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In some natural underwater environments, however, autonomous navigation can become less tractable. Geological formations (e.g., faults, canyon walls, hydrothermal vents) are highly unstructured and rarely resemble simplified geometric shapes that conventional localization algorithms can distinguish and use to aid AUV navigation. For this reason, close proximity surveys are generally performed by ROVs using human-in-the-loop interpretation. In these cases, attending surface support ships are required, increasing the infrastructure requirements and complexity of operations. If AUVs are used, these vehicles can conduct survey operations a few meters from the seafloor if a relatively smooth gradient is expected. If not, they operate from extended standoff distances that relax obstacle avoidance requirements but sacrifice observing resolution and intervention capability. Extremely challenging environments for autonomous navigation, such as underwater caves, often require complex vehicle trajectories in close proximity to unstructured hazards. Umbilical entanglement is a major concern that limits ROV operation in cave systems, thus human divers remain the dominant explorers of these environments.

Diver-operated survey technologies increase the accuracy of *in situ* human exploration and mapping (Stone, Ende, Wefer, & Jones, 2000). The complexity and scale of caves that can be kilometers in length with multiple pathways make surveys very difficult and slow, with numerous dives conducted over several weeks (Farr, 1991). Unfortunately, the limited endurance of human physiology and life support systems (i.e., breathing gases supply) require that cave divers conduct inherently dangerous explorations, and many have lost their lives, making cave diving one of the riskiest exploration activities (Fock, 2013).

Like caves, marine wreckage sites also present extreme challenges for underwater navigation. During or following a shipwreck, an initial assessment is carried out as quickly as possible in order to minimize loss of life, stabilize the vessel, and prevent or mitigate environmental damage. In shallow water, these tasks are performed by divers with entanglement and entrapment risks similar to cave diving. In deeper water, ROVs are used for external wreck inspection and limited penetration within the wreckage because of vehicle entrapment and umbilical entanglement hazards. AUVs have the potential for accident response, particularly in early response phases requiring rapid initial assessment within the wreckage without creating additional risk to humans. A common misconception is that once a vessel capsizes or sinks, all of its entrapped occupants are immediately killed. Multiple cases over the past years have been documented in which survivors have been rescued from within submerged wreckage (BBC News, 2013; Gray, 2003).

An AUV capable of safe navigation in complex physically restrictive environments will be an invaluable tool in industry, science, and society. Improved localization is, however, a necessary next step for transitioning robotic

operations into confined underwater environments. This paper presents results from an experimental deployment in an underwater cave system based on a rigorous approach to simultaneous localization and mapping (SLAM) in confined and unstructured underwater environments.

## 2. BACKGROUND AND CLOSELY RELATED WORK

During the past 20 years, AUVs have become one of the standard tools for underwater exploration. Modalities using optical sensors (Eustice, Singh, Leonard, Walter, & Ballard, 2005; Marks, Rock, & Lee, 1995) and acoustic sensors (Lucido, Opderbecke, Rigaud, Deriche, & Zhang, 1996; Paduan, Caress, Clagueand, Paull, & Thomas, 2009) are applied to dam inspections (Ridao, Carreras, Ribas, & Garcia, 2010), marine geology (Escartín et al., 2008), and underwater archaeology (Bingham et al., 2010; Henderson, Pizarro, Johnson-Roberson, & Mahon, 2013). The majority of commercially available autonomous platforms are currently optimized for side scan sonar and bathymetric multibeam survey operations. Other functionalities, particularly two-dimensional (2D) and three-dimensional (3D) optical mapping, are not yet commonplace, although these techniques have been demonstrated extensively in field applications, and they remain an active area of research (Ferrer, Elibol, Delaunoy, Gracias, & Garcia, 2007; Inglis, Smart, Vaughn, & Roman, 2012; Johnson-Roberson, Pizarro, Williams, & Mahon, 2010; Nicosevici, Gracias, Negahdaripour, & Garcia, 2009; Pizarro, Eustice, & Singh, 2009; Richmond and Rock, 2006; Singh, Howland, & Pizarro, 2004).

Maps constructed by AUVs can be used to improve vehicle navigation estimation, either in real-time or in postprocessing, through the application of SLAM. This technique relies on filtering algorithms, which merge the noisy sensor measurements with information from a kinematic or a dynamic motion model of the system. SLAM was first addressed in a probabilistic framework in the early 1990s in the seminal work from Smith, Self, and Cheeseman (1990). Since then, a significant amount of research has been conducted and a number of algorithms have been proposed to formulate and solve the problem with notable achievements predominantly in land mobile robotics. Filtering algorithms commonly used for SLAM can be separated into Gaussian filters, such as extended Kalman filters (EKF), extended information filters (EIF), and nonparametric filters such as particle filters (PF). A method that has recently gained popularity is the pose-based graph (also known as Graph-SLAM), which offers a natural representation for solving the full SLAM problem. Pose-graphs are abstract representations of an optimization problem consisting of pose nodes, which represent the variables to be estimated and edges that represent constraints on the variables they connect. We refer the reader to Durrant-Whyte and Bailey (2006) and Bailey and Durrant-Whyte (2006) for a comprehensive review, and

Paull, Saeedi, Seto, and Li (2013) for a review focused in the underwater domain.

In the majority of SLAM algorithms, features are recognized and extracted from the images (optical or acoustic) represented as points or lines. For example, Ribas, Ridao, Tardós, and Neira (2008) represent the underwater walls of a marina as line features and use a robust voting algorithm that extracts these line features, together with their uncertainty, from the continuous sonar data flow of a mechanically scanned imaging sonar (MSIS). This technique then fuses the resulting information into a feature-based EKF-SLAM algorithm incorporating submapping techniques. Nevertheless, in a natural underwater environment, it may be difficult to recognize features via sonar, as their appearance can change significantly, depending on the point of view, making it extremely difficult to extract robust features. For this reason, a number of researchers have focused their efforts on using featureless methods, such as occupancy grids and scan matching.

AUV navigation in open waters often relies upon generally accepted solutions, and research efforts are now focusing on more complex environments such as manmade structures (Ridao, Carreras, Ribas, Sanz, & Oliver, 2014) and ship hull inspections (Hover et al., 2007). Walter, Hover, and Leonard (2008) describe a SLAM implementation for ship hull inspection using forward looking sonar (FLS) data from a highly maneuverable hovering AUV. This method applies an exactly sparse extended information filter (ES-EIF) algorithm to perform SLAM based upon features manually selected within FLS images. To automate the process, Hurtós, Ribas, Cufí, Petillot, and Salvi (2013) proposed the use of Fourier-based techniques to register 2D images from a multibeam FLS. The estimated registrations are used within a pose-graph optimization framework to obtain a globally consistent trajectory and to render acoustic mosaics of underwater environments.

Under ice regions is another example of complex overhead environment for AUV operations. An AUV must be able to return to its recovery location because aborting and surfacing while under ice is not a vital option. Moreover, in Arctic regions the ice is often moving, preventing recovery locations from being determined in advance, so the AUV must be able to relocalize a new recovery location in real time. To aid navigation, acoustic localization systems, such as LBL, are used (Jakuba et al., 2008; Plueddemann, Kukulya, Stokey, & Freitag, 2012). Since the first reported Arctic AUV deployment in 1972 (Francois & Nodland, 1972), there have been numerous missions with many notable examples. The Theseus AUV successfully and autonomously laid 175 km long fiber-optical cable (Thorleifson et al., 1997). Maridan Martin 150 AUV gathered the first side-scan imagery of the underside of the ice (Wadhams, Wilkinson, & Kaletsky, 2004), and the Autosub-II AUV obtained the first under-ice multibeam measurements (Wadhams, Wilkinson, & McPhail, 2006). In the ALTEX project,

an AUV capable of ranges between 1,500 and 3,000 km and with a depth rating of up to 4,500 m surveyed the water column under the Arctic (Bellingham, Cokelet, & Kirkwood, 2008). The Puma and Jaguar AUVs have explored hydrothermal vents in the Arctic ocean (Kunz et al., 2009). Explorer AUV collected under-ice bathymetry for 12 days without surfacing (Kaminski et al., 2010). On the other side of the earth, ENDURANCE AUV successfully surveyed an ice covered lake in Antarctica (Gulati et al., 2010; Stone et al., 2010).

Despite these advances, very few underwater robots have been operated in confined and overhead environments where external navigation aid is not feasible. One notable exception is a modified REMUS AUV for internal inspection of New York City's 72 km long, 4 m diameter aqueduct (Stokey et al., 2005; Vision Systems Design, 2004). This inspection survey relies on acoustic ranges from two Doppler velocity log (DVL) sensors that enable the vehicle to stay in the center of the aqueduct while it travels from one end of the pipe to the other end, in an assumed obstacle-free environment. Survey imagery is generated by digital still cameras positioned around the vehicle that provide a 360 degree field of view around the vehicle's main axis. In another application, White et al. (2010) tested different mapping and localization techniques across horizontal distances of less than 30 m in ancient Maltese cisterns with an MSIS-equipped ROV. Among the tested techniques are sonar image mosaics using stationary sonar scans, SLAM while the vehicle was in motion, SLAM using stationary sonar scans, and localization using previously created maps. However, the resulting sonar mosaic was produced by manually registering the scan images. In the same expedition, McVicker et al. (2012) used a combination of particle filter and least squares to estimate the ROV pose and to feed an octree-based occupancy grid map.

Pioneering work in natural confined environments was reported by Stone et al. (2000) mapping an underwater cave system (Wakulla Springs, Florida). Although the vehicle, called a digital wall mapper (DWM), was guided by divers and not designed as a robotic system, it successfully mapped 6.4 km of passages in 3D. The DWM was equipped with 32 narrow-beam sonar transducers located in a spiral array around the nose of the 2 m long, 150 kg (in air) instrument. It used a ping rate of 4 Hz, and dead-reckoning (DR) trajectory was estimated from an inertial measurement and a ring-laser gyro unit. To bound the inherent DR drift, custom designed georeferenced radio beacons were placed every few hundred meters along the path traveled. Diver-portable sonar survey systems with updated technology can allow for accurate mapping, but they remain fundamentally limited by the diver's risk and operational endurance.

