

THE COPPERBELT UNIVERSITY
SCHOOL OF MATHEMATICS AND NATURAL SCIENCES
SESSIONAL EXAMINATION 2015/16 Marking guide

TITLE OF PAPER: GENERAL CHEMISTRY

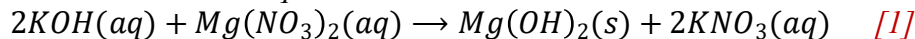
COURSE NUMBER: CH110/CH120/FO130

Question 1 (20 marks)

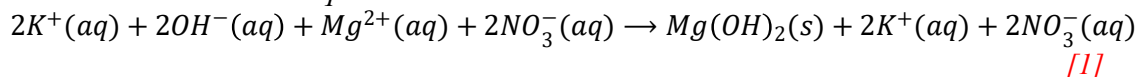
- a) A 100.0ml aliquot of 0.200 M aqueous potassium hydroxide is mixed with 100.0 ml of 0.200 M aqueous magnesium nitrate [Total Marks – 6]

i) Write a balanced chemical, ionic and net ion equation for the reaction [3]

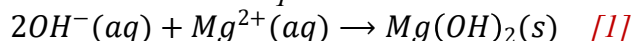
Balanced chemical equation



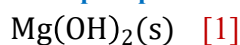
Balanced ionic equation



Balanced net ionic equation



ii) What precipitate is formed from this reaction? [1]



iii) Calculate the mass of the precipitate formed [3]

Mole ratios: 2 moles of KOH produce a mole of 1 of $\text{Mg}(\text{OH})_2$ [0.5]

Moles of KOH used up in this reaction is

$$M_{\text{KOH}} \times V_{\text{KOH}} = 0.1\text{L} \times 0.2\text{M} = 0.020 \text{ mol} \quad [0.5]$$

Therefore 0.010 mol $\text{Mg}(\text{OH})_2$ is formed [0.5]

The mass formed is given by the formula $m = n \times M_r$ [0.5]

since

$$M_r = M_{\text{Mg}} + 2 \times M_{\text{OH}} = 24.31 + 2 \times 17.008 = 58.33 \text{ g/mol}, \quad [0.5]$$

$$m = n \times M_r = 0.010 \text{ mol} \times 58.33 \frac{\text{g}}{\text{mol}} = 0.58 \text{ g} \quad [0.5]$$

b) Specify which of the following are Redox reactions. For the Redox reactions, identify the reducing agent, the oxidizing agent, the substance oxidized, and the substance reduced [3]



Not a redox reaction! [0.5]



Redox reaction [0.5]

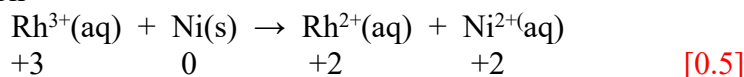
Hydrogen in water is the oxidising agent [0.5], it oxidises carbon in methane [0.5]. Carbon is the reducing agent [0.5], it reduces hydrogen [0.5]

c) Balance the following Redox reaction equations using oxidation numbers [2]

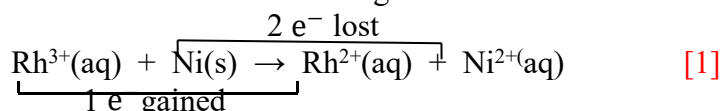


Step 1. Unbalanced equation is: $\text{Rh}^{3+}(\text{aq}) + \text{Ni}(\text{s}) \rightarrow \text{Rh}^{2+}(\text{aq}) + \text{Ni}^{2+}(\text{aq})$

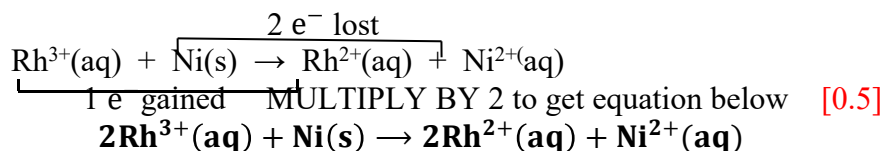
Step 2. We start by writing the oxidation numbers of each species in the equation



Step 3. We show how electrons are gained and lost



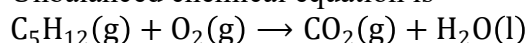
Step 4. Show coefficients needed to equalize the electrons gained and lost



