a reasonable number of decimal places and shown to the human user, but matters quite a lot when these results are compared both to each other and to the expected ideal results of these computations.
- The floating point encoding cannot represent exactly some numbers that we humans would consider "simple". For example, the expression 0.1 + 0.2 does not equal 0.3, but equals 0.30000000000000001 instead. This is because none of the three seemingly simple values 0.1, 0.2 and 0.3 has an exact representation in floating point using base two, even though they are trivially representable exactly in base ten.
- Even worse, floating point operations are not **associative**. For example, the expression (0.1 + 0.2) + 0.3 gives a different result than 0.1 + (0.2 + 0.3).
- This is not Python's fault, but inherent in the floating point encoding itself. All floating point arithmetic is done on the processor hardware anyway, with Python merely reporting the outcomes. Changing the encoding would not help either; using 64 bits, there exist at most 2⁶⁴ representable values out of the infinite continuum of real numbers, so the vast majority of real numbers cannot possibly have a fixed size floating point representation.
- (Yes, Virginia, there also exists an infinity of integers, but unlike real numbers, **integers** are **discrete**, so we can provide a unique encoding as bits to each one up to some arbitrary but fixed limit. The higher you make this upper limit, the more bits you need to encode each integer value up to that upper limit.)

- No matter what base b you choose to encode your numbers in the fraction 1/n can be exactly represented in base b only if all prime factors of n are also prime factors of b. With computers, b = 2. (In the sixties, Russians reputedly experimented with **ternary** base b = 3. Fill in your own "In Soviet Russia..." joke in the style of Yakov Smirnoff.)
- The floating point encoding also has special values for **positive and negative infinity**, and the special value NaN ("not a number") to indicate that the arithmetic operation does not have a meaningful result.
- The library module decimal defines the data type Decimal for arbitrary precision decimal numbers expressed in base 10. The Decimal data type is even smart enough to understand the concept of **significant digits** of a number, so that the nominally equal values 0.5 and 0.5000 produce different precision results in arithmetic operations.
- Another module fractions defines the datatype Fraction for exact integer fractions. For example, 3 * Fraction(1, 3) equals exactly 1, not one iota more or less.
- To generate random numbers from uniform distributions or to sample and choose random items from sequences, use the functions defined in the library module random.
- The modules datetime and calendar define data types and functions for calculations on dates and times, often needed in applications that deal with things in the real world.
- The modules os and sys define functions that allow your code to access the underlying computer and its file system.

Week 2: Functions that make decisions

2.1. Defining your own functions

- A **function** is a **named block of statements** that performs some operation that we intend to perform more than once. Functions are objects in Python, and can therefore be assigned to names the same way as strings or integers.
- Function objects are defined using the special def statement that first creates the function name in the current namespace, and then immediately assigns this name to refer to the object that contains the function body **compiled** to a more efficient internal form.
- Whenever some function is **invoked** (**called**), the statements in its body are executed in the order that they were written into the program source code. The function object acts as a **black box** that hides its internal implementation from the caller who cares only about the results produced by that function, but not the mechanism that produced those results.
- As long as the caller receives the correct result in a reasonably speedy fashion, that caller shouldn't even think about how exactly the function produced that result, but can think of each function as if it were some brand new statement in the language itself.

- When you write functions, you essentially extend the language to contain higher level operations that can then be used to define even higher level operations, thus building a complex program bottom up from simpler pieces that you are able to understand in isolation. This is important once the problem domain becomes so big that it is impossible to implement as a single function, but must somehow be sliced into smaller pieces.
- A function can expect to receive **parameters** from the caller, who must provide the actual values to be processed during that particular call as **arguments**. In the next call, the function can receive different arguments.
- The caller is responsible for providing arguments that are meaningful for the function and its execution. Unlike some other programming languages, the Python language has no mechanism to enforce this in the source code level. In practice this is never a problem, at least in any seriously designed and implemented real world program.
- Even when some function takes no parameters, the syntax for its call still requires the empty pair of parentheses, since the function name itself is just a reference to the function object in the memory. Applying the parentheses to the function object can be thought of as the ignition key to make that function to execute, whereas the name itself is a mere acknowledgment that the function object exists in the first place, sitting pretty in the memory waiting for somebody to give it something to do.
- Named parameters can be given **default values** to be used when the caller does not provide a value as argument for them.
- In Python, every function will **return** some result at the end. If no result is explicitly returned with a **return** statement, the special value **None** is automatically returned.
- The return statement can also be used to conditionally terminate the execution of the function body as soon as the result becomes certain, without need to fool around until the execution reaches the end of the function.
- Any names defined in the function body are created in a **local namespace** of the function that exists only during that function call. This namespace ceases to exist when the execution returns to the caller, assuming that there are no names in the caller's namespace that either directly or indirectly refer to the names of the local namespace. (If there are such names, perhaps inside the function object created in and returned from the function, the namespace continues to exist in memory as a **closure**.)
- The keyword global used inside a function causes its following name to be created and accessed in the global namespace.
- If the first statement inside a function is a triple quoted string, it is treated as a **docstring** that documents what the function is supposed to do. Many editors and other programming tools can properly handle and display function docstrings automatically.

2.2. Simple two-way decisions

- Most functions need to be able to make **decisions** so that they behave differently in different situations. **Two-way decisions** are the fundamental building blocks that all computational operations are internally composed of.
- Within the hardware of the computer processor and memory, all operations such as adding two integers or comparing them for order internally break down into two-way decisions executed by the electronic logic gates as the laws of physics dictate.
- A problem is computable if and only if it can be broken down into a tree structure of two-way decisions, possibly looping back to an earlier decision. **Flowcharts** are a more human-friendly way to visualize such a decision structure, often leading to humorous conclusions if intended to be read by humans instead of being executed by a mindless machine.
- In high-level languages such as Python, same as in almost all other programming languages, two-way decisions are created with the if-else statement.
- The if-else statement executes **precisely one of its two branches** depending on whether its **condition** is True or False at the time the execution enters the statement.
- Often, there is nothing to do when the condition is False. The else-branch is optional and can be left out altogether in such situations. Otherwise, since the syntax of Python does not allow an empty block of statements, the do-nothing statement pass would have to be used to serve as filler, in spirit of those self-refuting "This page intentionally left blank" proclamations in printed books and documents.
- To choose from three or more possibilities, this decision tree must be somehow broken down into simpler two-way decisions. This can **always** be done in many different ways, either nested or sequential, that are equivalent in the results that they produce. Your programming and thinking styles ultimately determine which of these equivalent ways to organize a **decision tree** you end up writing.
- As an additional shorthand to embed a small two-way decision inside a larger statement, you can use expr1 if cond else expr2 that evaluates to either expr1 or expr2 depending on cond. (This roughly corresponds to the **ternary selection operator** found C or Java or similar languages.)
- Technically, the expression used as a condition does not have to evaluate to either True or False, but can be a value of any type. Other data types have predefined rules for which values are considered "truthy" and "falsy" depending on which result the conversion function bool produces from them.
- For numerical types, zero values are falsy, others are truthy. Empty lists, sets and dictionaries are falsy, and all others are truthy (yep, even the singleton list [False]).

- In many situations, writing the comparison out explicitly such as x != 0 instead of being maximally terse by writing just x to test whether an integer x is nonzero makes the code harder to misunderstand.
- On the other hand, if x is already a proper truth value, beware the common pointless redundancy of writing the test in the form x == True. The simplest and clearest way to test whether x == False is to write not x.
- The special value None is always considered to be falsy. This allows the handy Python programming idiom of defining some function to take an optional argument whose default value is None, and then treating the argument as a condition inside the function to cause special behaviour if and only if the caller provided some value to that argument.

2.3. Outcomes of equality

- Truth-valued conditions can be created with the comparison operators <, >, <=, >=, == and != that compare the operands given to them. Note that the equality comparisons are done with == instead of =, since the latter operator already stands for assignment.
- The **Unicode** character set, of course, contains the comparison operators familiar from math textbooks, but the syntax of Python predates the Unicode standard and uses only characters that existed among the 128 characters of the original **ASCII** encoding.
- The same silliness remains in basically all programming languages today. If only = stood for equality like it does everywhere else in our lives, and assignments were denoted by some kind of left arrow character to make it plain for all what happens...
- Python 3.8 introduced :=, the humorously named walrus operator. Reminiscent of **pseudocode** examples seen in printed textbooks from the last century, this symbol unambiguously means that an assignment is intended, not a comparison. This allows the "chad" walrus operator to be used inside comparisons, unlike the "virgin" = operator.
- The operator == compares its operands for their content, not their identity. The is operator checks whether its two operands are the very same object in the same memory address. The test a is b could always be equivalently written as id(a) == id(b).
- Be especially cautious in the minefield of comparing floating point numbers for equality. The best practice is to use floating point numbers only in situations where they are understood to be approximations.
- However, the moment that equality comparison affects the logic of the rest of the program, the entire situation changes. Any program that, for any reason whatsoever, performs an equality comparison between results of floating point arithmetic operations is fundamentally broken inside, and cannot be fixed except by a complete redesign.
- Etch that one in your memory, and remember it for the rest of your days.

• Even if you consciously avoid using any floating point arithmetic, you might still accidentally end up creating floating point values by using the floating point division operator / to divide an integer by another integer, instead of the correct integer division operator //. Oh, how we all wish that those two operators were the other way around...

2.4. Complex conditions

- Python allows comparisons to be **chained**, in style of a < b < c > d, instead of having to use the logical and operator to combine individual comparisons. In most of the other mainstream programming languages, such conditions have to be broken down into a series of individual conditions, as in a < b and b < c and c > d.
- Condition chaining is a special case of building complex conditions with the **propositional logic** operators and, or and not.
- Same way as multiplication has a higher **precedence** than addition, logical and has a higher precedence than logical or. It is then often useful to clarify your intention with parentheses to make the structure clearer for human readers.
- Unless your logic was redundant to begin with, the two operators and and or are never interchangeable. Replacing one operator with the other one will always change the behaviour of your function for some argument values.
- The operator and has a higher precedence than or, and not has the highest precedence, so the machine will have no difficulty deciphering the expression without ambiguity. Even so, it is never wrong to add redundant parentheses to an expression to clarify your intent about what that expression should do.
- The Python compiler uses parentheses only to direct its **parsing** algorithm, and the parentheses do not appear anywhere in the generated low level executable. Human readers, on the other hand, benefit from the refreshing extra clarity.
- Both operators and and or are guaranteed to **short-circuit** so that if the first operand already determines the result, the second operand will not be evaluated at all. This is very important if the second operand has **side effects**, or could potentially crash the program.
- All the discrete math intro stuff about **propositional logic** is in full effect here. Most importantly **De Morgan's rules** for simplifying negations and double negations, since those could become as tricky in programming languages as in our natural languages.

2.5. If-else ladders

• A multiway decision from a known fixed number of possibilities is often best written as an **if-else ladder**, a generalization of a single if-else, with the keyword **elif** denoting the individual steps from the second step onwards.

- Writing multiple if-statements separately in sequence makes them all to be executed independently of others, so that none of them, all of them, or anything in between, could be executed. In an if-else ladder, exactly one of the steps will be executed.
- When the execution of a script reaches the if-else ladder, its conditions are evaluated in the order in which they are listed in the source code. The first condition that is True decides which branch is executed. The execution then skips all the remaining branches, even the ones whose conditions also happen to be True.
- The order in which you write the steps of the if-else ladder is therefore immensely important. Rearranging these steps will usually change the behaviour of the ladder and the function that it computes.
- During the design of an if-else ladder, each step and its condition can be written while enjoying the airtight guarantee that all previous conditions have been False. (Had any one of them been True, the execution would not have reached the current step!) Therefore, you don't need to test anything that you have already tested in the conditions of the preceding steps. Knowing this may allow you to simplify the later conditions, especially if you arrange all the steps in some clever way to begin with.
- An if-else ladder whose last step is not an unconditional else is perfectly legal, but it still seems a bit hinky, and is often somehow wrong. (This is not an airtight rule either, though.) Such a ladder will then behave as if there really were an unconditional else branch at the end whose body simply does nothing at all.

Week 3: Sequence types string, list and tuple

3.1. String literals from Unicode characters

- In reality, all computers merely store and move around small integers as **bytes** inside the computer memory. Any other types of data must be internally expressed as **aggregates** of bytes.
- Standardized ways of doing this exist for often needed data types of **floating point decimal numbers** and text strings. All these details are taken care of by the computer processor so that you normally don't need to think about them while writing Python.
- Unlike its predecessor, Python 3 represents characters and text strings internally in **Unicode** to guarantee portability of text processing between computer systems. The exact internal representation of these Unicode strings is hidden from Python programmers, who should not worry about it anyway in the first place.
- To create a **text string literal** inside an expression, write characters between a pair of either **single** or **double quotes**, such as 'Hello there' and "I'm here!"

- Escape sequences starting with the backslash character are a standard way to include special characters inside text strings. The most common escape sequences are \t and \n to produce tab and newline characters, and \" and \' to embed a double or single quote character inside a string that was delimited in the source code with that quote character.
- To embed an arbitrary Unicode character inside your string, use the extended escape sequence "\uXXXX" where XXXX is the Unicode codepoint of that particular character expressed in four digit **hexadecimal**, amply available on Unicode tables online. For emojis and other characters in the higher planes, use the form "\UXXXXXXXXX".
- String literals delimited with **triple quotes** can span multiple lines. Line break characters (yes, they are characters just like any other Unicode character) are taken as part of that string literal that continues until the closing triple quote. These are most commonly seen in **docstrings** of functions as the do-nothing first line that becomes the documentation.
- The <u>bytearray</u> data type of Python grants you access to the bytes in memory. Unicode strings can be converted back and forth to byte arrays with their methods decode and encode. This lets us take a peek at how exactly the Unicode characters, each needing between one and four bytes of memory to store, are stored inside a Python string.