The *DEPTHX* AUV (Stone, 2007), which evolved from the DWM, was designed to explore flooded caverns and tunnels, and to collect water column, wall samples, and environmental data. The vehicle used a full navigation sensor

suite and an array of 54 narrow-beam sonar transducers that provided range measurements around the vehicle. For pose estimation and map building, Fairfield, Kantor, Jonak, and Wettergreen (2010) implemented a SLAM method consisting of a Rao-Blackwellized particle filter for which the map is stored within a 3D evidence grid. To reduce the memory requirements, it relied on a deferred reference counting octree data structure. The algorithm was tested onboard the vehicle in real time in a series of dives in flooded natural cenotes to 318 m depth. Because of the cenotes nature, most of the AUV's trajectory was in the vertical axis where accurate pressure sensors provide absolute measurements, thus minimizing localization drift errors that can occur in horizontal trajectories. Nevertheless, to the best of our knowledge, this experiment remains the only autonomous exploration example in confined natural environments.

In our previous research (Mallios, Ridao, Ribas, & Hernández, 2014), we presented a pose-based algorithm to solve the full SLAM problem of an AUV localization in a confined, unknown, and possibly unstructured environment. This algorithm does not rely on features or any structural information, which is potentially advantageous when applied in natural environments. The method first estimates the local path traveled by the robot while forming the acoustic image (scan) with range data coming from an MSIS, providing position estimates for correcting the distortions that the vehicle motion introduces in the scans. Each new pose of a scan is maintained in an augmented state EKF (ASEKF) and is compared with previous scans that are in the nearby area using probabilistic scan matching. If sufficient scan points overlap, a match between the scans will introduce a constraint between the poses and update the ASEKF. These constraints help to identify and close the loops, which correct the entire trajectory, thus bounding the drift. The algorithm was tested with a dataset from the structured environment of a marina, and ground truth validation confirmed that this method could bound the mean error to 1.90 m with a variance of  $\pm 1.09$  m for a 600 m trajectory path.

Here we report the results of this ASEKF SLAM method in the natural environment of an underwater cave system. AUV compactness and long endurance is an overriding consideration for mapping confined overhead environments, which can extend in multiple branches with tight cross sections. For this work, we used a small-sized AUV equipped with low power sensors.

### 3. FIELD OPERATIONS SETUP

In this section, we detail the AUV experimental setup for the survey at the underwater cave system, focusing on the AUV systems configuration, including the robotic platform itself, its onboard sensors, and key issues of conducting the survey.

#### 3.1. Platform: A Testbed AUV

The *Sparus* AUV (Figure 1) was developed in the underwater robotics lab at Universitat de Girona (UdG), Spain, for participation in the Student Autonomous Underwater Challenge - Europe (SAUC-E) 2010. After winning this competition, *Sparus* transitioned to a research platform for the development and testing of new algorithms as well as for collecting datasets in real environments. It is a small torpedo-shaped vehicle with hovering capabilities and modularity that enables reconfiguration of hardware components. It has three degrees of vehicle motion control, and the propulsion consists of three thrusters (two controlling surge and yaw and one controlling heave) that are integrated in its hull. As opposed to most typical single-hull, torpedo-shaped AUVs that rely on forward motion and control surfaces to ascend and descend, the hovering capability of the *Sparus* vehicle allows it to operate close to the seafloor and in confined environments. The vehicle dimensions are 1.22 m in length by 0.23 m diameter and it weighs 25 kg in air, allowing it to be deployed from a wide variety of vessels, including small boats or from shore.

During the experiment, three types of sensors were onboard the *Sparus* AUV: navigation sensors for DR estimation, acoustic sensors for long-range perception and mapping, and optical sensors for ground truth validation. The vehicle's sensor suite, as configured for the cave survey, is listed in Table I. The software architecture of the vehicle is based on the open-source robot operating system (ROS) framework, which provides a structured communication, synchronization, and logging between the vehicle's subsystems and sensors (Quigley et al., 2009).

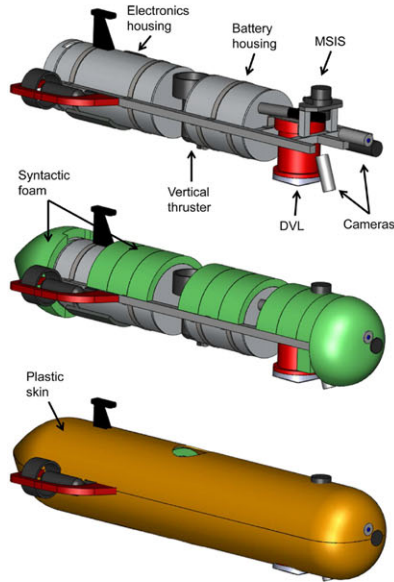
#### 3.2. Payload: Optical Sensors for Ground Truth

Optical imaging is a common choice for AUV survey operations, but it is generally limited to just a few meters (normally  $< 10$  m). Although it is difficult in practice to capture the full cave scene with vision systems, they can be used for trajectory estimation and ground truth. If the vehicle is keeping constant visual distance from the bottom, then visual-odometry algorithms can be applied to verify the trajectory (Furgale and Barfoot, 2010; Scaramuzza and Fraundorfer, 2011). In most cases, due to the natural structure of caves, the vehicle will return from the same path and visual features can be identified to close loops in a visual-SLAM framework (Elibol, Gracias, & Garcia, 2010) and estimate the trajectory error.

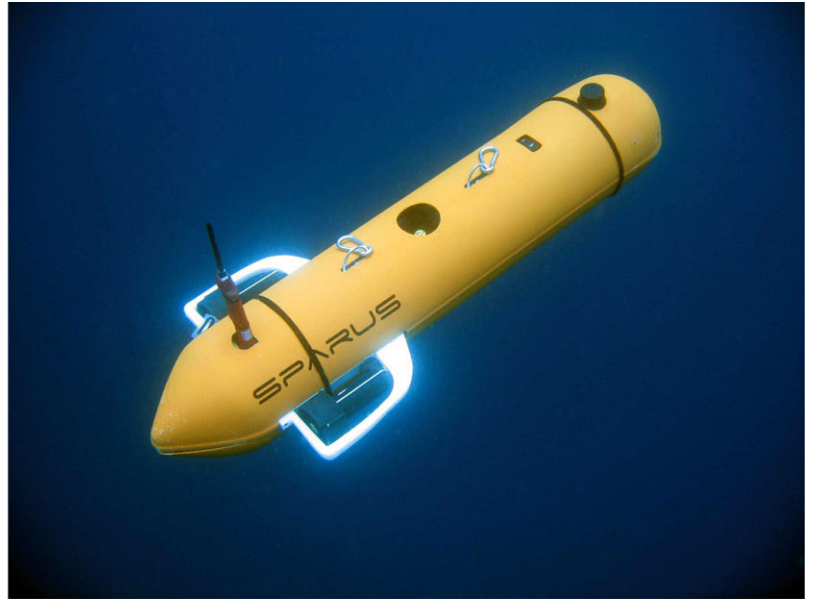
#### 3.3. Payload: Acoustic Sensors for Long-range Perception

Because through-water propagation of light is poor (Medwin and Clay, 1998), acoustic sonar sensing (instead of vision or laser sensors) is more appropriate for long-range



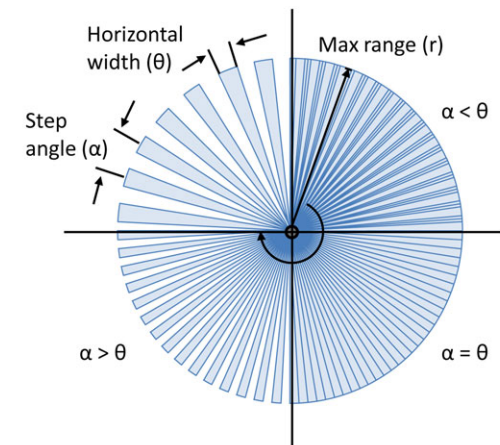


(a) Solid model

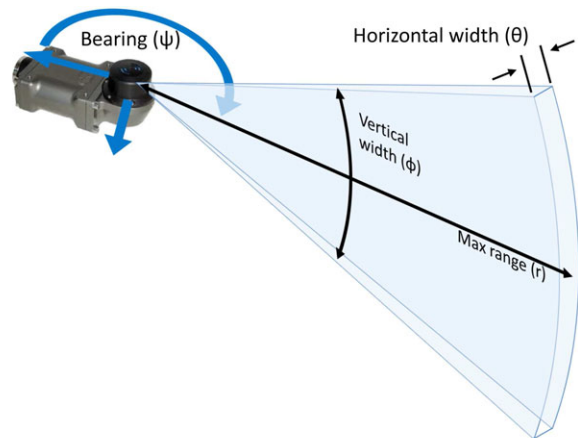


(b) Vehicle being deployed in standard configuration

**Figure 1.** Solid model of *Sparus* AUV and photo as deployed in standard configuration. The 1.22 m in length by 0.23 m diameter vehicle weighs 25 kg in air and the stored energy allows for 4–5 h of operations. It is mainly used as a research platform for development and testing of new algorithms



(a) Planar view of beam coverage. Step angle and horizontal width determines beam overlap.



(b) Perspective view of a beam.

**Figure 2.** MSIS acoustic coverage

perception and autonomous navigation tasks such as mapping, path planning, and obstacle avoidance. For our research, a MSIS was chosen because it enables a 360 deg field of view [Figure 2(a)], wider than commercially available multibeam imaging sonars (which are typically limited to  $\sim 120$  deg). Significant drawbacks to MSIS systems are their relatively low resolution and slow rotating mechanical heads.

Although the specifications regarding operating frequency, acoustic beamwidth, frame rate, and the internal beamforming technology depend on the specific sonar model and manufacturer, the principle of operation is the same. First, the sonar insonifies the scene with an acoustic wave, spanning its field of view in the azimuth ( $\theta$ ) and elevation ( $\phi$ ) directions, and then the acoustic return is sampled by an array of transducers as a function of range ( $r$ ) and

**Table I.** Summary of the *Sparus* AUV and sensor suite specifications.

Sensor	Specifications	Value	Description
Vehicle	Depth rating	50 m	UdG in-house design and assembly
	Size	$1.22(L) \times 0.23(D)$ m	
	Mass	25 kg	
	Survey speed	0.15 – 1.0 m/s	
	Energy	890 Wh	
Navigation	Propulsion	$3 \times 80$ W	Li-ion battery pack
	Velocity	$0.2\% \pm 1$ mm/s	Seabotix BDT150
	Pitch/Roll	0.1 deg	LinkQuest NavQuest600Micro
	Heading	0.3 deg	Analog Devices ADIS16480
	Depth	$\pm 0.25\%$	Analog Devices ADIS16480
Acoustic	<b>Imaging sonar</b>		DS2806 HPS-A
	Max range:	75 m	Tritech Micron DST
	Horizontal beam width:	3 deg	
	Vertical beam width:	35 deg	Tritech Super SeaKing DFP
	Scan rate (360 deg sector):	5 – 20 s	
	Frequency:	Chirped 650–750 kHz	
	<b>Profiling sonar</b>		
	Frequency:	0.6   1.1 MHz	
	Max range:	80   40 m	
	Beam width:	2   1 deg	
Optical	Scan rate (360 deg sector):	4 – 25 s	
	Vision system 1	Forward and down-looking	Analog cameras (PAL)
	Vision system 2	$1,920 \times 1,080$ pixels	GoPro Hero2 3D
	Lighting	$2 \times 24$ W	High-intensity discharge (HID)

bearing ( $\psi$ ) [Figure 2(b)]. Because of the sonar construction, it is not possible to disambiguate the elevation angle of the acoustic return originating at a particular range and bearing. In other words, the reflected echo could have originated anywhere along the corresponding elevation arc. Hence, the 3D information is lost in the projection into a 2D scan image.