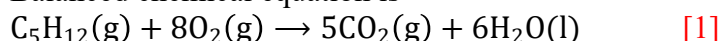
Step 5. All elements are balanced therefore the above equation is the required balanced equation

- (d) Consider the unbalanced chemical equation for the combustion of pentane (C_5H_{12}) given as $\text{C}_5\text{H}_{12}(\text{g}) + \text{O}_2(\text{g}) \rightarrow \text{CO}_2(\text{g}) + \text{H}_2\text{O}(\text{l})$. If 20.4 g of pentane are burned in excess oxygen, what mass of water can be produced, assuming 100% yield? [4]

Unbalanced chemical equation is



Balanced chemical equation is



Stoichiometry requires that every mole of pentane burnt gives 6 moles of water [1]

20.4 g (or m_{pentane}) of pentane has n_{pentane} moles given as

$$n_{\text{pentane}} = \frac{m_{\text{pentane}}}{M_{\text{pentane}}} \text{ where } M_{\text{pentane}} \text{ is the molar mass of pentane}$$

$$\text{But } M_{\text{pentane}} = 12 \times M_{\text{H}} + 5 \times M_{\text{C}}$$

where M_{H} and M_{C} are molar mass of hydrogen and carbon

$$M_{\text{pentane}} = 12 \times 1.008 + 5 \times 12.01 = 12.096\text{g} + 60.05\text{g} = 72.146\text{g}$$

$$\text{So that } n_{\text{pentane}} = \frac{20.4\text{g}}{72.146\text{g}} = 0.283 \text{ moles} \quad [0.5]$$

The moles water produced (n_{water}) is $6 \times n_{\text{pentane}}$, that is

$$n_{\text{water}} = 6 \times n_{\text{pentane}} = \frac{6 \times 20.4\text{g}}{72.146\text{g}} = 1.697 \text{ moles} \quad [0.5]$$

The mass of water produced (m_{water}) is

$$m_{\text{water}} = M_{\text{water}} \times n_{\text{water}} = \frac{6 \times 20.4\text{g}}{72.146\text{g}} \times 18.016\text{g} = \underline{\underline{30.6\text{g}}} \quad [1]$$

- (e) The empirical formula of styrene is CH ; the molar mass of styrene is 104.14 g/mol. What number of H atoms are present in a 2.00-g sample of styrene? [4]

The empirical formula of styrene is given as, CH . This gives a molar empirical mass

$$M_{\text{em}} = n_{\text{C}} \times M_{\text{C}} + n_{\text{H}} \times M_{\text{H}} \text{ that is } M_{\text{em}} = 12.01 + 1.008 = 13.018\text{g} \quad [0.5]$$

The molecular mass of styrene (M_{r}) is given as 104.14 g.

The integer obtained from dividing molecular mass with empirical formula mass, n_{integer} , is

$$n_{\text{integer}} = \frac{M_{\text{r}}}{M_{\text{em}}} = \frac{104.14}{13.018} = 8 \quad [1]$$

$$\text{The number of moles of styrene, } n \text{ is } n = \frac{m_{\text{s}}}{M_{\text{r}}} = \frac{2}{104.14} = 0.0192 \quad [0.5]$$

The number of molecules of styrene, $N_{\text{molecules}}$ is

$$N_{\text{molecules}} = n \times N_{\text{Avogadro}} = 0.0192 \times 6.023 \times 10^{23} = 1.157 \times 10^{22} \quad [1]$$

For each mole of styrene, there are 8 atoms of hydrogen, therefore, number of hydrogen atoms, N_{H} in 2 grams of styrene is

$$N_{\text{H}} = n_{\text{integer}} \times N_{\text{molecules}} = 8 \times 1.157 \times 10^{22} = \underline{\underline{9.254 \times 10^{22} \text{ H atoms}}} \quad [1]$$

Question 2 (20 marks)

- (a) KClO_3 is decomposed by the following reaction:**



The O_2 produced was collected by the displacement of water at 22°C at a total pressure of 760 torr. The volume of gas collected was 1.20 liters, and the vapour pressure of water at 22°C is 21 torr.