3.2. String literals from arbitrary pieces

- The easiest way to build up a long string from smaller pieces of strings is to use the operator + to concatenate these pieces together, in the style of Java language.
- Especially useful for console output, **formatted strings** with the f prefix replaces **format placeholders** denoted inside the string with curly braces with the evaluated value of the expression inside the braces. These are most commonly seen inside a print statement, but they can be used anywhere that you want to define a string literal.
- When printing out floating point numbers, always **round** them to some reasonable number of decimal places. For example, print(f"{0.1 + 0.2:.1f}") correctly prints 0.3, even though the actual computed result is something slightly different.
- Alternative ways to achieve the same thing would be the old-time C-style string interpolation with the % operator, which for string objects means format substitution instead of integer division remainder, or using explicit Template instances.
- Since text processing is so important in computing, Python strings have a ton of operations built in the language and as methods inside the string objects, as demonstrated in the example scripts. Furthermore, the library modules string and re (for regular expressions) provide even more powerful operations.
- For purposes of output, non-string objects such as integers, truth values and higher level entity objects can be automatically converted to a string representation for human consumption. For example, the integer object 42 is converted to a two-character string "42" when printed.

- Make sure that you understand that **the string representation is used only for output**, but the integer object 42 in memory does not consist of any characters at all, but the bytes that encode an integer value consist of something entirely different!
- To explicitly convert any object to a string representation, use the built-in function str. Again note that this function does not modify the content or the type of the original object, but produces a whole new object as result of conversion.
- Alternatively, the function repr produces a string that when evaluated as an expression using the built-in function eval, produces an object that is identical to the one whose representation was acquired with this function call.
- However, the repr function cannot always be meaningfully defined for all objects. Python convention to document this fact to the users of this function without raising any kind of error is to begin and end this representation string with angle brackets, to guarantee that any attempt to evaluate this string will crash with a SyntaxError.

3.3. String slicing

- Any desired part of the string, or any other **sequence** data type in Python, can be extracted by **slicing**, denoted with the **square bracket** operator.
- Inside the sequence, the character **offsets** from the beginning are numbered starting from zero, since the first character is located zero steps away from itself. For example, the five-character string "Hello" has five possible offsets 0, 1, 2, 3, and 4.
- The last legal offset is therefore always exactly one less than the length of the sequence. If the sequence is empty, it has no legal offsets at all to access its elements.
- To extract a single character from a string, use square brackets with just one offset. To extract a longer substring than just once character, give the **start** and **end** offsets separated by a colon character to create a **slice**.
- Note that **the end offset of a slice is exclusive**, one step past the last character that you want to include in the slice. This initially perhaps a rather strange counting convention simplifies the mental arithmetic on these slices, such as computing the length of the slice without any danger of **fencepost error** to create an **off by one error**.
- ("If a fence is 50 meters long and has a post at every 10 meters, how many posts does that fence contain altogether?" Nope, the correct answer is not the obvious five that nearly everyone will instantly and confidently blurt out. But walk along the fence mentally and count all those dang varmints again, using your fingers if you have to.)
- Negative offsets would be impossible by definition, akin to asking "What letter comes before the letter A in the English alphabet?" Python has therefore chosen to use these negative offsets to count the **positions from the end** instead of the beginning. For example, the expression "Hello" [-4:-1] evaluates to "ell".

- Even when using a negative offset to tell the slicing operator what you want, the end index of a slice is still exclusive, so be careful with that.
- Step size can be given as third operand to slicing, with the negative step size defined to iterate the elements in reverse order. For example, "Hello"[0::2] evaluates to "Hlo", and "Hello"[::-1] evaluates to "olleH", this being the canonical way to reverse the given Python string.
- (To iterate through a reversed sequence without creating a separate copy of it, use the sequence decorator reversed.)
- When using the colon character, leaving out the start offset means to start from the beginning, and leaving out the end offset means to continue all the way to the end. For example, 'Hello world'[3:] evaluates to 'lo world'. Leaving out the start offset similarly means "all the way from beginning".
- For strings and lists, slicing operates on the principle of **random access**, meaning that it will need the same amount of time to access the first element as it needs to access the millionth element.
- Many lazy sequences do not allow random access to their contents, but only the operation of producing the immediate next element. There are no no boats, no trains, no planes that would take you directly to the millionth element, but the only way to get there is to walk on, one step at the time.
- Since Python string objects are **immutable** (that is, their content cannot change after object creation), slicing will always create a separate string object to represent the result. The original string object still continues to exist as the unbroken original whole.
- Immutability of data has several surprising benefits in programming. For example, string objects created by slicing and dicing, theoretically even by concatenating, could share the underlying bytes that are set in stone, instead of redundantly duplicating these bytes for everybody. This makes many operations such as slice extraction more efficient in time and space.
- Unfortunately, immutability also has one huge general downside, which is why all data types in programming are not made immutable, at least outside the beardy school of thought of pure functional programming. If some program needs to iterate through some large range of possible values, all data being immutable would require creating a separate object to memory for each value during the iteration.
- With mutable data types such as lists from the next section, the same memory bytes can be reused to store each value one at a time, and the program does not run out of memory even if it were iterating through trillions of values inside some loop.

3.4. Lists made of things

- If all names in Python could only ever refer to **scalar values**, it would be practically impossible for some program to handle millions or even billions of items of data that it reads from the outside world, since each data item would have to be talked about using a separate name that is distinct from all other names. Nobody would have the time or patience to type in all those millions of names in the program, and even if they did, there would be no point in doing that anyway.
- Every programming language needs to have some mechanism to store an arbitrary large number of objects under a single name. In the Python language, **lists** are special objects that contain an entire **sequence** of **object references** inside them.
- Python lists are **heterogeneous** so that the same list can simultaneously contain objects of different types. These objects can even themselves be lists, resulting in a **nested list** or a **multidimensional list structure**, depending on how you wish to view it.
- Python lists work like **random access arrays** of other programming languages so that an element at any position can be read and written in the same constant time. However, unlike the immutable strings, Python lists are **mutable** in both length and content.
- (The term "random access" would be more accurately called "arbitrary access" since there is nothing "random" about it in any meaningful sense of that word, but this barnacle is already established in its inaccurate form. I am *literally* foaming in my mouth at this insanity that ought to make Noah Webster spin in his grave.)
- The internal implementation of Python lists is optimized for appending new elements to the end by maintaining an unused "slack space" as room for additional elements. Once this slack space runs out, Python allocates more room in some other corner of the memory, and copies the data stored inside the list there.
- Trying to slice out a substring out of bounds is not an error in Python, but this operation simply treats the nonexistent part to be the empty string. For example, the rather optimistically indexed expression "Hello"[2:100] would evaluate to "llo".
- The built-in function len tells you the length of the sequence that you give it.
- The canonical trick to create a separate but identical copy of the list a is to say a[:]. This is mostly used in situations where you want to iterate through the elements of the list while simultaneously modifying its structure. Since that would create all kinds of wacky and unintentional misbehaviour, you follow the letter and the spirit of the law by iterating through the elements of the copy whose contents you never modify as you mutate the original, so that these modifications do not affect the logic iterating through each original element exactly once.
- However, note that slicing and copying a list creates a **shallow copy**, meaning that the references stored inside the result still point to the same original elements as the

- references inside the original list. Whenever those outside elements are **mutable**, modifying their state through one of these lists makes these elements to also have changed when they are viewed through the other list.
- To create a separate **deep copy** of not just the list but its elements, use the function **deepcopy** in the Python standard library module <u>copy</u>. It is rather unlikely that you will be needing this operation in this course, but still, all grizzled and salty programmers have to grok the difference between a = b, a = copy(b) and a = deepcopy(b).)
- Python lists are also more flexible than **arrays** of other programming languages in that they can be **concatenated** and **extended**. A common programming idiom in writing a function that returns a list of answers is to initialize the local answer list to be empty, and then **append** individual solution elements to that list whenever a new one is found.
- Note again that it must be possible for a list to be empty, if no solutions exist. There must exist some way for a function to effectively say that "Your question is perfectly legal and valid, buddy, but unfortunately, there are zero solutions to what you are looking for, so this empty list is what I shall return as my answer to you now."

3.5. List comprehensions

- **List comprehensions** are a handy technique to create lists in a concise way inspired by the mathematical notation used in set theory in math textbooks, by converting the values from an existing iterator or sequence into another sequence, possibly filtering out some elements along the way.
- In most programming languages, programmers often have to shoulder this work by writing explicit **for-loop statements** that iterate through the elements one by one, choose some of them inside the loop with a conditional statement, and **append** the results into an initially empty result list. List comprehension does all that in one swift swoop.
- A list comprehension needs some existing list or other sequence to act as a **source of elements** that the actual list comprehension will then **filter** and **modify** in a way that you can freely specify to create a whole new list for the result.
- The syntax of list comprehension consists of square brackets, followed by three components of (1) the expression used to modify each element, (2) the **for-block** to iterate through the elements of the existing sequence, and (3) the **if-block** to filter out the elements that we do not wish to process but skip out entirely.
- The lazy iterator of integer objects range is often used as the source sequence. For example, the comprehension [x*x*x for x in range(1, 11)] would produce the list of cubes of the integers from 1 to 10.
- As seen in the previous example, **the if-block is optional** when no elements are filtered from the source sequence. The result of such list comprehension without an if-block will then necessarily have the same length as the original underlying sequence.

• A list comprehension can contain more than just one for-block. That expression will then go through all possible combinations of the individual values produced by the individual for-blocks. Assuming that the first for-block produces 8 elements, and that the second for-block produces 5 elements, the resulting list will contain a total 8 * 5 = 40 elements for all the possible combined pairs between these two sequences.

3.6. Nested list comprehensions

- Same as all expressions in Python, list comprehensions can be **nested** to arbitrary depths to create **nested lists**, that is, **lists whose elements are themselves lists**.
- In computer programming, a two-dimensional grid of values is typically represented as a list of rows, each one itself a list of elements in that row.
- For example, [[x+a for x in range(3)] for a in range(4)] would produce a list whose four individual elements are themselves lists that contain three elements each, generated by the nested list comprehension.
- Note how very different the previous expression is when compared to the deceptively similar expression [x+a for x in range(3) for a in range(4)] that produces a list that contains twelve separate integers as its elements, as opposed to four lists that each contain three integers. You should meditate on the difference between these two examples until you understand why exactly they are different.
- That second expression also demonstrates the order in which these for-blocks advance through their values. The second for-block goes through all its values before the first for-block advances one notch forward, at which point the second for-block goes back to beginning to go through all of its values once again from the beginning.
- To make this example more intuitive by using an analogy of an ordinary clock, the second for-block corresponds to the minute hand, whereas the first for-block corresponds to the hour hand.
- (If a list comprehension contained three for-blocks, that third for-block would then correspond to the fastest of these three hands, the hand that ticks through the seconds.)
- The comprehension [(h, m, s) for h in range(24) for m in range(60) for s in range(60)] would therefore produce a list with a total of 86,400 elements, one for each second that takes place during one entire day, each second represented as a three-element tuple (hour, minute, second) from (0, 0, 0) to (23, 59, 59).
- The later loop of a nested list comprehension can also depend on the current value of the earlier loop, so that the comprehension [x for y in range(2, 6) for x in range(1, y)] produces the list [1, 1, 2, 1, 2, 3, 1, 2, 3, 4].

Week 4: Sequence iteration

4.1. Sequential processing with for-loops

- Many computational problems performed on a sequence of data can be expressed as performing the exact same computation to every element, one element at the time.
- In computing, the problem is always coming up with a way to do something just once. Once you have discovered some way that works, you can place a **loop** around that code to make it perform that same thing a billion, or however many times you want!
- Complex problems in general are best solved "inside out" by breaking them down into simpler problems, many of which already have functions in the standard library to handle. You will then use loops and functions as a glue to bind these lower level functions into some useful higher-level wholity.
- The **for-loop** is the powerful and flexible Python language feature to automatically execute the **nested body of statements** for every element of the given sequence. The for-loop is **polymorphic** so that the same statement can handle any sequence, be it a list, tuple, string or whatever fancy sequence type somebody will think up.
- In the syntax for elem in items, the term items is the arbitrary sequence to iterate through, and elem is a made-up name that refers to the element that is currently being processed inside the loop.
- The same nested body of statements will be executed for every element in the sequence. However, unlike in a list comprehension, this body can be arbitrarily complex and maintain additional **state** in other variables that will then affect the processing of the current element, whereas list comprehension assumes that the processing of the current element can be done without knowing anything about the other elements.
- Whole bunch of common idioms and techniques abound with for-loops, as illustrated in the example functions, and are hopefully applicable to the graded labs that you will be solving on your own.
- A common situation has the processing of the current element depend on the value of both that current element and the element processed in the previous round. Simply maintain a local name (canonically named prev) that remembers the element from the previous round of the loop. At the end of the body of the loop, the current element is assigned to become this previous element for the next round.
- Sometimes processing either the first or the last element of the sequence has to be done in some special way. This situation is known as "a loop and a half", since we often end up duplicating some of the code in the loop body either before or after the loop body.

- As a general rule, the more of your own code you end up duplicating, the more you ought to feel like being in a state of sin of not solving your computational problem the best way.
- Giving the variable prev some tactically chosen initial value occasionally allows the processing of every element to be done in uniform fashion. (To paraphrase the famous Zen riddle, "What was the value of the previous element back when you were still processing the first element?")
- Python offers plenty of sequence decorators for more advanced processing of the given sequence, such as enumerate, zip, reversed and sorted. These should be used without hesitation to make your code more concise, readable and Pythonic.
- The sequence decorator enumerate should be used whenever the processing of the current element depends on both the element value and its position in the sequence. Writing a for-loop of the form for idx in range(len(items)) and then using idx inside the loop body to access the actual element has a non-Pythonic feel akin to C, Java and other such low-level languages where such nitty-gritty drudgery was the only way to access the elements of a sequence.
- Since the body of the for-loop can contain any statements, other loops can be nested inside the loop body, same way as with nested list comprehensions.
- Among others, the itertools module has a handy function combinations as a more succinct alternative for using two nested for-loops to iterate all possible ways to choose exactly k elements from the sequence, with k=2 iterating through all possible pairs of elements.