For the cave survey presented here, two MSIS were installed on the vehicle, one horizontal and one vertical, which operated simultaneously.

**Horizontal scanning sonar** The horizontal scanning sonar is the main sensor used for the SLAM algorithm. As the vehicle moves, it provides the planar views (2D scan points) of the environment that the scan matching algorithm then registers and uses to extract the relative displacement of the vehicle, as described in Mallios et al. (2014). If the scans are sufficiently different, then the scan matching algorithm will be unable to register them. In a natural constraint environment such as the caves, the walls can have sufficiently large variations in vertical relief. For that reason, the decreased vertical resolution of a sonar with a wide vertical beam width can be exploited to aid horizontal scan matching. If the beam is sufficiently wide to overlap at differing vertical displacements, then the intensities per range will be more similar and the resulting scans will be more likely to match. On the other hand, if a sonar with

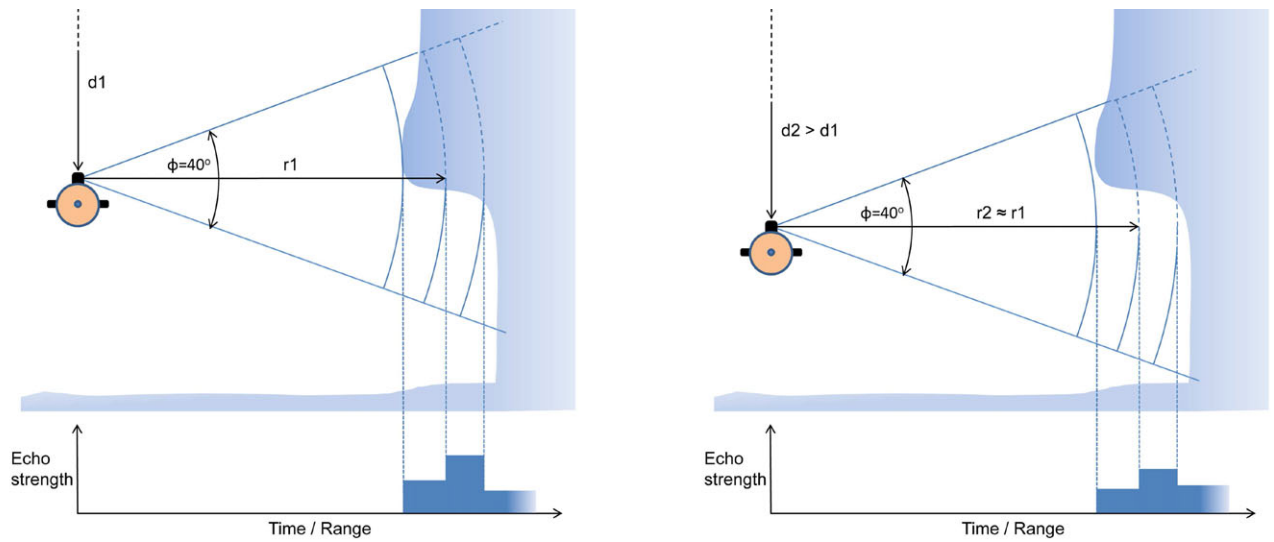
a narrow beam is used, then the scans will depend highly on the vertical position of the vehicle at scan acquisition (Figure 3).

**Vertical scanning sonar** In addition to the horizontal scanning sonar, a vertical MSIS was mounted to scan perpendicular to the vehicle's forward motion. The vertical MSIS's high frequency (1.1 MHz) and narrow beam (1 deg) can provide resolution up to 15 mm in order to capture as accurately as possible the 3D shape of the cave. However, because the beam is rotating, the final scan accuracy is correlated with the localization accuracy and the speed of the vehicle.

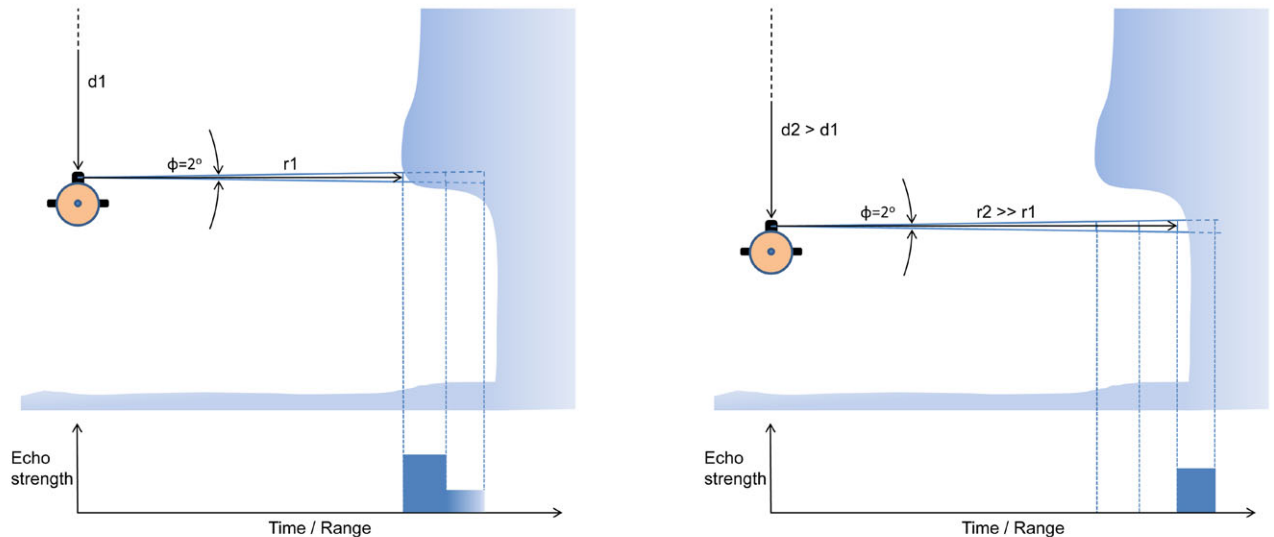
### 3.4. Dataset: The Underwater Caves Complex

The dataset was obtained in the underwater cave complex "Coves de Cala Viuda," located in the L' Escala area of Costa Brava, Spain (Lat: 42.103883, Lon: 3.182550) [Figure 4(a)]. The complex consists of three single-branch caves and several tunnels of different sizes, and it is part of a broader cave complex in the area that is popular among recreational divers (Llamas and Cáceres, 2010).

The survey was performed in June 2012 and was designed to provide quantified acoustic, optical, and inertial measurements for research in autonomous navigation. The dataset was collected with the *Sparus* AUV guided by a



(a) MSIS with 40 deg beam height. Vehicle's depth change has relatively small effect in output beam pattern.

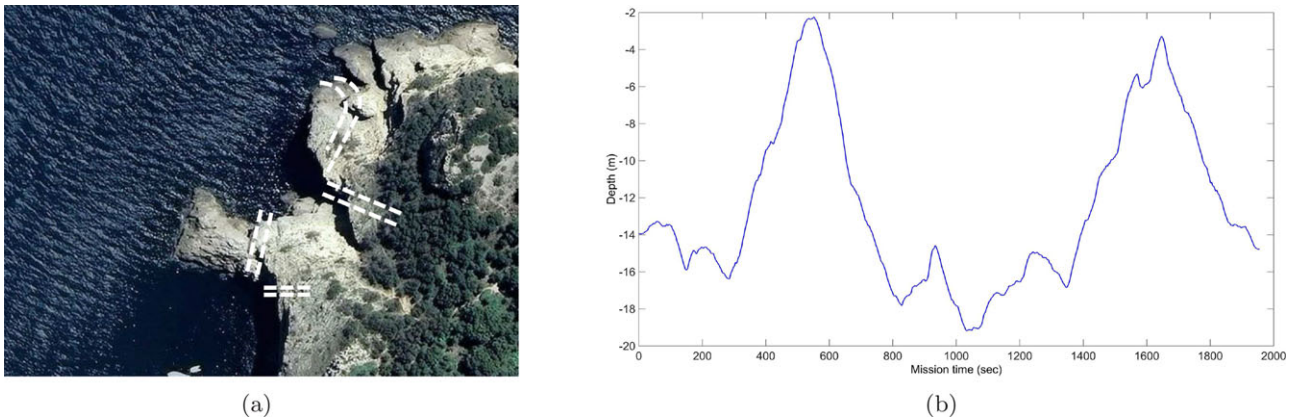


(b) Pencil beam MSIS with 2 deg beam height. Vehicle's depth change can have relatively large effect in output beam pattern.