- (i) Define the term partial pressure**

The portion of the total pressure that one gas in a mixture of gases contributes. Assuming ideal gas character, the partial pressure of any gas in a mixture is the pressure that the gas would yield if it were alone in the container **[1 mark]**

- (ii) Calculate the partial pressure of O_2 in the gas collected and the mass of KClO_3 in the sample that was decomposed**
- [3]**

$$P_{\text{total}} = P_{\text{O}_2} + P_{\text{H}_2\text{O}};$$

$$P_{\text{O}_2} + 21 \text{ torr} = 760 \text{ torr},$$

$$\text{thus, } P_{\text{O}_2} = \mathbf{739 \text{ torr}} \text{ [1 mark]}$$

Converting pressure in torr to pressure in atm,

$$P = \frac{739 \text{ torr}}{760 \text{ torr}} \cdot \text{atm} = 0.9724 \text{ atm}$$

$$n = \frac{PV}{RT} = \frac{(0.9724 \times 1.2)}{(0.08206 \times 295.15)} = 0.0482 \text{ mol Oxygen gas}$$

No. mol (KClO_3) = $0.0482 \text{ mol O}_2 \times (2 \text{ mol KClO}_3 \div 3 \text{ mol O}_2) = 0.0321 \text{ mol}$ according to the stoichiometry of the reaction equation. Student should be able to balance the reaction equation.

$$\begin{aligned} \text{Mass } (\text{KClO}_3) &= \text{No. mol} \times \text{Molar mass} \\ &= 0.0321 \text{ mol} \times 122.5 \text{ gmol}^{-1} \\ &= \mathbf{3.93 \text{ g KClO}_3} \text{ [2 marks]} \end{aligned}$$

- (b) Incandescent light bulbs “burn out” because their tungsten filament evaporates, weakening the thin wire until it breaks. Argon gas is added inside the bulbs to reduce the rate of evaporation. (Argon is chosen because, as a noble gas, it will not react with the components of the bulb, and because it is easy to obtain in significant quantities. It is the third most abundant element in air).**

- (i) At what temperature would 0.0315 g of Ar in a 25.0-mL incandescent light bulb have a pressure of 952 mmHg?**
- [3]**

$$PV = \frac{gRT}{M} \quad \text{where } g = \text{mass, } M = \text{molar mass}$$

$$\begin{aligned} T = \frac{PVM}{gR} &= \frac{(952 \text{ mmHg} \times 25.0 \text{ mL} \times \frac{39.948 \text{ g}}{\text{mol}})}{(0.0315 \text{ g} \times 0.08206 \text{ L atm K}^{-1} \text{ mol}^{-1})} \times \frac{1 \text{ atm}}{760 \text{ mmHg}} \times \frac{1 \text{ L}}{1000 \text{ mL}} \\ &= \mathbf{484 \text{ K}} \text{ [3 marks]} \end{aligned}$$

- (ii) What would be the density of argon gas in an incandescent bulb at 79.9°C and 129.8 kPa?**
- [3]**

$$P = 129.8 \text{ kPa}, T = 79.9 + 273.15 = 353.05 \text{ K}$$

$$\text{Density} = \frac{g}{V} = \frac{PM}{RT} = \frac{(129.8 \text{ kPa} \times 39.948 \times 10^{-3} \text{ kg/mol})}{(8.3145 \text{ J K}^{-1} \text{ mol}^{-1} \times 353.05 \text{ K})} = 1.77 \text{ kg/m}^3$$

(= 1.77 g/L) L[3 marks]

(c) In the study of gases in CH110, it is important that undergraduate students understand ideal and real gases with respect to the conditions surrounding these two types of gases.

(i) Define the term ideal gas and explain how it differs from a real gas. [3]

An ideal gas is a hypothetical gas which obeys the equation $PV = nRT$.