4.2. Iterator objects

- Real programs have to be able to handle millions, billions or possibly even trillions of items of data. Python 3 unifies this logic for various types of data with the ubiquitous concept of lazy iterators that permeate the language in a highly useful form behind the scenes, the same way that everything in Python is an object even though we don't need to talk about this in the language itself.
- An iterator is a special kind of object that has the ability to produce a sequence of
 objects on command, one object at the time. This implicitly generated sequence can be
 arbitrarily long, even infinite. Since the generation of these objects is lazy so that the
 next object of the sequence is generated only when it is explicitly requested, this process
 will not run out of memory even for infinitely long sequences.
- In computer science and programming, being "<u>lazy</u>" is usually a good thing and a term of endearment to indicate that somebody is doing exactly what is required and not one inch more. (In fact, perhaps we ought to call such programs "elegant" or "optimal", as much as we dislike actual people who try to optimize their actions in a similar manner.)

- Every iterator object remembers its **internal state** of where it currently stands in the production of its sequence. Even if the execution of the program moves on to do something else altogether, the iterator object will sit there paused in memory, waiting for somebody to ask for the next value in its generated sequence.
- The sequence of objects produced by an iterator can even be empty. This is an important possibility in all programming that many non-programmers tend to have difficulty in grasping. Unlike in real life where everything is always designed for there being one or more items to process, program logic needs to correctly handle the edge case possibility that there really turns out to be nothing to do.
- Whenever there is nothing to do, the correct thing is to do nothing. (Meditate upon this seemingly simple but very important principle a few times.)
- As a downside, iterators do not in general support random access operations such as slicing and indexing the elements of the sequence at an arbitrary position or position slice, but the elements must be generated and processed in strict sequential order. To find out the element in some desired position, all preceding elements must first be produced one by one, with no "royal road" leading directly to the desired element.
- When writing functions that operate on sequences, stretch as far as you can to only use
 operations that maintain the laziness of the argument sequences, such as for and
 enumerate. Using len or the square bracket slicing, the two most common offenders in
 this respect, usually forces the lazy sequence to become explicit, potentially filling your
 process memory with all the elements of that sequence.
- For the same reason, iterators in general cannot know how many more items they will be producing, and therefore cannot respond to the len function call asking this.
- Once an element has been consumed from the iterator sequence, it is gone for good, since no memory is wasted storing the elements that the iterator has previously produced. Iterators in general do not support **rewinding** or restarting the sequence, but an entirely new iterator object has to be created.

4.3. Integer sequences as range objects

- Proper style of writing functions in Python is to have them take iterators as arguments, without having to care of exactly what type iterator the function receives. Such parameter polymorphism makes functions more powerful and flexible, instead of having to write separate functions for different types of data.
- Python's built-in function range creates and returns an object that produces an integer sequence one number at the time. The arguments for range, separated by commas, work exactly the same as for the string slicing operator. (Given just one argument n, range produces the sequence 0, 1, ..., n 1.)

- Additionally, you can give the sequence step size as the third argument to range. Using a negative step size makes the sequence count down instead of up. For example, the call range(5, 0, -1) would produce the sequence 5, 4, 3, 2, 1, the end value again being exclusive.
- <u>Surprisingly in Python, range objects are not technically iterators</u>, but can always be turned into one by calling the function iter.
- Any iterator can be explicitly asked for its next item of the sequence with the Python built-in function next. If the series generated so far is complete so that no more values remain, this function raises the StopIteration error.
- In practice, for x in iter is the standard way to execute a **body** of statements once for each value produced by some iterator iter. Inside the body, the name x will then contain the current value of the sequence that is being **processed** by the **loop**.
- The common idiom for x in range(n) will execute its body exactly n times. This is useful for problems where you know exactly how many steps you need to take to reach your intended goal, the same way a human would do if asked to repeat some operation for, say, exactly five times.
- These range objects are even smart enough to use integer arithmetic to quickly deduce that -1 not in range(10**100), and that len(range(10**10)) == 10**10. In general, answering these same questions for arbitrary lazy iterators requires producing all objects one at the time to find out what happens, but the special case of range is easy enough to handle with integer arithmetic.
- However, since the following quantities can be easily computed with integer arithmetic, range objects can implement len and slicing efficiently while maintaining their laziness. Most lazy sequences are not equally fortunate.
- The built-in function list can be used to build the full list of the elements that its argument iterator produces so that all these elements exist in memory simultaneously. This should be used with care, basically only when the range needs to become mutable for some reason.
- Unlike an iterator that steps through the values one at the time, this conversion can run out of memory in situations where the iterator produces a long series of objects, since all these objects will have to exist simultaneously in separate memory locations for the entire list to exist. (A couple of billion objects would surely suffice, even in our current petabyte age.)

4.4. Files as sequences

• Names and objects inside the Python interpreter cease to exist when the Python interpreter terminates. Real programs need to be able to store data in some **persistent** fashion, typically into a file, so that the data outlives the process that created it.

- Following its "batteries included" design philosophy, Python makes reading and writing text files easy. To open a file for reading or writing, use the built-in function open that returns a **file handle object** that represents the file inside the Python interpreter.
- When opening a file, the keyword argument encoding can be used to choose how the raw bytes of the file are interpreted as Unicode characters. In practice, the most common and space-efficient character encoding is UTF-8 that uses only one byte per characters and punctuation that normally occur in English text, but allows other Unicode characters to be included freely with multibyte sequences where necessary.
- Conveniently for reading text files one line at the time, the file object can work as an iterator that produces the lines one at the time. However, since the line break character is included in the string that contains the current line, we often use the string method strip to eliminate the redundant whitespace characters from the edges of the string.
- For more sophisticated processing of files, the file object has methods that can be used to move around the file, and read and write characters and bytes into the file.
- When a file is opened, the file system **locks** it so that other processes in the computer cannot access it. This prevents files from being corrupted by multiple processes trying to read and write them simultaneously. When you are done with the file, you should call the method close to give up the lock.
- Note that close is a method name that exists inside the file objects, instead of a Python built-in function in the same vein as the function open.
- As a superior alternative these days, Python's compound with statement that allows declaring a **context manager**, a local name that exists only for the duration of the nested block of code, is perhaps most often used with file handling.
- The same construct can be applied in any situation of the form "acquire a resource, use that resource, then release that resource no matter how things went during the acquisition and use". As those British like to say, "Let George do it!" (Or their classic answer to the trick question about the command sequence that a freshly minted second louie should issue to get a flagpole erected: "Sergeant, erect that flagpole!")
- The with statement guarantees that the file will be closed automatically after this statement no matter which way the execution leaves the body of the with statement, even if the nested body of this statement throws some error during its execution.
- (Interested students can check out the article "Context Managers" at Python Tips that explains what context managers are in general and what they are useful for, and how you could even write your own context managers using generators and classes that you learn later in this course.)

4.5. Tuples as immutable sequences

- Sequences of fixed size whose contents are intended to be immutable are often more memory-efficient to represent as **tuples**, which are syntactically denoted by separating the elements with commas.
- Tuples are still heterogeneous, and can contain any kinds of elements in them. These elements could even themselves be tuples, but keep in mind that the structure will make a difference even when the "bottom-level" elements would otherwise be equal.
- The tuple (42, 99, 17) contains three elements, whereas the tuple (42, (99, 17)) contains two elements, the first one an integer and the second one another tuple made of two integers. Neither tuple is also equal to the tuple (42, 99), 17).
- Most of the time ordinary parentheses are placed around the tuple elements, but in many cases this is optional. Using parentheses is strictly necessary when creating a **singleton** tuple such as (42,), or when a tuple is passed as an argument to a function, to distinguish between the commas that separate the tuple elements from the commas that separate the function arguments.
- It never hurts to use parentheses around a tuple or, for that matter, around any ambiguous expression to clarify your intention to the human reader of the source code, even when there is no ambiguity in the language rules.
- Tuples are **random access sequences the same** way as lists, so all non-mutating operations work for them the same way as they do for lists and other sequences.
- In practice, tuples tend to be much shorter than strings, lists and other sequences types due to their typical use cases. For example, we would represent a playing card as a pair of (suit, rank), and three-dimensional coordinates as a tuple (x, y, z).
- The language does not set any limits to the size of a tuple any more than for lists and other sequences. It just tends to be rather difficult in practice to create a big immutable tuple instance in one swoop with all its elements existing right away...
- The important **zero-one-infinity principle** of software engineering says that once two of something is allowed, the language should not set any kind of limits to that something. This principle can be observed in action in many places in computer science and programming.
- Only the tuple object itself is immutable; the objects that it contains do not magically also become immutable due to their containment inside some tuple. In general, since objects only ever contain references to other objects, the same object can simultaneously be "inside" many objects. (Unlike with those Russian nesting dolls, some sequence object could even be its own member without any paradoxical consequences!)
- All references are unidirectional in memory so that there is no mechanism to efficiently list all the tuples and lists that some object is presently inside of. You can find

out with sys.getrefcount(obj) how many references are currently pointing to obj, although this count does not specify what those names are and where they are stored.

4.6. Breaking tuples into components

- A handy quirk of the Python language is that multiple assignments can be performed in a logically simultaneous fashion with assignment into a tuple made up from the names to be assigned. For example, swapping the values that the two names x and y are currently associated with can be achieved in a single swoop with the assignment x, y = y, x without having to use a temporary third name tmp to first store one of these values.
- (In other languages, a weird unwritten law requires that third variable be named tmp.)
- Tuples and other sequences can be order-compared with each other. This ordering is done **lexicographically**, that is, in **dictionary order** so that the first position where the two sequences differ determines their ordering, regardless of the remaining elements. For example, 'aardvark' < 'zebra', and (9,) > (1, 2, 3, 10**100).
- This rule for ordering between sequences will come especially handy when **sorting** elements with a **key** function that uses multiple comparison criteria expressed as a tuple whose first element is the primary key, second element is the secondary key, and so on.
- Of course, comparison of two tuples can work only if their components are pairwise comparable. Asking whether (42, 99) < ('hello', 'world') would only cause a runtime error with the impossible comparison 44 < 'hello'.
- Sometimes we would like to "break up" a tuple into its individual components, typically when we want to pass those components as separate arguments to some function.
- Suppose some function foo takes three parameters, and a = (42, 17, 99). Once you get used to the asterisk character not automatically representing the multiplication operator, the call foo(*a) looks a lot cleaner and more Pythonic than its explicit version foo(a[0], a[1], a[2]).
- This works out even better if foo can accept any number of parameters with the special *args parameter, since then we don't even need to know how many elements the tuple contains to make the call foo(*a), and yet we are still sure that it will work out!
- The unary asterisk operator performs the desired breakdown not just in function calls but also in the parallel assignment so that assigning a, *b, c = (1, 2, 3, 4, 5) works out the same as the assignment a, b, c = 1, (2, 3, 4), 5.
- As an aside, in teaching materials for computer science and programming, whenever some theoretical discussion needs some function to serve as an example, but for the purposes of that example it does not matter what that function actually does, the canonical names to use are foo, bar, baz and qux to instantly tell the reader not to look for any meaning or purpose in this function or its name that would be relevant to the discussion.

- Since these four are essentially **placeholder names** for something whose exact identity is meaningless, these names should never appear in any real program in which everything exists for some purpose and therefore its exact identity and behaviour do matter.
- 17, 42, and 99 are similar made-up placeholder values whenever an integer value is needed for some meta-level discussion. For text strings, the canonical placeholder value is the famous 'Hello, world!'
- (Some wag joked that when quantum computers become commonplace, their first example should be 'Hello, worlds!')
- Other sciences and fields of human endeavour have their own canonical placeholder names used for analogous purposes, such as the term "widget" in economics for some product whose exact identity and purpose does not matter for the discussion at hand.

4.7. Members only

- Many programming tasks become much easier when aided with some cleverly chosen
 data structure to store and represent the data, instead of keeping all your data in one
 unsorted list and then writing functions to plough through this entire list every time that
 you need to do something on some data element.
- Especially useful are **sets** and **dictionaries** that exist as **first class citizens** inside Python, whereas in older languages these concepts existed in the standard library, if even there.
- A dynamic set instance can be created either by calling set(), making it initially empty, or by writing a set literal by listing its keys inside curly braces.
- A set is especially powerful for the operations x in coll and x not in coll that determine whether the set currently contains the given element x.
- Checking whether an unsorted list contains the element x has no choice but to iterate through the entire list and painstakingly compare its elements to x one by one. However, when coll is a set, it has already organized its internal data structures in a far more efficient fashion that allows these element query operations to still work at the proverbial blink of an eye, even if that set has been rammed and jammed to contain hundreds of millions of elements!
- The set data type also offers important **methods** (that is, functions defined inside the datatype, as opposed to being used from the outside) add and remove to modify its contents dynamically, plus many others as documented in the Python library reference.
- (The data type frozenset is otherwise like a set but without any mutation operations, analogous to how the immutable Python tuples relate to the mutable lists.)
- Unlike lists and strings, sets are not sequences, so they cannot be sliced or indexed. The question "What is the seventh element of this set?" is nonsensical from the get-go.
- A given set instance can be converted to a list with the function list. It is possible to directly iterate through the keys of a set using the for x in coll statement. However,

this iteration will not generally go through these keys in any kind of meaningful (especially sorted) order, but in a seemingly random fashion in which these elements are internally stored in the underlying **hash table** data structure.