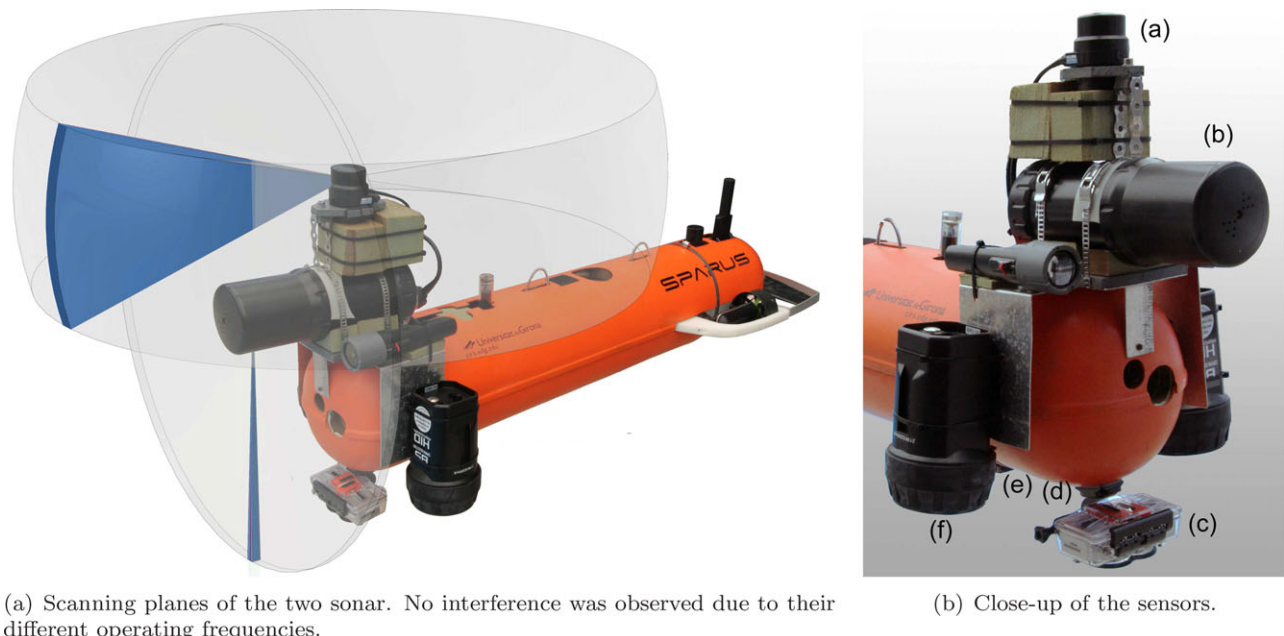
**Figure 3.** Effect of the sonar beam height in wall with strong relief

diver. It required three dives, all completed in a single day. The first dive was without the AUV for installing ground truth features (described subsequently). The second dive was with the AUV and was devoted to the acquisition of an initial dataset in order to test the trajectory and sensor settings. The third dive was the actual survey. This dataset explores two of the caves and tunnels, closing a loop of approximately 500 m length. The floor of the cave entrances is at a depth of approximately 20 m and ascends upward, following corridors with diameters varying from 1 to 17 m to interior surface air chambers at the end of each cave [Figure 4(b)].

The horizontal MSIS was configured to scan the entire 360 deg sector at a 20 m range, with a 0.05 m resolution at a 1.8 deg angular step that also defines the sensor's standard deviation. For this survey, the payload of the *Sparus* AUV was augmented with additional sensors (Figure 5). A 3D video system (Hero2, GoPro) together with two high-intensity discharge (HID) lights were mounted downward-looking in front of the main camera to collect imagery from the cave floor. The data recording of this unit was uncoupled from the vehicle system, and time synchronization was achieved by comparing specific frames with the main camera, which time-stamped its frames in the vehicle's



**Figure 4.** Gathering the dataset: (a) The approximate position of the underwater caves and tunnels are identified by the dotted white lines. (b) The depth profile of the AUV trajectory in this dataset



(a) Scanning planes of the two sonar. No interference was observed due to their different operating frequencies.

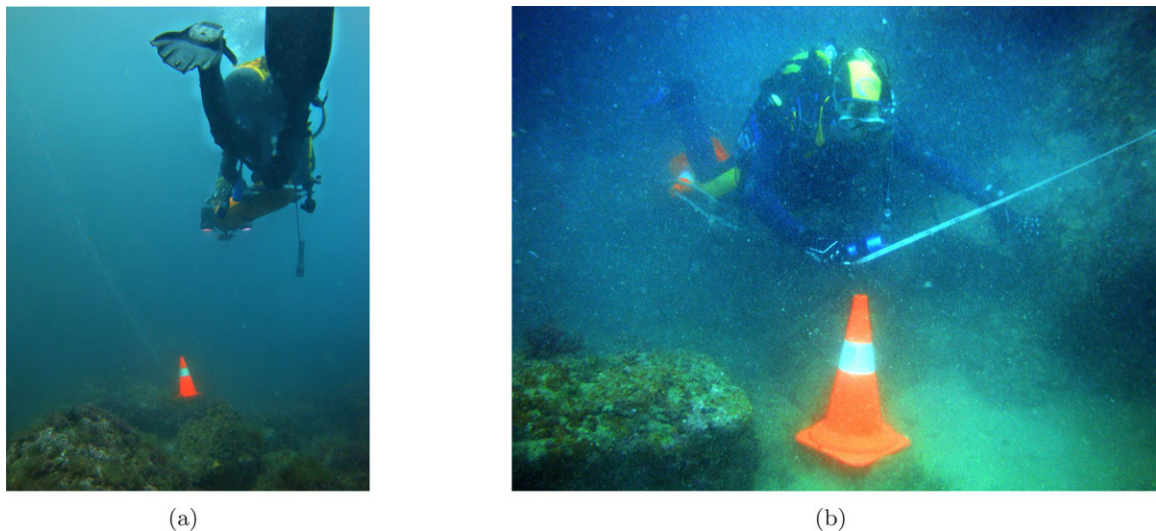
**Figure 5.** The *Sparus* AUV extended payload for the cave experiment included: (a) horizontal MSIS, (b) vertical MSIS, (c) 3D video camera, and (f) HID lights. Standard payload at the bottom part of the vehicle include (d) analog camera and (e) DVL

software architecture. Finally, in order to capture the 3D shape of the caves, the mechanically scanned profiling sonar was mounted in front and parallel to the forward axis of the AUV. The vertical MSIS emits a conical shape beam with a 1 deg angle at 1.1 MHz, and it was configured to scan the whole 360 deg sector in a 10 m range, with a 0.2 m resolution and a 1.8 deg angular step. In that configuration, a full sector scan requires approximately 4 s to complete.

For algorithm validation, the dataset includes six traffic cones as ground truth points [Figure 6(a)]. The cones were placed in strategic locations along the AUV trajectory over

which the vehicle passed twice, including the entrances of the caves and the beginning and end of the survey. The relative position of the cones can be found by extracting the timestamps from the video frames where the cones appear closest to the center of the image and comparing them with the time stamps of the trajectory. Then the distance of the cone from the reference frame of the vehicle can be found by using the existing camera calibration (Bouguet, 2004). An additional ground truthing step was included to manually measure and record the distances between the cones with a tape measure. Due to long distances and rock





**Figure 6.** Ground truth points for the cave dataset. In (a) *Sparus* AUV is guided over the cone. (b) Measuring the distances between cones

outcrops between the cones, the tape did not always follow a straight line, and these measurements are the upper bound of unknown variance [Figure 6(b)]. These tape measurements bound scaling error (a problem that is very common with scan matching algorithms in corridor areas) by providing a maximum length scale.

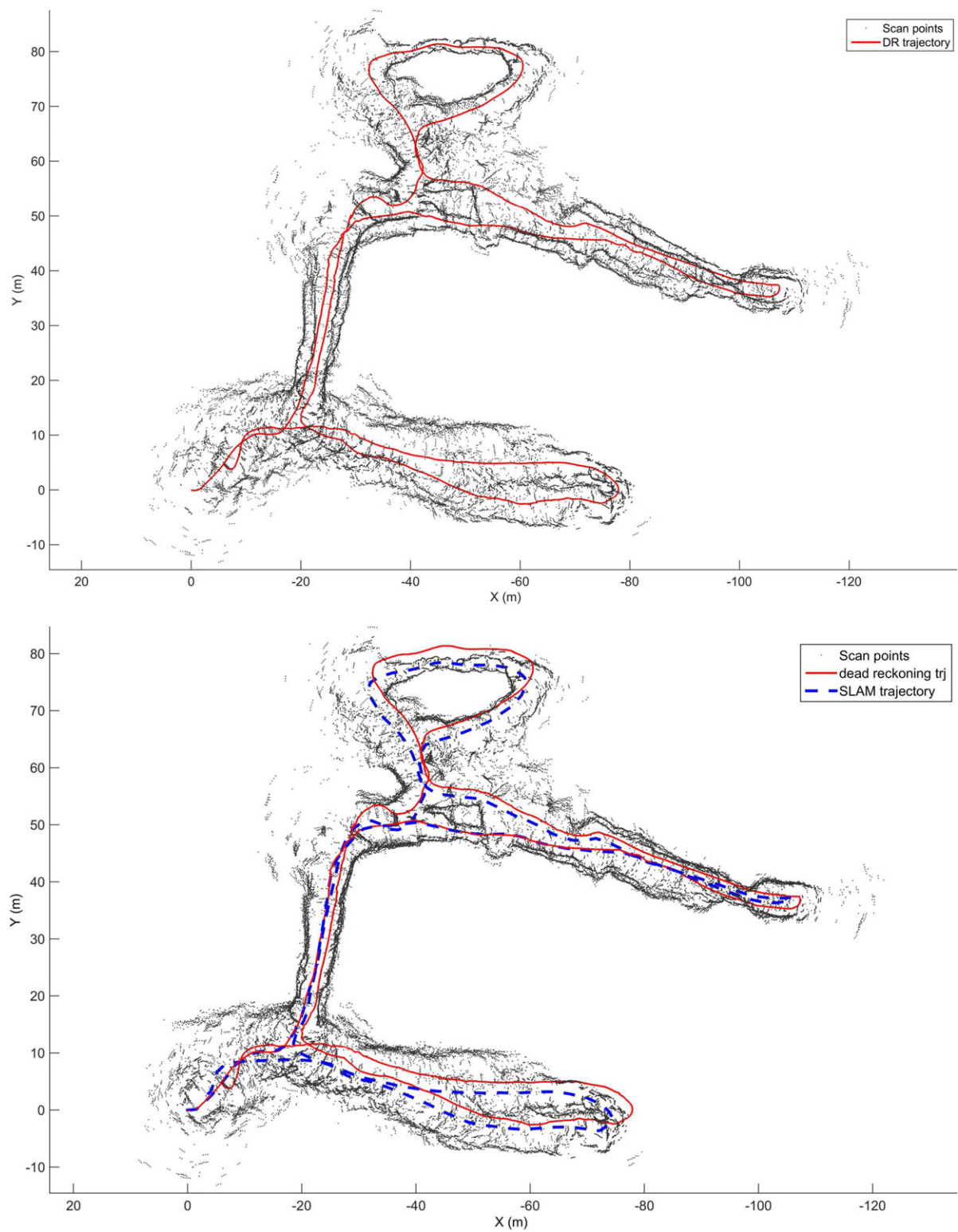
#### 4. RESULTS

Survey data indicate that the AUV's DR estimate, derived from the onboard DVL and the attitude and heading reference system (AHRS), drifted at a mean rate of 2.12% of distance traveled (based on errors measured at the cones). This drift was sufficient to generate observable inconsistencies in the resulting map (Figure 7, top), such as the corridor of the top cave and the corridor of the vertical tunnel. Figure 7 (bottom) shows the trajectory and the map estimated with the proposed SLAM algorithm, where these inconsistencies have been greatly reduced. The SLAM algorithm was able to bound the drift by cross-registering the majority of the scans in areas that the vehicle visited more than once. Figure 8 (top) shows the constraints from the cross-registration between the scan poses. The trajectory and map reconstruction can be seen as a video file in the supplementary material that accompanies this paper (Online Resource 1).