How it differs from a real gas:

- Particles in an ideal gas move randomly in straight line motion while real gases move in non-straight line motion (Brownian Motion)
- An ideal gas does not experience any attractive forces due to the distance among molecules. Forces of attraction exist among molecules of a real gas (weak IMF)
- Ideal gas particles do not lose energy during collisions (collisions are perfectly elastic). Real gas molecules lose energy during collisions.
- Ideal gases are hypothetical; used in Science for easier calculations and analyses whereas real gases are real! **[Any 3 of these, 1 mark each]**

(ii) Calculate the pressure exerted by 1.00 mol ammonia when it is confined at 25 °C in 500 cm³ (a = 4.169 atm dm⁶ mol⁻², b = 3.71 × 10⁻² dm³ mol⁻¹) behaving as:

1) an ideal gas; [2]

$$PV = nRT$$

$$P = \frac{nRT}{V} = \frac{1.00 \times 0.08206 \times 298.15}{0.500} = 48.9 \text{ atm} \quad [2 \text{ marks}]$$

2) a van der Waals gas. [5]

$$\left(p + \frac{an^2}{V^2}\right)(V - nb) = nRT \quad [1 \text{ mark}]$$

$$\left(p + \frac{4.169 \times 1.00^2}{0.500^2}\right)(0.500 - 1.00(3.71 \times 10^{-2})) = (1.00 \times 0.08206 \times 298.15)$$

$$p = 36.2 \text{ atm} \quad [4 \text{ marks}]$$

Question 3 (20 marks - alternative)

(a) Define a system and state the three types of systems [2]

A system is a part of the universe that we choose to focus our attention on **(1)**

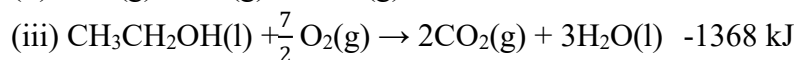
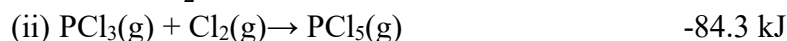
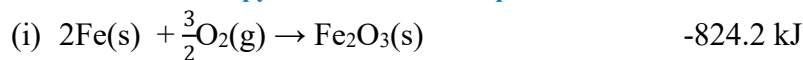
The three types of system are: open system, closed system and isolated system. **(1)**

(b) Write thermochemical equations corresponding to the following descriptions.

(i) The standard enthalpy of formation of iron(III) oxide at 298 K is -824.2 kJ/mol.

(ii) The standard enthalpy change at 298 K for the reaction between gaseous phosphorus trichloride and chlorine gas to give gaseous phosphorus pentachloride is -84.3 kJ.

(iii) The standard enthalpy of combustion of liquid ethanol is -1368 kJ/mol. [6]



(1 mark for correct eqn and 1 mark for enthalpy change)

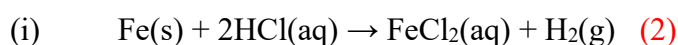
(c) The reaction between a metal and an acid yields a salt and hydrogen gas. 50 g of iron is reacted with excess hydrochloric acid.

(i) Write a balanced equation for the above reaction [2]

(ii) State the equation employed in calculating the work done by the surrounding on a system. [1]

(iii) Calculate the work done if the reaction takes place in a closed vessel [2]

(iv) Calculate work done if the reaction takes place in an open beaker at 25°C. [3]



(ii) $W = P\Delta V$ (1)

(iii) Since $\Delta V = 0$ (container is closed) $w = -P\Delta V = 0$ (2)

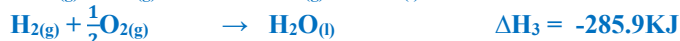
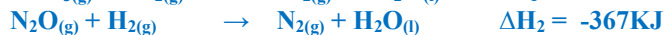
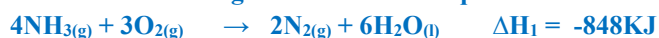
(iv) $w = -P\Delta V = -n_{\text{H}_2}RT$ (1)

number of mols of Fe in 50 g is $= 50 \text{ g Fe} \times \frac{1 \text{ mol Fe}}{55.85 \text{ g Fe}} = 0.895 \text{ mol Fe}$ (½)

From balanced eqn $n_{\text{Fe}} = n_{\text{H}_2} = 0.895 \text{ mol H}_2$. (½)

$W = -0.895 \text{ mol} \times 8.314 \text{ JK}^{-1} \text{ mol}^{-1} \times 298 \text{ K} = -2.2 \text{ kJ}$ (1)

