

# Design Of Data Structures

Course Code : 21SC1202

Target = 40

L - T - P - S : 3 - 0 - 2 - 4

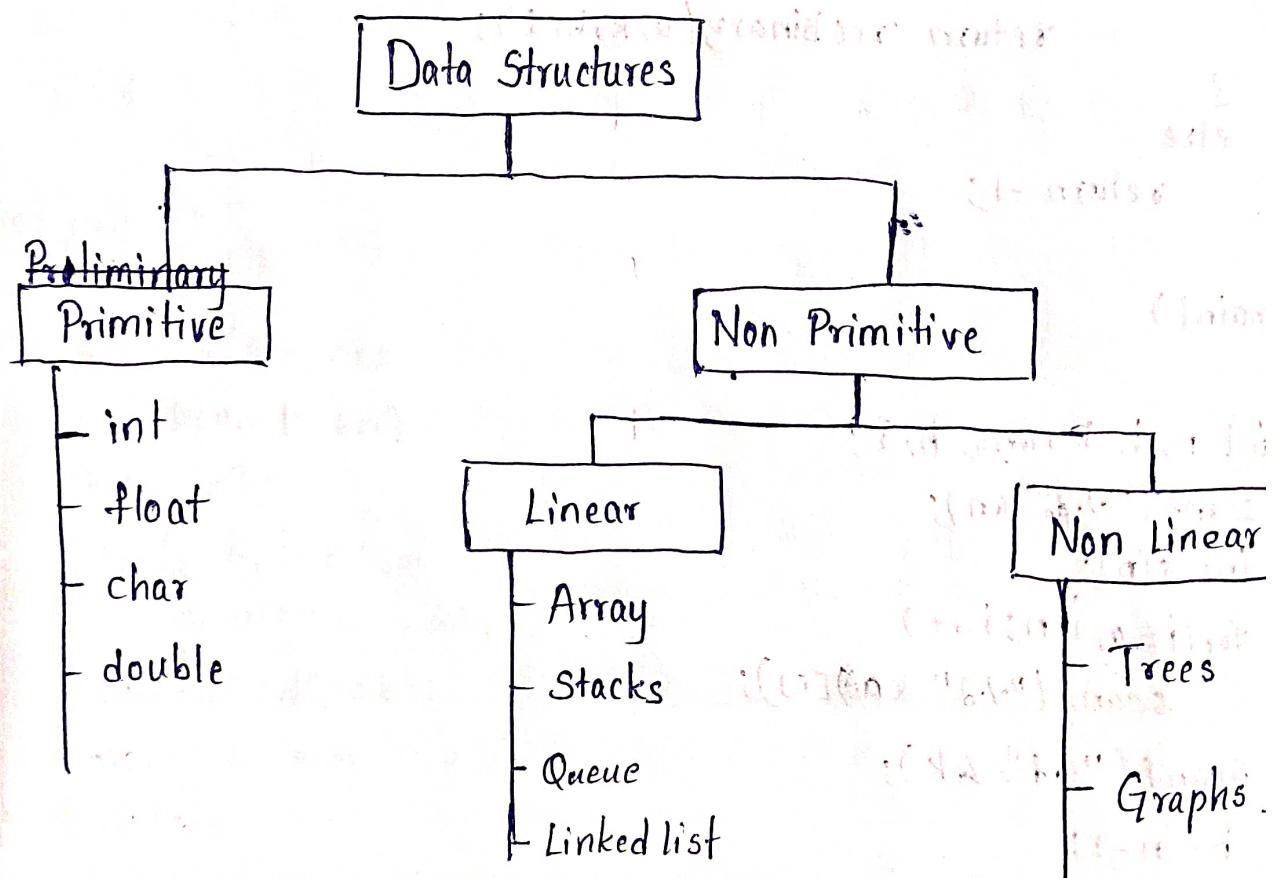
CO-1 : Algorithm Analysis & Sorting Techniques

CO-2 : Linear Data Structures

CO-3 : Hashing, Trees

CO-4 : Graphs

Credits : 5



Data Structures:

Organisation of data in well mannered order to facilitate its processing.

# Algorithm Analysis and Sorting Techniques.

## → Objective :

To implement different sorting techniques and evaluate their efficiency.

1. Mathematical Background

2. Model

3. Analyse

4. Running time calculations.

5. Introduction to sorting techniques

6. Insertion Sort

7. Shell Sort

8. Heap Sort

9. Merge Sort

10. Quick Sort

11. Bucket Sort

12. External Sort.

## → Introduction to Sorting Techniques.

Sorting: Arranging elements in ascending order or descending order in an array is called Sorting.

Time complexity of linear search is  $\frac{O(n)}{\downarrow}$ , where 'n' represents no of elements in array.  $\frac{\text{big O of } n}{\downarrow}$

Time complexity of binary search is  $O(\log n)$ .

## 1. Insertion Sort

- Insertion sort is in-place comparison sorting algorithm.
- Shell, insertion, bubble, selection sort comes under in-place comparison.
- In in-place comparison, we don't use additional memory for sorting.

### Algorithm

Step 1: Start

Step 2: If the array is having single element, it is already sorted.

Step 3: First element is already sorted, so pick the next element

Step 4: Compare this element with the elements in sorted sublist

Step 5: If the element is less than the elements in sorted sublist, then bring it into its place.

Step 6: Repeat step 3 to step 5 until the array gets sorted.

Step 7: Stop

Eg:

4	1	23	17	27	10	31	18	26
0	1	2	3	4	5	6	7	8

Pass 1:

4	1	23	17	27	10	31	18	26
1	4	23	17	27	10	31	18	26

Pass 2:

1	4	23	17	27	10	31	18	26
1	4	23	17	27	10	31	18	26

Pass 3:

1	4	23	17	27	10	31	18	26
1	4	17	23	27	10	31	18	26

Pass 4: 1 4 17 23 | 27 10 31 18 26  
no swap

1 4 17 23 27 10 31 18 26

Pass 5: 1 4 17 23 27 | 10 31 18 26

1 4 17 23 | 10 27 31 18 26

1 4 17 | 10 23 27 31 18 26

1 4 10 17 23 27 31 18 26

Pass 6: 1 4 10 17 23 27 | 31 18 26  
no swap

1 4 10 17 23 27 31 18 26

Pass 7: 1 4 10 17 23 27 31 | 18 26

1 4 10 17 23 27 | 18 31 26

1 4 10 17 23 | 18 27 31 26

1 4 10 17 18 23 27 31 26

Pass 8: 1 4 10 17 18 23 27 31 | 26

1 4 10 17 18 23 | 27 26 31

1 4 10 17 18 23 26 27 31

Final Sorted Array - 

1	4	10	17	18	23	26	27	31
0	1	2	3	4	5	6	7	8

## → Implementation

```
#include <stdio.h>
void insertionSort(int a[], int n)
```

```
{
```

```
printf("Before sorting ");
```

```
int t, i, j, k;
```

```
for(i=1; i<n; i++)
```

```
{
```

```
for(j=i; j>=0; j=j-1)
```

```
{
```

```
if(a[j] < a[j-1])
```

```
{
```

```
t = a[j];
```

```
a[j] = a[j-1];
```

```
a[j-1] = t;
```

```
}
```

```
}
```

```
printf("\n After 1st pass: ");
```

```
for(k=0; k<n; k++)
```

```
printf("%d", a[k]);
```

```
.
```

```
printf("\n After Sorting: ");
```

```
for(i=0; i<n; i++)
```

```
printf("%d", a[i]);
```

```
}
```

```
int main()
```

```
{
```

```
int n, i;
```

```
printf("Enter size of array: ");
```

```
scanf("%d", &n);
```

```
int a[n];
```

```
for(i=0; i<n; i++)
```

```
scanf("%d", &a[i]);
```

```
insertionSort(a, n);
```

```
return 0;
```

- Insertion sort is in-place comparison sorting algorithm.
- Insertion sort is flexible when list is having less no of elements.
- It is adaptive if the array is partially sorted.
- It is space efficient as it is using single variable (temp) for swapping.
- The worst case time complexity of insertion sort is  $O(n^2)$

Eg: Given an array of elements 30 -14 29 26 -37 11 -9 10 90  
 Represent the sorted list for every pass and give the final sorted array using insertion sort

30	-14	29	26	-37	11	-9	10	90
0	1	2	3	4	5	6	7	8

Pass 1 : 30 -14 29 26 -37 11 -9 10 90

-14 30 29 26 -37 11 -9 10 90

Pass 2 : -14 30 (29) 26 -37 11 -9 10 90

-14 29 30 26 -37 11 -9 10 90

Pass 3 : -14 29 30 (26) -37 11 -9 10 90

-14 29 26 30 -37 11 -9 10 90  
-14 26 29 30 -37 11 -9 10 90

Pass 4 : -14 26 29 30 (-37) 11 -9 10 90

-14 26 29 -37 30 11 -9 10 90

-14 26 -37 29 30 11 -9 10 90

-14 -37 26 29 30 11 -9 10 90

-37 -14 26 29 30 11 -9 10 90

Pass - 5 : -37 -14 26 29 30 | 11 -9 10 90

-37 -14 26 29 11 30 -9 10 90

-37 -14 26 11 29 30 -9 10 90

-37 -14 11 26 29 30 -9 10 90

Pass - 6 : -37 -14 11 26 29 30 | -9 10 90

-37 -14 11 26 29 -9 30 10 90

-37 -14 11 26 -9 29 30 10 90

-37 -14 11 -9 26 29 30 10 90

-37 -14 -9 11 26 29 30 10 90

Pass - 7 : -37 -14 -9 11 26 29 30 | 10 90

-37 -14 -9 11 26 29 10 30 90

-37 -14 -9 11 26 10 29 30 90

-37 -14 -9 11 10 26 29 30 90

-37 -14 -9 10 11 26 29 30 90

Pass - 8 : -37 -14 -9 10 11 26 29 30 | 90

~~no swap~~

-37 -14 -9 10 11 26 29 30 90

Final Sorted Array

-37	-14	-9	10	11	26	29	30	90
0	1	2	3	4	5	6	7	8

## 2. Shell Sort

Shell sort is in-place comparison sorting algorithm, it is generalized version of insertion sort.

$O(n \log n)$

9	8	3	7	5	6	4	1
0	1	2	3	4	5	6	7

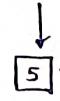
$n \approx 8$

$n = 8$

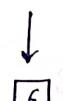
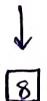
$$\text{gap} = n/2 = 8/2 = 4$$

9/8/3/7

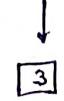
Pass - 1    9    8    3    7    5    6    4    1



5    8    3    7    9    6    4    1

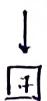


5    6    3    7    9    8    4    1



4    no swap

5    6    3    7    9    8    4    1



5    6    3    1    9    8    4    7

Pass 2  $\rightarrow$   $\text{gap} = \text{gap}/2 = 4/2 = 2$

5    6    3    1    9    8    4    7



3    6    5    1    9    8    4    7



6    1    5    9    8    4    7

3    6    5    6    9    8    4    7



5    9    6    4    7

3 1 5 6 9 8 4 7

↓  
[6] [8]

3 1 5 6 9 8 4 7

↓  
[9] [4]

3 1 5 6 4 8 9 7

↓  
[8] [9]

3 1 5 6 4 7 9 8

Part - 3 :  $\text{gap} = \text{gap}/2 = 2/2 = 1$

When  $\text{gap} = 1$ , insertion sort take place.

3 | 1 5 6 4 7 9 8

1 3 | 5 6 4 7 9 8

1 3 5 | 6 4 7 9 8

1 3 5 6 | 4 7 9 8

1 3 5 4 6 | 7 9 8

1 3 4 5 6 | 7 9 8

1 3 4 5 6 7 | 9 8

1 2 4 5 6 7 9 | 8

1 2 3 4 5 6 7 8 9

$\therefore$  Final Sorted Order : 1 3 4 5 6 7 8 9

10	7	35	9	25	23	86.
0	1	2	3	4	5	6.

$$n = 7$$

$$\text{gap} = n/2 = 7/2 = 3$$

Pass-1:

10 7 35 9 25 23 86



9 7 35 10 25 23 86



9 7 35 10 25 23 86.



9 7 23 10 25 35 86.



9 7 23 10 25 35 86.

Pass-2:  $\text{gap} = \text{gap}/2 = 3/2 = 1$

When  $\text{gap} = 1$ , insertion sort take place

9 7 | 23 10 25 35 86

7 9 | 23 10 25 35 86

7 9 23 | 10 25 35 86

7 9 10 23 | 25 35 86

7 9 10 23 25 | 35 86

7 9 10 23 25 35 | 86

7 9 10 23 25 35 86

∴ Final Sorted Array: 7 9 10 23 25 35 86.

→

35	33	42	10	14	19	27	44
0	1	2	3	4	5	6	7

$$n = 8$$

$$\text{gap} = n/2 = 8/2 = 4$$

Pam-1: 35 33 42 10 14 19 27 44



14 33 42 10 35 19 27 44



14 19 42 10 35 33 27 44

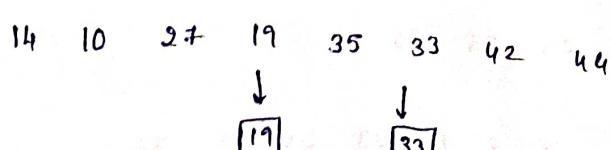
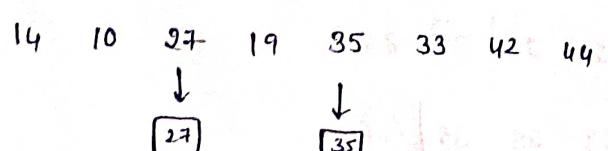
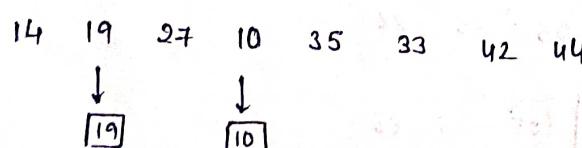
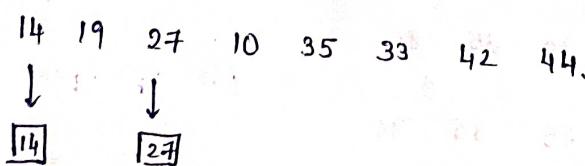


14 19 27 10 35 33 42 44



14 19 27 10 35 33 42 44

Pam-2 :  $\text{gap} = \text{gap}/2 = 4/2 = 2$



14 10 27 19 35 33 42 44



14 10 27 19 35 33 42 44.



14 10 27 19 35 33 42 44.

Pass - 3 :  $\text{gap} = \text{gap}/2 = 2/2 = 1$

When  $\text{gap} = 1$ , insertion sort take place.

14 | 10 27 19 35 33 42 44.

10 14 | 27 19 35 33 42 44.

10 14 27 | 19 35 33 42 44.

10 14 19 27 | 35 33 42 44.

10 14 19 27 35 | 33 42 44.

10 14 19 27 33 35 | 42 44

10 14 19 27 33 35 42 | 44

10 14 19 27 33 35 42 44.

∴ Final Sorted Array : 10 14 19 27 33 35 42 44.