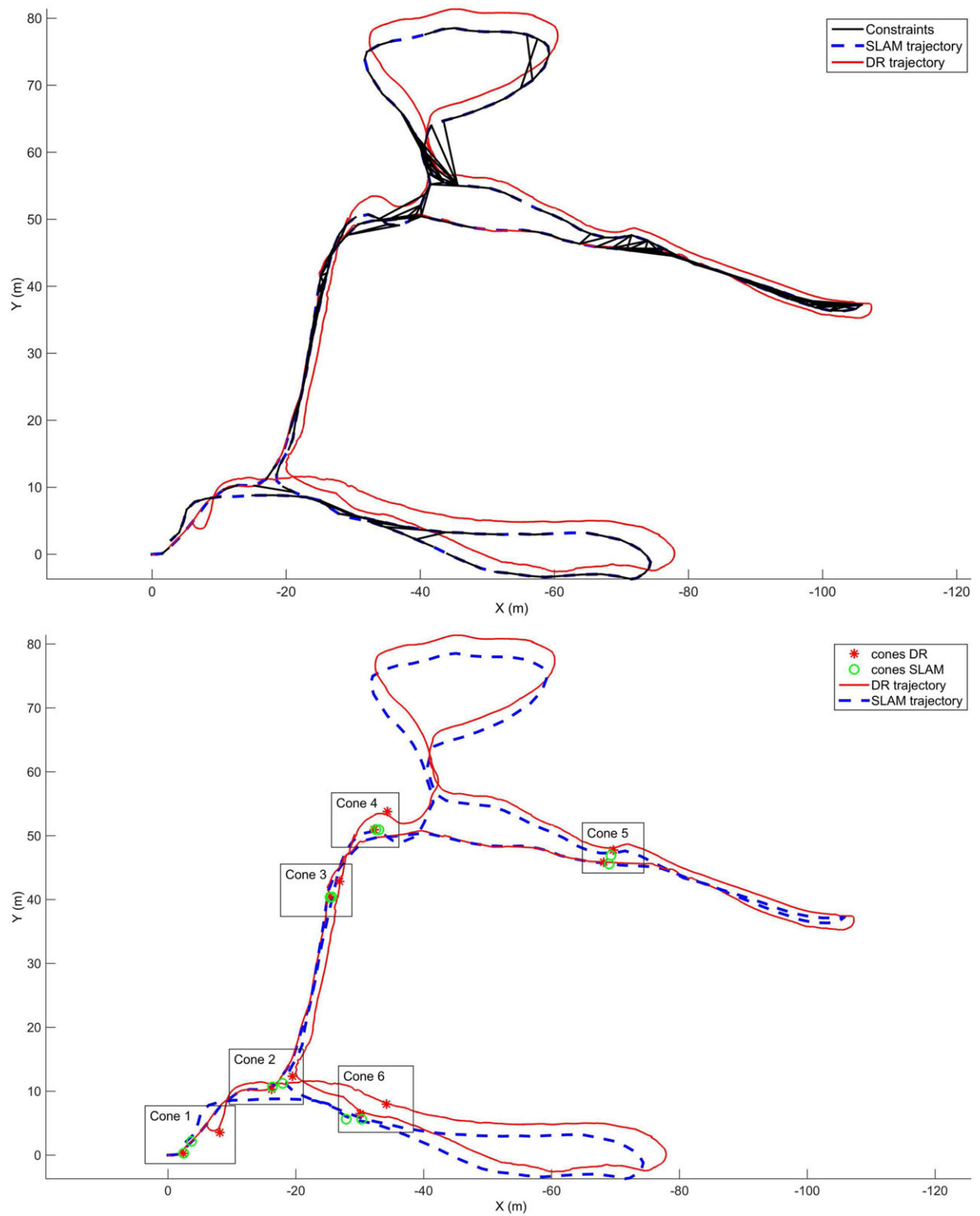
Due to turbidity conditions in most of the trajectory, data from the AUV's video systems could not be used for comparison with visual-odometry or visual-SLAM techniques. Fortunately, the visibility was adequate to record the traffic cones. These ground truth cones provide two metrics for evaluating the performance of the algorithm relative to DR using DVL and AHRS.

The first metric is the apparent difference in position (based on AUV trajectory estimate) between an initial and a subsequent appearance of a single cone when the vehicle passes over it twice. Table II summarizes these errors for the DR and the SLAM trajectory. Both are visualized in Figure 8 (bottom) and with additional detail in Figure 9. The maximum error can be observed at cones 1 and 6. Cone 1 is in an open area where there is not enough vertical information for the scan matching algorithm to identify and close the loop. At cone 6, the algorithm successfully cross-registered nearby scans, but the relatively large distance from the walls to the vehicle increases the uncertainty of the scans, resulting in larger error. For cones located in well-confined areas, the algorithm was able to significantly reduce the error. The overall performance of the SLAM algorithm, compared to DR, decreased the error from 0.5 to 1.0 order of magnitude.

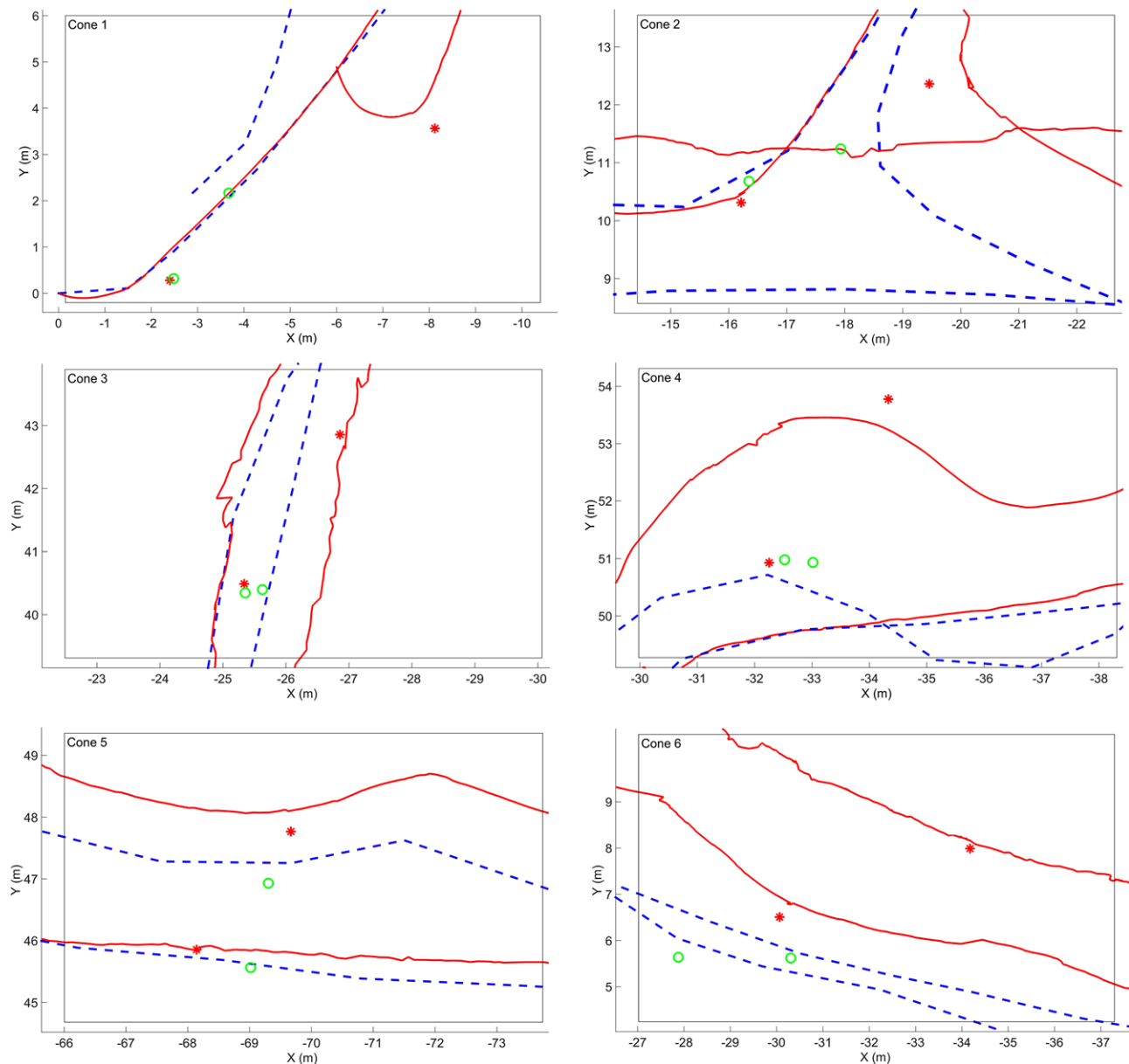
The second metric is the difference between the cone to cone distances recorded by divers using tape measures with those estimated from AUV trajectories. As previously described, the diver measurements represent the upper bound of variance due to obstructions preventing the tape from following a straight line. Table III summarizes all the measured and estimated distances. All of the AUV trajectory estimated distances are smaller than the diver measured distances, demonstrating that the algorithm does not suffer from a significant scaling problem, which can be very common in corridor areas. Unfortunately, due to the aforementioned tape measure obstruction issues, there is no accurate way of determining which estimated distance is most accurate. However, we can observe that the consistency of measurements between the same pairs using the SLAM algorithm has greatly improved compared with the DR estimation.



**Figure 7.** Cave complex trajectories and maps in 2D as seen from above. Top: map based on dead-reckoning estimation. Bottom: map based on SLAM result



**Figure 8.** Cave complex map of constraints and ground truth points. Top: map of constraints. Bottom: ground truth points as estimated from dead-reckoning (red asterisks) and from SLAM (green circles)



**Figure 9.** Zoom-in at the cone areas of the bottom of Figure 8. Ground truth points as estimated from dead-reckoning (red asterisks) and from SLAM (green circles)

Additional results validating the algorithm are shown in Figure 10. The top figure is the DR acoustic map, which was generated using sonar measurements from the complete dataset. The bottom figure is the acoustic map using the complete dataset and based on the SLAM estimated trajectory. The diffuse appearance of the DR image is caused by erroneous trajectory estimates. The SLAM trajectory provides a more self-consistent placement of the measurements, which results in a sharper image.