4.8. From keys to values

- The **dictionary** data type **dict** is very much like the type **set**, but instead of storing individual keys, a dictionary stores **associations** to map **keys** to **values**. For example, a phone book could be implemented as a dictionary that maps names to phone numbers.
- This simplistic example of a phone book assumes that there do not exist two people with the same name, so that we can use the name as the unique key to identify the person. For each such key, the dictionary can hold at most one value. Associating a new value to the same key erases the previous association for that same key.
- The operations of a dictionary data structure are **efficient on keys** so that given a key, its associated value can be quickly computed. Same as in an old-time printed phone book, the phone number for the given name can be found efficiently with **binary search**, but it is not so efficient to go backwards from the phone number to the name!
- A dictionary from keys to integers can be used as a **counter map** that can be used to keep track of how many times we have seen something. For example, counting how many times each word occurs in the given source text such as "*War and Peace*".
- For convenience, Python dictionaries define the square bracket indexing operation as shorthand for accessing individual keys and their associated values, and the for-loops work directly for dictionary keys right away.
- Like all other data types in Python, sets and dictionaries are **heterogeneous**, so that different types of keys can be freely added to the same set or dictionary. However, the data elements that are used as keys should be **immutable** to guarantee the correct behaviour of the data structure and its internal organization.
- Dictionaries are an immensely powerful tool that can be used to concisely solve various computational problems, often doing at least half of your work for you, compared to trying to solve that same problem without using any dictionaries.
- Sets and dictionaries allow each key to occur in the set only once. If you need a dictionary where each key can be simultaneously mapped to multiple values, you should map the individual keys to either a list or a tuple of values they are associated to.
- Every Python object actually contains the namespace dictionary __dict__ that stores the names defined inside that object.
- To access the name foo inside object x, use the syntax x.foo. Alternatively, the square bracket indexing can be used to access a name inside an object when the name is given as a string, such as x["foo"]. This comes handy when the name is not even known at the time the program is being written, but will be decided at runtime.

• Two special Python built-in functions locals and globals return dictionaries that contain the names in the current local and global namespaces, respectively.

4.9. Assorted list, set and dictionary goodies

- Python already offers several handy built-in functions for common operations on sequences, such as min, max and sum that do not need to be reinvented all the time.
- Elements can be added to and removed from any position in a list. However, due to the way that the list elements are stored internally in memory, these operations are fastest when done to the end of the list, since the list object internally maintains some slack space in the end to better accommodate these appends.
- (Removing an element from the middle requires Python to move all further elements one step to the left, since no gaps may be left inside the sequence stored in the memory.)
- To check whether a list, set or dictionary contains a particular key, use the operator in. Lists also have the method named find that returns the actual position where the element given as argument is located.
- **Set and dictionary comprehensions** are analogous to list comprehensions, with syntax identical to list comprehensions but with curly braces instead of square brackets.
- In fact, Python 3 even allows **iterator comprehensions** to create lazy iterator objects on the fly, typically when an iterated sequence is passed as an argument to a function. These can be a life saver if the generated sequence would be too long to fit all at once into the heap memory of the Python virtual machine, just by changing the list comprehension square brackets to parentheses to turn the sequence into a lazy one.
- Strings and lists often need to be converted to each other. To break down a string into the list of the individual words that it contains, use the string method split, whose argument defines the **separator** between the words. This separator defaults to the space bar character. For example, "Hello there, world!".split() would produce the result list ["Hello", "there,", "world!"]
- To convert a list into a string, call the method join for the string you want as the separator between entries. For example, ":".join(["Hello", "there,", "world!"]) would produce the result 'Hello:there,:world!'
- The collections library module defines other handy data structures that make many advanced programming tasks simpler, such as **double-ended queue** and **priority queue**, and a Counter data structure to simplify common **counting operations** on data.
- The data types in **collections** module behave from the outside as if they were sets and dictionaries, so they can be used wherever a set or a dictionary is required, but they internally organize their data in a different way to speed up some other useful operations such as "Find the ten largest elements" or "Find the current median element" faster and more conveniently than these operations work for an ordinary set or dictionary.

- Of course, this internal organization comes with a price in both time and space, which is why the data types set and dict in the core language do not offer these operations. It would be silly to make everyone pay the premium for frills that most will never need.
- Python functions can be defined to accept arbitrary additional arguments. Special parameters *args and **kwargs must be placed at the end of the function parameter list. These two automatically collect the additional positional arguments and keyword arguments into a list and a dictionary that are available as local names inside the function.
- (Both of these parameters could actually be named something else than their canonical names args and kwargs, since the preceding asterisk and double asterisk already syntactically denote these special arguments. However, consistent **naming conventions** make it easier for people to understand each other's code.)

Week 5: General iteration

5.1. Unlimited repetition

- In general, you should always let the computer do your repeating for you. Whenever you feel the urge to repeat yourself in code, even if "just for this one time, what could be the harm, I don't feel like thinking about this any deeper now herp derp", that is a surefire symptom that you are doing something wrong, or at least not in the best possible way.
- It is perfectly fine to copy-paste some useful chunk of code from **Stack Overflow** and similar places, but whenever you copy-paste some chunk of your own code inside the same project, stop what you are doing right there, go back to the proverbial drawing board, and try to think about what you are doing in a higher level of abstraction.
- Some functions need to be able to do something a number of times that cannot possibly be known at the time the script is written, and thus this number of repetitions cannot be hardcoded into the function.
- In some problems, this number of times cannot even be known until the function has been executed and we can only find out in retrospect what happened. The only way to proceed is to keep going for however long it takes to reach the desired goal, and keep hoping that you will soon get to your destination.
- Before structured programming in the seventies (and even today in low-level machine code), the control of execution consists of jumping back and forth within the code with the **goto statements** that were once famously **considered harmful**.
- For nontrivial programs, using **goto** to control their execution produces unstructured **spaghetti code** whose logic, once grown to be large enough, could not be followed or modified in a controlled fashion

- For examples of such an approach that were awesome at their time but are unintentionally comical for all us sophistos in the Current Year, see "Basic Computer Games", the classic homebrew computing book from the seventies that your instructor has fond memories of poring through as a kid. (Everything that we do will eventually become comical as time goes by, no matter how earnest in our lofty intentions we happened to be at the time.)
- Of course, things could always be worse: in the <u>esoteric programming language INTERCAL</u>, originally designed as a joke and parody of other programming languages of its era, has a comefrom statement instead of goto. (Think about this for a while.)

5.2. While not there yet, take one step towards it

- The purpose of every while-loop ever written is to reach some **goal** that is some distance ahead, in most of the interesting problems this distance being unknown. We cannot directly jump to the goal, but can get closer to it with some simple steps that we know how to take, instead of trying to swallow the whole problem down in one big gulp.
- The infinite-way decision of how many steps we need to take to get there gets broken down into a series of small two-way decisions "Have we reached the goal yet?" that we can solve just by taking a look at where we are currently at, without needing to know how far ahead in the unknown darkness the goal resides.
- (All computations ultimately boil down to some series of two-way decisions. Those are the only things that a mechanical and mindless computing machine can do on its own. Anything higher than that, we need to tell the computer how to break it down to a series of two-way decisions.)
- The logic of while-loop is best understood as "As long as you have not reached your goal, take one step that will take you closer to that goal." Assuming that you can recognize the goal when you get there, this logic will reach the goal whenever the goal is reachable to begin with, and take exactly as many steps as needed, no more and no less.
- The while-loop will correctly do nothing if you are already standing on the goal to begin with, since its condition to keep going is False from the get-go. (Again, when there is nothing to do, it is correct and essential to really do nothing. It is harder than it looks!)
- In this course, **infinite loops** that never reach their goal but run forever are always a logic error. However, some loops work out the prettiest when they are nominally written as infinite loops, but a suitable conditional **break** is used inside the loop body to escape from the loop once you realize that you have reached your goal.
- Any loop in Python can be prematurely terminated with the break statement. A similar, somewhat strangely named statement continue will skip the rest of the loop body and go directly to the next iteration round, although unlike in the classic board game of *Monopoly*, we get to "pass Go in between" to update the loop variable accordingly.

- In fact, would it not be far more truthful if this keyword had been donotcontinue?
- Python loops also allow the curious construct of an else block after the loop. This seemingly nonsensical block of statements gets executed if and only if the execution of the loop reaches its natural end without encountering a break or return in its body.
- Such else block can come in handy when the loop looks for a counterexample for something, terminating as soon as the first counterexample is found, since finding more counterexamples would not change anything. Only if no counterexamples were found, we then execute the code placed in the loop's else block.
- (Implemented in other languages, this type of loop typically maintains some truth-valued local variable indicating whether any counterexamples have been found, and the else block is replaced by an if-statement testing for that boolean variable.)
- For more observations of how to write loops properly in Python, see the talk "Loop Like a Native" for the Pythonic constructs for various common iterative situations.

5.3. Binary search

- To find an element from an unsorted list, there can be no essentially faster approach than **linear search** through that list one element at the time, comparing the current element to the element being searched until either you find it somewhere in the list, or you have looked at every element without success.
- Such a repetitive approach will get slow once the lists start growing large, especially when the number of searches grows in a roughly equal fashion. (If you never search for at least a significant fraction of the list elements, then why are you wasting time and memory adding them to that list in the first place?)
- To boost the speed of searching, you could snap your fingers and convert the list into a set with those same elements that is optimized for this very purpose, making search blazingly fast even for millions of elements. This will pay off if you know that you will perform multiple searches to offset the one-time investment of building the internal data structures used inside the data type set.
- However, if the elements of the list are known to already be in sorted order, **binary search** is a much faster way to find an element in a sequence. (If the list is not sorted, it can always be sorted with much less effort than would be required to build a **set**.)
- Once the list is in sorted order, looking at any individual element tells you something not only about that one element, but about all the elements that come before it, and about all the elements that follow after it.
- Binary search is a funny algorithm in the sense that everybody most certainly already knows it (and in fact, has surely known it since they were little kids), but they paradoxically don't know that they know it! We see this from the fact when looking up

- something in a printed dictionary or a phone book, nobody starts reading through all entries in order from A to Z until they arrive at the particular entry they were looking for.
- The binary search algorithm, invented back in the smoke-filled fifties by Top Men sporting crew cuts and horn-rimmed glasses, is rather tricky to get right in all its edge and corner cases. Instead of the intuition of one finger jumping back and forth in the phonebook zeroing in on the name, we use two fingers that approach each other in a way that the name that we are looking for will always remain between these fingers.
- Binary search repeatedly compares the middle element between the two list indices start and end to the element being searched. Depending on the result of this comparison, eliminate either the left half or the right half by moving the corresponding index halfway towards the other index.
- If the **midpoint** index m between the indices start and end is computed with the formula m = (start + end) // 2, we must note the asymmetry start <= m < end between the two endpoints and also make the correct steps to update each endpoint asymmetric. The algorithm must be implemented correctly to advance at least one step no matter what, and never potentially jumping over the element being searched.
- Once these two indices start and end meet somewhere so that start == end, that is the only place where the searched after element can be. Either it is in that place, or it is not. (If it is not, then adding that element to that location would keep the entire list sorted.)
- Python standard library module bisect contains battle-tested implementations of binary search that guarantee finding the leftmost or rightmost occurrence of the given element, or in the absence of the said element from the list, the place where that element would be correctly inserted to maintain the list in sorted order.
- We can apply the same idea to quickly find all the words in a sorted wordlist that begin with the given **prefix** that need not be a complete word by itself. For example, in our vocabulary data file words_sorted.txt, the list of words that start with the prefix 'jims' turns out to be ['jimsedge', 'jimson', 'jimsonweed'].
- To quickly find all the words that end with a given **suffix**, simply reverse all the words and sort the resulting wordlist, then reverse the results of the same search.

5.4. The power of repeated halving

- Binary search and other algorithms based on the idea of **repeated halving** are tremendously fast even for astronomically large lists, since each element comparison effectively cuts the problem size in half by discarding half of the elements that were still in contention for becoming the final answer.
- In linear search on an unsorted array, each element comparison eliminates only that particular element from consideration, thus requiring n comparisons to eliminate n

- elements. (Same as in that famous puzzle of "How many individual matches are played during a tennis cup between n players?" this answer does not change when these comparisons are organized into whatever tree or other structure you wish.)
- Binary search, on the other hand, needs roughly only $\log n$ comparisons. Logarithms grow very slowly, so $\log n$ is for all practical purposes a constant for any reasonable n.
- To estimate the number of halvings required to cut down a problem into one remaining possibility, for all intents and purposes, 2^{10} equals 10^3 , and thus in general, 2^{10n} equals 10^{3n} . Good enough for government work. ("A billion here and a billion there...")
- For example, binary search in a billion-element list would require roughly only thirty comparisons to cut it down, considering that 10⁹ equals roughly 2³⁰.
- If you were granted a "God's eye view" onto the entire universe, you would have to cut your view in half roughly 250 times for a single elementary particle to remain. Within any realistic framework of computation, a sorted list big enough to make binary search to spend any noticeable amount of time simply cannot exist inside our physical universe.
- The powerful ideas of repeated halving and binary search can be applied more generally to other search problems that have a sorted range of possible answers for you to find the correct one. For example, if you are supposed to **guess the secret number** between a and b, make your first guess to be (a+b)//2, and proceed accordingly from there depending on whether the secret number is smaller or greater than your guess.
- (Integers and their arithmetic may seem simple and silly, but isn't it great how integers, no matter which philosophical view you subscribe with respect to the sense that they and other mathematical objects finger-quotes "exist", come in sorted order right out of the box? Integers sure would not be anywhere as useful, were this not the case!)
- To find a **root** of an arbitrary but **continuous** real-valued function f(x) given as a **black box** that allows you to evaluate it at any point x of your choosing, use binary search to repeatedly cut down the interval [start, end] initially chosen to be wide enough so that f(start) and f(end) have different signs, which guarantees that the continuous function f has at least one root between start and end.
- If the function f for natural numbers is known to be **monotonic** so that f(x) > f(y) whenever x > y, you can quickly find some working values for *start* and *end* by first initializing these variables to 0 and 1. Then, as long as f(end) < 0, bring *start* to *end* and multiply *end* by 10 or some other suitable factor that guarantees exponential growth.
- Once it is known that the desired result is between *start* and *end*, look at the sign of the **middle point** value f((start + end) / 2), and move one of your current endpoints *start* and *end* to middle, depending on in which one of them the function f has that same sign as it has in the middle. This move cuts your remaining interval in half. Keep going until the distance between the start and *end* is small enough for your needs.