## Implementation

```
#include <stdio.h>
void shellSort(int a[], int n)
{
    int gap = n/2, i, j, t;
    for (gap = n/2; gap >= 1; gap = gap/2)
    {
        for (i = gap; i < n; i++)
        {
            for (j = i; j >= gap; j = j - gap)
            {
                if (a[j] < a[j - gap])
                {
                    t = a[j];
                    a[j] = a[j - gap];
                    a[j - gap] = t;
                }
            }
        }
    }
    for (i = 0; i < n; i++)
        printf("%d", a[i]);
}

int main()
{
    int n, i;
    scanf("%d", &n);
    int a[n];
    for (i = 0; i < n; i++)
        scanf("%d", &a[i]);
    shellSort(a, n);
    return 0;
}
```

### 3. Quick Sort (Partition Exchange)

#### Algorithm for Quick Sort

Step 1: Start

Step 2: Set the pivot element as  $a[0]$

Step 3: Set two pointers  $i$  and  $j$ ,  $i = a[0] \& j = a[n-1]$

Step 4: Move  $i$  pointer towards right till the no is greater than pivot

Step 5: Move  $j$  pointer towards left till the no is less than pivot

Step 6: if  $i$  and  $j$  cross each other swap  $a[j]$  and pivot

Step 7: if  $i$  and  $j$  don't cross each other swap  $a[i]$  and  $a[j]$

Step 8: Stop

Eg:

35	33	42	10	14	19	27	44
pivot	0	1	2	3	4	5	6

$\uparrow i$

$\uparrow j$

$\uparrow i$

$\uparrow j$

$\uparrow i$

( $i \& j$  didn't cross each other, so  $a[j]$  &  $a[i]$  swapping take place)

$\uparrow j$

$\uparrow i$

( $i \& j$  crossed each other, so  $a[j]$  & pivot swapped)

19	33	27	10	14	35	42	44
pivot	$\uparrow i$	$\uparrow j$	$\uparrow i$	$\uparrow j$			

19	33	27	10	14	35	42	44
$\uparrow i$	$\uparrow j$	$\uparrow i$	$\uparrow j$				

$\rightarrow i \& j$  didn't cross

19	14	27	10	33			
$\uparrow i$	$\uparrow j$						

$\rightarrow i \& j$  didn't cross

19 14 10 27 33

$i \uparrow$

$j \downarrow$

$\rightarrow i < j$  crossed

pivot 10 14 19 27 33  
 $i \uparrow$   $j \downarrow$

[From here, no changes will be appeared.]

$\therefore$  Final sorted array obtained is.

10 14 19 27 33 35 42 44

pivot 10 14 19 27 33  
 $i \uparrow$   $j \downarrow$

Here  $j$  becomes -1

$\therefore$  Process stopped.

Final Sorted Array 10 14 19 27 33 35 42 44



Quick Sort is a Divide and conquer algorithm.

It picks an element as pivot and partitions the given array around the picked pivot.

There are many different versions of quickSort that pick pivot in different ways.

1. Always pick first element as pivot.

2. Always pick last element as pivot (implemented below)

3. Pick a random element as pivot.

4. Pick median as pivot.

Quick Sort Algorithm

1. if  $n \leq 1$ , then return.

2. Pick any element  $V$  in  $a[]$ . This is called the pivot.

3. Rearrange elements of the array by moving all elements  $x_i > V$  right of  $V$  and all elements  $x_i \leq V$  left of  $V$ .

4. If the place of the  $V$  after re-arrangement is  $j$ , the array by is partitioned as below.

all elements with value less than V, appear in  $a[0], a[1], a[2], \dots, a[j-1]$ . and those with value greater than V appear in  $a[j+1], \dots, a[n-1]$

5. Apply quick sort recursively to  $a[0], \dots, a[j-1]$  and to  $a[j+1], \dots, a[n-1]$ .

Eg: 35, 33, 42, 10, 14, 19, 27, 44, 26, 31

Eg: 10, 80, 30, 70, 40, 50, 90

Eg: 2, 8, 7, 1, 3, 5, 6, 4

### Implementation

```
#include <stdio.h>
void quickSort(int arr[100], int, int);
int partition(int arr[100], int, int);
int main()
{
    int arr[100], n, i;
    printf("Enter no of elements in array: ");
    scanf("%d", &n);
    printf("\nEnter %d elements: \n\n", n);
    for(i=0; i<n; i++)
        scanf("%d", &arr[i]);
    quickSort(arr, 0, n-1);
    printf("\nThe Sorted Array is: \n\n");
    for(i=0; i<n; i++)
        printf("%d", arr[i]);
    return 0;
}
```

```
void quickSort(int arr[], int low, int high)
{
```

```
    int j;
    if(low < high)
    {
        j = partition(arr, low, high);
        quickSort(arr, low, j-1);
        quickSort(arr, j+1, high);
    }
}
```

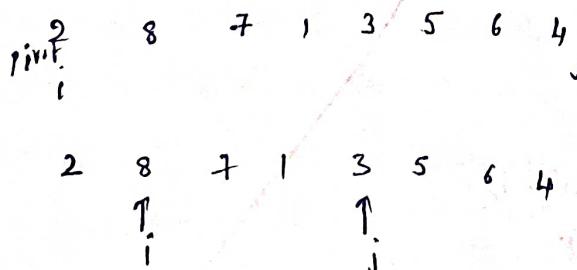
```

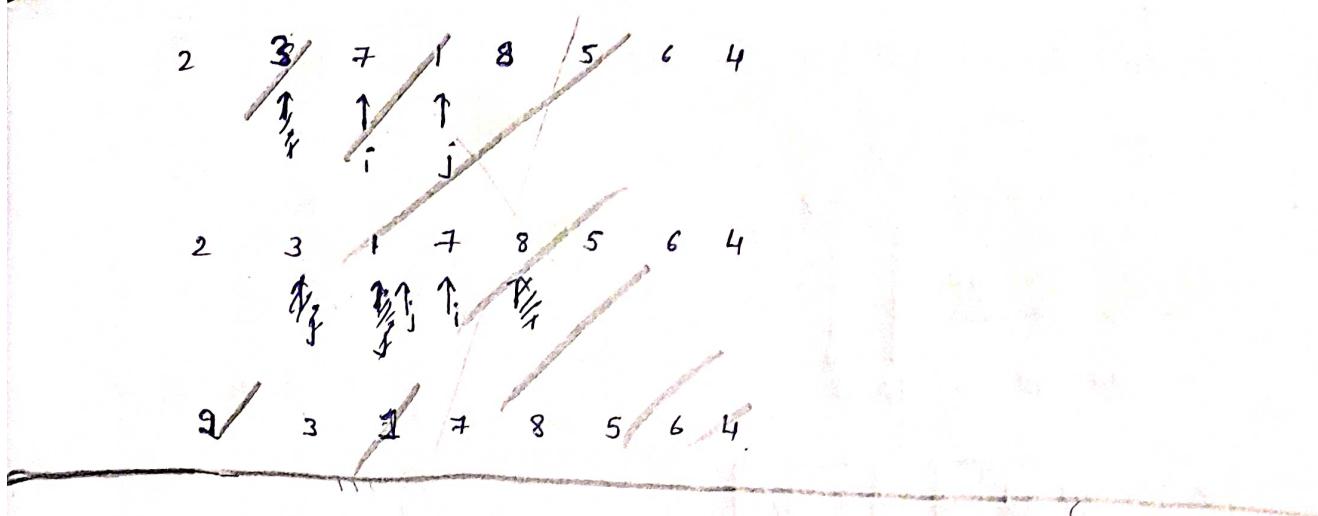
int partition(int arr[100], int low, int high)
{
    int pivot, j, temp, i, k;
    if (low < high)
    {
        pivot = arr[high];
        i = low;
        j = high;
        while (i < j)
        {
            while (arr[i] <= pivot) && (i < high)
            {
                i++;
            }
            while (arr[j] > pivot)
            {
                j--;
            }
            if (i < j)
            {
                temp = arr[i];
                arr[i] = arr[j];
                arr[j] = temp;
            }
        }
        arr[pivot] = arr[j];
        arr[j] = temp;
    }
    return j;
}

```

Eg

$\rightarrow$  25 33 14 2





→ 

35	33	42	10	14	19	27	34	26	31
0	1	2	3	4	5	6	7	8	9

35 33 42 10 14 19 27 44 26 31<sup>P</sup>

(31) 33 42 10 14 19 27 44 26 35

26 33 42 10 14 19 27 44 (31)<sup>P</sup> 35

26 (31)<sup>P</sup> 42 10 14 19 27 44 33 35

26 27 42 10 14 19 (31)<sup>P</sup> 44 33 35

26 27 (31)<sup>P</sup> 10 14 19 42 44 33 35.

26 27 (31) 19 10 14 (31)<sup>P</sup> 42 44 33 (35)<sup>P</sup>

(14)<sup>P</sup> 27 19 10 26

10 27 19 (14)<sup>P</sup> 26

10 (14)<sup>P</sup> 19 27 (26)<sup>P</sup>

10 14 19 26 27 31

(35)<sup>P</sup> 44 33 42

33 44 (35)<sup>P</sup> 42

33 (35)<sup>P</sup> 44 (42)<sup>P</sup>

33 35 42 44

Final Sorted Array obtained = 10 14 19 26 27 31 35 42 44

→ 

10	80	30	90	40	50	70
0	1	2	3	4	5	6

10 80 30 (90)<sup>P</sup> 40 50 70

10 80 30 70 40 50 (90)<sup>P</sup>

10 80 30 (70)<sup>P</sup> 40 50

10 80 30 40 (70)<sup>P</sup> 50

10 80 30 40 50 (70)<sup>P</sup>

10  $\textcircled{70}^P$  30 40 50 80

10 50  $\textcircled{30}^P$  40  $\textcircled{70}^P$  80



$\textcircled{10}^P$   $\textcircled{30}^P$   $\textcircled{50}^P$  40

↔ ↔

10 30 40 50 70 80



2	8	7	1	3	5	6	4
0	1	2	3	4	5	6	7

$\textcircled{2}^P$  8 7 1 3 5 6 4

1 8 7  $\textcircled{2}^P$  3 5 6 4

↔  $\textcircled{2}^P$   $\textcircled{7}^P$  8 3 5 6 4  
↔  $\textcircled{7}^P$  8 3 5 6 4

4 8 3 5 6  $\textcircled{7}^P$

4  $\textcircled{7}^P$  3 5 6 8

$\textcircled{4}^P$  6 3 5  $\textcircled{7}^P$  8

3 6  $\textcircled{4}^P$  5

3  $\textcircled{4}^P$   $\textcircled{6}^P$  5

Final sorted Array obtained : 1 2 3 4 5 6 7 8

$\rightarrow$	<table border="1"> <tr> <td>3</td><td>2</td><td>6</td><td>5</td><td>7</td><td>4</td> </tr> </table>	3	2	6	5	7	4	<table border="1"> <tr> <td>3</td><td>2</td><td>6</td><td>5</td><td>7</td><td>4</td> </tr> </table>	3	2	6	5	7	4
3	2	6	5	7	4									
3	2	6	5	7	4									
	i	j	p	i	j									
	$\uparrow_i$	$\uparrow_j$	$\uparrow_p$	$\uparrow_i$	$\uparrow_j$									
	3 2 6 5 7 4			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$	$\uparrow_p$		$\uparrow_i$ $\uparrow_j$	$\uparrow_p$									
	3 4 6 5 7 6			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_i$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										
	3 2 4 5 6 7			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_i$ $\uparrow_i$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										
	3 2 4 5 6			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_i$ $\uparrow_i$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										
	3 2 4 5 6			3 2 6 5 7 4										
	$\leftarrow$ $\rightarrow$	$\uparrow_j$		$\leftarrow$ $\rightarrow$										
	3 2 4 5 6			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_i$ $\uparrow_i$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										
	3 2 4 5 6			3 2 6 5 7 4										
	$\leftarrow$ $\rightarrow$			$\leftarrow$ $\rightarrow$										
	3 2 4 5			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_i$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										
	3 2 4			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										
	3 2			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										
	2 3 4 5 6 7			3 2 6 5 7 4										
	$\uparrow_i$ $\uparrow_j$ $\uparrow_p$			$\uparrow_i$ $\uparrow_j$ $\uparrow_i$										

Having first and last term

87. In 60 sec we have to do 100000

$$\rightarrow \begin{array}{|c|c|c|c|c|c|c|c|c|} \hline 54 & 26 & 93 & 17 & 77 & 31 & 44 & 55 & 20 \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ \hline \end{array} \text{pivot}$$

54 26 93 17 77 31 44 55 (20)<sup>P</sup>

(20)<sup>P</sup> 26 93 17 77 31 44 55 54.

17 26 93 (20)<sup>P</sup> 77 31 44 55 54.

17 (20)<sup>P</sup> (26) 93 26 77 31 44 55 (54)<sup>P</sup>.

(54)<sup>P</sup> 26 77 31 44 55 93.

(54)<sup>P</sup> 44 26 77 31 (54)<sup>P</sup> 55 93.

44 26 (54)<sup>P</sup> 31 77 55 93.

44 26 (31)<sup>P</sup> (54)<sup>P</sup> 77 55 (93)<sup>P</sup>

(31)<sup>P</sup> 26 44

77 (55)<sup>P</sup> (93)<sup>P</sup>

17 20.

26 31 44

54.

55 77 93

Final Sorted Array Obtained :

17 20 26 31 44 54 55 77 93.



## → Merge Sort

$O(n^2)$

Merge sort is a divide & conquer algorithm, it divides the input array into 2 halves, calls itself for the 2 halves and then merges the sorted halves.

Algorithm (divide → sort → merge)

Step 1: Start

Step 2: if the array is of length 0 or 1, then it is already sorted.

Step 3: Otherwise, divide the unsorted array into 2 sub arrays of about half the size

Step 4: Use merge sort algorithm recursively to sort each sub array.

Step 5: Merge two sub arrays to form a single sorted list.

Step 6: Stop

Eg: 

5	3	8	9	1	7	0	2	6	4
0	1	2	3	4	5	6	7	8	9

$$n = 10$$

$$l = 0$$

$$h = 9$$

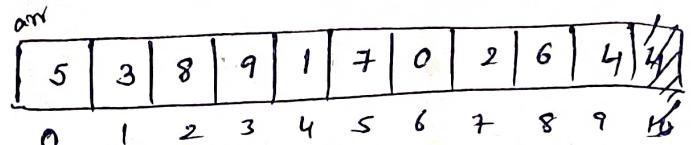
$$m = \frac{0+9}{2} = 4$$

5	3	8	9	1	7	0	2	6	4
0	1	2	3	4	5	6	7	8	9

5	3	8	9	1
0	1	2	3	4

7	0	2	6	4
5	6	7	8	9

Eq.



Print larger and smaller to continue

$$n=10$$

$$l=0$$

$$h=9$$

$$m = \frac{9+0}{2} = 4$$

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

$$m = \frac{0+4}{2} = 2 \quad m = \frac{5+9}{2} = 7$$

After

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

$$m = \frac{0+2}{2} = 1 \quad m = \frac{5+7}{2} = 6 \quad m = \frac{8+9}{2} = 8$$

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

$$m = \frac{0+1}{2} = 0 \quad m = \frac{2+4}{2} = 3 \quad m = \frac{5+6}{2} = 5 \quad m = \frac{8+9}{2} = 8$$

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

[5   3   8   9   1]	[7   0   2   6   4]
0 1 2 3 4	5 6 7 8 9

temp.