The survey dataset was acquired in approximately 32 min. The SLAM algorithm was implemented as a post-process in MATLAB, requiring approximately 19 min to complete using an Intel Core2 Quad @ 3.00 GHz CPU. The SLAM algorithm's limited computational requirements suggest that it may be appropriate for real-time operations under optimized implementation.

As previously described, during the survey the vehicle's vertically mounted MSIS scanned 360 deg



**Table II.** Cave experiment cones errors (\*relatively to distance traveled).

Cone #	DR error		SLAM error		Improvement %
	(m)	%*	(m)	%*	
1	6.60	1.36	2.20	0.45	66.67
2	3.84	1.16	1.68	0.51	56.25
3	2.81	1.05	0.28	0.10	90.04
4	3.53	1.47	0.49	0.20	86.12
5	2.44	3.06	1.40	1.75	42.62
6	4.37	4.59	2.43	2.55	44.39

**Table III.** Cave experiment error analysis. Cone pairs distance (\*see text about ground truth accuracy).

Cone pairs from - to	Ground truth* (m)	DR (m)	SLAM (m)
1 - 2	19	17.07	17.31
2 - 1	19	14.35	16.91
2 - 3	32	31.53	31.00
3 - 2	32	31.38	30.16
3 - 4	16	12.52	12.83
4 - 3	16	13.23	12.87
4 - 5	n.a.	n.a.	n.a.
5 - 4	n.a.	n.a.	n.a.
1 - 6	30	28.36	25.95
6 - 1	30	26.42	26.86

perpendicular to the traveling direction. This dataset was combined with the SLAM trajectory estimates to build a 3D map of the cave system.

To accomplish this, the collected scans were first segmented and the range points were extracted using the same process as the horizontal scanning sonar. Next, a cloud of points (Figure 11 top) was generated by projecting the scan points over the SLAM trajectory (taking into account depth, roll, and pitch). This cloud of points is the input of the splats distance normalized cut (SDNC) algorithm (Campos, Garcia, Alliez, & Yvinec, 2013) that is used to build the 3D surface model of the cave system. For each input point, a local quadratic surface was constructed using its k-nearest neighbors inside a RANSAC procedure (Figure 11 bottom). These local surfaces were merged in an unsigned distance function evaluated on a tetrahedral grid adapting to the density of the input points. Next, the distance function was signed by using a normalized cut algorithm to segment the volume of the object into its inside and outside. Finally, the surface was extracted at the interface of the two volumes using the restricted Delaunay triangulation surface mesher (Boissonnat & Oudot, 2005).

It is worth noting that the final three-dimensional reconstruction reveals passages that were not visible to the divers due to low water clarity. The cave map can be seen as an interactive 3D figure and video file in the supplementary material that accompanies this paper (Online Resource 2 & 3).

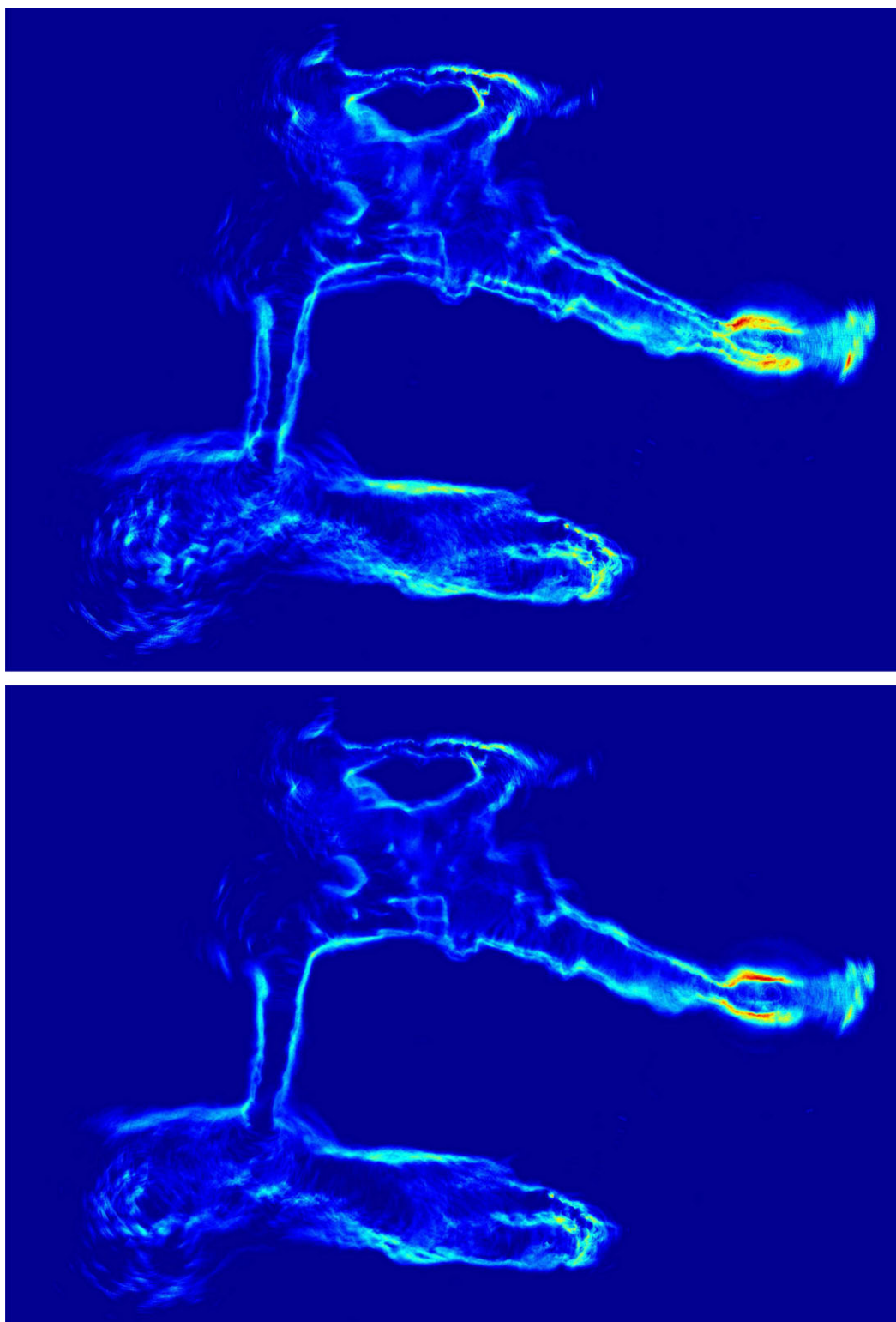
## 5. DISCUSSION

The experimental methods described here performed satisfactorily as a proof-of-concept in the complex environment of the cave system; however, there remains significant potential for improvement.

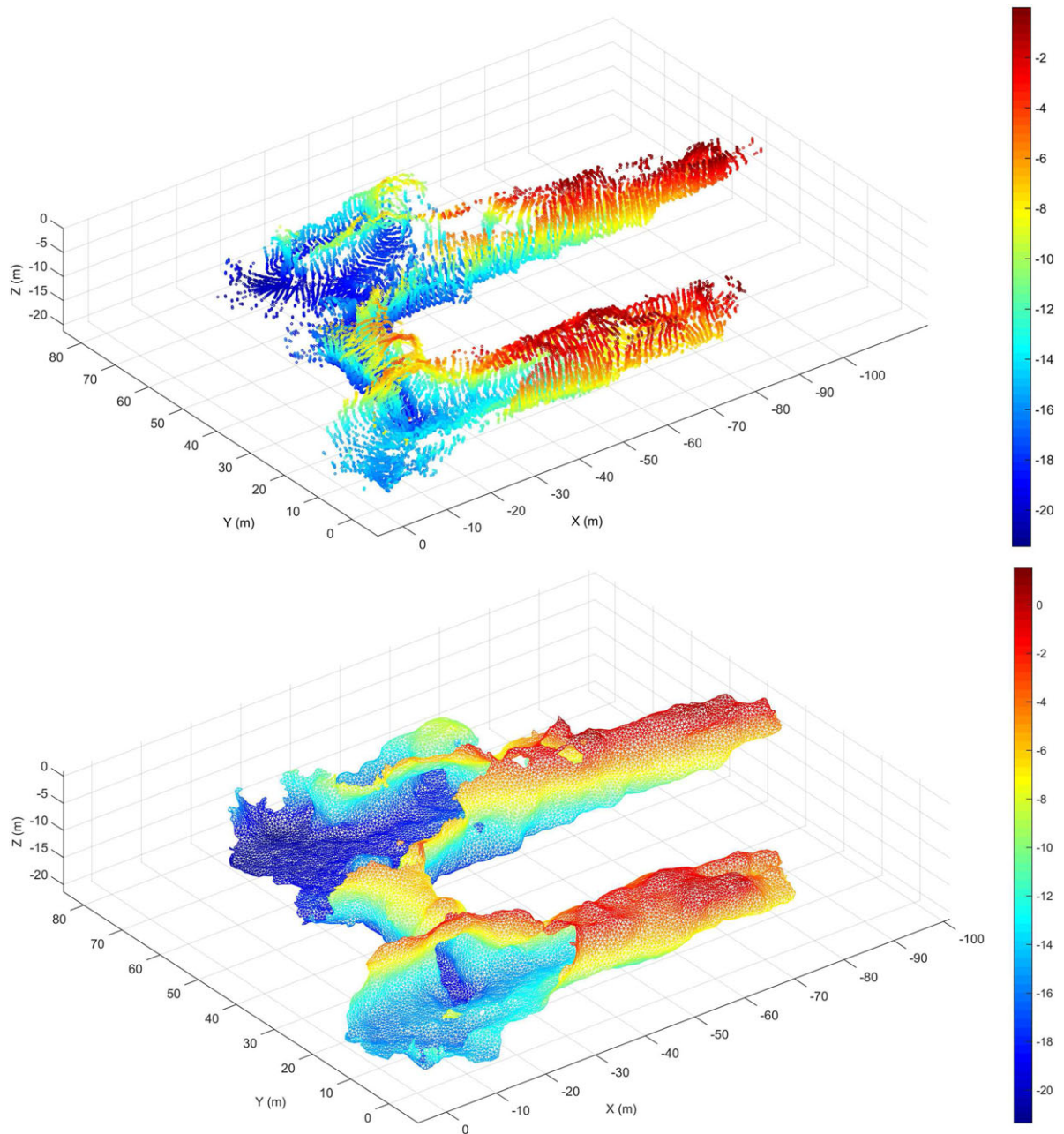
**Perception and data interpretation.** The horizontal MSIS, the main perception sensor used for localization in this experiment, provides 2D information that can be adequate for obstacle avoidance and path planning in areas where the vehicle explores at constant or gradually changing depths. In more complex environments (e.g. in a dead-end tunnel where the path continues above the vehicle or at an odd angle), the information from a native 3D sensor will be invaluable in order to find the correct path. Relevant research in the underwater domain in confined environments is in its infancy, with a lack of low power/size 3D sensors and relevant experiments (Poppinga, Birk, Pathak, & Vaskevicius, 2011).