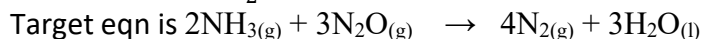
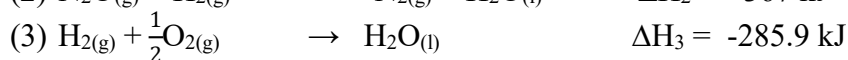
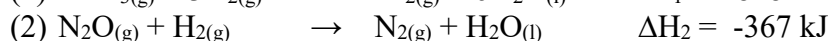
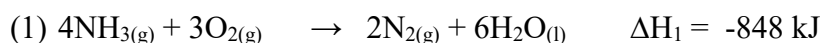
(d) Given the following thermochemical equations:



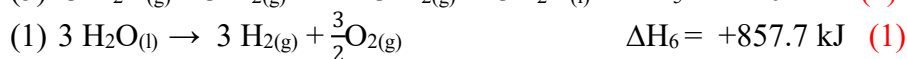
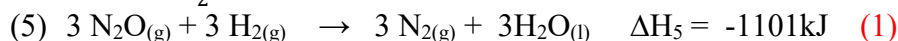
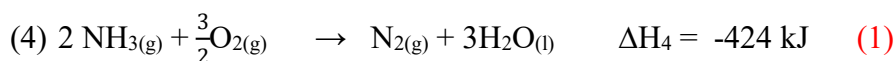
Calculate the value of ΔH for the reaction;



Number the equations as follows



Multiply eqn (1) by ½, eqn (2) by 3 and reverse eqn (3) and multiply it by 3



Adding these three gives the target eqn. Hence

$\Delta H = \Delta H_4 + \Delta H_5 + \Delta H_6 = (-424 + -1101 + 857.7) \text{ kJ} = -667 \text{ kJ}$. (1)

Question 4 (20 marks)

(a) In the quantum mechanical model of an atom

- (i) When given the sublevels E_{4s} , E_{4p} , E_{4d} , E_{4f} of a polyelectronic atom, state whether these are degenerate or not. [1]
- (ii) If they are not degenerate, show how the quantum levels of the orbitals vary in energy. Zumdahl and Zumdahl, 9th Edition, pp. 345. [1]
- (iii) For each Subshell above, copy the table below and fill the last column [4]

Answer:

- (i) The levels are different sublevels belonging to the same shell of a polyelectronic atom. Such levels are not degenerate. [1]
- (ii) Their energy order is $E_{4s} < E_{4p} < E_{4d} < E_{4f}$ [1]
- (iii) Elements in the table are

Subshell	Element with final Subshell electron configuration given as	Element name or symbol
E_{4s}	$4s^2$	Calcium or Ca [1]
E_{4p}	$4p^6$	Krypton or Kr [1]
E_{4d}	$4d^{10}$	Cadmium or Cd [1]
E_{4f}	$4f^{14}$	Lutetium or Lu [1]

(b) Classify the elements in the last column of the table of (c) into following element groups

- (i) main group elements (ii) alkali metals (iii) alkaline earth metals (iv) transition metals (v) Actinides (vi) Noble gas [6]

Answer: (i) Ca [1] (ii) None [1] (iii) Ca [1] (iv) Cd [1] (v) Lu [1] (vi) Kr [1]

(c) Wave particle duality: Neutron diffraction is used in determining the structures of molecules. Calculate the de Broglie wavelength of a neutron moving at 1.00% of the speed of light. Zumdahl and Zumdahl, 9th Edition, Question 7.54 pp. 369 [5]

Answer:

Using the de Broglie equation, $\lambda = \frac{h}{mv}$ [1]

where Planck's constant is $h = 6.63 \times 10^{-34} \text{ J} \cdot \text{s}$,

mass of a neutron is $m = 1.675 \times 10^{-27} \text{ kg}$ and

velocity of the neutron is $v = 0.01c = 0.01 \times 3.00 \times 10^8 \text{ ms}^{-1}$ [1]

Thus, $\lambda = \frac{6.63 \times 10^{-34}}{1.675 \times 10^{-27} \times 3.0 \times 10^6} \text{ m}$ [1]

$= 1.32 \times 10^{-15} \text{ m}$ [2; 1 mark for correct answer & 1 mark for correct units]

(d) Photoelectric Effect: At the conclusion of the study of the photoelectric effect, the phenomenon of the dual nature of light was demonstrated. Explain what is meant by this phenomenon. What was the name of the scientist who demonstrated the dual nature of light using the photoelectric effect. Zumdahl and Zumdahl, 9th Edition, pp. 328. [3]

Answer:

Light exhibits both wave properties [1] and shows certain characteristics of particulate matter as well [1].