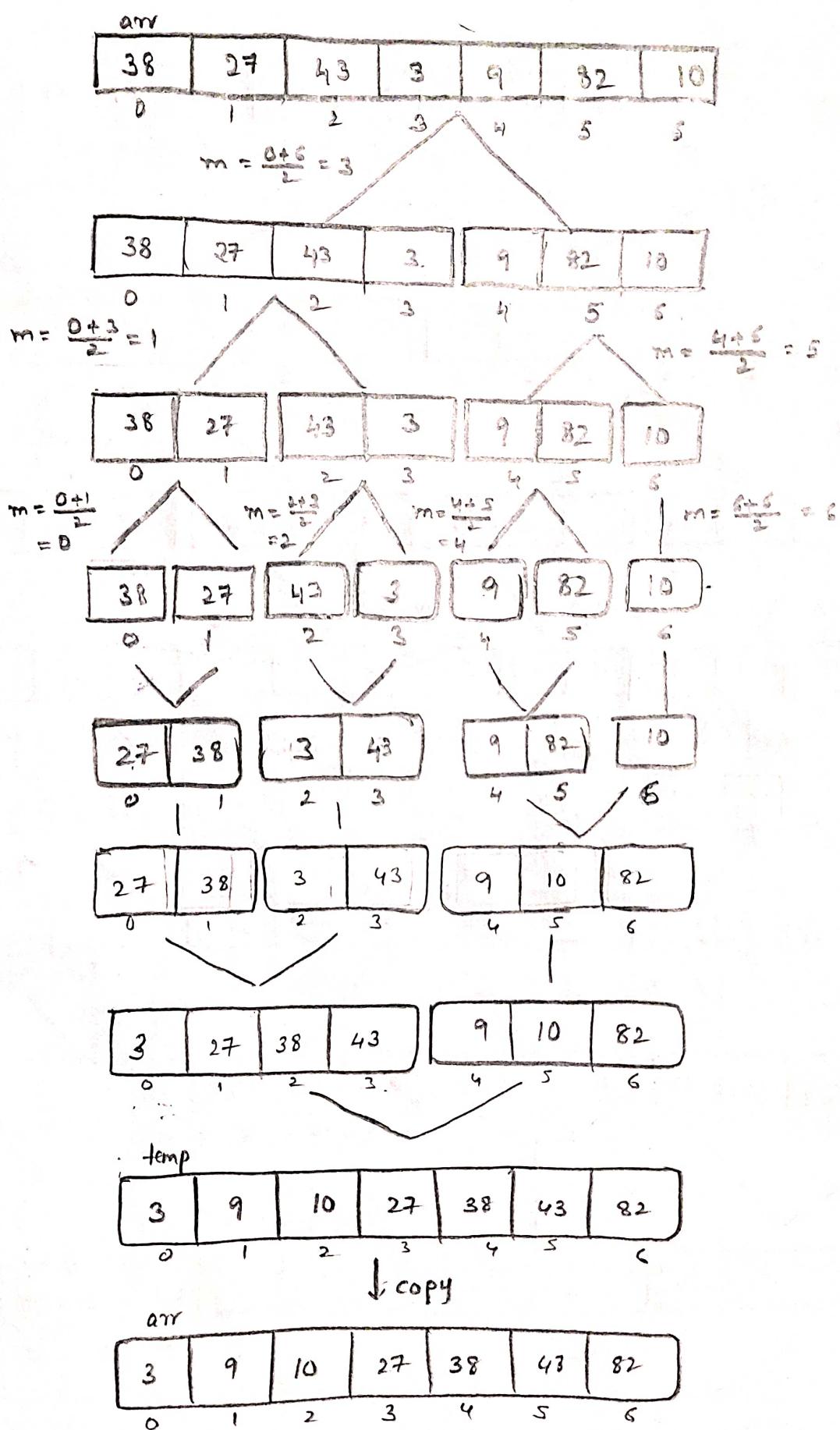
[1   3   5   8   9]	[0   1   0   6   7]
0 1 2 3 4	5 6 7 8 9

[1   3   5   8   9]	[0   1   0   6   7]
0 1 2 3 4	5 6 7 8 9

copy

[0   1   2   3   4   5   6   7   8   9]
0 1 2 3 4 5 6 7 8 9

Eg: 38 27 43 3 9 82 10



Eg: 55 11 22 99 55 11 22 99 55 33 77

33

55	11	22	99	55	11	22	99	55	23	77	88
0	1	2	3	4	5	6	7	8	9	10	11

$$n = 13$$

$$m = \frac{0+12}{2} = 6$$

$$h = 12$$

55	11	22	99	55	11	22	99	55	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11

$$m = \frac{0+6}{2} = 3$$

$$m = \frac{7+12}{2}$$

55	11	22	99	55	11	22	99	55	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11

$$m = \frac{0+3}{2} = 1$$

$$m = \frac{4+6}{2} = 5$$

$$m = \frac{7+9}{2} = 8$$

$$m = \frac{10+12}{2} = 11$$

55	11	22	99	55	11	22	99	55	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11

55	11	22	99	55	11	22	99	55	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11

55	11	22	99	55	11	22	99	55	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11

55	11	22	99	55	11	22	99	55	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11

11	55	22	99	11	22	55	33	55	99	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11	12

11	22	55	99	11	22	55	33	55	99	33	77	88
0	1	2	3	4	5	6	7	8	9	10	11	12

11	11	22	22	55	55	99	33	33	55	77	88	99
0	1	2	3	4	5	6	7	8	9	10	11	12

11	11	22	22	33	33	55	55	55	77	88	99	99
0	1	2	3	4	5	6	7	8	9	10	11	12

## Implementation

```
#include <stdio.h>
void mergeSort(int, int);
void mergeArray(int, int, int, int);
int main()
{
    _____
    mergeSort(0, n-1)
    ret
    _____
}
```

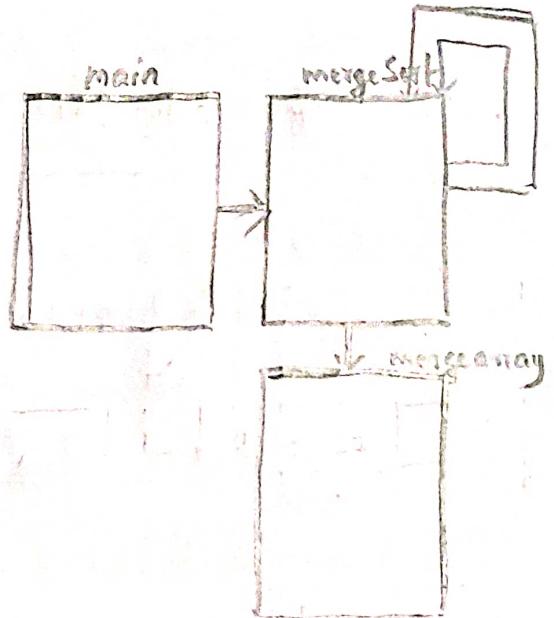
```
void mergeSort(int l, h)
```

```
{  
    int m = (l+h)/2;  
    mergeSort(l, m);  
    mergeSort(m+1, h);  
    mergeArray(l, m, m+1, h);  
}
```

void mergeArray (int a, int b, int c, int d)

```
{  
    int temp[100];  
    int i, j, k=0;  
    i=a;  
    j=c;  
    while (i<=b & j<=d)  
    {  
        if (a[i]<a[j])  
            temp[k++] = a[i++];  
        else  
            temp[k++] = a[j++];  
    }  
    for (i=k; i<=d; i++)  
        temp[i] = a[i];  
}
```

```
for (i=k; i<=b; i++)  
    temp[i] = a[i];  
}
```



```

while(j < d)
{
    temp[j++] = a[j++];
}

for(k = 0; k <= d; k++)
{
    a[k] = temp[k];
}

```

### → Drawbacks of Merge Sort

- Slower comparative to other sorting algorithm for smaller tasks
- It requires an additional memory space of  $\Theta(n)$  for the temporary array.
- It goes through the whole process even if input array is sorted.

### → Bucket Sort

Bucket Sort or Bin sort is a sorting algorithm that works by distributing the elements of an array into a no of buckets.

Each bucket is then sorted individually either using a different sorting algorithm or by recursively applying bucket sort algorithm.

Bucket sort is applied with elements that are uniformly distributed over a range and with the floating point values.

### Algorithm.

Step 1: Start

Step 2: Create  $n$  number of buckets or lists.

Step 3: Do the following for every element,  $\text{arr}[i]$ .

Step 3.1: Insert the element  $\text{arr}[i]$  in bucket  $\lfloor n * \text{arr}[i] \rfloor$

Step 4: Apply either insertion sort or bucket sort recursively on every individual bucket

Step 5: Concatenate all the bucket elements to form a sorted list

Step 6: Stop

→   
0 1 2 3 4 5 6 7 8 9

All elements are in range 1-23.

We can take any number of buckets; here we are taking

5 buckets each having range - 5.

(Scattering elements into buckets)



1-5



6-10



11-15



16-20



21-25

(Sorting in each bucket)



1-5



6-10



11-15



16-20



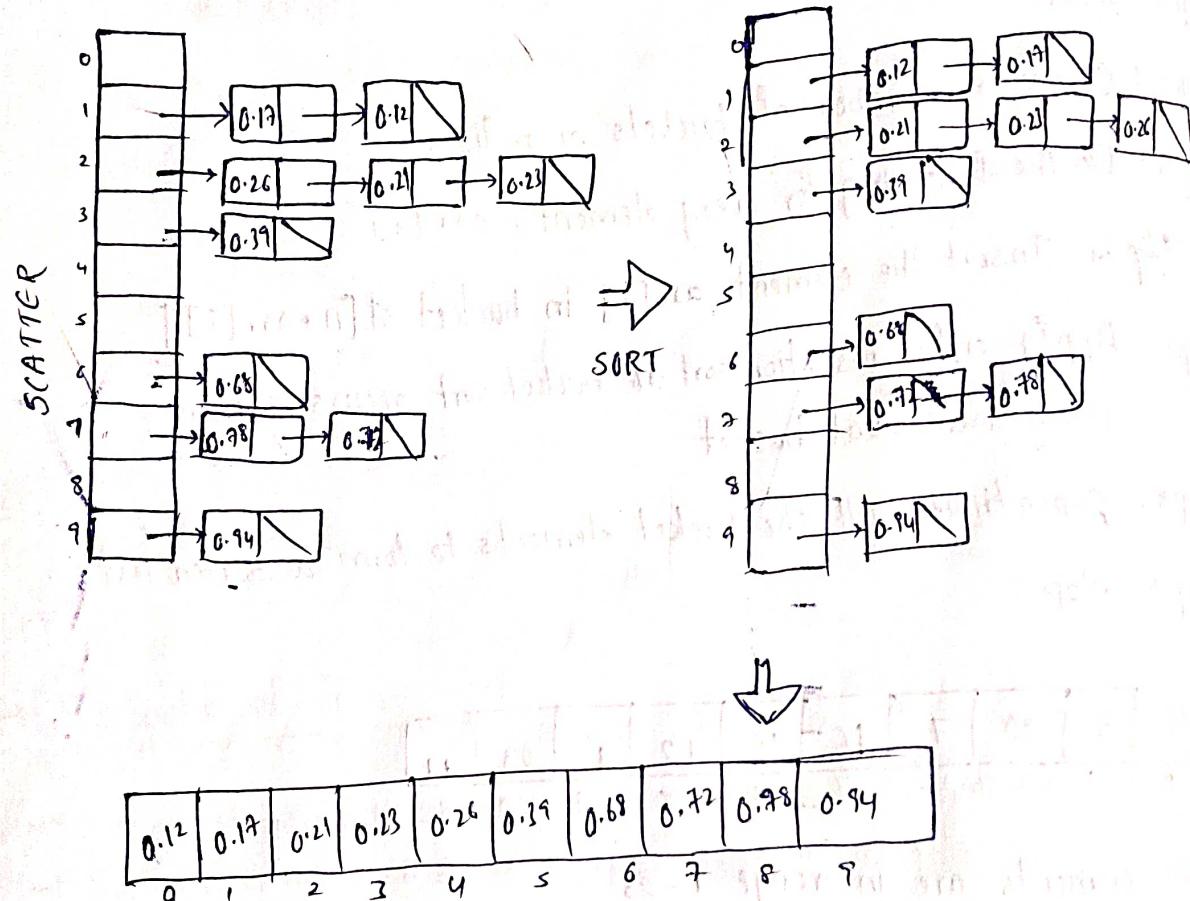
21-25

(Concatenation)

  
0 1 2 3 4 5 6 7 8 9

→ 10.78, 0.17, 0.39, 0.26, 0.72, 0.94, 0.21, 0.12, 0.23, 0.68

10	1	9							
0.78	0.17	0.39	0.26	0.72	0.94	0.21	0.12	0.23	0.68



### Advantages

- Reduce no of comparisons.
- It is asymptotically fast, as the elements are uniformly sorted.

### Disadvantages

- may or maynot be stable
- not useful when large array is taken as input.
- We require extra space to sort each bucket

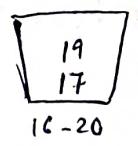
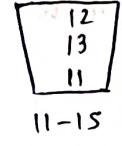
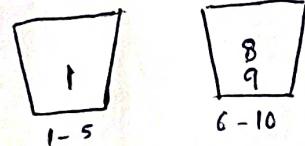
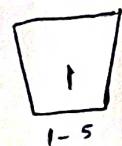
Best & Avg Time Complexity =  $O(n+k)$

Worst case Time complexity =  $O(n^2)$

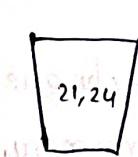
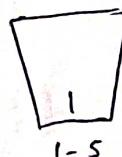
Space Complexity  $O(n*k)$

→ 11 9 21 8 17 19 13 7 24 12

↓ Scatter



↓ Sort

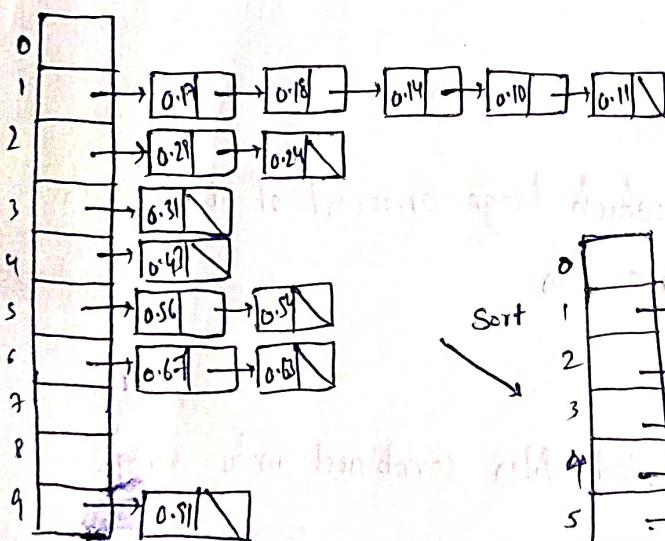


↓ Concatenation.

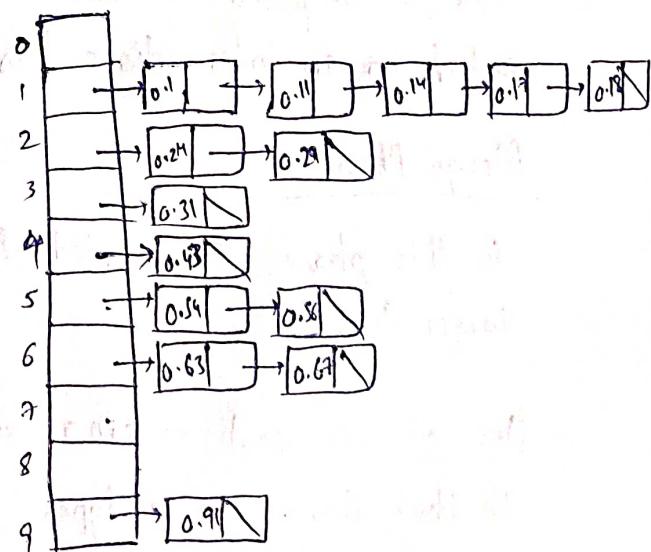
1	8	9	11	12	13	17	19	21	24
0	1	2	3	4	5	6	7	8	9

→ 0.17 0.31 0.29 0.56 0.24 0.18 0.14 0.91 0.10 0.67 0.54 0.63.  
↔ 0.11 0.43

(scatter)



Sort



↓ Concatenation.

0.10	0.11	0.14	0.17	0.18	0.24	0.29	0.31	0.43	0.54	0.56	0.63	0.67	0.91
------	------	------	------	------	------	------	------	------	------	------	------	------	------

## External Sorting

- In external sorting, we have 2 phases:
  1. Sorting phase
  2. Merging phase

It is used

- It is a technique in which data is stored in the secondary memory, in which part by part data is loaded into the main memory and then sorting can be done over there

Then, this sorted data will be stored in the intermediate files, finally these files will be merged to get sorted a sorted data.

Thus, by using external sorting technique, a huge amount of data can be sorted easily.