5.5. Nested loops

- Since the body of either a while- or a for-loop can consist of arbitrary statements, and loops themselves are also statements, it is not only possible but perfectly legal and good technique to solve many problems by **nesting** an **inner loop** inside an **outer loop**.
- The language sets no limit how deep this nesting could reach. As the famous **zero-one-infinity principle** of computer programming states, the moment that you allow there to be two of something, you should actually allow any number of that something. This important design principle pops out its head all over software engineering in design, programming and execution.
- Like all other software engineering principles, this principle is not a law of either nature
 or man. Therefore it can be violated at will, and same way as with other semantic
 properties of the program, the compiler has no way to verify that such principles are
 properly followed.
- (This principle should in fact more accurately be called **zero-one-arbitrary principle**, but the term is already too established in its incorrect form. Why can't people realize that words actually mean things?)
- Even when a programming language allows an unlimited number of something, its interpreter and the finite physical machine that executes this interpreter must necessarily have some upper limit to how many of those somethings there can be. But the language itself, residing in the timeless Platonic plane of ideas and mathematical abstractions, must not impose any such limitations from our imperfect physical world.
- The behaviour of the nested loops might not initially be that intuitive to grasp. You should especially note that the inner loop is executed in its entirety from the beginning every time the outer loop moves forward one notch.
- To get an intuitive idea of this, again think of the behaviour of an ordinary clock that measures hours, minutes and seconds, implemented as three nested loops, same as we did with list comprehensions earlier.
- The outermost loop counts hours from 0 to 23. For each such hour, the inner loop for minutes would go through its entire range from 0 to 59. For each such minute, the innermost loop would go through its entire range from 0 to 59.
- In some other nested loops, the inner loop will run for a different number of rounds each time depending on the value of its outer loop counter.
- The operations break and continue always apply only to the innermost loop that they are in. (For clever ways to get around this restriction, see "Breaking out of two loops".)
- An often occurring need is to iterate through all n*(n-1)//2 possible pairs of elements of the given n-element sequence so that each pair (x, y) is processed only once. This is normally achieved in more primitive languages with the use of two nested for-loops, but

- a more Pythonic style is to apply the function itertools.combinations to produce the lazy sequence of such pairs of elements.
- The technique of itertools.combinations also immediately generalizes to iterating through all triples, quadruples and so on of elements, allowing us to, for example, to easily iterate through all 2,598,960 different poker hands of five cards chosen out of the ordinary deck of 52 cards.
- Theoretically, we could similarly iterate through all possible 13-card bridge hands, but since there are 635,013,559,600 of those, the computation might take all day. However, since the combinations are produced in a lazy manner instead of creating them all into an explicit list, the computation will not run out of memory since only one combination at the time is kept in memory.

Week 6: Some educational example scripts

6.1. Different levels of programming errors

- **Syntax error**: the program code does not conform to the syntax rules of the Python language. These are detected during the compilation and prevent any execution of the script, even from the parts that precede the syntax error. These always prevent the code from even starting to execute even its first statement.
- Runtime error: the program crashes during execution because it tries to do something that is logically impossible, such as divide the string "Hello" by the integer 17. (Multiplying a string by an integer is hunky dunky, though, as a convenient shorthand for repetition.)
- Even though types are not expressed explicitly in Python language, Python execution is strongly typed so that every Python object knows its own type. If some operation is not meaningfully defined for some types of object, the Python engine has no choice but to give up and raise an exception.
- Explicitly typed languages such as Java require the programmer to explicitly declare the type of each variable. That variable may then be assigned only to objects compatible with that type. This boilerplate in triplicate where you have to tell the compiler that "Hello" is a string and 42 is an integer is a hassle in writing code, but guarantees that a successfully compiled Java program cannot crash at runtime because of some type error.
- **Logic error**: the program is legal and produces some results without crashing, but at least for some possible inputs, the produced result is not what the programmer wanted it to be. From the pool of infinitely many possible programs, you just happened to pick and write the wrong one.

- Logic errors are by far the most difficult level of these programming errors, in fact the
 bane of our existence as programmers. Logic errors can only be detected by you, or if you
 miss them, eventually by your customers and end users. No interpreter or other execution
 tool can possibly read your mind to determine what your mind intended to do, as opposed
 to what your stubby fingers actually did type in.
- Above the logic errors there exists even the higher level of **specification errors** where you have understood and defined the problem incorrectly, thus by definition making it impossible for you or anybody else to write the correct program to solve your problem.
- Sometimes even well understood problems cause us to write specifications that contain some hidden contradiction and are thus impossible to realize. These contradictions are revealed when we actually try to write the program and become aware of their existence, and have to slink back to the proverbial drawing board to update the specification.
- Since the Python language is so concise and performs essentially zero type checking at compile time, **unit testing** has to shoulder the responsibility in revealing errors. Other languages such as Java are "heavier" than Python, with their design goal of wanting to reveal as many errors as possible at compile time by forcing the programmers to be verbose and explicit about what they want. (Testing is still needed in those languages, since no compile time checking can catch but a small range of all possible errors.)
- Runtime errors can be handled dynamically with the try-except mechanism in some situations where it is still possible to recover from the error. Uncaught errors terminate the execution of the program.
- The try-except block can be followed by a finally block that is guaranteed to be executed no matter which way the execution tries to leave the try-except block (returning from function, raising an error, flowing through normally), provided that the Python interpreter does not itself crash or terminate.

6.2. Software testing

- It is important to test your functions with many different **test cases** to root out the errors that are lurking inside them. Each test case consists of the arguments given to the function, and the correct result expected for those arguments.
- Whenever the actual result differs from the expectations, that test case has shown its
 worth by uncovering the existence of some previously hidden bug (more formally, a
 fault or a defect), an error in the logic of the code that will occasionally cause the results
 computed with that code to be incorrect.
- The **frequency** of a bug depends on the portion of all possible inputs to the program that will make the bug **manifest** itself in form of incorrect results. It is important to try out different test cases to maximize your chances of revealing as many bugs as possible in

- this imaginary game of *Battleships* played on an infinite board, instead of trying out slight variations of essentially the same test case.
- Automated tools exist to run through the entire **test suite** with one command, preferably with just one mouse click. (Or maybe even zero clicks.) This allows the entire test suite to be rerun every time the code is somehow modified.
- Standard practice in professional programming when building large systems of millions
 of lines of code is to rebuild the entire system from the clean slate of nothing but source
 code on a daily basis, and rerun the entire existing test suite on the current state of the
 codebase. Programmers can then peruse the test report with their morning coffee, and are
 prohibited from writing any new code until they have fixed all revealed bugs in the
 current code.
- Especially when testing your own code, you need to put on a different "hat" so that you
 are honestly trying to reveal the weaknesses and cracks inside your program, instead of
 just trying to stroke your ego as a great coder and breeze through that boring testing stage
 by giving your code only some simple test cases that you already know it will handle
 correctly.
- The purpose of testing is to reveal the existence of defects. The purpose is not to build a false sense of security as your code correctly handles a dozen possible argument combinations from the infinite number of its potential arguments.
- The fact that a function correctly handles some small number of example test cases does not establish that the function will also correctly handle all possible arguments that somebody might give it in the future.
- Testing that did not reveal any errors was a failure, not a success! (Read this sentence many times over and over until you have come to embrace its fundamental message.)
- For a multitude of reasons, people tend not to be good at seeing their own mistakes and blind spots. In all serious organizations, testing any code must always be performed by a different person than the one who designed and wrote it.
- However, test driven design where no code is allowed to be written until you have written a set of test cases for it is also a perfectly valid software engineering principle. Being required to first write a set of test cases that the existing code does not pass forces the programmer to prove the need for the new code (which is important in the reality of limited time and other resources versus potentially unlimited needs of expansion), and also to think about the various aspects and details of that problem, which then gets him off to good start in typing in the code to solve that problem.

6.3. Designing good test cases

• Since you cannot possible try out all possible inputs for any function that is sufficiently complex for somebody in the real world to pay you actual money to write it, you need to

maximize your chances to hit some bug with the limited "shots" that you get to take with your test cases (not unlike the spirit of the game of *Battleships*) except that this version of the game is played on an infinite board where the size and shape of the enemy ships and their total numbers are initially unknown.

- Once a program crosses a certain threshold of size and complexity, it will always have one more bug remaining in it, no matter what you do. **Always**. No matter what you do. Really. There is always some unexpected possibility lurking that you did not think of.
- Also the relevant application of Murphy's Law where somebody has carefully tested their program and then proudly demonstrates it for the first time to somebody else who then makes it immediately crash with some unexpected inputs that the original author never thought of is common enough to be practically a cliche.
- Software engineering techniques used by critical entities such as NASA (who have no option of pressing the reset button or calling in a repairman to fix a system that has crashed) can achieve bug rates close to zero, but their techniques are not feasible for real world software projects that are run under practical constraints of time and money.
- A simple but good strategy to improve your chances of hitting some bug is to try out all
 combinations of edge cases and corner cases of your function inputs, especially the
 smallest possible value and the largest possible value of some argument, and all
 combinations thereof.
- Most importantly, remember that **zero is always a possibility in programming**. When testing functions that take a list or a string as an argument, remember to test that these functions work correctly when given an empty list or an empty string. After that, try out the function with a **singleton** list or string that has exactly one element.
- If you have access to the source code of the system being tested, you can think up new test cases to cause the code to go through different execution paths through it, to improve the **test coverage** metrics of your test suite. Modern **fuzz testing** techniques that feed the system **pseudo-random** arguments trying to make it crash can automate this process and reveal bugs overnight while the programmers are sleeping.
- Testing can only reveal the existence of some bug. Testing is followed by **debugging** where the test case that revealed the bug is used as a guide to find the logic error in that function. The bug fix must work for all possible arguments in the equivalence class of the test case that make that particular bug manifest its ugly little head, not merely for that one particular test case.
- Our automated test suite for the graded labs tries out all functions with a large number of pseudo-randomly generated test cases that are always the same in all Python environments, regardless of the underlying hardware and operating system. A cryptographic checksum is computed from the results that your function returned to these test cases, and that checksum is compared to the checksum generated from the answers produced by the private model solution by the instructor.

• Whenever the checksums of two things are different, that reveals that those two things are somehow different. Unfortunately, the checksum only reveals the existence of at least one difference, but does not tell us how many differences there are in total, nor allow us to pinpoint where exactly those differences reside in the sequences of returned results.

6.4. **JSON**

- **JSON** (for JavaScript Object Notation, pronounced "Jason") is a widespread modern standard to **encode arbitrary structured data into linear Unicode text** in an unambiguous fashion that is portable between different types of computers and programming languages.
- Despite the name that reveals its historical origins, JSON is designed to be **language-independent** so that the exact same JSON files can be read and written by different programs written in different programming languages.
- Unlike many other file formats, JSON is readable by normal humans (although less so than even simpler <u>YAML</u>) and trivial to modify with any text editor and Unix command line scripts.
- The format is insensitive to whitespace outside string literals in the sense of one whitespace character being the same in effect as any nonempty sequence of whitespace characters. This allows large JSON documents that are intended to be read only by machines to be squeezed smaller by eliminating the air of redundant whitespace.
- The JSON format expresses structured data using JavaScript lists and dictionaries, whose syntax by happy coincidence just happens to be exactly the same as that of Python. In fact, the content of every JSON file by itself is already a legal Python expression that could theoretically be evaluated as Python code!
- However, for security reasons, the **atomic elements** of the encoded structure in a JSON file are allowed to only be strings, truth values, integers and floating point numbers, so that no executable code is allowed. This prevents various forms of **code injection** attacks.
- The atomic elements can be combined into lists and dictionaries with square brackets and curly braces. These lists and dictionaries can be nested arbitrarily deeply.
- The json library module makes reading and writing JSON files trivial. The function load reads the given file and returns the object structure encoded in it. Furthermore, the parser inside the module treats the JSON data as pure text, and is guaranteed never to execute any part of it as code. This makes it safe for the programmer to read any JSON files even if those files were dug up from the darkest swamps of our shared information superhighway.
- Of course, any data can still be **semantically misleading** in that behaving as if that data were actually true will result in suboptimal actions. The real distinction between data and code is a question of semantics, since all data will eventually turn into some concrete

- decision at some point of execution. (Otherwise that data was redundant to begin with, so what could be the harm of somebody modifying it?)
- The function dumps turns the structure into a properly formatted JSON string that can then be written into a file.

Week 7: Lazy sequences

7.1. Generators

- Those of you who are familiar with writing **classes** to define your own high level data types, could write your own iterator types to produce arbitrary sequences simply by defining certain **magic methods** to those classes.
- That feat is not actually too difficult once you have learned how classes and **methods** work, but since lazy iterators thoroughly permeate the spirit of Python 3, the language also offers a simple way to define lazy iterator types as **generators** using the familiar function definition syntax.
- A generator is a function that uses the keyword yield instead of return to return the result. This fact alone tells the Python compiler that when called, this function actually creates and returns an **iterator** object. The body of the function is not executed at the call.
- Only when this iterator object is actually asked to produce the next element of the sequence, the function body starts execution. When this execution reaches any yield statement inside the decorator body, the execution pauses and the yielded result becomes the next object of the sequence produced by this generator.
- The local namespace and the execution state remain in memory until the next element of the sequence is requested. Unlike an ordinary function that always starts from the beginning each time it is called, the generator object continues to exist in this paused state. When the iterator object is eventually asked to produce the next object of the sequence, the function execution resumes from the statement that follows the yield statement instead of starting from the beginning.
- To end the production of the sequence inside a generator function, you can either explicitly raise the **StopIteration** error, or far simpler, simply return from the generator function in the ordinary fashion.
- As with all iterators, multiple instances of the same generator can coexist in memory, each with its own local namespace and execution state.
- As a handy little piece of **syntactic sugar**, **yield from** can be used to **yield** all items produced by another generator as part of the sequence produced from the current one, instead of writing a full on **for**-loop for such a common purpose.