Albert Einstein demonstrated the dual nature of light using the photoelectric effect. [1]

Question 5 (20 marks)

(a) Predict the order of increasing electronegativity in each of the following groups of elements: [2]

- (i) Si, Ge, Sn

- $Sn < Ge < Si$
- (ii) **Tl, Cl, Ge**
 $Tl < Ge < Cl$
- (iii) **B, O, Ga**
 $Ga < B < O$
- (iv) **S, O, F**
 $S < O < F$
- (b) Identify the noble gas that has the same electron configuration as each of the ions in the following compounds: [3]
- (i) **Strontium fluoride**
 Strontium ion (Sr^{2+}) – Krypton
 Fluoride ion (F^-) – Neon
- (ii) **Calcium nitride**
 Calcium ion (Ca^{2+}) – Argon
 Nitride ion (N^{3-}) – Neon
- (iii) **Cesium bromide**
 Cesium ion (Cs^+) – Xenon
 Bromide ion (Br^-) – Krypton
- (c) Arrange the following atoms/ions in order of increasing size: [2]
- (i) **Ni²⁺, Pd²⁺, Pt²⁺**
 $Pt^{2+} > Pd^{2+} > Ni^{2+}$
- (ii) **Cu, Cu⁺, Cu²⁺**
 $Cu > Cu^+ > Cu^{2+}$
- (iii) **O, O⁻, O²⁻**
 $O^{2-} > O^- > O$
- (iv) **Cs⁺, K⁺, Rb⁺**
 $Cs^+ > Rb^+ > K^+$
- (d) Arrange the bonds in order of increasing ionic character in the molecules: LiF, K₂O, N₂, SO₂ and ClF₃. [1]
 $N_2 < SO_2 < ClF_3 < LiF < K_2O$
- (e) For each of the following molecules: PF₃ and COCl₂: [2]
- i) **Draw the Lewis Structure.**
- Structure for PF₃

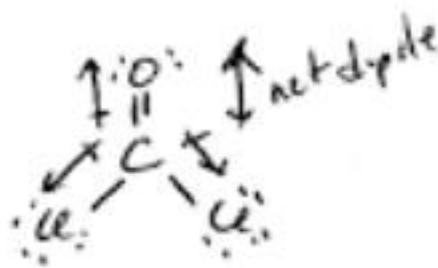
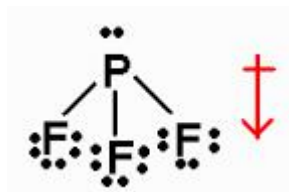
```

      ..      ..
      :F—P—F:
      ..      |
              :F:
              ..
          
```

Structure of COCl₂

```

      :O:
      ||
  :Cl—C—Cl:
      ..
          
```
- ii) **Determine the geometry of the molecule. [2]**
 PF₃: Trigonal pyramidal
 COCl₂: Trigonal planar
- iii) **Sketch the molecule to show the dipoles. [2]**
 For PF₃ For COCl₂



- iv) **Indicate if the molecule is polar or non polar. [1]**
PF₃: Polar
COCl₂: Polar
- v) **What intermolecular force exists in each of them? [1]**
Dispersion and dipole-dipole attraction forces in both molecules.
- vi) **Determine the number of lone pairs of electrons on each atom.[1]**
PF₃: one pair
COCl₂: zero pair
- (f) **Given the following molecules: C₂H₂, H₂, C(CH₃)₄, N₂.**
- i) **Identify the type of intermolecular force present in the compounds. [1]**
Dispersion forces/London forces/instantaneous dipole forces
- ii) **Are the compounds polar or non polar? [1]**
All the molecules are non polar
- iii) **Arrange the molecules in order of increasing intermolecular force. [1]**
H₂ < N₂ < C₂H₂ < C(CH₃)₄

Question 6 (20 marks)

- (a) Give the condensed structural formula and name of a hydrocarbon containing five carbon atoms that is
- | | | | | |
|---------------|--------------------|-----------------|----------------|-----|
| (i) an alkane | (ii) a cycloalkane | (iii) an alkene | (iv) an alkyne | [4] |
|---------------|--------------------|-----------------|----------------|-----|