In case of external sorting, all the data cannot be accommodated on single memory. In this case, some amount of memory needs to be kept on memory such as hard disk, compact disk & memory chips.

### Sorting Phase

This is the phase in which large amount of data is sorted in an intermediate files

### Merge Phase

In this phase, the sorted files combined into single larger file.

One of the best external sorting is external merge sort.

In that, there are 2 types

2-way merge sort (taking 2 at a time)

k-way merge sort (taking k at a time).

a	69
e	7
d	11
a	25
b	16
f	17
a	31
b	45
g	69
c	75

Sorting

a	69
e	7
d	11
a	25
b	16
f	17
a	31
b	45
g	69
c	75

a	69
e	7
d	11
a	25
b	16
f	17
a	31
b	45
c	75
g	69

a	69
e	7
a	25
d	11
b	16
f	17
a	31
b	45
c	75
g	69

a	25
a	69
d	11
e	7
a	31
b	16
b	45
f	17
c	75
g	69

a	25
a	31
a	69
b	16
b	45
d	11
e	7
f	17
c	75
g	69

a	25
a	31
a	69
b	16
b	45
c	75
d	11
e	7
f	17
g	69

Merge part 1

Merge Part 2

Merge Part 3

## → Algorithm Analysis

1. Mathematical Background.
2. Model - Computer
3. How to analyse.
4. Running time calculation.
5.
  1. Time Complexity (by means of Asymptotic notations)
  2. Space Complexity

## → Asymptotic Notations

1. Big-Oh -  $O$  (upper bound or worst case)
2. Big-Theta -  $\Theta$  (Avg case or Avg bound)
3. Big-Omega -  $\Omega$  (lower bound or best case)

## \* Algorithm: Sum of n numbers

Step 1 : Start

Step 2 : Read  $n$

Step 3 :  $Sum = 0, i = 1$

Step 4 :  $Sum = Sum + i$

Step 5 :  $i = i + 1$

Step 6 : check if  $i <= n$ , goto step 4

Step 7 : display sum

Step 8 : Stop

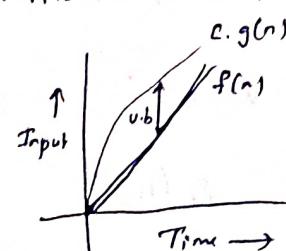
$$f(n) = 3n + 4$$

1. If  $f(n) = O(g(n))$  where  $c, n$  are constants iff  $f(n) \leq c g(n)$

$$f(n) \leq c \cdot g(n)$$

$$3n + 4 \leq 3n + 4n$$

$$3n + 4 \leq 7n$$



$$\text{for } n=1 \quad f_0 \leq f_1$$

$$n=2 \quad 10 \leq 14$$

$$\therefore g(n) = \lceil n \rceil$$

$$\therefore \text{or is } g(n) = n$$

$\therefore \text{Time complexity} = O(n)$

Q.

$f(n) = \Theta(g(n))$  where  $c_1, c_2$  are constants iff

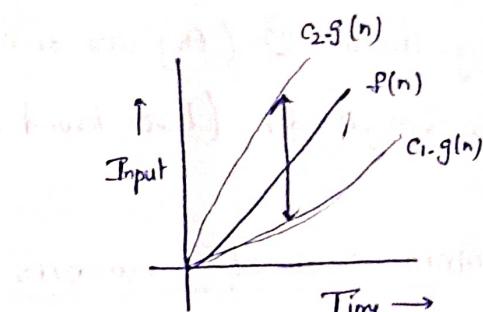
$$c_1 \cdot g(n) \leq f(n) \leq c_2 \cdot g(n)$$

$$2n+3 \leq 3n+4 \leq 3n+4n$$

Checking

$$i=1 \rightarrow 5 \leq 7 \leq 7$$

$$i=2 \rightarrow 7 \leq 10 \leq 14$$



$$g(n) = n, \text{ Average} = \frac{n}{2}$$

$$\Rightarrow \Theta(n/2) \rightarrow \Theta(n)$$

3.  $f(n) = \Omega(g(n))$  where  $c, n_0$  are constants iff  $f(n) \geq g(n), \forall n \geq n_0$

$$c \cdot g(n) \leq f(n)$$

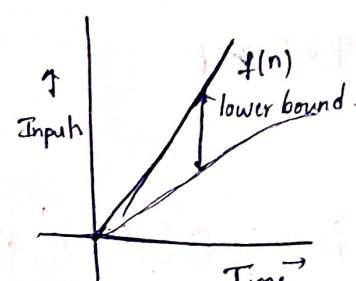
$$3n^2n+3 \leq 3n+4$$

$$n=1 \Rightarrow 5 \leq 7$$

$$n=2 \Rightarrow 7 \leq 10$$

$$\therefore g(n) = \lceil n \rceil$$

$$\Rightarrow \Omega(n)$$



$\rightarrow O(1) - \text{constant rate}$

## Time Complexity

### Insertion Sort

$$\begin{aligned}
 & \text{for } (i=1; i < n; i++) \{ && 1 + n + (n-1) \\
 & \quad \text{for } (j=i; j > 0; j--) \{ && n-1 + 2 + 3 + \dots + (n-1) + (1+2+3+\dots+n-1) \\
 & \quad \quad \text{if } (a[j] < a[j-1]) \{ && 2(2+3+\dots+n-1) \\
 & \quad \quad \quad t = a[j]; && 2(2+3+\dots+n-1) \\
 & \quad \quad \quad a[j] = a[j-1]; && 2(2+3+\dots+n-1) \\
 & \quad \quad \quad a[j-1] = t; && 2(2+3+\dots+n-1) \\
 & \quad \quad \} && 2(2+3+\dots+n-1) \\
 & \quad \} && 1 + 3n + 10(2+3+\dots+n-1) - i \\
 & \} && 3n + 10 \times \frac{n(n-1)}{2} \\
 & && = 5n^2 - 2n - 10 \\
 & && = O(n^2)
 \end{aligned}$$

For Insertion sort,

Worst Case :  $O(n^2)$

Avg Case :  $\Theta(n^2)$

Best Case :  $O(n)$

Space Complexity :  $O(1)$

## Merge Sort

$$T(n) = T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + n \xrightarrow{\text{eq ①}} (\text{Divide \& conquer algorithm})$$

Substitute  $T\left(\frac{n}{2}\right)$  in eq ①

$$T\left(\frac{n}{2}\right) = T\left(\frac{n}{4}\right) + T\left(\frac{n}{4}\right) + \frac{n}{2} \xrightarrow{\text{②}} \text{divide and conquer method}$$

Substitute eq ② in ①

$$T(n) = 2 \left( 2T\left(\frac{n}{4}\right) + \frac{n}{2} \right) + n$$

$$= 2^2 T\left(\frac{n}{2^2}\right) + 2n \xrightarrow{\text{③}}$$

Sub  $T(n/4)$  in eq ①

$$T(n/4) = T(n/8) + T(n/8) + n/4.$$

$$T\left(\frac{n}{4}\right) = 2T\left(\frac{n}{8}\right) + \frac{n}{4} \rightarrow ④$$

Substitute in eq ④.

$$\begin{aligned} T(n) &= 2^2 \left[ 2T\left(\frac{n}{2^2}\right) + \frac{n}{4} \right] + 2n \\ &= 2^3 T\left(\frac{n}{2^3}\right) + 3n. \end{aligned}$$

For  $i$ th form

$$T(n) = 2^i T\left(\frac{n}{2^i}\right) + i \cdot n$$

$$= n \cdot T(1) + \log_2^n + n$$

$$= n \log_2^n + n \cdot T(1)$$

$$= O(n \log_2^n)$$

$$\begin{aligned} \frac{N}{2^i} &= 1 \\ N &= 2^i, \\ \log_2^N &= i \log_2^2 \\ i &= \log_2^N \end{aligned}$$

Space Complexity =  $O(n)$

Best Case Time Complexity:  $O(n \log n)$

Avg Case Time Complexity:  $O(n \log n)$

Worst Case Time Complexity:  $O(n \log n)$

Merge Sort is stable

## Quick Sort

Time complexity for entire recursive quick tree is equal to no of levels into time taken for 1 lvl.

$$\text{No of levels} \leq \log_2^M = T(n/2) + T(n/2)$$

Best Case:  $O(n \log n)$       Worst Case:  $O(n^2)$

Avg Case:  $O(n \log n)$

$$\begin{aligned}
 \text{No. of levels} &= T(n/2) + T(n/2) \\
 &= T\left(\frac{n}{4}\right) + T\left(\frac{n}{4}\right) + T\left(\frac{n}{4}\right) + T\left(\frac{n}{4}\right) \\
 &\vdots \\
 &= \Sigma^j T\left(\frac{n}{2^j}\right)
 \end{aligned}$$

Total no. of levels =  $\log_2 n$

Space complexity:  $O(\log n)$

### Best/Worst Case Time Complexity

When array elements are in descending order and is to be sorted in ascending order, it takes  $O(n^2)$  as time complexity.

Quick sort is not stable.

Q/A.

For brief

→ For shell sort,

Best Case Time complexity:  $O(n)$

Avg Case:  $O(n^2)$

Worst:  $O(n^2)$  Space Complexity:  $O(1)$ .

→ Bucket sort

Best:  $O(n+k)$

Avg:  $O(n+k)$

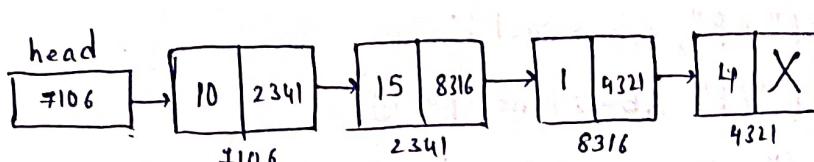
Worst:  $O(n^2)$

Space Complexity:  $O(n)$

# Dynamic memory implementation of Linear Data Structures

1. Single Linked list.: Creation, Insertion, Deletion, Display
2. Double Linked list: Creation, Insertion, Deletion, Display
3. circular Linked list: Creation, Insertion, Deletion, Display.
4. Stack Using Single linked list
5. Queue using Single linked list
6. Infix to Postfix Conversion
7. Postfix evalution
8. Balancing Symbols.
9. Types of Queues
  1. Circular Queue
  2. DQueue
10. Single Linked list:

It is a linear data structure. It is collection of nodes. The node contains two parts.: data & link to the next node.



## Operations:

Create()	Search()
InsertAtBegin()	length()
InsertAtMiddle()	count()
InsertAppend()	Sort()
Deletion()	max()
Display()	min()

→ Define a structure Bike with members model, make, cost, tank capacity & mileage. Read & display bike details using DMA

```
#include <stdio.h>
#include <stdlib.h>
struct Bike {
    char model[30];
    char make[20];
    float cost;
    float tankcapacity;
    float mileage;
};

int main() {
    struct Bike *b;
    printf("Enter bike details: ");
    gets(b->model);
    gets(b->make);
    b = malloc(sizeof(struct Bike));
    printf("Enter bike details: ");
    gets(b->model);
    gets(b->make);
    scanf("./f", &b->cost);
    scanf("./f", &b->tankcapacity);
    scanf("./f", &b->mileage);
    printf("Bike details:\n");
    printf("%s\n", b->model);
    printf("%s\n%f\n%f\n%f\n", b->model, *b->make,
        b->cost, b->tankcapacity, b->mileage);
    return 0;
}
```

## Implementation:

```
#include <stdio.h>
#include <stdlib.h>

struct Node {
    int data;
    struct node *next;
};

struct node *head, *current, *p, *q;
struct node*create()
{
    current = (struct node*)malloc(sizeof(struct node));
    printf("Enter data: ");
    scanf("%d", &current->data);
    current->next = NULL;
    return current;
}

void append()
{
    current = create();
    if(head == NULL)
        head = current;
    else {
        p = head;
        while(p->next != NULL)
            p = p->next;
        p->next = current;
    }
}

void insertAtBegin()
{
    current = create();
    if(head == NULL)
        head = current;
    else {
        current->next = head;
        head = current;
    }
}
```

## Self referential structure

The member of structure pointing to another structure of same type

```

int length()
{
    int l=0;
    p = head;
    while(p!=NULL){
        p = p->next;
        l++;
    }
    return l;
}

```

```
void insertAtMiddle()
```

```
{
    int k, i=2;
    current = create();
    printf("enter position:");
    scanf("./d", &k);
    if(k < (length(1)))
}
```

```

    p = head;
    while(i < k)
    {
        p = p->next
        i++;
    }

```

```

    current->next = p->next;
    p->next = current;
}
```

```
else
```

```
    printf("Insertion not possible");
```

```
}
```

```
void deletion()
```

```
{
```

```

    int k, i=2;
    coutprintf("enter position:");
    scanf("./d", &k);
    if(k > (length(1)))

```

```
        printf("Deletion not possible");
```

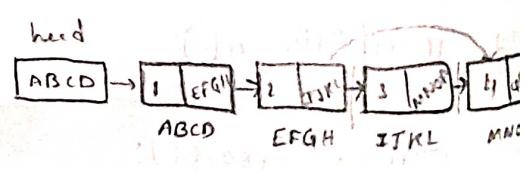
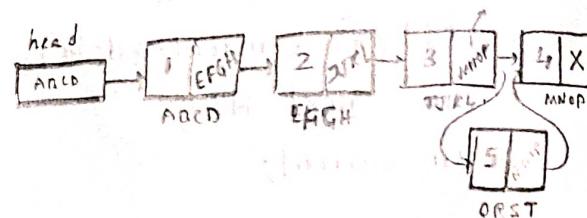
```
    else if(k==1){
```

```
        p = head;
```

```
        head = p->next;
```

```
        p->next = NULL;
```

```
        free(p);
```



```

else {
    p = head;
    while(i < k) {
        p = p->next;
        i++;
    }
    q = p->next;
    p->next = q->next;
    q->next = NULL;
    free(q);
}

```

3.

#### 4. Stack Using Linked list

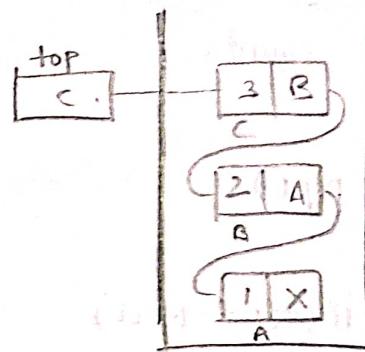
- Always insertion at begin take place & deletion at begin take place as operations on stack takes place at one end.
- As we are using linked list for stack implementation, stack overflow is not possible.
- If top == NULL, then stack is empty.

#### Implementation

```

#include <stdlib.h>
#include <stdlib.h>
struct node {
    int data;
    struct node* next;
};
struct node *current, *top=NULL, *p, *q;
int count;
struct node *create()
{

```



```
struct node * create()
{
    current = (struct node *) malloc (sizeof (struct node));
    printf("enter data: ");
    scanf("%d", &current->data);
    current->next = NULL;
    return current;
}
```

```
void push() (insert At Begin)
{
```

```
    current = create();
    if (top == NULL)
        top = current;
    else {
        current->next = top;
        top = current;
    }
    count++;
}
```

```
void pop() (delete At Begin)
{
```

```
    if (top == NULL)
        printf("stack is empty");
    else {
        p = top;
        top = p->next;
        p->next = NULL;
        free(p);
        count--;
    }
}
```

```
void peak()
```

```
{ if (top == NULL)
    printf("stack is empty");
else
    printf("%d", top->data);
}
```

```

void display()
{
    if (top == NULL)
        printf("stack is empty");
    else {
        p = top;
        while (p != NULL) {
            printf("\t%d", p->data);
            p = p->next;
        }
    }
}

int main()
{
    int ch;
    printf("1. push\n2. pop\n3. peak\n4. display\n5. exit\n"
           "count\n6. exit\n");
    while (1) {
        printf("enter choice : ");
        scanf("%d", &ch);
        switch (ch) {
            case 1: push();
                      break;
            case 2: pop();
                      break;
            case 3: peak();
                      break;
            case 4: display();
                      break;
            case 5: printf(" no of elements : %d", count);
                      break;
            case 6: exit(0);
            default: printf(" invalid !! ");
        }
    }
    return 0;
}

```

## 5. Linked list implementation of Queue

→ Queue is a linear data structure which follows first in first out principle (FIFO).