- Since generators behave like functions with the sole difference that their internal state does not get automatically erased every time the control returns from the function, generators can handle arbitrary arguments, even default and keyword arguments.
- When one of these arguments is an existing **underlying sequence** whose behaviour this generator modifies, this generator is said to be a **sequence decorator**.
- For example, a decorator that is given an existing sequence and lets through only those elements that are strictly larger than the previous element. From outside, this decorator is still a black box generator that spits out such elements one at the time on command, hiding the process that allowed these elements to pass while discarding some others.
- When writing code for decorators, it is important to try to maintain the laziness of the underlying sequence whenever possible. Again, this means avoiding the operations of len and sequence slicing, and using instead Pythonic tools such as for and enumerate, along with the various decorators defined inside the itertools module. These tools keep the potentially humongous, even infinite, underlying sequence in its lazy form.
- It is always possible to turn a lazy sequence into an explicit one, but not possible to turn an explicit sequence back into a lazy one. Therefore, your code should maintain the laziness of sequences given to it as long as possible.

7.2. Functional programming tools

- As an alternative to loops and conditions, the functional programming tools map, filter and reduce can occasionally be used to express computation logic in a more clear and succinct fashion and, in some rare cases more efficiently.
- List and iterator comprehensions can these days do the work of map and filter.
- The built-in function map takes a one-parameter function f and an iterator it as parameters, and returns an iterator that produces a sequence of values that you get by applying the function f to all elements of the sequence from the iterator it.
- For example, map(lambda x: x*x, [1, 2, 3, 4, 5]) would produce the iterator for the series 1, 4, 9, 16, 25. As usual, use the function list to get all these values in one swoop as a list, instead of stepping through them one at the time.
- The function filter cherrypicks those elements from the sequence for which the given function produces a True result, discarding those that are considered False.
- The function reduce (in some other functional programming languages, this function is more vividly called fold) turns a sequence back into a single element by repeatedly combining two consecutive elements into one element, using the two-parameter function given to it as the first parameter.
- Iterators can be a surprisingly powerful model of computation. Using the functions defined in the itertools standard library module, many functions implemented in

- traditional fashion with loops and conditions can be expressed far more succinctly using functional programming applied to iterators.
- The example implementations of itertools functions, followed by the recipes for more functions that did not make the cut of being important enough to be included into this module, make great studying of how to solve problems in the spirit of iterators.
- The module <u>more-itertools</u> offers even more such shorthands for concise expression of many common patterns of loops and iteration. (If you choose to install additional packages from <u>Python Package Index</u>, make sure to use the conda installer instead of pip if you are working in the Anaconda environment.)
- The library module functools offers the function decorator partial that can be used to **curry** some function that takes *n* parameters into another function that takes *n k* parameters, by fixing the values of the *k* missing parameters into constant values.

7.3. Dynamic evaluation of text as code

- The dynamic nature of Python is illustrated by the infamous eval statement that can evaluate an arbitrary string as a single expression, compiled on the fly before evaluation. The program could therefore build up a string that contains an expression, and then evaluate that string as code.
- In **dynamic languages** where executable code is not set in stone at compile time but can be generated at runtime, **eval** can be a very powerful tool to do various cool things, but its inherent danger is when it is used to evaluate strings that originate from the potentially hostile outside world, thus opening the system up for **code injection** attacks. This is an especially serious danger in **web services** written in a Python **back end**.
- (See the Internet-famous **xkcd** comic of "Bobby Tables" about this phenomenon with the **SQL** database language. Never forget, "The client is in the hands of the enemy!")
- One pithy comment in a Hacker News thread about this issue put it the following way: There's no such thing as "data". Every piece of "data" eventually gets interpreted, thus becoming a "command" in some level of abstraction. The core of every security vulnerability is the belief that "this is just a piece of data".
- (Keanu says "whoa", suddenly realizing that there never was a spoon since all of reality is one, despite our tendency of seeing this reality made up from individual parts that we can name.)
- Remember the "ha-ha only serious" maxim that the word eval is a common misspelling of "evil", to be used only when no safer techniques can possibly do the job. Usually, safer and better techniques exist to achieve the same end without any risk.
- For some additional safety, eval can be given dictionaries as named arguments that are used as local and global namespaces during the evaluation, so that the malicious

- expression is restricted to this virtual **sandbox** inside the Python environment and does not get to modify the actual local and global namespaces of the Python interpreter.
- However, even this does not prevent all the damage that could potentially be done by direct access to the filesystem, and many other known (and more seriously, yet unknown and perhaps defined in future versions of Python and its standard libraries) forms of mischief and mayhem.
- The interactive Python interpreter is an example of a **REPL**, "read-eval-print-loop". This small program, written in Python itself, repeatedly reads in an input string, evaluates it, and prints the result on the console.
- In fact, once you understand the core Python, you should by now be able to write a small but working Python REPL in Python, including the **command history** and other bells and whistles to help the user!
- A more powerful function exec allows arbitrary Python code to be executed. Statements given as the string must be separated with either line break characters or semicolons to make the language syntax unambiguous.

7.4. Pseudorandom numbers

- Generating random numbers from various probability distributions is needed not only in various games of cards and other things, but more serious programs may occasionally benefit from a touch of randomness, carefully controlled to keep the overall behaviour of the program predictable.
- Since deterministic computers cannot produce genuine randomness without the aid of specialized additional hardware not included in our everyday off-the-shelf computers, **pseudorandom number generation** takes place at software level.
- Pseudorandom numbers are not truly random, but once the **seed** value of the generator has been set, the random bits produced by such a generator are as deterministic as a train running on its tracks. However, the internal operation of such a generator is highly **chaotic** so that its future sequence is highly sensitive to the details of its initial state.
- If no seed value is explicitly given, it is initialized from the system clock inside your computer. The millisecond precision guarantees that if the same program is run twice, the different starting times make their future sequences of random bits completely different.
- Modern pseudorandom generators generate "good enough" randomness in the sense that
 no program that uses such a pseudorandom generator would become more accurate in its
 intended task if that generator were replaced by an **oracle** that magically produces truly
 "random" bits.
- Careful design and mathematical analysis are required to construct a deterministic process that emits bits in such sufficiently random fashion. Randomly chosen methods will rarely produce sufficiently random results!

- Python 3 is standardized to use the **Mersenne Twister** generator, independent of the underlying operating system and physical hardware. This generator passes all major tests for quality randomness, and its **period** so long that the sequence will never start repeating itself in any possible use case within the confines of our physical universe.
- The function **getrandbits** in the Python standard library module <u>random</u> functions is used internally by all other functions in that module to generate the random bits they will then combine into values from other probability distributions.
- Most programs need only one instance of a pseudorandom number generator, and should therefore access the functions of random as functions. However, some programs benefit from the existence of separate instances of the type random.Random that will advance independently of each other.
- Functions randint and randrange must surely be the most commonly used functions to produce random integers from the given range, such as rolling a die with the possible results between one and six.
- These two functions internally consult the getrandbits function for just enough random bits that they can produce their result integer value fairly from the given range, even if this range is not some convenient power of two, or if the width of that entire range were somewhere in the high googols.
- The common task of **random sampling** of elements from the given sequence are handled by the functions **choices** and **sample**, respectively **with and without replacement**.
- The task of **shuffling** the elements of the given list into a random permutation seems deceptively simple. However, the obvious algorithm of "repeatedly choose two elements from the list and swap them, repeat this for some energetic hand waving number of times") is not only inefficient but incorrect.
- The correct **Knuth shuffle** algorithm to produce each of the n! possible permutations with the same probability of 1/n! is implemented as the function shuffle.

Week 8: Recursion

8.1. Recursive functions for self-similar problems

- A thing is said to be **self-similar** if it contains a strictly smaller version of itself inside it as a proper part. (As an aside, in mathematics an entity is **infinite** if it fully contains something as its proper part that is **isomorphic** to the entire entity.)
- **Recursion**, a function calling itself for smaller parameter values, is often a natural way to solve self-similar problems, once that underlying self-similarity has been spotted. Spotting the self-similarity is the most difficult step of recursive problem solving in practice, but once the self-similarity has been revealed, the rest is nearly mechanical.

- The exposed self-similarity allows us to write **recursive definitions** for self-similar phenomena that we wish to compute out. For example, the non-recursive definition for factorial $n! \triangleq 1 * 2 * ... * (n 1) * n$ can be converted into an equivalent recursive definition $n! \triangleq (n 1)! * n$.
- (The variation ≜ of the equality symbol is used instead of the classic symbol = to denote **equality by definition**, as opposed to some equation that we must solve by sufficiently constraining the values of its variables.)
- To avoid **infinite regress** in principle and **stack overflow** in practice, every recursive method must have at least one **base case** where no further recursive calls are made. For the factorial function, the base case is 0! = 1.
- Recursive definitions are a surprising way to solve complex problems. The harder the complexity and power of the function F(n) are pulling against you, the harder they will also be pulling for you on the right hand side of the definition $F(n) \triangleq s(F(n-1))$, where s is some simple function, since both sides of the equation balance by definition in this game of tug-of-war between both sides.
- From a technical point of view, there is no difference whatsoever in what happens during the execution of a function call, whether that function is recursive or not.
- Just like with every function call, recursive invocations of the same function each have their own local namespaces. This way the same parameter and local names can exist independently of each other in different levels of recursion.
- In theory, both recursion and iteration are computationally universal, both of these essentially being syntactic sugar for the more fundamental concept of mathematical induction. Any computational problem that could be solved one way, can always somehow also be solved the other way. However, problems that exhibit self-similarity are better suited for recursion than iteration.
- Also, any **linear recursion** where each function call produces at most one more function call can always be converted to loops and iteration in a straightforward fashion, so recursion as a technique does not gain anything in such problems compared to iteration.
- The true power of recursion is unleashed in its ability to **branch** to two or more different directions, going as far and deep in each direction as needed before trying out the next direction, possibly branching even further to easily explore an exponential number of possibilities. Contrast this to the while-loop that will only keep going to one direction, missing the goal unless there exists some goal along this straight and narrow path.

8.2. Practical application of recursion

• To solve a recursively defined problem, first solve a smaller **subproblem**, a smaller instance of that very same problem, by having the function call itself. Just like with the

- cliched factorial example, then use the result of that subproblem to solve the original problem in a much easier way than computing that problem from scratch.
- The subproblem is solved by first solving an even smaller subproblem, which is in turn solved by first solving an even smaller subproblem, and so on.
- Every recursive function must have at least one **base case**, when the subproblem is sufficiently simple so that you can solve it on the spot without any more recursive calls. Every recursive function should always begin by testing for the base case.
- A recursive function can have more than one base case. In fact, there could even exist infinitely many base cases, especially if the recursive function takes two or more parameters.
- Fractals are pleasant and aesthetic geometric shapes that are self-similar and have a non-integer dimensionality in their infinitely deep nesting that can at its best give an appearance of organic and natural structure. Subdivision fractals such as the Sierpinski triangle or quadric cross that consist of smaller copies of themselves are natural to compute and render with recursion.
- In principle, every fractal is infinitely deep, but when its holiday portrait is rendered on a finite pixel raster on the screen, the base case is when the shape becomes "small enough", however you choose to define that. (For example, being smaller than the area of a pixel.)
- We are always free to adjust the subdivision rules and rendering effects for a maximally artistic effect. The only law that we truly have to follow here is the law of awesome!

8.3. Downsides of recursion

- Among those who **program by superstition**, recursion tends to have a reputation of being inefficient and bad, existing in some abstract fancy-nancy higher plane that is never to be used in actual programs.
- Few people seem to be able to coherently explain why, especially since the strengths of recursion don't really show up until third year or thereabouts in a decent computer science undergrad program with problems where the recursive ability to **branch** to multiple directions makes it a superior alternative to iteration with loops.
- That said, recursion really does have three downsides to be understood and avoided.
- First, every function call, recursive or not, creates a new namespace of local names. A deep recursion doing the work of a loop (for example, recursing through the position indices of some list) can therefore easily cause a **stack overflow**.
- Even with languages such as Python where namespaces are allocated from object stack
 and therefore in principle limited only by your process memory, recursion depth has been
 artificially limited to prevent an erroneous infinite regress from consuming all of the
 heap memory.

- The recursion limit can be changed with the function setrecursionlimit in the sys module, but any reasonable recursive function should be able to complete its execution within the default limit. Deep **linear recursions** should be implemented with loops that execute inside the same stack frame, instead of using recursion at all.
- Second, even without a stack overflow, the internal bookkeeping of the stack makes the recursive method a constant factor slower compared to the equivalent iterative solution.
- Third, a recursive method where each recursive call can generate more than one further recursive call can cause an **exponential chain reaction** of function calls. Sometimes this is inherent in problems whose search space truly is exponentially large. However, this is horrendously inefficient when the same subproblems are computed over and over from scratch an exponential number of times.
- Easiest way to fix this is **memoization**: use an auxiliary data structure to remember what subproblems you have already solved, and when the recursion comes to those subproblems again, just look up the previously cached result and return that as the result.
- (The odd spelling "memoize" for this technique instead of "memorize" is intentional, to clearly identify it as the technical term that refers to this particular technique.)
- Memoization is philosophically similar to solving a problem with a **lookup table**, except that the lookup table is now filled dynamically as encountered and needed, as opposed to being hardcoded into the program.
- As seen in the next section, the handy decorator <code>lru_cache</code> in <code>functools</code> can be used to memoize Python recursions without any further human effort.