- (i) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{CH}_3$ pentane (or any of its isomer 2-methylbutane, 2,2-dimethylpropane)

(ii)



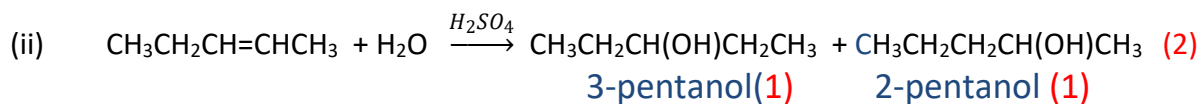
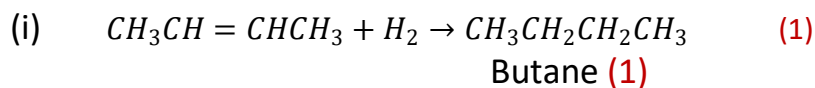
cyclopentane

- (iii) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}=\text{CH}_2$ 1-pentene or $\text{CH}_3\text{CH}_2\text{CH}=\text{CHCH}_3$ 2-pentene or an alkene derived from isomers of pentane see (i)
- (iv) $\text{CH}_3\text{CH}_2\text{CH}_2\text{C}\equiv\text{CH}$ 1-pentyne or $\text{CH}_3\text{CH}_2\text{C}\equiv\text{CCH}_3$ 2-pentyne or an alkene derived from isomers of pentane see (i)

½ mark for structural formula and ½ for correct name

- (b) Using condensed structural formulas, write a balanced chemical equations for each of the following reactions. In each case name the products.

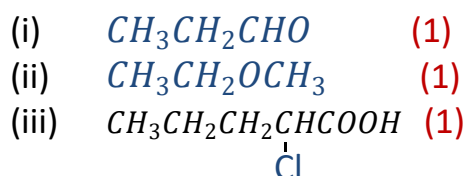
- (i) hydrogenation of 2-butene
 (ii) addition of H₂O to 2-pentene using H₂SO₄ as a catalyst (two products)



- (c) Give the condensed structural formula of

- (i) an aldehyde that is an isomer of acetone
 (ii) an ether that is an isomer of 1-propanol
 (iii) 2-chloro-pentanoic acid

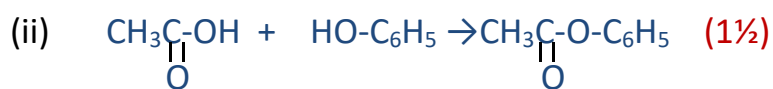
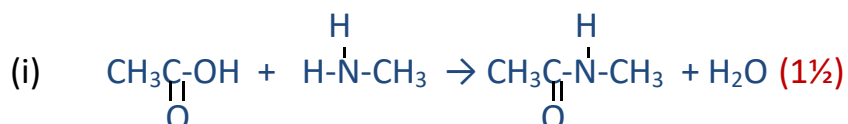
[3]



- (d) Draw the structural formula of the compound formed by the condensation reactions between

- (i) ethanoic acid and methylamine
 (ii) ethanoic acid and phenol

[3]



Question 7 (20 marks)

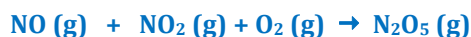
- (a) Given the following general reaction,



Write down the instantaneous rate for each of the reactants and products. [2]

$$-\frac{1}{3} \frac{\Delta[A]}{\Delta t} = -\frac{1}{2} \frac{\Delta[B]}{\Delta t} = \frac{1}{4} \frac{\Delta[C]}{\Delta t}$$

- (b) Study the following experimental data for the reaction below which was conducted at 25 °C and answer the questions below:



Run	[NO] ₀	[NO ₂] ₀	[O ₂] ₀	Initial Rate, Ms ⁻¹
1	0.10 M	0.10 M	0.10 M	2.1 x 10 ⁻²
2	0.20 M	0.10 M	0.10 M	4.2 x 10 ⁻²
3	0.20 M	0.30 M	0.20 M	1.26 x 10 ⁻¹
4	0.10 M	0.10 M	0.20 M	2.1 x 10 ⁻²

- (i) Deduce the order of reaction with respect to each reactant and determine the overall order of reaction. [6]

Using the initial rate method;