### Implementation

```
#include <stdio.h>
struct node {
    int data;
    struct node* next;
};

struct node *current, *p, *f=NULL, *r=NULL;
int count=0;

struct node* create()
{
    current = (struct node*)malloc(sizeof(struct node));
    printf(" enter data:");
    scanf("%d", &current->data);
    current->next = NULL;
    return current;
}

void enqueue() (insertAtEnd)
{
    current = create();
    if(f==NULL && r==NULL) {
        rear = current;
        front = rear;
    }
    else {
        current->next = rear;
        rear->next = current;
        rear = current;
    }
    count++;
    printf(" enqueued successfully!");
}
```

```
void dequeue() {DeleteAtBegin}
{
    if (f == NULL)
        printf("Queue is empty!");
    else if (front->next != NULL) {
        p = front;
        front = p->next;
        p->next = NULL;
        free(p);
    }
    count--;
    printf("dequeued successfully!");
}
```

```
void display()
{
    if (f == NULL)
        printf("Queue is empty!");
    else {
        p = front;
        while (p != NULL) {
            printf("i.d", p->data);
            p = p->next;
        }
    }
}
```

```
void frontele()
{
    if (f == NULL)
        printf("Queue is empty!");
    else
        printf("front element: i.d", front->data);
}
```

```
void rear_ele()
```

```
{
```

```
    if (r == NULL)
```

```
        printf("Queue is empty!");
```

```
    else
```

```
        printf("rear element: %d", rear->data);
```

```
}
```

```
int main()
```

```
{
```

```
    int ch;
```

```
    printf("1. enqueue\n2. dequeue\n3. display\n4. front_ele\n5. rear_ele\n6. count\n7. exit\n");
```

```
    while(1) {
```

```
        printf("\nEnter choice: ");
```

```
        scanf("%d", &ch);
```

```
        switch(ch) {
```

```
            if(ch != 1),
```

```
                case 1: enqueue();
```

```
                break;
```

```
                case 2: dequeue();
```

```
                break;
```

```
                case 3: display();
```

```
                break;
```

```
                case 4: front_ele();
```

```
                break;
```

```
                case 5: rear_ele();
```

```
                break;
```

```
                case 6: printf("no. of elements in queue: %d", count);
```

```
                break;
```

```
                case 7: exit(0);
```

```
                default: printf("invalid!");
```

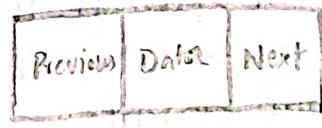
```
    }
```

```
}
```

```
return 0;
```

## Doubley Linked List

- It's a linear data structure in which it is collection of nodes.
- Each node has 3 fields
  - 1. Data part
  - 2. Link to previous node
  - 3. Link to next node.



### Operations

1. Create(), insert()

2. Insert

insertAtBegin()

insertAtMiddle()

insertAtEnd()

3. Delete

deleteAtBegin()

deleteAtMiddle()

deleteAtEnd()

4. Display

5. Search

6. Sort

7. Reverse

8. Update

### Implementation

```
#include<stdio.h>
struct node {
    int data;
    struct node* previous;
    struct node* next;
} *head=NULL, *current, *p, *q;
int count=0;
```

```

struct node * create()
{
    current = (struct node*) malloc(sizeof(struct node));
    printf("enter data:");
    scanf("%d", &current->data);
    current->previous = NULL;
    current->next = NULL;
    return current;
}

```

```

void insertAtEnd()
{

```

```

    current = create();
    if(head == NULL){
        head = current;
    }
    else{
        p = head;
        while(p->next != NULL)
            p = p->next;
        p->next = current;
        current->previous = p;
    }
    count++;
}

```

```

void insertAtBegin()
{

```

```

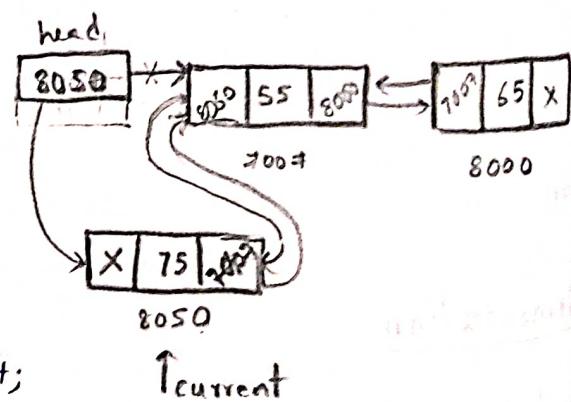
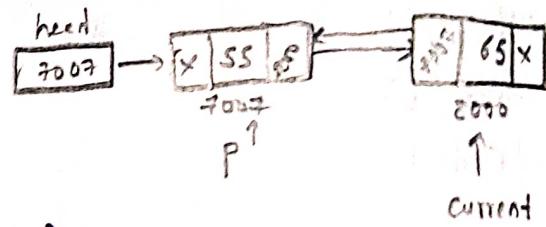
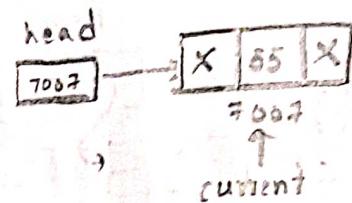
    current = create();
    if(head == NULL)
        head = current;
    else {
        current->next = head;
        head->previous = current;
        head = current;
    }
}

```

```

count++;
}

```



void insertAll

int to go that void display()

{

if(head == NULL)

printf("Doubly Linked list is empty!");

else {

p = head;

while(p != NULL) {

printf("./d ", p->data);

p = p->next;

}

}

}

void insertAtMiddle()

{

int k, i = 1;

printf("enter position: ");

scanf("./d", &k);

if(k > count)

printf("insertion not possible!");

else {

current = create();

p = head;

while(i < k)

p = p->next;

current->next = p->next;

(p->next)->previous = current;

current->previous = p;

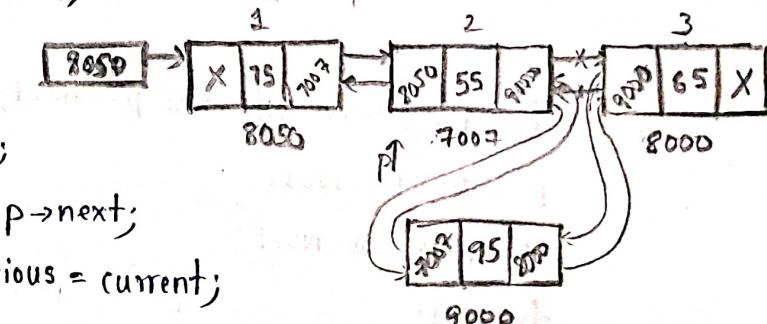
~~current~~

p->next = current;

count++;

}

}



Chaitin's algorithm

```

    int k;
    printf("enter position:");
    scanf("%d", &k);
    if (k > count)
        printf("deletion not possible!");

```

```
else if (k == 1) {
```

```
    p = head;
```

```
    head = p->next;
```

```
(p->next)->previous = NULL;
```

```
p->next = NULL;
```

```
free(p);
```

```
}
```

```
else {
```

```
    p = head;
```

```
    int i = 2;
```

```
    while (i <= k) {
```

```
        p = p->next;
```

```
        i++;
```

```
(p->next)->next =  
(p->next)->previous = p->previous;
```

```
(p->previous)->next = p->next;
```

```
p->next = NULL;
```

```
p->previous = NULL;
```

```
free(p);
```

```
count--;
```

```
}
```

```
void deleteAtBegin()
```

```
{
```

```
int k;
```

```
if (head == NULL)
```

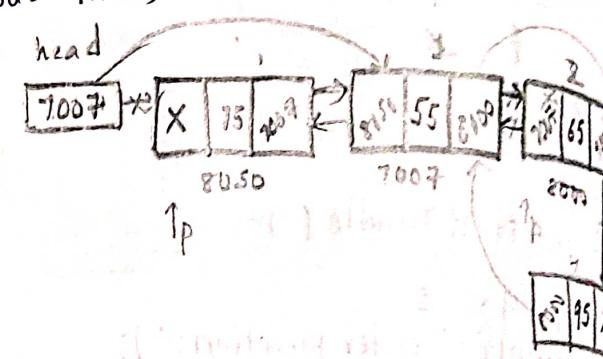
```
    printf("deletion not possible");
```

```
else if (head->next == NULL) {
```

```
    free(head);
```

```
    head = NULL;
```

```
    count--;
```



```
else {
```

```
    p = head;
```

```
    head = p->next;
```

```
    p->next->previous = NULL;
```

```
    p->next = NULL;
```

```
    free(p);
```

```
    count--;
```

```
}
```

```
{ void deleteAtMiddle()
```

```
{
```

```
    if(head == NULL)
```

```
        printf("List is empty!");
```

```
    else if(head->next == NULL){
```

```
        free(head);
```

```
        head = NULL;
```

```
        count--;
```

```
}
```

```
if
```

```
else {
```

```
    printf("enter position:");
```

```
    scanf("%d", &loc);
```

```
else { p = head;
```

```
    int i=2;
```

```
    while(i <= loc) {
```

```
        p = p->next;
```

```
        i++;
```

```
}
```

```
(p->next)->previous = p->previous;
```

```
(p->previous)->next = p->next;
```

```
p->next = NULL;
```

```
p->previous = NULL;
```

```
free(p);
```

```
count--;
```

```
}
```

```
}
```

```

Void deleteAtEnd()
{
    if (head == NULL)
        printf ("List is empty");
    else if (head->next == NULL) {
        free (head);
        head = NULL;
        count--;
    }
    else {
        p = head;
        while (p->next != NULL)
            p = p->next;
        (p->previous)->next = NULL;
        p->previous = NULL;
        free (p);
        count--;
    }
}

void search()
{
    if (head == NULL)
        printf ("List is empty!");
    else {
        printf ("enter element to search:");
        scanf ("%d", &k);
        p = head;
        while (p != NULL)
        {
            if (p->data == key) {
                break;
                printf ("element found at %d node", i);
            }
            i++;
            p = p->next;
        }
    }
}

```

```
    if (c == count+1)  
        printf("element not found ");
```

3. Write a C program to find the maximum element in an array.

4. Write a C program to find the minimum element in an array.

5. Write a C program to find the sum of all elements in an array.

6. Write a C program to find the average of all elements in an array.

7. Write a C program to find the product of all elements in an array.

8. Write a C program to find the difference between the largest and smallest elements in an array.

9. Write a C program to find the sum of even elements in an array.

10. Write a C program to find the sum of odd elements in an array.

11. Write a C program to find the sum of positive elements in an array.

12. Write a C program to find the sum of negative elements in an array.

13. Write a C program to find the sum of all elements in an array.

14. Write a C program to find the product of all elements in an array.

15. Write a C program to find the average of all elements in an array.

16. Write a C program to find the difference between the largest and smallest elements in an array.

17. Write a C program to find the sum of even elements in an array.

18. Write a C program to find the sum of odd elements in an array.

19. Write a C program to find the sum of positive elements in an array.

20. Write a C program to find the sum of negative elements in an array.

21. Write a C program to find the sum of all elements in an array.

22. Write a C program to find the product of all elements in an array.

23. Write a C program to find the average of all elements in an array.

24. Write a C program to find the difference between the largest and smallest elements in an array.

25. Write a C program to find the sum of even elements in an array.

26. Write a C program to find the sum of odd elements in an array.

27. Write a C program to find the sum of positive elements in an array.

28. Write a C program to find the sum of negative elements in an array.

29. Write a C program to find the sum of all elements in an array.

30. Write a C program to find the product of all elements in an array.

31. Write a C program to find the average of all elements in an array.

32. Write a C program to find the difference between the largest and smallest elements in an array.

33. Write a C program to find the sum of even elements in an array.

34. Write a C program to find the sum of odd elements in an array.

## → Circular Linked List

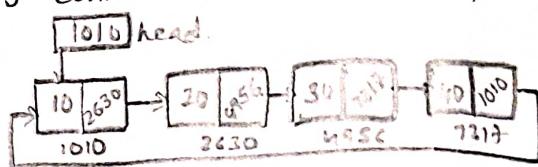
→ Circular Linked list is a linear data structure in which the last node is connected to first node.

It is of two types

- Circular Singly Linked list
- Circular Doubly Linked list

## → Circular Singly Linked list

- In which last node's next is connected to first node.



## → Differences with SLL

- Any node can be the first node
- Last node is connected to first node.

## → Operations

create()

insert()

delete()

display()

search()

sort()

length()

update()

# Implementation of Circular Single Linked List

```
#include <stdio.h>
struct node {
    int data;
    struct node* next;
};
```

int count = 0;

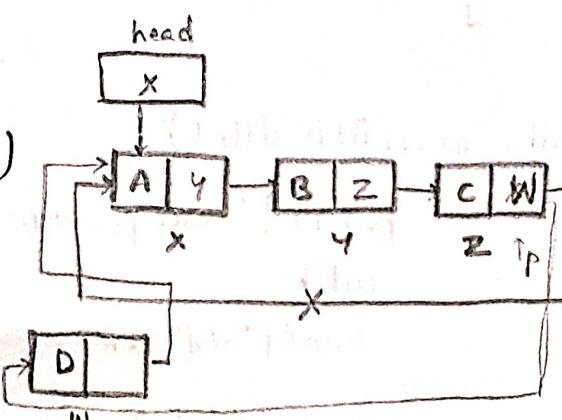
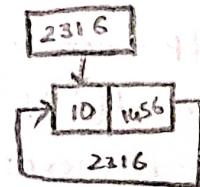
```
struct node* create() {
    current = (struct node*) malloc(sizeof(struct node));
    printf("Enter data: ");
    scanf("%d", &current->data);
    current->next = NULL;
    return current;
}
```

```
void insertAtBegin() {
```

```
    current = create();
    if(head == current) {
        head = current;
        current->next = head;
    }
}
```

```
else {
    p = head;
    while(p->next != head)
        p = p->next;
    p->next = current;
    current->next = head;
    head = current;
}
```

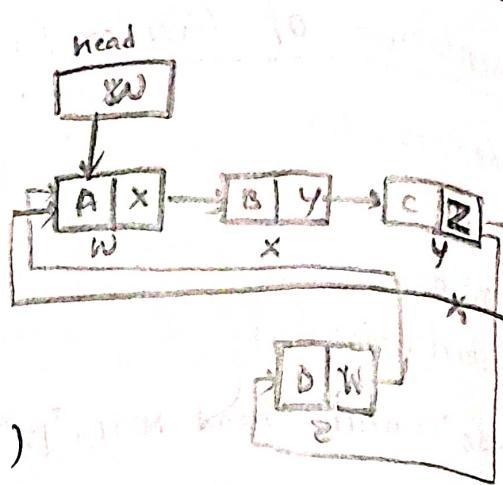
```
count++;
```



```

Void insertAtHead() {
    current = create();
    if (head == NULL)
        head = current;
    else {
        p = head;
        while (p->next != head)
            p = p->next;
        p->next = current;
        current->next = head;
    }
    count++;
}

```



```
void display() {
```

```
    p = head;
```

```
    if (head == NULL)
```

```
        printf("List is empty!");
```

```
    else {
```

```
        while (p->next != head) {
```

```
            printf("\t%d", p->data);
```

```
            p = p->next;
```

```
}
```

```
        printf("\t%d", p->data);
```

```
}
```

```
void insertAtMiddle() {
```

```
    printf("enter position: ");
```

```
    int k;
```

```
    scanf("%d", &k);
```

```
    if (k > count)
```

```
        printf("insertion not possible!");
```

```
    else {
```

```
        p = head;
```

```
        for (int i=1;
```

```
            while (i < k-2) {
```

```
                p = p->next;
```

```
                i++;
```

```
}
```

