

Problem Set 7

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- a) Regress the variable *survived* on *female*. Report and interpret the estimated (marginal) “effect” of being female.

Table 1: OLS

	<i>Dependent variable:</i>
	survived
female	0.536*** (0.024)
Constant	0.191*** (0.014)
Observations	1,309
R ²	0.280
Adjusted R ²	0.279
Residual Std. Error	0.413 (df = 1307)
F Statistic	507.059*** (df = 1; 1307)
<i>Note:</i> *p<0.1; **p<0.05; ***p<0.01	

The dependent variable *survived* is a binary variable. We are thus in the binary outcome framework. In this question we perform an OLS regression of the *survived* variable on the *female* variable. The average survival rate was 0.191 (see Table 1) while a woman would survive with a probability $0.191 + 0.536 = 0.727$. Being a female increases your probability of survival by 0.536. As the *female* variable is binary, those numbers can be interpreted

as probabilities. The result is very significant, being a female on board dramatically increased your chances of survival.

- b) Construct a 95% confidence interval for the estimated (marginal) effect.**

Using the robust estimated variance we find a confidence interval at the 95% level for the estimated marginal effect equal to $[0.488, 0.585]$.

- c) Repeat (a) using the probit. What do you find ? Are you surprised ?**

Table 2: Probit Regression

	<i>Dependent variable:</i>
	survived
female	1.479*** (0.080)
Constant	−0.874*** (0.050)
Observations	1,309
Log Likelihood	−684.052
Akaike Inf. Crit.	1,372.103

Note: *p<0.1; **p<0.05; ***p<0.01

The coefficient of interest in the probit regression is $\beta = 1.479$ (see Table 2) which means that the marginal effect is positive which was expected, this is not the marginal effect however. Using the margins package, I find a marginal effect of 0.434. I do not find those results very surprising, it seems that the average marginal effect is lower than the one OLS came up with however.

- e) Continuing with the probit model from (c), add a numeric copy of the variable `pclass` to the “regression”. Interpret your results.

As in the previous question, we find a significant positive impact of being a female on board and a significant negative impact of the `pclass` variable (see Table 3). Using the library margins, I find a marginal effect of 0.406 for the female variable and -0.133 for the `pclass` variable. The intuition is clear, the `pclass` goes from 1 to 3 from the most expensive seat to the cheapest. Being in first class increased your chances of survival by a significant amount, but still less than being a female. Leonardo DiCaprio increased both coefficients in absolute value even though there was enough space on this little piece of wood...

Table 3: Probit Regression

	Dependent variable:
	survived
female	1.503*** (0.083)
pclass	-0.494*** (0.048)
Constant	0.245** (0.117)
Observations	1,309
Log Likelihood	-629.609
Akaike Inf. Crit.	1,265.218
Note: *p<0.1; **p<0.05; ***p<0.01	

- f) Instead of adding a numeric copy of the variable `pclass` to the regression in (c), add the variable `pclass` to it (`pclass` is coded as a “factor”). Interpret your results.

This time the model estimates two coefficients for two dummy variables, `pclass2` which is equal to 1 when the passenger is in second class, and similarly for `pclass3`. This regression adds information to the previous one as only

Table 4: Probit Regression

	<i>Dependent variable:</i>
	survived
female	1.503*** (0.083)
pclass2	−0.537*** (0.115)
pclass3	−0.994*** (0.097)
Constant	−0.236*** (0.083)
Observations	1,309
Log Likelihood	−629.527
Akaike Inf. Crit.	1,267.055
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

one coefficient was used to describe an incrementation in the *pclass* variable. Results are displayed in table 4. We see that, as expected, the cheaper the seat you bought, the less chances of survival you had. Using the library margins, I find a marginal effect of 0.406 for the female variable, -0.169 for the *pclass2* variable and -0.295 . It means that the impact from moving from first class to the third is about twice as bad as moving from first class to the second. Put otherwise, the effect of a one unit incrementation of the *pclass* variable seems constant.

- g) **The model in (e) constitutes a restricted version of the model in (f). What is the restriction? Test it using a LR test. What do you find?**

The model estimated in question (f) writes

$$survived = \phi(\alpha + \beta_1 female + \beta_2 pclass2 + \beta_3 pclass3)$$

while the model the model in question (e) imposes the restriction $\beta_3 = 2\beta_2$. Performing the LR test using the *lrtest* function from the *lmtest* package, we find that the number of interest is 0.16 derived from a $\chi^2(1)$ distribution under the null. This value is below the rejection threshold at the 10 % level, we cannot reject the null hypothesis.