Comparing (dividing) run 1 and run 4, the order of reaction (a) with respect to (w.r.t) O₂ can be calculated as follows:

$$(0.1/0.2)^a = (2.1 \times 10^{-2})/(2.1 \times 10^{-2})$$

$$(0.5)^a = (1)^0$$

$$\text{Thus, } a = 0$$

The order of reaction w.r.t O₂ is 0. [1.5 marks]

For NO, compare run 1 and run 2 as follows,

$$(0.1/0.2)^b = (2.1 \times 10^{-2})/(4.2 \times 10^{-2})$$

$$(0.5)^b = (0.5)^1$$

$$\text{Thus, } b = 1$$

The order of reaction w.r.t NO is 1. [1.5 marks]

For NO₂, compare run 2 and run 3 as follows,

$$(0.1/0.3)^c \cdot (0.1/0.2)^a = (4.2 \times 10^{-2})/(1.26 \times 10^{-1})$$

$$\text{Since } a = 0,$$

$$(0.33)^c = (0.33)^1$$

$$\text{Thus, } c = 1$$

The order of reaction w.r.t NO₂ is 1. [1.5 marks]

The overall reaction order = 1 + 1 + 0 = 2 [1.5 marks]

- (ii) Write down an expression for the rate law for the above reaction and calculate the value of the rate constant for the reaction. [3]

$$\text{Rate} = k[\text{NO}] [\text{NO}_2] \quad [2 \text{ marks}]$$

To calculate the value of the rate constant k , plug in the values of $[\text{NO}]$ and $[\text{NO}_2]$ with their corresponding reaction rate for any run in the table above. Thus,

$$k(0.1)(0.1) = 2.1 \times 10^{-2}$$

$$k = 2.1 \text{ M}^{-1}\text{s}^{-1} \quad [1 \text{ mark}]$$

- (c) Derive an expression for the half life for a first order reaction and use this result to show that in a first order reaction the time taken for the reactant concentration to drop by three quarters of its initial value is double that for the initial concentration to drop by one half. [5]

$$\ln\left(\frac{[A]_0}{[A]_t}\right) = kt$$

$$\text{At } t = t_{1/2}, \quad [A]_t = \frac{[A]_0}{2}$$

The integrated rate law for $t = t_{1/2}$ becomes,

$$\ln\left(\frac{[A]_0}{[A]_0/2}\right) = kt_{1/2}$$

Therefore,

$$\ln(2) = kt_{1/2}$$

Replacing the value of $\ln(2)$ and then solving for $t_{1/2}$ gives the required equation for half life,

$$t_{1/2} = \frac{0.693}{k} \quad [3 \text{ marks}]$$

If the reactant concentration drops by three quarters, the remainder is 25 % (0.25). Thus,

$$\ln(0.25) = -kt$$

$$t_1 = 1.386/k$$

If the reactant concentration drops by one half, the remainder is 50 % (0.5).

Thus,

$$\ln(0.5) = -kt$$

$$t_2 = 0.693/k$$

Since the rate constant remains the same throughout,

$$t_1 = 2t_2 \text{ (Hence shown)} \quad [2 \text{ marks}]$$

- (d) Consider the reaction: $2\text{B} \rightarrow \text{C} + 3\text{D}$. In one experiment it was found that at 300 K the rate constant was 0.134 L/ (mol.s). A second experiment showed that at 450 K, the rate constant was 0.569 L/ (mol.s). Determine the activation energy for the reaction. [4]

$$\text{At } 300 \text{ K: } k_{300} = Ae^{\frac{-E_a}{RT}}$$

$$\text{At } 450 \text{ K: } k_{450} = Ae^{\frac{-E_a}{RT}}$$

$$\ln\left(\frac{k_{450}}{A}\right) = \frac{-E_a}{RT} \quad \text{where } \ln(A) = \ln(K_{300}) - \frac{-E_a}{RT}$$

So that,

$$\ln(k_{450}) - \left[\ln(k_{300}) - \frac{-E_a}{RT} \right] = \frac{-E_a}{RT}$$

$$\ln\left(\frac{k_{450}}{k_{300}}\right) = \frac{E_a}{R} \left(\frac{1}{T_{300}} - \frac{1}{T_{450}} \right)$$

Plugging and solving for E_a ,

$$\mathbf{E_a = 10.8 \, kJ} \quad \text{[4 marks]}$$