**Scans registration.** Scan matching is a well-established technique for registering scans in a wide variety of environments. This technique, in tandem with the horizontal MSIS, performed as intended within the cave system complex where its internal walls provided sufficient data points. However, in areas with insufficient acoustic returns or self-similar regions, scan reconstruction will be inaccurately represented because of the relatively low number of scan points. The result is a high rate of rejected registrations and increased dependence on the DR estimation as an initial displacement step. Thus, the accuracy of the DR can have a direct impact on the final scan matching result. Exploitation of 3D information from the vertical MSIS (or, in principle, a native 3D sonar) can form dense scans that can be used to improve accuracy by minimizing false-positive registrations and increasing the scan registration rate, thereby improving overall robustness.

**Trajectory estimation.** The pose-based SLAM algorithm used in this experiment is built around an ASEKF stochastic map implementation for estimating scan poses. For our purposes, the well-known quadratic expansion problem of the map covariance matrix is partially relaxed because of the relatively low rate of pose additions and the short duration of the mission. Recent research in Graph-SLAM (Carlone, Aragues, Castellanos, & Bona, 2012; Kaess et al., 2012) and octomaps (Hornung, Wurm, Bennewitz, Stachniss, & Burgard, 2013) approaches offer



**Figure 10.** Acoustic maps obtained after an averaged composition of the sonar readings. Top: projected over the dead-reckoning trajectory. Bottom: projected over the SLAM estimated trajectory. Color represents the averaged intensities strength



**Figure 11.** Top: Cloud of points of the cave dataset as extracted from the profiling sonar and projected over the SLAM trajectory. Bottom: Meshed map using the SDNC algorithm. Color map represents depth in meters

promising efficiency gains and data consistency for longer missions.

**Mapping.** In our experimental setup, the map quality is a function of the trajectory estimation quality, vertical scanning sonar resolution, and vehicle speed. Assuming accurate trajectory estimation, speed becomes a limiting factor. Increased sonar resolution and range requires decreased

scanning speed (typical rotational rates can be on the order of tens of seconds), hence vehicle speed directly influences point cloud density. Multibeam profiling sonars can provide high resolution with rapid ping rates (on the order of a few Hz); however, because of their limited swath angle ( $\sim 120$  deg), multiple devices operating simultaneously would be needed in order to cover a full sector, significantly

increasing the vehicle’s dimensions, power consumption, and cost.

**Robotic platform.** An initial goal for exploration in confined environments would be robotic operations in areas where a human diver can transit. The *Sparus* AUV is well suited for operation at this size scale. However, there will be cases (such as inside a wreck) where the flexibility of a diver’s body will permit maneuvering in places difficult or impossible for a rigid AUV. Assuming that navigation and control requirements are solved, there are two possible solutions: a smaller AUV, the size of which may be limited by hardware component requirements, or advancements in an articulating/flexible body AUV.

**Ground truth.** Acoustic positioning and localization methods are prone to multipath effects and limited to line of sight telemetry. Radiofrequency methods have been successfully used in the past (Stone et al., 2000), however they require specialized hardware, attenuate rapidly over short distances, and they are challenging to calibrate. Visual features, such as the traffic cones used here, provide a simple point of reference for relative comparison. These markers, however, require prior installation and surveying, and an accurate georeferenced position is not always possible. Accurate ground truthing is an unresolved issue, and a unified approach has not yet been developed for all possible deployment cases.

**Scene complexity.** Navigating an AUV in complex and confined environments represents a step forward in field robotics. Although the cave system in which we contacted our experiment was well explored and mapped over a period of many years (Llamas and Cáceres, 2010), our work has demonstrated the ability to substantially improve the accuracy and spatial resolution of the map in a single 30 min dive. This field experiment offers the possibility to foster research toward autonomous investigation in other confined and potentially hazardous underwater environments, including shipwrecks, debris fields, deep caves, and unexplored natural systems.

6. SUMMARY AND CONCLUSIONS

This AUV experiment represents one of the very few field demonstrations in confined underwater environments, and to our knowledge it is the first reported demonstration of horizontal traversal through a cave system, with a trajectory loop closing of more than 500 m. Furthermore, this field experiment demonstrates localization and mapping using a compact AUV equipped with a modest (i.e., low power, small, and low cost) MSIS sonar as the main perception input for posed-based SLAM. This approach using rudimentary AUV hardware is enabled by a localization method that first estimates the local path traveled by the robot while forming the acoustic image (scan) with range data coming from an MSIS. Position estimates are then used to correct the distortions that the vehicle’s motion produces in the

scans. Next, the corrected scans are cross-registered under a probabilistic scan-matching technique for estimating the displacements of the vehicle, including the uncertainty of the scan-matching result. Successful registrations introduce constraints that an ASEKF uses to close loops, estimating a bounded error trajectory. The overall performance of the SLAM algorithm has been evaluated at six ground truth points, and the comparison to DR showed an error decrease from 0.5 to 1.0 orders of magnitude.

A second MSIS, which scanned perpendicular to the traveling direction, captured cross-sections of the cave system. These scans were projected over the SLAM trajectory estimates, and, after meshing, they were used to build a 3D surface model of the cave system.

Results indicate that the trajectory can be estimated in real time and the SLAM algorithm may be useful for autonomous obstacle avoidance and path planning. Moreover, this field experiment provides a new dataset for autonomous underwater navigation research in confined environments where surfacing or predeployment of localization equipment is not feasible.

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APPENDIX: INDEX TO ELECTRONIC SUPPLEMENTARY MATERIAL

Online resource	Media type	Description
1	Video file	SLAM algorithm visualization in the cave dataset
2	Video file	3D cave visualization
3	Interactive PDF	3D cave visualization



## REFERENCES

- Bailey, T., & Durrant-Whyte, H. F. (2006). Simultaneous localization and mapping (SLAM): Part II, state of the art. *IEEE Robotics and Automation Magazine*, 13(3), 108–117.
- BBC News (2013). Nigerian cook tells how he survived for three days trapped under sunken ship. <http://www.bbc.co.uk/news/world-africa-22888828>. Retrieved Dec. 18, 2013.
- Bellingham, J., Cokelet, E., & Kirkwood, W. (2008). Observation of warm water transport and mixing in the Arctic basin with the ALTEX AUV. In *IEEE/OES Autonomous Underwater Vehicles* (pp. 1–5).
- Bingham, B., Foley, B., Singh, H., Camilli, R., Dellaporta, K., Eustice, R., Mallios, A., Mindell, D., Roman, C., & Sakellariou, D. (2010). Robotic tools for deep water archaeology: Surveying an ancient shipwreck with an autonomous underwater vehicle. *Journal of Field Robotics*, 27(6), 702–714.
- Boissonnat, J.-D., & Oudot, S. (2005). Provably good sampling and meshing of surfaces. *Graphical Models*, 67, 405–451.
- Bouguet, J.-Y. (2004). Camera calibration toolbox for Matlab.
- Campos, R., Garcia, R., Alliez, P., & Yvinec, M. (2013). Splat-based surface reconstruction from defect-laden point sets. *Graphical Models*, 75(6), 346–361.
- Carlone, L., Aragues, R., Castellanos, J., & Bona, B. (2012). A linear approximation for graph-based simultaneous localization and mapping. *Robotics: Science and Systems VII* (pp. 41–48).
- Carrera, A., Carreras, M., Kormushev, P., Palomeras, N., & Nagappa, S. (2013). Towards valve turning with an AUV using learning by demonstration. In *Proceedings of the MTS/IEEE Oceans Conference*, Bergen (pp. 1–7).
- Durrant-Whyte, H. F., & Bailey, T. (2006). Simultaneous localization and mapping (SLAM): Part I, the essential algorithms. *IEEE Robotics and Automation Magazine*, 13(2), 99–108.
- Elibol, A., Gracias, N., & Garcia, R. (2010). Augmented state-extended Kalman filter combined framework for topology estimation in large-area underwater mapping. *Journal of Field Robotics*, 27(5), 656–674.
- Escartín, J., García, R., Delaunoy, O., Ferrer, J., Gracias, N., Elibol, A., Cufi, X., Neumann, L., Fornari, D. J., Humphris, S. E., & Renard, J. (2008). Globally aligned photomosaic of the Lucky Strike hydrothermal vent field (Mid-Atlantic Ridge, 37°18.5'N): Release of georeferenced data, mosaic construction, and viewing software. *Geochemistry, Geophysics, Geosystems*, 9(12).
- Eustice, R., Singh, H., Leonard, J., Walter, M., & Ballard, R. (2005). Visually navigating the RMS Titanic with SLAM information filters. In *Proceedings of Robotics: Science and Systems*. Cambridge, MA: MIT Press (pp. 57–64).
- Evans, J., Redmond, P., Plakas, C., Hamilton, K., & Lane, D. (2003). Autonomous docking for intervention-AUVs using sonar and video-based real-time 3D pose estimation. In *Proceedings of the MTS/IEEE Oceans Conference*, San Diego (vol. 4, pp. 2201–2210).
- Fairfield, N., Kantor, G., Jonak, D., & Wettergreen, D. (2010). Autonomous exploration and mapping of flooded sinkholes. *The International Journal of Robotics Research*, 29(6), 748–774.
- Farr, M. (1991). *The darkness beckons: The history and development of cave diving*. Cave Books.
- Ferrer, J., Elibol, A., Delaunoy, O., Gracias, N., & Garcia, R. (2007). Large-area photo-mosaics using global alignment and navigation data. In *Proceedings of the MTS/IEEE Oceans Conference*, Vancouver.
- Fock, A. W. (2013). Analysis of recreational closed-circuit rebreather deaths 1998–2010. *Diving and Hyperbaric Medicine*, 43(2), 78–85.
- Francois, R., & Nodland, W. (1972). Unmanned Arctic research submersible (UARS) system development and test report. Technical Report APL-UW 7219, University of Washington.
- Furgale, P., & Barfoot, T. D. (2010). Visual teach and repeat for long-range rover autonomy. *Journal of Field Robotics*, 27(5), 534–560.
- Gray, E. (2003). *Disasters of the deep: A comprehensive survey of submarine accidents & disasters*. Leo Cooper.
- Gulati, S., Richmond, K., Flesher, C., Hogan, B. P., Murarka, A., Kuhlmann, G., Sridharan, M., Stone, W. C., & Doran, P. T. (2010). Toward autonomous scientific exploration of ice-covered lakes—Field experiments with the ENDURANCE AUV in an Antarctic Dry Valley. In *IEEE International Conference on Robotics and Automation (ICRA)* (pp. 308–315). IEEE.
- Henderson, J., Pizarro, O., Johnson-Roberson, M., & Mahon, I. (2013). Mapping submerged archaeological sites using stereo-vision photogrammetry. *International Journal of Nautical Archaeology*.
- Hornung, A., Wurm, K. M., Bennewitz, M., Stachniss, C., & Burgard, W. (2013). OctoMap: An efficient probabilistic 3D mapping framework based on octrees. *Autonomous Robots*, 34(3), 189–206.
- Hover, F., Vaganay, J., Elkins, M., Willcox, S., Polidoro, V., Morash, J., Damus, R., & Desset, S. (2007). A vehicle system for autonomous relative survey of in-water ships. *Marine Technology Society Journal*, 41(2), 44–55.
- Hurtós, N., Ribas, D., Cufi, X., Petillot, Y., & Salvi, J. (2013). Fourier-based registration for robust FLS mosaicing in low visibility underwater environments. *Journal of Field Robotics*, 32(1), 123–151.
- Inglis, G., Smart, C., Vaughn, I., & Roman, C. (2012). A pipeline for structured light bathymetric mapping. In *IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)* (pp. 4425–4432). IEEE.
- Jakuba, M. V., Roman, C. N., Singh, H., Murphy, C., Kunz, C., Willis, C., Sato, T., & Sohn, R. A. (2008). Long-baseline acoustic navigation for under-ice autonomous underwater vehicle operations. *Journal of Field Robotics*, 25(11–12), 861–879.
- Johnson-Roberson, M., Pizarro, O., Williams, S., & Mahon, I. (2010). Generation and visualization of large-scale three-dimensional reconstructions from underwater robotic surveys. *Journal of Field Robotics*, 27(1), 21–51.