- i) **Starting with your model specification in (e), add the variable *fare*. Use the Wald test and the LR test to test whether the coefficient on *fare* is equal to zero. What do you find?**

The LR does not reject the null as the outcome of the $\chi^2(1)$ distribution is 0.59 and is below the rejection threshold at the 10 % level meaning that the *fare* coefficient is not statistically different from 0. We see in table 5 that the coefficient is not significant at the 10 % level according to the Wald test automatically performed. Both tests fail to reject the null. Fare does not seem to have any impact on the survival rate on board.

- j) **Starting with your model specification in (e), add the variable *age*. Compute the partial effect of age for a female passenger in 1st class with “average” age.**

Denoting \bar{age} as the mean age of the population and denoting the model

$$survived = \phi(\alpha + \beta_1 female + \beta_2 pclass + \beta_3 age),$$

Table 5: Probit Regression

	<i>Dependent variable:</i>
	survived
female	1.494*** (0.084)
pclass	−0.470*** (0.057)
fare	0.001 (0.001)
Constant	0.169 (0.152)
Observations	1,308
Log Likelihood	−629.200
Akaike Inf. Crit.	1,266.399
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

Table 6: Probit Regression

	<i>Dependent variable:</i>
	survived
female	1.484*** (0.094)
pclass	−0.641*** (0.062)
age	−0.019*** (0.004)
Constant	1.160*** (0.215)
Observations	1,046
Log Likelihood	−492.797
Akaike Inf. Crit.	993.594
<i>Note:</i>	*p<0.1; **p<0.05; ***p<0.01

the partial marginal impact of age the partial marginal impact of interest is given by $\beta_3\phi(\alpha + \beta_1 + \beta_2 + \beta_3\bar{age})$ and we find -0.0176 .

- k) Using your model specification in (j), compute the average partial effect of age. What do you find?

Computing the average marginal effect using the prediction package, I find -0.007 .

- l) Using your model specification in (j), plot the sorted marginal effect of age. What do you find ?

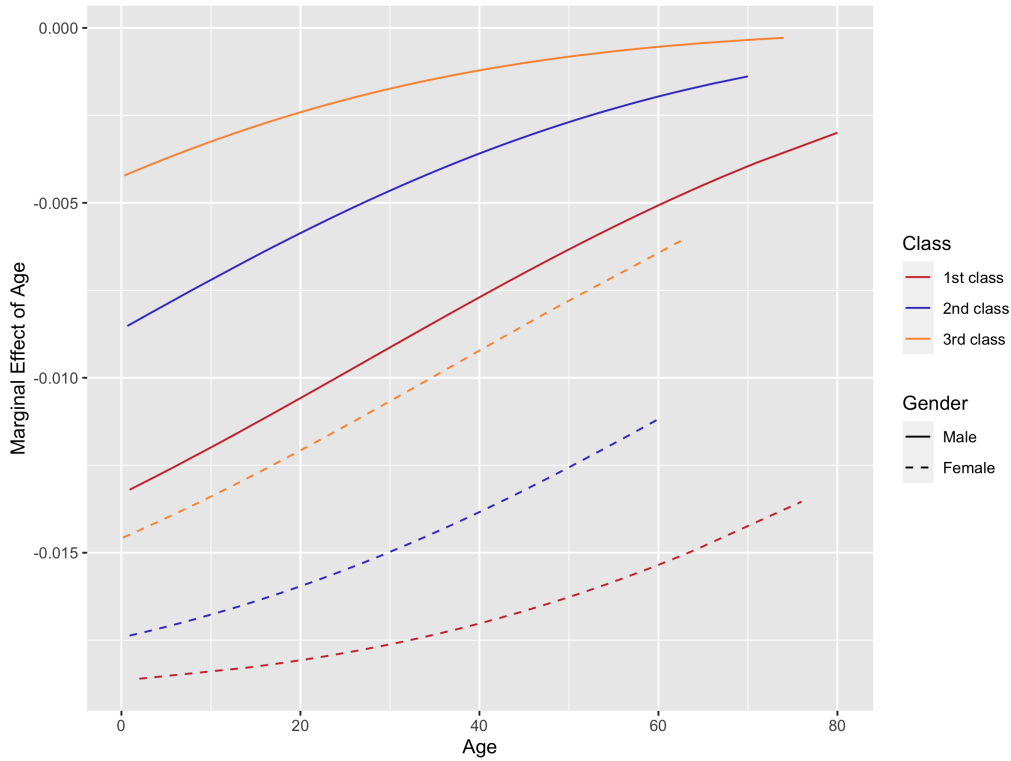


Figure 1: Marginal effect of Age per Class and Gender

We find that the marginal effect of the age on the survival rate is decreasing in absolute value for every subgroup of people.