Current  $\rightarrow$  next = p  $\rightarrow$  next;

p  $\rightarrow$  next = current;

count++;

}

void deleteAtBegin() {

if (head == NULL)

printf("List is empty");

else {

p = head; q = head.

while (p  $\rightarrow$  next != head) {

p = p  $\rightarrow$  next;

p  $\rightarrow$  next = head  $\rightarrow$  next;

head  $\rightarrow$  next  $\rightarrow$  head = head  $\rightarrow$  next;

free(q);

head = count--;

}

}

void deleteAtEnd() {

if (head == NULL)

printf("List is empty");

else {

p = head; q = head;

while (p  $\rightarrow$  next  $\rightarrow$  next != head)

p = p  $\rightarrow$  next;

q = p  $\rightarrow$  next;

p  $\rightarrow$  next = head;

q  $\rightarrow$  next = NULL;

free(q);

count--;

}

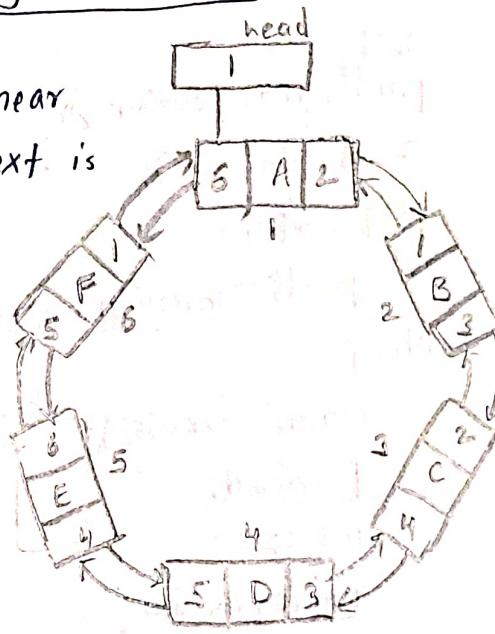
}

```
void deleteAtMiddle() {  
    int k;  
    printf("enter position:");  
    scanf("%d", &k);  
    if (k > count)  
        printf("List is empty");  
    else {  
        int i=2;  
        p = head;  
        while (p->next < k) {  
            p = p->next;  
            i++;  
        }  
        q = p->next;  
        p->next = q->next;  
        q->next = NULL;  
        free(q);  
        count--;  
    }  
}
```

```
int main() {  
}
```

# Implementation of Circular Doubly Linked List

Circular doubly linked list is a linear data structure in which last node's next is connected to first node and first node's previous is connected to last node.



```
#include<stdio.h>
```

```
struct node {
    int data;
    struct node *prev;
    struct node *next;
}
```

```
{ *head=NULL, *current, *p, *q;
```

```
int count=0;
```

```
struct node** create() {
```

```
    current = (struct node*)malloc(sizeof(struct node));

```

```
    printf("enter data: ");

```

```
    scanf("%d", &current->data);

```

```
    current->prev = current->next = NULL;

```

```
    return current;
}
```

```
}
```

```
void insertAtBegin() {
```

```
    current = (struct node*)create();

```

```
    if(head==NULL) {
```

```
        head = current;

```

```
else current = head;

```

```
    current->prev = head;

```

```
    current->next = head;

```

```
}
```

```
else {
```

```
    current->next = head;

```

```
    current->prev = head->prev;

```

```
    head->prev->next = current;

```

```
    head->prev = current;

```

```
    head = current;

```

```
} count++; }
```

```
void insertAtMiddle()
```

```
{
```

```
    int k;  
    printf("enter position: ");  
    scanf(".%d", &k);  
    if(k > count)
```

```
        printf("insertion not possible!");
```

```
    else {
```

```
        current = create();
```

```
        p = head;
```

```
        int i = 2;
```

```
        while(i < k) {
```

```
            p = p->next;
```

```
            i++;
```

```
}
```

```
        current->next = p->next;
```

```
        p->next->prev = current;
```

```
        current->prev = p;
```

```
        p->next = current;
```

```
        count++;
```

```
}
```

```
void insertAtEnd()
```

```
{
```

```
    if(head == NULL) {
```

```
        head = current;
```

```
        current->prev = head;
```

```
        current->next = head;
```

```
}
```

```
else {
```

```
    head->prev->next =
```

```
    current->prev = head->prev;
```

```
    head->prev->next = current;
```

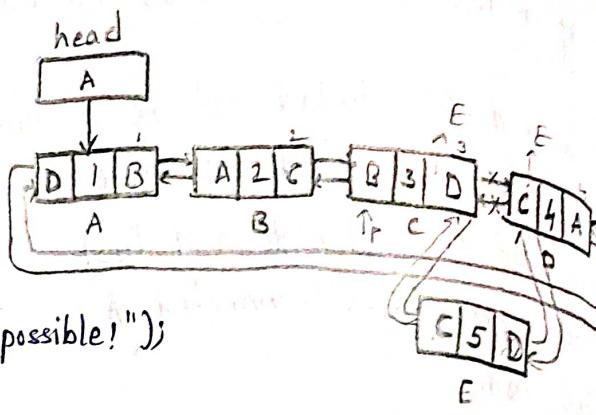
```
    current->next = head;
```

```
    head->prev = current;
```

```
}
```

```
count++;
```

```
}
```



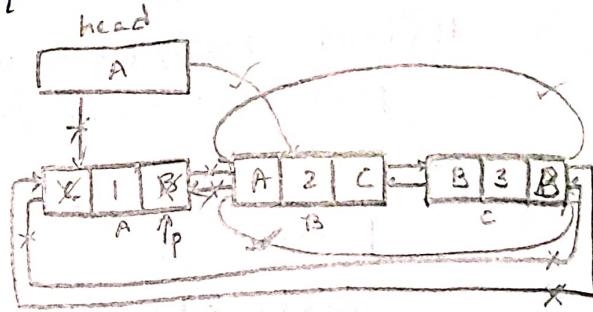
```
head
```



```
C  
4  
A  
P
```

```
void deleteAtBegin()
```

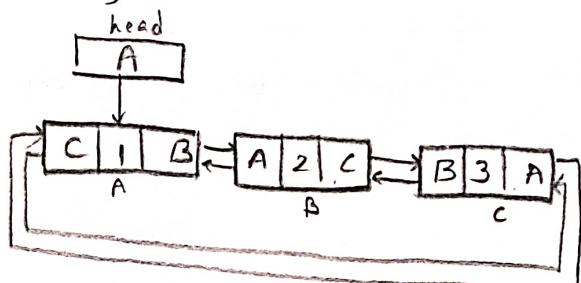
```
{  
    if (head == NULL)  
        printf("list is empty");  
    else if (head->next == head) {  
        head->prev = NULL;  
        head->next = NULL;  
        free(head);  
    }  
    else {
```



```
        initSize  
        p = head;  
        p->prev->next = p->next;  
        p->next->prev = p->prev;  
        head = p->next;  
        p->prev = p->next = NULL;  
        free(p);  
    }  
}
```

```
void deleteAtEnd()
```

```
{  
    if (head == NULL)  
        printf("list is empty!");  
    else if (head->next == head) {  
        head->prev = head->next = NULL;  
        free(head);  
    }  
    else {  
        p = head->prev;  
        p->prev->next = head;  
        head->prev = p->prev;  
        p->prev = p->next = NULL;  
        free(p);  
    }
```



```
void deleteAtMiddle() {
    int k, i=1;
    printf("enter position:");
    scanf("%d", &k);
    if (head == NULL || k > count)
        printf("deletion not possible");
    else {
        p = head;
        while (i < k) {
            p = p->next;
            i++;
        }
        (p->next)->prev = p->prev;
        p->prev->next = p->next;
        p->next = NULL;
        p->prev = NULL;
        free(p);
        count--;
    }
}
```

# Application of Stacks Data Structure

1. Infix to Postfix Expression Conversion.
2. Postfix expression Evaluation
3. Balancing brackets.
4. String reversal
5. Memory management
6. Recursive function calls.
7. Lexical analysis.
8. Syntax Parsing.
9. Backtracking Algorithms.
10. Undo and Redo operations.

## 1 Infix to Postfix Expression Conversion

Expression: It is combination of operands and operators

### Infix expression:

$\langle \text{operand} \rangle \langle \text{operator} \rangle \langle \text{operand} \rangle$

→ If operator is in b/w the operands then that expression is called.

### Infix expression.

Eg:  $a^+b + b^+c$

### Postfix expression:

→ If the operator is succeeded by the operands then it is called.

### Postfix expression.

$\langle \text{operand} \rangle \langle \text{operator} \rangle \langle \text{operand} \rangle$

Eg:  $a+b \Rightarrow ab+$

## Algorithm to convert Infix to Postfix expression

Step 1 : Start

Step 2 : Scan the given input expression (Infix) from left to right

Step 3 : If the symbol is operand write it into postfix notation, if it is operator push it on to stack.

Step 4 : If the symbol is '(' push it on to the stack.

Step 5 : Always ensure that the operator which is at the top of the stack with highest priority.

Step 6 : If the incoming operator is having highest priority than the operator at the top of the stack then push the incoming operator on to the top of the stack.

Step 7 : If the incoming operator is having less <sup>or equal</sup> priority than the operator at the top of the stack then pop that operator and push it on to the stack.

Step 8 : If incoming operator is having equal priority with operator at the top of the stack, then pop the top of the stack, push the incoming operator on to the stack.

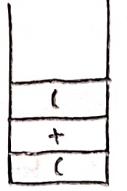
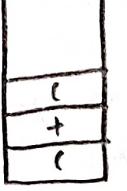
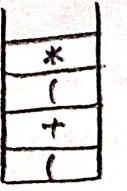
Step 9 : If the scanned operator is closed parenthesis, then pop all the operators in the stack until the open parenthesis and add these operators into postfix notation.

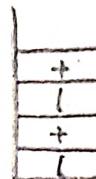
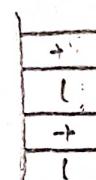
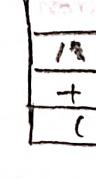
Step 10 : Repeat Step 2 to Step 9 until stack becomes empty

Step 11 : Display the postfix notation

Step 12 : Stop.

$$\rightarrow A + (B * C + D) / E$$

S NO	Symbol	Stack	Postfix Notation	Description
1.	(		-	'(' is pushed into stack.
2.	A		A	A is written in postfix notation.
3.	+		A	'l' is considered as negligible and don't affect incoming operator. + is pushed into stack.
4.	(		A	( is pushed into stack.
5.	B		AB	B is written into postfix notation.
;	*		AB	* is pushed into stack.

s.no	symbol	stack	Postfix notation	Description
7	c		ABC	c is written into postfix notation.
8	+		ABC*+	* is popped out from stack and added to postfix notation and + is pushed to stack.
9	D		ABC*D	D is written into postfix notation.
10	)		ABC*D+	popped + and written in postfix notation
11	/		ABC*D+ /	push / on to the stack
12	E		ABC*D+E	E is written in postfix notation.
13	)		ABC*D+E/+	/ and + are popped out and written in postfix notation

The postfix notation obtained

ABC\*D+E/+

→  $A + B * C / D$

s.no	symbol	stack	Postfix Notation	Description
1.	(	(	-	( is pushed onto the stack
2.	A	( A	A	A is written into postfix notation
3.	+	( +	A	+ is pushed onto stack
4.	B	( +	AB	B is written into postfix notation
5.	*	( + *	AB	* is pushed onto stack
6.	C	( + *	ABC	c is written into postfix notation.
7.	/	( + */	ABC*	* is popped out & / is pushed onto stack
8.	D	( + */	ABCD	D is written into postfix
9.	)	-	ABCD*/+	+ & / are popped out

Postfix notation: ABC\*D/+

→  $A + B * C / D - K + L ^ U$

s.no	symbol	stack	Postfix Notation	Description
1.	(	(	A -	( is written onto postfix notation, stack
2.	A	( A	A	A is written onto stack.
3.	+	( +	A	+ is pushed onto stack
4.	B	( +	AB	B is written into postfix notation

sno	symbol	stack	Postfix notation	Description
5.	*	( + *	AB	* is pushed onto stack.
6.	c	( + * c	ABC	c is written into postfix notation.
7.	/	( + / )	ABC* <sup>1</sup>	* is popped out and / is pushed onto stack.
8.	D	( + / D	ABC* <sup>1</sup> D	D is written into postfix notation.
9.	-	( -	ABC* <sup>1</sup> D / +	+ & / are popped out and - is pushed onto stack.
10.	K	( - K	ABC* <sup>1</sup> D / + K	K is written into postfix notation.
11.	+	( - +	ABC* <sup>1</sup> D / + K -	- is popped out & + is pushed onto stack.
12.	L	( - + L	ABC* <sup>1</sup> D / + K L	L is written into postfix notation.
13.	^	( - + ^	ABC* <sup>1</sup> D / + K L U	+ & - are popped and ^ is pushed onto stack.
14.	U	( - + ^ U	ABC* <sup>1</sup> D / + K L U V	^ is popped out & U is written into postfix notation.
Postfix Expression : ABC* <sup>1</sup> D / + K L U V + ^				
15.	)	( - + ^ U )	ABC* <sup>1</sup> D / + K L U V + ^	, +, - are popped out.

Final Postfix Notation: ABC\*<sup>1</sup> D / + K L U V + ^

$$\rightarrow (300^{*}23)^{*}(43-21)/(84+7)$$

$$\rightarrow (a^*(b+c)) + (b/d)^*a$$

5.no symbol : stack : Postfix Notation Description

1. ( ( - ( is pushed onto stack

2. ( ( ( - ( is pushed onto stack.

3. 300 ( ( 300 - 300 is written into postfix notation

4. \* (( \* 300 300 \* is pushed onto stack

5. 23 (( \* 300 23 23 is written into postfix notation

6. ) ( 300 23 \* \* is popped out

7. \* ( \* 300 23 \* \* is pushed onto stack

8. ( (\* ( 300 23 \* ( is pushed

9. 43 (\* ( 300 23 \* 43 43 is written

10. - (\* (- 300 23 \* 43 - is pushed

11. 21 (\* (- 300 23 \* 43 21 21 is written

12. ) (\* 300 23 \* 43 21 - - is popped out

13. / (/ 300 23 \* 43 21 - \* \* is popped & / is pushed

14. ( (/ 300 23 \* 43 21 - \* ( is pushed

15. 84 (/ ( 300 23 \* 43 21 - \* 84 84 is written

16. + (/ (+ 300 23 \* 43 21 - \* 84 + is pushed

17. / (/ (+ 300 23 \* 43 21 - \* 84 / is pushed

18 ) ( / 300 23 \* 43 21 - \* 84 7 + + is popped

19 ) - 300 23 \* 43 21 - \* 84 7 + / 1 is popped out

Postfix Notation - 300 23 \* 43 21 - \* 84 7 + /

$$\rightarrow (a^*(b+c)) + (b/d)^*a$$

s.no	symbol	stack	Postfix notation	Description
0.	c	c	-	c is pushed
1.	(	(	-	( is pushed
2.	a	( a	a	a is written
3.	*	(* a	*	* is pushed
4.	(	(* (	ba	( is pushed
5.	b	(* ( b	ab	b is written
6.	+	(* (+	ab	+ is pushed
7.	c	(* (+ c	abc	c is written
8.	)	(* +	abc+	+ is popped out
9.	)	'*	abc+*	* is popped out
10.	(	(	abc+*	( is pushed
11.	b	( b	abc+*b	b is written
12.	/	( /	abc+*b	/ is pushed.
13.	d	( / d	abc+*bd	d is written
14.	)	( /	abc+*bd /	/ is pushed.
15.	*	( / *	abc+*bd /	* is pushed

16 a  $\rightarrow abc + * bd / a$  'a' is written

17 )  $\rightarrow abc + * bd / a *$  \* is popped out

Postfix Notation -  $abc + * bd / a *$

## → Implementation

```
#include <stdio.h>
```

```
#include <ctype.h> → used to differentiate characters
```

```
char stack[100];
```

```
int top = -1;
```

```
void push(char x) {
```

```
    stack[++top] = x;
```

```
}
```

```
char pop() {
```

```
    if (top == -1)
```

```
        return -1;
```

```
    else {
```

```
        return stack[top--];
```

```
}
```

```
int priority(char c) {
```

```
    if (c == '^')
```

```
        return 3;
```

```
    else if (c == '/' || c == '*' || c == '%')
```

```
        return 2;
```

```
    else if (c == '+' || c == '-')
```

```
        return 1;
```

```
    else
```

```
        return 0;
```

```
}
```

```
int main() {
```

```
    char exp[100];
```

```
    char *e, x;
```

```
    printf("Enter the infix expression: ");
```

```
    scanf("%s", exp);
```

```
    printf("\n");
```

```

printf("\n Final Postfix Expression: ");
while(*e != '\0'){
    if(isalnum(*e))
        printf("./c", *e);
    else if(*e == '(')
        push(*e);
    else if(*e == ')'){
        while((x = pop()) != '(')
            printf("./c", x);
    }
    else{
        while(priority(stack[top]) >= priority(*e))
            printf("./c", pop());
        push(*e);
    }
    e++;
}
while(top != -1){
    printf("./c", pop());
}
return 0;
}

```

### Input

Enter the infix expression: A + B^C / D - K + L ^ U

### Output

Final Postfix Expression: A B C ^ D / + K - L U ^ +

→ POS

## Postfix Expression Evaluation

### Algorithm

Step 1: Start

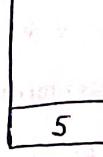
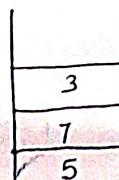
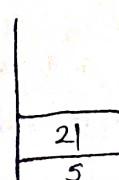
Step 2: Scan the given postfix expression from left to right.