- Kaess, M., Johannsson, H., Roberts, R., Ila, V., Leonard, J. J., & Dellaert, F. (2012). iSAM2: Incremental smoothing and mapping using the Bayes tree. *The International Journal of Robotics Research*, 31(2), 216–235.
- Kaminski, C., Crees, T., Ferguson, J., Forrest, A., Williams, J., Hopkin, D., & Heard, G. (2010). 12 days under ice—An historic AUV deployment in the Canadian High Arctic. In *IEEE/OES Autonomous Underwater Vehicles (AUV)* (pp. 1–11).
- Kinsey, J., Eustice, R., & Whitcomb, L. (2006). A survey of underwater vehicle navigation: Recent advances and new challenges. In *Proceedings of the 7th Conference on Maneuvering and Control of Marine Craft (MCMC)*. IFAC, Lisbon.
- Kunz, C., Murphy, C., Singh, H., Pontbriand, C., Sohn, R., Singh, S., Sato, T., Roman, C., Nakamura, K., & Jakuba, M., et al. (2009). Toward extraplanetary under-ice exploration: Robotic steps in the Arctic. *Journal of Field Robotics*, 26(4), 411–429.
- Llomas, A., & Cáceres, P. (2010). *Guía submarina de les Illes Medes i la Costa del Montgrí*. Anthias.
- Lucido, L., Opderbecke, J., Rigaud, V., Deriche, R., & Zhang, Z. (1996). A terrain referenced underwater positioning using sonar bathymetric profiles and multiscale analysis. In *Proceedings of MTS/IEEE OCEANS* (vol. 1, pp. 417–421).
- Mallios, A., Ridao, P., Ribas, D., & Hernández, E. (2014). Scan matching SLAM in underwater environments. *Autonomous Robots*, 36(3), 181–198.
- Marani, G., Choi, S., & Yuh, J. (2009). Underwater autonomous manipulation for intervention missions AUVs. *Ocean Engineering*. Special Issue: AUV, 36(1), 15–23.
- Marks, R. L., Rock, S. M., & Lee, M. J. (1995). Real-time video mosaicking of the ocean floor. *IEEE Journal of Oceanic Engineering*, 20(3), 229–241.
- McVicker, W., Forrester, J., Gambin, T., Lehr, J., Wood, Z., & Clark, C. (2012). Mapping and visualizing ancient water storage systems with an ROV—An approach based on fusing stationary scans within a particle filter. In *Proceedings of IEEE International Conference on Robotics and Biomimetics (ROBIO)* (pp. 538–544).
- Medwin, H., & Clay, C. S. (1998). *Fundamentals of acoustical oceanography*. Boston: Academic Press.
- Nicosevici, T., Gracias, N., Negahdaripour, S., & Garcia, R. (2009). Efficient three-dimensional scene modeling and mosaicing. *Journal of Field Robotics*, 26(10), 759–788.
- Paduan, J. B., Caress, D. W., Clagueand, D. A., Paull, C. K., & Thomas, H. (2009). High-resolution mapping of mass wasting, tectonic, and volcanic hazards using the MBARI mapping AUV. In *International Conference on seafloor mapping for geohazard assessment* (pp. 181–186).
- Paull, L., Saeedi, S., Seto, M., & Li, H. (2013). AUV navigation and localization: A review. *IEEE Journal of Oceanic Engineering*, PP(99), 1–19.
- Pizarro, O., Eustice, R. M., & Singh, H. (2009). Large area 3-D reconstructions from underwater optical surveys. *IEEE Journal of Oceanic Engineering*, 34(2), 150–169.
- Plueddemann, A., Kukulya, A., Stokey, R., & Freitag, L. (2012). Autonomous underwater vehicle operations beneath coastal sea ice. *IEEE/ASME Transactions on Mechatronics*, 17(1), 54–64.
- Poppinga, J., Birk, A., Pathak, K., & Vaskevicius, N. (2011). Fast 6-DOF path planning for autonomous underwater vehicles (AUV) based on 3D plane mapping. In *IEEE International Symposium on Safety, Security, and Rescue Robotics (SSRR)* (pp. 345–350).
- Quigley, M., Conley, K., Gerkey, B. P., Faust, J., Foote, T., Leibs, J., Wheeler, R., & Ng, A. Y. (2009). ROS: An open-source robot operating system. In *ICRA Workshop on Open Source Software*.
- Ribas, D., Ridao, P., Tardós, J., & Neira, J. (2008). Underwater SLAM in man made structured environments. *Journal of Field Robotics*, 25(11-12), 898–921.
- Richmond, K., & Rock, S. M. (2006). An operational real-time large-scale visual mosaicking and navigation system. In *Proceedings of the MTS/IEEE Oceans Conference*. IEEE.
- Ridao, P., Carreras, M., Ribas, D., & Garcia, R. (2010). Visual inspection of hydroelectric dams using an autonomous underwater vehicle. *Journal of Field Robotics*, 27(6), 759–778.
- Ridao, P., Carreras, M., Ribas, D., Sanz, P. J., & Oliver, G. (2014). Intervention AUVs: The next challenge. In *19th World Congress. The International Federation of Automatic Control* (pp. 12146–12159).
- Scaramuzza, D., & Fraundorfer, F. (2011). Visual odometry: Part I: [Tutorial]. *IEEE Robotics & Automation Magazine*, 18(4), 80–92.
- Singh, H., Howland, J., & Pizarro, O. (2004). Advances in large-area photomosaicking underwater. *IEEE Journal of Oceanic Engineering*, 29(3), 872–886.
- Smith, R., Self, M., & Cheeseman, P. (1990). *Estimating uncertain spatial relationships in robotics* (pp. 167–193). New York: Springer-Verlag.
- Stokey, R., Roup, A., von Alt, C., Allen, B., Forrester, N., Austin, T., Goldsborough, R., Purcell, M., Jaffre, F., Packard, G., & Kukulya, A. (2005). Development of the REMUS 600 autonomous underwater vehicle. In *Proceedings of the MTS/IEEE Oceans Conference* (vol. 2, pp. 1301–1304).
- Stone, W. (2007). Design and deployment of a 3D autonomous subterranean submarine exploration vehicle. In *Conference on Un-manned, Un-tethered Submersible Technology*, Durham, NH.
- Stone, W., Hogan, B., Flesher, C., Gulati, S., Richmond, K., Murarka, A., Kuhlman, G., Sridharan, M., Siegel, V., & Price, R., et al. (2010). Design and deployment of a four-degrees-of-freedom hovering autonomous underwater vehicle for sub-ice exploration and mapping. *Proceedings of the Institution of Mechanical Engineers, Part M: Journal of Engineering for the Maritime Environment*, 224(4), 341–361.
- Stone, W. C., Ende, B., Wefer, F., & Jones, N. (2000). Automated 3D mapping of submarine tunnels. In *Robotics 2000: ASCE Conference on Robotics for Challenging Environments*.

- Thorleifson, J., Davies, T., Black, M., Hopkin, D., Verrall, R., Pope, A., Monteith, I., Den Hertog, V., & Butler, B. (1997). The Theseus autonomous underwater vehicle. A Canadian success story. In *Proceedings of the MTS/IEEE Oceans Conference* (vol. 2, pp. 1001–1006).
- Vision Systems Design, (2004). Submersible imaging system inspects NYC water supply. [www.vision-systems.com](http://www.vision-systems.com), 9(4), 9.
- Wadhams, P., Wilkinson, J., & Kaletzky, A. (2004). Sidescan sonar imagery of the winter marginal ice zone obtained from an AUV. *Journal of Atmospheric and Oceanic Technology*, 21(9), 1462–1470.
- Wadhams, P., Wilkinson, J. P., & McPhail, S. D. (2006). A new view of the underside of Arctic sea ice. *Geophysical Research Letters*, 33(4), L04501.
- Walter, M., Hover, F., & Leonard, J. (2008). SLAM for ship hull inspection using exactly sparse extended information filters. In *Proceedings of IEEE International Conference on Robotics and Automation (ICRA)* (pp. 1463–1470).
- White, C., Hiranandani, D., Olstad, C. S., Buhagiar, K., Gambin, T., & Clark, C. M. (2010). The malta cistern mapping project: Underwater robot mapping and localization within ancient tunnel systems. *Journal of Field Robotics*, 27(4), 399–411.