8.4. Applying functions to other functions

- In many ways, Python sits snugly halfway between the **imperative** and **functional** programming paradigms. Especially in Python there is no real distinction between code and data, but functions and code are objects exactly the same way as strings or integers are objects in memory.
- The spirit of functional programming is to pass back and forth functions that are combined to create new functions. Functions can even be passed themselves as arguments for truly mind-blowing results, as with the famous **Y-combinator**.
- A more down to earth application from such a lofty view is passing a strategy function as an argument to another function to be used as part of its execution. Whenever the function needs to make some particular decision internally, it consults the strategy function to ask its opinion, so to speak, and uses that result.
- For example, a function that sorts a list can receive a **key function** that is used to convert mutually incomparable elements to integers or some other comparable values that are then used in element comparisons during the sorting. This way, the sorting algorithm

- itself needs to be written only once, and it can be used to sort data according to arbitrary different criteria that are not even known when the sorting function itself is being written.
- The key function can be used to implement **sorting by multiple criteria** by having this key function return a tuple of these criteria. This conveniently produces the desired effect, since the Python tuple order comparison is lexicographic.
- A **function decorator** is a function that receives the underlying function as a parameter, and then creates and returns a function object that calls the underlying function, possibly modifying its arguments or result in some way, and possibly performs some other computation about the usage of the underlying function.
- The original underlying function can then be called through the decorator without knowing that there is a decorator that does its work invisibly in between the caller and the original underlying function.
- As an example of the usefulness of function decorators, you could decorate a key function with a decorator that keeps a count of how many times it has been called, to measure the number of operations performed internally by some sorting algorithm.
- As a powerful testament to the dynamic and higher-order nature of the language, Python
 functools module offers the handy function decorator lru_cache that can be applied
 to any function (typically only to recursive functions, but this is not a law of nature or
 man) to automatically memoize it to remember the previously computed results for quick
 lookup.
- The abbreviation prefix 1ru stands for "least recently used". Should the memoization data structure ever become full, the result that has been previously queried the longest time ago and therefore probably will not spark joy in the future is tossed out to make room for storing the next result, in the best spirit of Marie Kondo.
- To ensure that the memoized results don't stick around to waste memory after the desired result has been achieved, a good technique is to define the memoized recursive function inside the actual function solving the problem. Once this outer function returns its result, its local namespace ceases to exist, allowing Python to release the memory for all the objects defined inside that function, including the memoization cache.

8.5. Defining small functions as lambdas

- It would often be handy to define a small one-liner function on the spot, without having to go through the whole rigmarole of the function definition syntax.
- An **anonymous function**, which are for historical reasons called **lambdas**, can be defined using the keyword **lambda**, followed by the parameter names separated by commas, followed by a semicolon and the function body.
- For example, the expression lambda x,y: x*x + y*y defines an anonymous function object that takes two parameters, which are named x and y inside the function, and

- returns the sum of their squares. This object is typically passed as an argument to some function that uses it internally to make the decisions that it needs.
- For syntactic reasons, Python lambdas are restricted to one-liners. If you need a more complicated function, you have to actually define it as a proper function like some caveman. Other languages with their required delimiters have an edge here over Python, since their lambdas can be arbitrary code blocks.
- The Python style guide advises that you should only use lambda expressions inside some larger statement, and never use lambdas as a substitute for def for a function declaration, to make function declaration look like object assignments to names.
- In many situations, you would like to pass some operator of the Python language itself, for example + or <, as an argument to some other function. You cannot do this directly within the Python syntax, as the language low-level operators are not objects that could be passed back and forth, so Python will only give you a syntax error message trying to apply the operator directly to its surroundings in the source code.
- To achieve this, you have to first wrap that operator inside a lambda expression, such as lambda x,y: x+y for addition. For convenience, the module operator defines named lambda expressions for all built-in operators in the Python language.

Week 10: Efficient numerical computation

10.1. The numpy array data type

- The dynamic flexibility of Python data structures such as heterogeneous lists and dictionaries makes for fun and concise programming, but can be inefficient in both time and memory when dealing with large datasets, especially in the present **big data** era.
- To represent a heterogeneous list in computer memory using only simple bytes (the only thing that really exists inside computer memory), additional bookkeeping and waypoint information needs to be stored for each element.
- When doing real work in science and engineering, all this dynamic flexibility is usually not needed, since all data is known to be some simple uniform types such as integers or decimal numbers. Furthermore, these numbers are often known to be inherently restricted to some limited range of possible values (for example, in the population data of the cities of the world, no city has more than about thirty million people). This makes Python's internal unlimited integer representation massive overkill for such data.
- The important Python extension **numpy** offers a data structure **ndarray** (short for "n-dimensional array") to represent large 1-D **vectors**, 2-D **matrices** and even arbitrary higher-dimensional **tensors** of **homogeneous** elements.

- Since all elements inside a numpy array are of the exact same numerical type, they can be stored in memory consecutively without any extra information in between, and processed directly in efficient machine code functions that can even be **parallelized** for even more speed with today's **multicore** processors.
- Inside the ndarray, integer elements have a fixed maximum value, instead of being able to contain arbitrarily large numbers such as 1234 ** 5678 the way that the Python native integer type can easily do.
- If some computation produces a larger value than would fit into a fixed number of bytes allocated to it, the result silently **overflows** and is truncated to fit inside those bytes in a cruel Procrustean fashion. Such results are essentially useless nonsense.
- Each ndarray knows its dimensions and element data type, and uses efficient and low level code written in C and assembler to perform various mathematical operations orders of magnitude faster than they would be for heterogeneous Python lists where the Python virtual machine has to check the type of each element to choose the appropriate Python function to execute, and the same thing happens inside the statements of that function.
- Integer elements can be defined to be of type intX (signed) or uintX (unsigned) where X stands for the number of bits used, by necessity some multiple of eight. For example, the element type int32 would denote a signed four-byte integer. Unsigned types offer twice as large a range of positive values, since the highest bit is not needed to store the sign of some integers that are known to never be negative.
- The element types int8 and uint8 pack each element into a single byte, thus offering the possible ranges of -128, ..., +127 and 0, ..., 255 respectively. (Signed integers encoded in **two's complement** always have one more negative value than they have positive values, zero being the "odd man out" in the middle of this discrete range.)
- All these computations are done by the processor machine code instructions that the numpy module operates on directly. As it is with many other things in life, you don't need to know their exact details to be able to use those things. However, you do need to be aware of the external consequences that those details impose on you!
- More generally, in many places of life you get to pretty freely choose the rules. However, you still never get to choose the **consequences** of your chosen rules, since those will not be determined by your wishes and intentions, but by the external objective reality inside which your rules continue to operate even after you have "left the room", so to speak.

10.2. Operations over numpy arrays

• The functions defined in numpy modules operate **element-wise** on the entire **ndarray** at once. You should always use these rather than Python built-in functions, even when Python already has that function such as **sum** or **max**.

- As a general principle, whenever you are using Python for-loops or other methods outside numpy to iterate over numpy arrays, you are most likely doing something wrong, or at least not anywhere close to the best possibly Pythonic way of using numpy.
- Note that the multiplication operator * between two numpy arrays performs element-wise multiplication. If you want to perform proper matrix multiplication as defined in the linear algebra textbooks, use the function np.dot that computes the dot product of the individual rows and columns.
- Whenever some numpy function is applied to numpy arrays where the other array has a lower dimensionality, that smaller array is **broadcast** into virtual multiple copies to make the dimensions of the two arrays match. For example, adding a two-dimensional matrix of shape (10, 20) and a one-dimensional vector of shape (20,) broadcasts the second array into the same (10, 20) shape as the first array by duplicating that row vector ten times, so that the matrix addition can be performed elementwise.
- Of course, no actual duplication of data in memory occurs during such broadcast, since the numpy engine is smart enough to perform the modular arithmetic computations necessary to locate the data from memory.
- As a special case of broadcasting, any scalar value can be thought as a 1-element numpy vector that broadcasts itself into any number of dimensions. For this reason, we only need one function np.ones to create an array whose all elements equal 1, since we can always multiply that array by a suitable scalar value c that gets automatically broadcast to the same shape, resulting in an array whose elements are all equal to c.
- Matrix multiplication in the sense of linear algebra using the dot product of individual vectors is another special case of broadcasting.
- The ndarray data type is an iterable and looks and feels like a Python object, with all the usual operators such as list slicing working the way a reasonable person would expect them to. However, note that slicing produces another **view** to the same underlying data, instead of creating a new ndarray and copying the data there. This is the opposite of how Python list slicing operation works.
- Many extensions have been written on top of numpy to perform even more advanced operations on ndarray objects. The most important of these are scipy for numerical analysis and matplotlib for rendering pretty graphs based on numeric data, on top of which many other extensions (such as pandas for data analysis) have been written.
- Scikits are third party modules built on top of scipy, specific to some particular field of
 science. These days, the biggest buzz there is surely about <u>scikit.learn</u> that offers a host of
 machine learning algorithms for anybody to discover interesting underlying regularities
 in their own datasets.
- Machine learning is used to extract the hidden regularities behind the given dataset of observations. This allows exploiting these hidden regularities to extrapolate to the unseen values from the problem domain. This hidden superpower let you make decisions as if

- you had been granted some kind of "God's eye view" to see the parts of reality that you cannot normally directly observe.
- Even as writing this, the results of machine learning work their invisible magic while writing this document, instantly pointing out not merely syntax errors, but these days even grammatical and style errors.
- All these fancy machine learning algorithms are available for laymen with only a couple of simple lines of Python code to execute the appropriate machine learning function on the given numpy dataset. Despite everything, it is an interesting time to be alive!
- Even under the most conservative estimates of the future growth of computing power, anyone who can program the computer of the year 2050 (it will be just "the" computer then, not merely "a" computer) will effectively wield the powers of Loki or some other caped *übermensch* in the beloved *Avengers* film series.

10.3. Processing pixel images as numpy arrays

- Before it has been converted to actual visible colours of your display device, a **raster image** is a three-dimensional **cuboid** of numbers. Two dimensions are for the pixel coordinates on the image plane, and the third dimension encodes the total colour of that pixel as the sum of (usually either one or three) **colour components**.
- The colour components are interpreted as colour encoding in a standard representation scheme, the vast majority of times this representation being **RGB** (red, green and blue) and occasionally **HSB** (hue, saturation and brightness). RGB is used directly in the computers and their display hardware, but HSB and similar encodings are more intuitive for humans to think about colours and perform transformations on them.
- To encode a **grayscale image**, the colour dimension needs only one brightness value, and the entire image is therefore a two-dimensional **ndarray**.
- The colour component intensities are given either as floating point numbers from 0 to 1, or as one-byte **unsigned integers** from 0 to 255. With colour transformations, proper care should be taken to ensure that the computed result values stay within these limits.
- In principle, any image operation could be written as a Python function that operates on these numbers, and this way theoretically build up all of Photoshop from scratch. (After all, that is what the Adobe engineers did and still continue to do, although using a very different programming language!) To get us going, a whole bunch of **filters** and other common image operations have been implemented in the scipy.ndimage module.
- Image convolution with the given kernel matrix is a powerful operation to achieve a multitude of cool things. Many important image processing operations such as edge detection can be expressed as convolutions with a suitable kernel.

- If the convolution is not supposed to cause the pixel intensity of the image to overflow, the kernel matrix elements should add up to 1.0 to maintain the intensity of the image, but this is not any kind of law of nature or man.
- An uncompressed audio recording given as a **wav** file is a one-dimensional vector of intensity numbers for each sound channel, one channel for mono and two channels for stereo sound.
- (The more famous **mp3** format compresses this raw data in a clever fashion that slightly corrupts the sound but in a way that the human ear cannot detect. In graphics, the **jpeg** image encoding scheme works on the same principle. Increasing the compression rate makes the resulting file correspondingly smaller, but introduces disturbing artifacts that the human eye and ear can notice.)
- The intensity of the sound has to vibrate and fluctuate for the human ear to detect a sound. Simple **pure notes** are produced with **sine waves** of the desired frequency. Other waveform shapes produce different sounds that consist of multiple frequencies and therefore sound more natural and thus far more pleasant to the ear.
- Human senses in general dislike and are suspicious of signals that are too pure and
 monotonous to have emanated from natural sources. On the other hand, there needs to be
 some underlying sense of order for the signal to not degenerate into noise that is equally
 unpleasant for humans. Aesthetics is the art of finding the sweet spot between these two
 extremes.
- (As is known in mathematics, arbitrary curves can be broken down into sums of sine waves of different frequencies and intensities with **Fourier analysis**.)
- The intensity of any sound given as a vector of numbers can be modified by multiplying the numerical values (again being careful to avoid overflow), and adding and averaging simple sounds produces a sound that contains them both in desired portions.
- Completely random sound intensities produce **noise** whose type depends on the properties of the random distribution used to produce these random intensities. Different types of noise with different properties can be produced with statistical and mathematical methods.

Week 11: Classes and objects

11.1. Thinking in abstractions instead of implementations

• Python mixes imperative, functional and object oriented programming paradigms in a concise and relaxed fashion that allows programmers not only to freely choose the extent they wish to follow each paradigm, but mix and match these paradigms within the same program depending on what is most convenient for their needs at the moment.