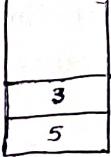
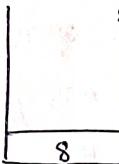
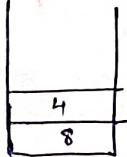
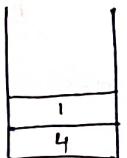
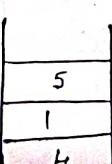
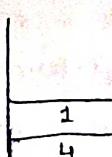
Step 3: If the reading symbol is operand then push it onto the stack.

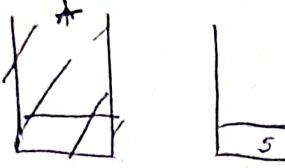
Step 4: If the reading symbol is operator then perform two pop operations and store the op two popped operands. in 2 different variables (operand<sub>1</sub>, operand<sub>2</sub>). Then perform reading symbol operation using operand<sub>1</sub> and operand<sub>2</sub>. and push result back to the stack.

Step 5: Finally perform a pop operation and display the popped value as final result.

Eg: 5 7 3 \* 6 / + 4 - 1 5 ^ +

Step no	Symbol	Stack	Evaluation	Description
1.	5		-	5 is pushed onto stack
2.	7		-	7 is pushed onto stack
3.	3		-	3 is pushed onto stack
4.	*		$op1 = 3$ $op2 = 7$ $op2 * op1 = 7 * 3$ = 21	3 & 7 is popped out, performed $7 * 3$ and. 21 is pushed onto stack

<u>s.no</u>	<u>symbol</u>	<u>stack</u>	<u>Evaluation</u>	<u>Description</u>
5.	6		-	6 is pushed onto stack
6.	/		$op1 = 6 \ op2 = 21$ $op2 / op1 = 21 / 6$ $= 3$	6 & 21 are popped out performed $21 / 6$ 3 is pushed onto stack
7.	+		$op1 = 3 \ op2 = 5$ $op2 + op1 = 5 + 3$ $= 8$	3 & 5 are popped out performed $5 + 3$ 8 is pushed onto stack
8.	4		-	4 is pushed onto stack
9.	-		$op1 = 4 \ op2 = 8$ $op2 - op1 = 8 - 4$ $= 4$	4 & 8 are popped out performed $8 - 4$ 4 is pushed onto stack
10.	1		-	1 is pushed onto stack
11.	5		-	5 is pushed onto stack
12.	^		$op1 = 5 \ op2 = 1$ $op2 ^ op1 = 1^5$ $= 1$	5 & 1 are popped out performed $1^5$ 1 is pushed onto stack

s.no	<u>symbol</u>	<u>stack</u>	<u>Evaluation</u>	<u>Description</u>
t3			$\text{op1}=1 \text{ op2}=4$ $\text{op2}+\text{op1}=4+1=5$	1 & 4 are popped out performed $4+1$ 5 is pushed onto stack

$$\text{pop}() = 5$$

Final Result = 5.

$$① A + B^* (C + D) / F + D^* E$$

s.no	<u>symbol</u>	<u>stack</u>	<u>Evaluation</u>	<u>Description</u>
1	A	-	A	A is printed in postfix evaluation
2	+	+	A	+ is pushed onto stack.
3	B	+	AB	B is printed in postfix notation
4	*	**	AB	* is pushed onto stack
5	(	**()	AB	( is pushed onto stack
6	C	**()	ABC	C is printed in postfix notation
7	+	**(+	ABC	+ is printed pushed onto stack.
8	D	**(+	ABCD	D is printed in postfix notation.
9	)	**	ABCD+	+ is popped out.
10	/	*/	ABCD+*	* is popped out.
11	F	+/	ABCD+*F	F is written into postfix notation

<u>s.no</u>	<u>symbol</u>	<u>stack</u>	<u>Evaluation</u>	<u>Description</u>
12	+	+	ABCD+*F/+	+ is pushed onto stack after / & + are popped out.
13	D	+	ABCD+*F/+D	D is written onto stack
14	*	+*	ABCD+*F/+D*	* is pushed onto stack after * is popped out.
15	E	+*	ABCD+*F/+D*E	E is written into postfix notation.
16	-	-	ABCD+*F/+D*E*-	+ & * are popped out.

Final Postfix Notation: ABCD+\*F/+D\*E\*-

Given A=5, B=2, C=3, D=4, E=6, F=7

5 2 3 4 + \* 7 / + 4 \* 6 \* -

<u>s.no</u>	<u>symbol</u>	<u>stack</u>	<u>Evaluation</u>	<u>Description</u>
1	5	5	-	5 is pushed onto postfix notation
2	2	5 2	-	2 is pushed onto postfix notation
3	3	5 2 3	-	3 is pushed onto postfix notation
4	4	5 2 3 4	-	4 is pushed onto postfix notation
5	+	5 2 7	$\begin{aligned} op_1 &= 4 \\ op_2 &= 3 \\ op_2 + op_1 &= 4 + 3 \\ &= 7 \end{aligned}$	4 & 3 are popped out and $4+3$ is performed and 7 is pushed onto stack.

<u>s.no</u>	<u>symbol</u>	<u>stack</u>	<u>Evaluation</u>	<u>Description</u>
6	*	5 14	$op_2 = 7$ $op_2 = 2$ $op_2 * op_1 = 14$	7 & 2 are popped out and $7 * 2$ is performed and 14 is pushed onto stack
7	7	5 14 7	$op_1 = 7$ $op_2 = 14$ -	7 is pushed onto stack
8	/	5 2	$op_1 = 7$ $op_2 = 14$ $op_2 / op_1 = 14 / 7$ = 2	2 is pushed onto stack after performing $14 / 7$ when 14 & 7 are popped out
9.	+	7	$op_1 = 5$ $op_2 = 2$ $op_2 + op_1 = 7$	5 & 2 are popped out and $5 + 2$ is performed and 7 is popped out pushed onto stack
10.	4	7 4	-	4 is pushed onto stack
11	*	28	$op_1 = 7$ $op_2 = 7$ $op_2 * op_1 = 28$	4 & 7 are popped out and $4 * 7$ is performed and 28 is pushed onto stack
12	6	7 4 28 6	-	6 is pushed onto stack
13	*	18 7 24	$op_1 = 6$ $op_2 = 7$ $op_2 * op_1 = 6 * 6$ = 36	6 & 7 are popped out $6 * 6$ is performed and 36 is pushed onto stack
14	+	31	$op_1 = 24$ $op_2 = 7$	24 & 7 are popped out $7 + 24$ is performed and 31 is pushed onto stack

Final Value Obtained: 37

$\rightarrow ABC + * DE / -$

$$A = 5 \quad B = 6 \quad C = 2 \quad D = 12 \quad E = 4$$

5 6 2 + \* 12 4 / -

s.no	symbol	stack	Evalution	Description
1.	5	5	-	5 is pushed onto stack
2.	6	5 6	-	6 is pushed onto stack
3.	2	5 6 2	-	2 is pushed onto stack
4.	+	5 8	$op_1 = 2$ $op_2 = 6$ $op_2 + op_1 = 6 + 2$ = 8	2 & 6 are popped out 6+2 is performed and 8 is pushed onto stack
5.	*	40	$op_1 = 8$ $op_2 = 5$ $op_2 * op_1 = 5 * 8$ = 40	8 & 5 are popped out 5 * 8 is performed and 40 is pushed onto stack
6.	12	40 12	-	12 is pushed onto stack
7.	4	40 12 4	-	4 is pushed onto stack
8.	/	40 12 3	$op_1 = 4$ $op_2 = 12$ $op_2 / op_1 = 12 / 4$ = 3	4 & 12 are popped out and $12/4$ is performed and 3 is pushed onto stack.
9.	-	37	$op_1 = 40$ $op_2 = 3$ $op_2 - op_1 = 40 - 3$ = 37	40 & 3 are popped out & $40 - 3$ is performed and 37 is pushed onto stack

Final Answer: 37

Evaluate  $7 \ 4 \ -3 * \ 1 \ 5 + / *$ .

s.no	symbol	stack	Evaluation	Description
1	7	7	-	7 is pushed onto stack
2	4	7 4	-	4 is pushed onto stack
3	-3	7 4 -3	-	-3 is pushed onto stack
4	*	7 -12	$op1 = -3$ $op2 = 4$ $op2 * op1 = -12$	-3 & 4 are popped out -3 * 4 is performed -12 is pushed onto stack
5	1	7 -12 1	$op = -$	1 is pushed onto stack
6	5	7 -12 1 5	-	5 is pushed onto stack
7	+	7 -12 6	$op1 = 5$ $op2 = 1$ $op2 + op1 = 5+1 = 6$	5 & 1 are popped out 1+5 is performed & 6 is pushed onto stack
8	/	7 -2	$op1 = 6$ $op2 = -12$ $op2 / op1 = -12 / 6 = -2$	6 & -12 are popped out -12 / 6 is performed -2 is pushed onto stack
9	*	-14	$op1 = -2$ $op2 = 7$ $op2 * op1 = 7 * (-2) = -14$	-2 & 7 are popped out -2 * 7 is performed -14 is pushed onto stack

Final Value: -14

## Implementation

```

#include<stdio.h>
#include <ctype.h>
#include <string.h>
#include <math.h>
int stack[20];
int top=-1;
Void push(int val)
{
    stack[++top] = val;
}
Void pop()
{
    return(stack[top--]);
}
int main()
{
    int op1, op2, len, result, i;
    char postfix[30], op;
    printf("\nEnter postfix expression:");
    scanf(" %s", postfix);
    len = strlen(postfix);
    for(i=0; i<len; i++) {
        if(isdigit(postfix[i])) {
            push(postfix[i] - '0');
        }
        else {
            op = postfix[i];
            op1 = pop();
            op2 = pop();
            switch(op) {
                case '+': push(op2 + op1);
                             break;
                case '-': push(op2 - op1);
                             break;
                case '*': push(op2 * op1);
                             break;
            }
        }
    }
}

```

```

        case '/': push(op2/op1);
                     break;
        case '%': push(op2%op1);
                     break;
        case '^': push(pow(op2, op1));
                     break;
    }
}

printf("Final value obtained : %d", pop());
return 0;
}

```

## → Balancing Brackets

### Algorithm

Step 1: Start

Step 2: Declare a ~~stack~~ character stack  $S$ , traverse the expression string from left to right.

Step 3: If the current character is:

Step 4: If the current character is starting bracket ( $'('$  or  $'['$  or  $'{'$ ) then push it onto the stack.

Step 5: If the current character is a closing bracket ( $')'$  or  $']'$  or  $'}'$ ) then pop from stack and if the popped character is matching starting bracket then balanced otherwise brackets are not balanced.

Step 6: After complete traversal, if there is some starting bracket left in the stack. then the expression is not balanced.

Step 7: Stop.

Eg:  $\left[ \{ ( ) ( ) ( ) ( ) \} \right]$  - Balanced.

$\left[ ( ) ( ) ( ) ( ) \right]$  - Not Balanced

$\left[ [ \{ \{ ( ) \} \} ] \right]$  - Balanced

## Implementation

```
#include<stdio.h>
#include<string.h>
#define MAX 100:
char stack[MAX];
int top=-1;
void push(char symbol){
    if (top == MAX-1)
        printf("stack is full\n");
    else
        stack[++top] = symbol;
}
void pop(){
    if (top == -1)
        printf("stack is empty\n");
    else
        top--;
}
int checkPair (char val1, char val2) {
    return ((val1 == 'x' && val2 == ')') || (val1 == '[' && val2 == ']') || (val1 == '{' && val2 == '}'));
}
int checkBalanced (char expr[], int len) {
    int /20; int i;
    for(i=0; i<len; i++){
        if (expr[i] == '(' || expr[i] == '[' || expr[i] == '{')
            push(expr[i]);
    }
}
```

```

        else {
            if (top == -1)
                return 0;
            else if (checkPair(stack[top], expr[i])) {
                pop();
                continue;
            }
            return 0;
        }
    }
    return 1;
}

int main() {
    char exp[MAX];
    printf("Enter expression string: ");
    scanf("%s", exp);
    int len = strlen(exp);
    checkBalanced(exp, len) ? printf("Balanced") : printf("Not Balanced");
    return 0;
}

```

Input

{ [ ] }

Output

Balanced

→ Test - 1

C01

- Derivation of Time complexities of Merge & Quick in 3 cases.
- Arranging time complexities.
- 6 Sorting Techniques . (4 programs)

- Algorithm
- Work Out
- Program
- Time Complexity . (Merge, Quick, Insertion, Shell)

## C02

- SLL, DLL, CSLL, CDLL, SSLL, QSLL, Infix to postfix, postfix, balancing brackets, CQ, PQ, Double Ended Queue.
- Search
  - reverse
  - delete a ~~not~~ key node.
  - min, max, duplicate, sum.

## → Types Of Queues

- Circular Queue
- Priority Queue
- DeQueue

## → Circular Queue

It is a linear data structure in which front & rear are both are adjacent to each other. (which means last is connected to first)

## Applications:

- Memory Management
- CPU Scheduling algorithms.
- Traffic systems.