- So far, we have expressed all our concepts using the data types that already exist inside the language or its standard library modules. For example, earlier we laid down the decision that an ordinary **playing card** is represented using a tuple of exactly two strings that encode the rank and suit descriptions, such as ('jack', 'diamonds').
- This decision could have been made differently in many other ways, depending on our needs on the behaviour of and allowed operations on these playing cards. In the end, we had to choose one of them, and then stick with that choice consistently.
- To be able to handle the playing cards correctly, the rest of the code now has to know that the implementation of the concept of a playing card is specifically this one. Once a critical mass of people has released code whose execution depends on the assumption that playing cards are represented specifically this way, we can no longer change the internal representation of these playing cards, even if we one day later think up some representation more suitable for the now-clarified needs that we did not realize we ever had during the original design phase.
- There is nothing inherently wrong with such a low-level approach to data. It just feels like programming way back in the Pleistocene era of computing in the sixties and seventies with machines that look like someone copied their design and sounds of operations from some Don Martin cartoon in *Mad Magazine*.
- The more modern **object oriented** paradigm allows programmers to define brand new data types of their own, along with the operations for that data type.
- These new data types can be used to create new **instances** as objects in the program in that these objects are not fundamentally any different from other objects such as lists, strings, Fraction objects or objects from any "native citizen" types defined in Python language and its standard library modules.
- Instead of thinking at the level of "To analyze a hand of cards, my code operates on the list whose elements are tuples that contain two strings for rank and suit", you get to think about the problem at the level of abstraction of "To analyze a hand of cards, my function operates on the list whose elements are playing cards".
- In fact, once you define the concept of "hand of cards" as a separate data type Hand, you get to think at an even higher level "My function operates on a Hand of Card objects", without knowing (nor even caring not one whit, jot or tittle) how those cards are internally represented inside that Hand object!
- In good **object oriented design**, the **nouns** of the problem domain become classes in the program, and **verbs** become methods in those classes. Especially when our programs grow larger, this approach makes the program design more **stable** and **robust** compared to a more old-time design where classes and functions stem from the internal organization of the program functionality, instead of the objective structure of the problem domain.

- The larger and more complicated some system is, the higher level concepts we need to be thinking about it! Within the confines of our small human brains and the slow conscious mind, a large system cannot be designed and understood trying to think about it as the sum of its nitty gritty low level details and operations.
- This is pretty much the same principle of why we don't write our programs directly in binary machine code, the true and honest underlying reality of all computation, but prefer higher level programming languages to express our ideas in terms of higher level concepts.
- (The obligatory quote in this context is always "Civilization advances by extending the number of important operations which we can perform without thinking of them", as noted by Alfred North Whitehead back in 1911. This world and our lives in it are a series of small decisions, and the more of those decisions we can automate, the fewer of them need to be solved with expensive humans and their brain cycles.)
- The ultimate ideal that the object oriented design and programming strives towards is that **no problem should ever have to be solved more than once**, after which that problem should never need to be solved again by anybody, unless they perhaps feel like getting some frisk programming exercise, or if they believe that they could come up with a more efficient solution to that particular problem.
- Useful and powerful concepts are turned into modules and released into the world so that other people can also use them. Really useful concepts will eventually become part of the language standard library, and the most useful ones such as "dictionary" or "set" eventually get absorbed into the very language itself.
- For example, try to imagine Python as an otherwise identical language, but without the dict data type in the standard library. How much more difficult would our various examples and lab problems have been to implement without this immensely powerful concept of the dictionary at our fingertips to do half our work for us?
- It has been said that if you are unable to solve some problem by programming, that merely proves that the concepts available in your language are insufficiently advanced. Any problem becomes trivial to solve once you have sufficiently high level concepts at your fingertips. (The real problem seems to be for somebody to first invent and implement those concepts in a way that is useful for us mere mortals!)

11.2. Defining your own classes

• To define your own data type as a **class**, use the keyword **class**. Executing this nested statement creates and defines a **class object**, from which an arbitrary number of **objects** can later be **constructed**.

- Classes are objects in Python like everything else. What makes classes special is that some other object can be an **instance** of that object, such as "hello" being an instance of str, or 42 being an instance of int.
- During the execution of the nested class statement, the statements inside it are executed normally, but whatever names they define are stored in the namespace inside the class object that is being defined, instead of in the usual global namespace.
- Functions defined inside the class object are called methods that can later be called for
 the individual instances of your class. These methods are defined as functions, but their
 first parameter is always a reference to the object for which the method is being called.
 This parameter can be named anything, but is canonically named self so that other
 people reading your code can tell at a glance what is what.
- A class can also have **class attributes** that are defined for the class as a whole, instead of being separate attributes inside individual objects. These are accessed through the class object just like all other object names, of course. Class attributes represent data that is the same for everybody throughout the class, instead of being stored separately for each individual object.
- Class attributes are usually "plain old data", but like anything else in Python, they can be any object, including functions, even entire **nested classes**.
- For example, inside a hypothetical BankAccount class, balance would be an instance attribute so that every instance could have its own separate balance, whereas the total count of how many bank account instances exist would be a class attribute.
- Unlike most other object oriented programming languages, Python does not support encapsulation by dividing the attributes into public and private subsets so that only the public attributes would be accessible from the outside. The Python convention of starting an attribute name with a single or double underscore informs the outside users that the name is an implementation detail that works today when accessed from the outside, but that fact might change at any time in future versions of this class.
- To keep your own code **future compatible**, it should never assume anything, let alone depend on such private parts of the classes that it uses, but **depend only on the stable public interface** that is guaranteed never to change in backwards incompatible ways.
- Of course, it is up to the class designers and maintainers to keep their end of this promise.
 For any serious and well-established class libraries that have thousands or even millions of users around the world, in practice they always will. The alternative is simply too absurd and revolting to realistically worry about, akin to the owner of some successful factory suddenly going cuckoo for cocoa puffs and intentionally setting the whole thing on fire.

11.3. Naturalized citizens of Pythonia

- To create a new instance of the class Foo, simply use Foo as a function. The arguments that you pass to this function are passed on to the special **constructor** method __init__ that gets automatically called for the new object every time a new object is created. This method typically creates and assigns the new object's internal attributes, in addition to performing whatever other initialization work is necessary.
- To call a method that exists inside an object whose type is the class where that method was defined, use the syntax object.method(arguments), that should already be familiar to us in data types that we have imported from various modules. The Python virtual machine finds the method in the class that the object was constructed from, and executes it using the object as the additional argument self.
- Parametric polymorphism of built-in functions such as str allows these functions work smoothly even for objects that will be created decades after these functions were written. Python makes this possible by defining these functions to call certain special methods inside the object that was passed to them as argument.
- This makes the Python core language **future compatible** with any classes and objects that anybody may happen to create in the future.
- For example, the Python function str(x) internally calls the method x.__str__() and then returns whatever that method returned. (In your own data types, __str__ is a good method to define right away to make your debugging printouts human-readable.)
- A similar method <u>__repr__</u> is supposed to return a representation that satisfies the equality x == eval(repr(x)). This is not possible even in principle for some data types. To denote such impossibility, the returned representation can be enclosed in angle brackets to guarantee that any attempt to eval it will crash with SyntaxError.
- Other special **dunder methods** (<u>complete list</u>, also known as "**magic methods**") can be used to define the behaviour of Python's arithmetic operators, comparisons, indexing, ...
- Whenever the Python compiler sees the code using some built-in operator of the language, such as a + b, it just silently turns it into the expression a.__add__(b). This is the little wizard hiding behind the large curtain whose completely mechanical pantomime then makes all this wonderful magic just work.
- Just like the words and grammar of natural languages, the corresponding rules in all programming languages are made up anyway. Of course, since the idea is to get other people to also use your language, the syntactic constructs must be familiar to other programmers and people who want to learn to program, for example the **infix notation** of arithmetic operators such as + and *. It is the job of the compiler to parse the syntax and turn it into something that the machine can actually execute.

- When defining their own data types, it is the programmer's responsibility to ensure that
 __add__ and similar methods do the right thing as is appropriate for that particular data
 type. Consequently, if some operator does not even make any sense for a particular data
 type, that dunder method should be left unimplemented.
- Many operators impose an implied contract on the corresponding dunder methods so that these methods ought to behave a certain way. For example, the order comparison __lt__ ought to be transitive so that whenever a < b and b < c, then also a < c.
- As proven by the work of **Alan Turing** way back in the thirties, way before even before the first room-sized mechanical computers with their mighty processing speed measured in kilohertz was built, **all semantic properties of programs expressed in any programming language that is capable of universal computation are algorithmically undecidable. No compiler can therefore enforce the contract and reject a function that violates it**
- However, if these implied contracts are violated, many other classes and data structures can silently start behaving in weird ways, resulting in difficult bugs in your program.
- To define your own **iterator** type as a class, simply define the methods **__iter__** to create and return an iterator object (for many types, this method can just return self) and in that object, the method **__next__** to either produce the next item of the sequence, or raise **StopIteration** if there are no more elements.
- However, these days it is far easier to write a **generator**, especially if this iterator does not need to allow external access and modification of its internal state, which would be a pretty bad programming practice anyway outside some rather special narrow domains.

11.4. Patching in new properties

- Since everything in Python is (still) an object, classes and the methods defined inside them are still objects, and therefore everything that has been taught earlier about Python objects still stands as tall and firm as ever.
- If only one particular object within its type needs to do something special for which we do not wish to create a whole new subclass, **monkey patching** means reassigning the name of some method to refer to some other object than which that name was originally bound in the class object.
- Alternatively, one object can be given additional special attributes that the other objects of the same type do not possess in general.
- Python 3 allows some attributes to be defined as **managed properties** using the decorator @property. From the outside, these managed properties look and feel like ordinary attributes, but reading and writing them causes the associated function to be silently executed.

- This makes the access to those properties more uniform when inside the same Temperature object, both K and C are accessed as attributes, even though one of them is in reality a method. ("Which one? Only her hairdresser knows for sure.")
- The **property setter function** is typically used to enforce some constraints on the possible intended values of that property. For example, no Person should have a negative height or weight. Were these defined as ordinary attributes instead of managed properties, nothing would stop anybody from assigning bob.height = -42. (Even worse, since any name can always refer to any object whatsoever regardless of our intentions about types, assign bob.height = 'Hello, world!')
- The **property getter function** can be used to make that property **virtual** so that its value is not actually stored anywhere inside the object, but is computed on the spot every time it is needed, based on the values of the concrete attributes stored inside the object.
- Virtual properties can be defined upon other virtual properties. However, make sure that your program does not accidentally get stuck in an infinite recursion where these virtual properties are circularly defined based on each other, instead of these definitions leading down to reach something concrete, your code in effect becoming the famous infinite stack of turtles all the way down!

11.5. Subtyping existing concepts

- A significant chunk of the power of object oriented programming comes from the possibility of creating **inheritance** relationships between classes to enforce certain consistency within all objects constructed from the same class hierarchy.
- Statically typed languages such as Java allow the compiler to enforce this consistency to catch various logic errors at compile time, whereas Python maintains the loose spirit of "anything goes" in what the **subclasses** can do in relation to their **superclasses**.
- To express that your class is a subclass of another existing class, write the superclass name in parentheses after the name of the class. For example, class Car(Vehicle).
- Inheritance is used to denote **subtyping** between the problem domain concepts that the classes represent inside our program, in the sense that for the class B to reasonably be a subclass of A, every instance of the problem domain concept B must also be an instance of the problem domain concept A.
- For example, it would be perfectly reasonable for Car to be a subclass of Vehicle, but it would be nonsense for Car to be a subclass of Engine. Every car has an engine, but the car itself is not an engine from the point of view of its users, nor is an engine kind of a car.
- As the famous pithy saying in programming puts it, you can always write nonsense in any language. No programming language or its compiler can possibly enforce any kind of

- **semantic consistency** within the program. The compiler and the virtual machine can only ever enforce the **syntax** and **typing** rules, but that's as high as they can go.
- Whenever some name is accessed inside some object, and the object itself does not contain that name in its internal dictionary of names, the Python virtual machine climbs up the inheritance chain of classes to find the first available occurrence of that name. This way, each subclass needs to define only the functionality that is new in that subclass, and inherit everything else from its superclass.
- When defining a subclass, you can **redefine** method names to provide a different implementation for some method. This allows instances of different subclasses to respond to the same request in different ways, depending on their particular types.
- To prevent the programmer from accidentally overriding some methods that the subclasses ought not to override since the rest of the class has tacitly assumed that those particular methods perform some particular thing exactly as promised, Python silently performs **name mangling** on all the names inside class that begin with a double underscore, so that these mangled names are guaranteed to be distinct from the same names defined in its subclasses.
- Sometimes the existing superclass method implementation does some good stuff that we wish to also be available as a useful part of the subclass method implementation, to avoid falling into the cardinal sin of repeating that exact same code in the subclass method. To call the superclass version of some method from a subclass method, you can prefix the call with the call super(). This is perhaps most commonly seen inside the __init__ method
- An abstract superclass represents some problem domain concept that is too abstract to allow any concrete instances to exist, because some of its methods cannot be given a reasonable implementation at the level of this abstract concept. For example, we can imagine and describe what kind of sound a dog or a chicken makes, but we cannot similarly describe what kind of sound an animal makes, without knowing what specific subtype of animal that particular object happens to be.
- To make a Python class abstract, first have it subclass ABC from the module abc, and then decorate those methods that you intend to be abstract with @abstractmethod.
- Python syntax still requires these methods to have some kind of body, typically just pass.

11.6. Multiple inheritance

• Python also supports **multiple inheritance**, so that some subclasses can have more than one **immediate superclass**. In general, multiple inheritance inherently opens up a whole can of complications that do not arise when only the normal single inheritance is used, so we need to tread a bit more carefully here than usual.

- The **method resolution order (MRO)** algorithm built in the Python virtual machine determines which method gets executed when multiple superclasses define the same method name. This discipline usually does the right thing that the programmer intended.
- Multiple inheritance is perhaps most commonly seen in the wild with **mixins**, small superclasses that define one particular method (or a handful of methods closely related to each other) and possibly some data to represent some concepts from the problem domain. Other classes, regardless of what they might otherwise themselves be about, can then simply extend these mixin classes to get that functionality for themselves for free.
- Functions defined inside a mixin need to be written only once inside the actual mixin, instead of having to duplicate their code inside all the classes that use those functions.
- The grand theme that permeates throughout CCPS 209 Computer Science II after this is the following: **DON'T REPEAT YOURSELF.** See you there.