## Operations

Enqueue( )

Dequeue( )

Display( )

## #14 Implementation

```
#include<stdio.h>
```

```
int cq[100], rear=-1, front=-1;
```

```
void enqueue( int ele)
```

```
{
```

```
if( front == (rear+1)%size)
```

```
printf("Circular Queue is full");
```

```
else if( front == -1 && rear == -1){
```

```
front=rear=0;
```

```
cq[rear]=ele;
```

```
}
```

```
else {
```

```
rear=(rear+1)%size;
```

```
cq[rear]=ele;
```

```
}
```

```
}
```

```
Void dequeue( )
```

```
{
```

```
if( front == rear)
```

```
printf("Circular Queue is empty");
```

```
else if( front == rear) {
```

```
printf("1st element is deleted!", cq[front]);
```

```
front=rear=-1;
```

```
}
```

```
else {
```

```
printf("1st element is deleted!", cq[front]);
```

```
front = (front+1)%size;
```

```
}
```

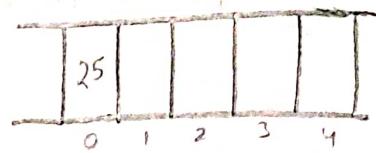
```
}
```

```
void display()
```

```
{
```

```
if( front == -1 && rear == -1)
```

```
printf("Circular Queue is Empty");
```



```

else {
    for(int i = front; i != rear; i = (i+1) % size)
        printf("%d", cq[i]);
    printf("%d", cq[rear]);
}
}

```

## → Priority Queue

It is a special type of queue in which each node will have predefined priority to service.

```

#include <stdio.h>
struct node {
    int data;
    int priority;
    struct node *next;
} *head == NULL, *current, *p, *q;
struct
void pEnqueue (int data, int priority)
{
    current = (struct node *) malloc (sizeof (struct node));
    current->data = data;
    current->priority = priority;
    current->next = NULL;
    if (head == NULL)
        head = current;
    else if (current->priority < head->priority) {
        p = head;
        head = current;
        current->next = head;
    }
    else {
        p = head;
        q = head;
        while (q->priority <= current->priority)
            q = q->next;
        p = q->next;
        current->next = p;
        q->next = current;
    }
}

```

```
while (p != NULL && (p->priority < current->priority)) {  
    p=p->next;  
    q=p;  
    p=p->next  
}  
current->next=p;  
q->next = current;
```

}

```
void pDequeue()
```

{

```
p;if (head == NULL)
```

```
printf("Queue is empty!");
```

```
else {
```

```
p=head;
```

```
head=p->next;
```

```
p->next=NULL;
```

```
free(p);
```

}

}

```
void display()
```

{

```
if (head == NULL)
```

```
printf("Queue is empty");
```

```
else {
```

```
p=head;
```

```
while (p != NULL) {
```

```
printf("%d ", p->data);
```

```
p=p->next;
```

}

}

## → Double-Ended Queue

① → WCP to convert an expression from infix to postfix and convert the following expression  $A^*B - (C+D)^*(F)$

② → Evaluate the following postfix expression using stack.

$$12 \ 7 \ 3 \ - \ 1 \ 2 \ 1 \ 5 \ 4 \ + \ +$$

③ → Write the algorithm for insertion sort and sort the following numbers 20, 35, 40, 100, 3, 10, 15, 1

④ → Write an algorithm to sort given list of names in alphabetical order using bucket sort.

⑤ → WCP to implement stack operations using `Kir SinglyLinkedList`.

⑥ → Write mergeSort Algorithm & sort following elements  
23, 11, 37, 28, 15, 19, 55, 9.

⑦ → Write a functional code for deleting a desired node in a DoublyLinked list.

⑧ → WCP to perform enqueue, dequeue and display operations in a priority queue.

⑨ →

```
#include <stdio.h>
struct node {
    int data;
    struct node* next;
}*top=NULL, *current, *p, *q;
void push() {
    current = (struct node*) malloc (sizeof(struct node));
    scanf ("%d", &current->data);
    current->next = NULL;
    if (head == NULL)
        head = current;
```

```
else {
    p=&head;
    while(p!=NULL) {
        current->next=top;
        top=current;
        current=p->next;
    }
}
```

```
} void pop()
{
    if(top==NULL)
        printf("Stack is empty");
    else {
        p=top;
        top=p->next;
        p->next=NULL;
        free(p);
    }
}
```

```
}.
void display()
{
    if(top==NULL)
        printf("Stack is empty");
    else
```

```
    p=top;
    while(p!=NULL) {
        printf("%d", p->data);
        p=p->next;
    }
}
```

```
}.
void peak()
```

```
{
    if(top==NULL)
        printf("Stack is empty");
    else
        printf("%d", top->data);
```

```

int main()
{
    int ch;
    printf("1. push\n2. pop\n3. peak\n4. display\n5. exit\n");
    while(1){
        scanf("%d", &ch);
        switch(ch){
            case 1: push();
                break;
            case 2: pop();
                break;
            case 3: peak();
                break;
            case 4: display();
                break;
            case 5: exit(0);
            default: printf("invalid");
        }
    }
}

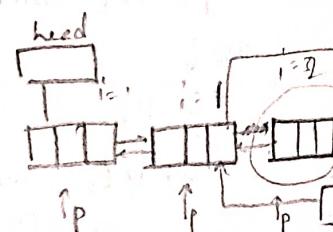
```

①

```

void deleteAtMiddle()
{
    int k, i;
    if scanf(".d", &k);
    if (k > c)
        printf("deletion not possible");
    else if (thead == NULL)
        printf("Not possible");
    else {
        p = head;
        i = 1;
        while (i < k) {
            p = p->next;
            p->prev->next = p->next;
            p->next->prev = p->prev;
            p->prev = p->next = NULL;
            free(p);
        }
    }
}

```



```

① #include <stdio.h>
struct node {
    int data, priority;
    struct node *next;
};
node *head = NULL, *current, *p, *q;
void enqueue()
{
    current = (struct node *) malloc (sizeof(struct node));
    scanf ("%d", &current->data);
    current->next = NULL;
    if (!head) scanf ("%d", &current->priority);
    if (head == NULL)
        head = current;
    else if (current->priority < head->priority)
        current->next = head;
        head = current;
}
else {
    p = head; q = head;
    while (p != NULL &&
           (current->priority > p->priority))
        q = p;
        p = p->next;
    current->next = q->next;
    q->next = current;
}
void dequeue()
{
    if (head == NULL)
        printf ("PQ is empty");
    else {
        p = head;
        head = p->next;
        p->next = NULL;
        free(p);
    }
}

```

```
void display()
```

```
{
```

```
    p = head;
```

```
    while (p != NULL) {
```

```
        printf("%d->%d->", p->data, p->priority);
```

```
        p = p->next;
```

```
}
```

```
}
```

```
int main()
```

```
{
```

```
    int ch;
```

```
    printf("1. enqueue\n2. dequeue\n3. display\n");
```

```
    while (1) {
```

```
        scanf("%d", &ch);
```

```
        switch (ch) {
```

```
            case 1: enqueue();
```

```
            break;
```

```
            case 2: dequeue();
```

```
            break;
```

```
            case 3: display();
```

```
            break;
```

```
            default: exit(0);
```

```
}
```

```
}
```

```
3
```

⑤

12 + 3 - 1 2 1 5 + \* +

Symbol

Stack

Evaluation

Description

12

12

-

12 is pushed onto stack

7

12 7

-

7 is pushed onto stack

3

12 7 3

.

3 is pushed onto stack

-

12 4

$op_1 = 3$

$op_2 = 7$

$op_2 - op_1 = 7 - 3$

$= 4$

3 & 7 are popped

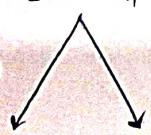
7 - is calculated

<u>Symbol</u>	<u>Stack</u>	<u>Evaluation</u>	<u>Description</u>
/	3	$op = /$ $op1 = 12$ $op2 = 12$ $op2/op1 = 12/12$ = 3	12 & 12 are popped & 12/12 is calculated & 3 is pushed onto stack.
2	3 2	-	2 is pushed onto stack
1	3 2 1	-	1 is pushed onto stack
5	3 2 1 5	-	5 is pushed onto stack
+	3 2 6	$op = +$ $op1 = 5$ $op2 = 1$ $op2 + op1 = 5 + 1$ = 6	5 & 1 are popped & 5+1 is calculated & 6 is pushed onto stack
*	3 12	$op = *$ $op1 = 6$ $op2 = 2$ $op2 * op1 = 2 * 6$ = 12	6 & 2 are popped & 6*2 is calculated & 12 is pushed onto stack
+	15	$op = +$ $op1 = 12$ $op2 = 3$ $op2 + op1 = 3 + 12$ = 15	12 & 3 are popped & 3+12 is calculated & 15 is pushed onto stack
-	-	-	15 is popped out

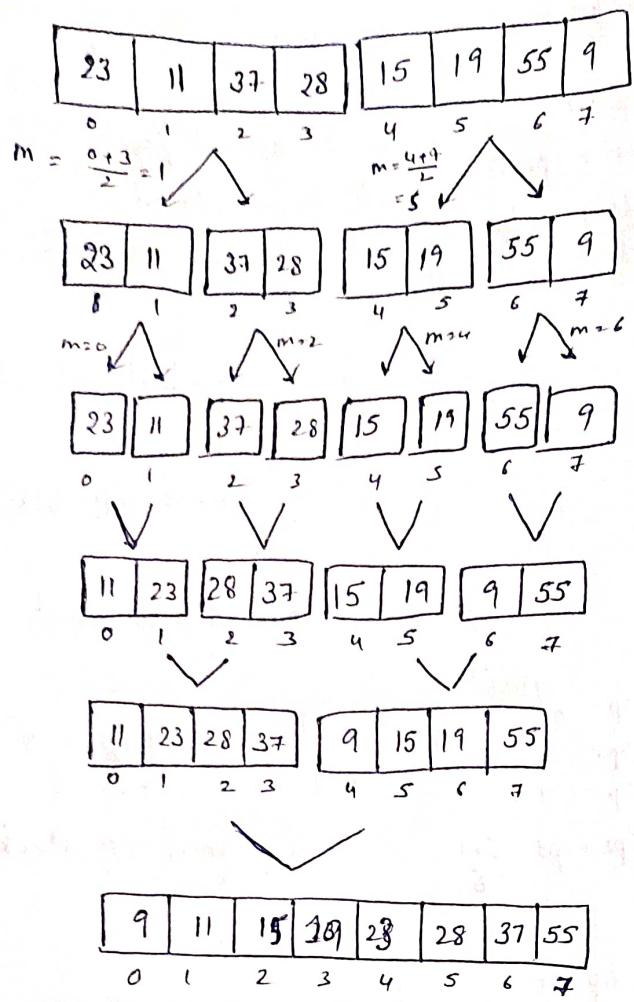
6.

23	11	37	28	15	19	55	9
0	1	2	3	4	5	6	7

$$m = \frac{0+h}{2} = \frac{0+7}{2} = 3$$



23	11	37	28	15	19	55	9
0	1	2	3	4	5	6	7



3.

[20]	[35]	[40]	[100]	[3]	[10]	[15]	[1]
0	1	2	3	4	5	6	7

P-1

$$20 \mid 35 \quad 40 \quad 100 \quad 3 \quad 10 \quad 15 \quad 1$$

$$\underline{P-20} \quad \underline{35} \quad 40 \quad 100 \quad 3 \quad 10 \quad 15 \quad 1$$

P-2

$$20 \quad 35 \mid 40 \quad 100 \quad 3 \quad 10 \quad 15 \quad 1$$

$$20 \quad 35 \quad \underline{40} \quad 100 \quad 3 \quad 10 \quad 15 \quad 1$$

P-3

$$20 \quad 35 \quad 40 \mid 100 \quad 3 \quad 10 \quad 15 \quad 1$$

$$20 \quad 35 \quad 40 \quad \underline{100} \quad 3 \quad 10 \quad 15 \quad 1$$

P-4

$$20 \quad 35 \quad 40 \quad 100 \quad \underline{\underline{3}} \quad 10 \quad 15 \quad 1$$

20 35 40 3 100 10 15 1

20 35 3 40 100 10 15 1

20 3 35 40 100 10 15 1

3 20 35 40 100 10 15 1.

P-5

3 20 35 40 100 | 10 15 1

3 20 35 40 | 10 100 15 1

3 20 35 | 10 40 100 15 1

3 20 | 10 35 40 100 15 1

3 10 20 35 40 100 15 1

P-6

3 10 20 35 40 100 | 15 1

3 10 20 35 40 | 15 100 1

3 10 25 35 | 15 40 100 1

3 10 25 | 15 35 40 100 1

3 10 15 25 35 40 100 1

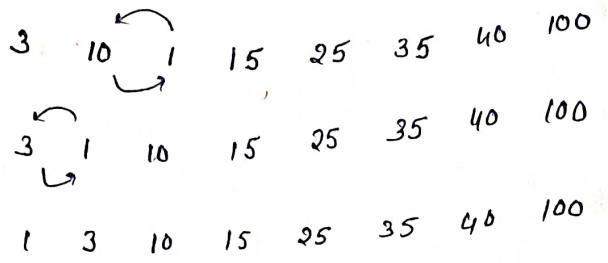
P-7

3 10 15 25 35 40 100 | 1

3 10 15 25 35 | 40 1 100

3 10 15 25 | 1 35 40 100

3 10 15 | 1 25 35 40 100



∴ Final Sorted Array: 1 3 10 15 25 35 40 100

1.

$$A^* B - (c + D)^* (P/Q)$$

<u>Symbol</u>	<u>stack</u>	<u>Postfix Notation</u>	<u>Description</u>
A	-	A	A is written in P.F.N
*	*	A	* is pushed onto stack
B	*	AB	B is written in P.F.N
-	* -	AB*	* is popped & - is pushed.
(	- (	AB*	( is pushed.
c	- (	AB*c	c is written in P.F.N
+	- (+	AB*c	+,( is pushed
D	- (+	AB*cD	D is written in P.F.N
)	-	AB*cD+	+ is popped
*	- *	AB*cD+	* is pushed.
(	- * (	AB*cD+	( is pushed.
P	- * (	AB*cD+p	p is written in P.F.N
/	- * ( /	AB*cD+p	/ is pushed
Ø	- * ( /	AB*cD+pØ	Ø is written on P.F.N

- )  $\rightarrow * \quad AB^*CD + PQ /$       / is popped and ( is neglected.
- $\rightarrow - \quad AB^*CD + PQ /* -$       all are popped.

Final Postfix expression :  $AB^*CD + PQ /*$ .

### Implementation

```
#include <stdio.h>
#include <ctype.h>
int stack[100], top = -1;
void push(char x) {
    stack[++top] = x;
}
int char pop() {
    if (top == -1)
        return -1;
    else
        return stack[top--];
}
int priority(char x) {
    if (x == '^')
        return 3;
    else if (x == '/' || x == '*' || x == '%')
        return 2;
    else if (x == '+' || x == '-')
        return 1;
    else
        return 0;
}
int main()
{
    char exp[100]; e;
    scanf("%s", exp);
    e = exp;
```

```

while ( e != NULL) {
    if (isalnum(*e))
        printf("./c", *e);
    else if (*e == '(')
        push(*e);
    else if (*e == ')') {
        while ((x = pop()) != '(')
            pop();
        printf("./c", x);
        push(*e);
    }
    else {
        while (priority(*e) < priority(stack[top]))
            pop();
        printf("./c", pop());
        push(*e);
    }
}
while (top != -1)
    printf(pop());
return 0;

```

### ③ Algorithm for Insertion Sort

Step 1: Start;

Step 2: If the array has 0 or 1 then it is already sorted.

Step 3: Otherwise, first element is already sorted. start from next element.

Step 4: Check the element with the elements in sorted array

Step 5: If the element is less than elements in sorted array keep it in its place.

Step 6: Continue the step 4 and 5 for all elements in array until we get sorted array

Step 7: Stop.

### ④ Algorithm for Bucket Sort

Step 1: Start

Step 2: Create  $n$  no of buckets.

Step 3: In an array, drop each element  $a[i]$  in bucket of range  $[n * a[i]]$ .

Step 4: Apply Insertion or bucket sort on each bucket, to get sorted elements.

Step 5: Combine all to get sorted array.

Step 6: Stop.

### ⑤ Algorithm for merge sort

Step 1: Start

Step 2: If array has 0 or 1 elements array is already sorted.

Step 3: Otherwise divide the array into 2 parts.

Step 4: Apply merge sort algorithm recursively on each part until we get single element in each part

Step 5: Merge All to get sorted array, using swapping.

Step 6: Stop.

## → Time Complexity

```
for(i=1; i<n; i++) {
```

```
    for(j=i; j
```