Assignment 4 The Circumnavigations of Denver Long



Prof. Darrell Long CSE 13S – Spring 2021

Due: May 2nd at 11:59 pm

1 Introduction

I wonder why it is that when I plan a route too carefully, it goes to pieces, whereas if I blunder along in blissful ignorance aimed in a fancied direction I get through with no trouble.

—John Steinbeck, Travels with Charley: In Search of Amerca

Denver Long decides to augment his income during his retirement years by selling the fine products produced by the Shinola Corporation. He enjoys driving his Lincoln, and so it's the life of a traveling salesman for him. Having accidentally taken a wrong turn near Chula Vista and winding up in Mexico, he asks his son to have his class create a computer program that will provide an optimal route to all the cities along his route and then return him to his home in scenic Clearlake.

2 Directed Graphs

A graph is a data structure $G = \langle V, E \rangle$ where $V = \{v_0, ..., v_n\}$ is the set of vertices (or nodes) and $E = \{\langle v_i, v_j \rangle, ...\}$ is the set of edges that connect the vertices. For example, you might have a set of cities $V = \{\text{El Cajon}, \text{La Mesa}, \text{San Diego}, ..., \text{La Jolla}\}$ as the vertices and write "El Cajon" \rightarrow "Lakeside" to indicate that there is a path (Los Coches Road) from El Cajon to Lakeside. If there is a path from El Cajon to Lakeside, as well as a path from Lakeside to El Cajon, then the edge connecting El Cajon and Lakeside is undirected.

Such a simple graph representation simply tells you how vertices are connected and provides the idea of one-way roads. But it really does not help Denver, since it does not provide any notion of distance. We solve this problem by associating a weight with each edge and so we might write "Santee \rightarrow El Cajon, 2" to indicate that there is a path of two miles long from Santee to El Cajon. Given a set of edges and weights, then we can then find the shortest path from any vertex to any other vertex (the answer may be that there is no such path). There are elegant (and quick) algorithms for computing the shortest path, but that is not exactly what we want to do. We want to find a path through all of the vertices, visiting each *exactly once*, such that there is a direct (single step) connection from the last vertex to the first. This is called a *Hamiltonian path*. This will address Denver's need to get home, but won't necessarily be the shortest such path. So, we need to go through every possible Hamiltonian path given the list of cities Denver is traveling through and pick the shortest path. Note: if you find yourself on a path that is longer than the current best found Hamiltonian path, then you can preemptively reject your current path.

3 Representing Graphs

Nothing can be more limiting to the imagination than only writing about what you know.

-John W. Gardner

Perhaps the simplest way to represent a graph is with an *adjacency matrix*. Consider an $n \times n$ adjacency matrix M, where n is the number of vertices in the graph. If $M_{i,j} = k$, where $1 \le i \le j \le n$, then we say that there exists a *directed edge* from vertex i to vertex j with weight k. Traveling through wormholes is considered hazardous, so any valid edge weight k must be non-zero and positive.

	0	1	2	3	4	5	• • •	25
0	0]	10 0 0 0 0 0 0	0	0	0	0	0	0]
1	0	0	2	5	0	0	0	0
2	0	0	0	0	0	3	0	5
3	0	0	0	0	21	0	0	0
4	0	0	0	0	0	0	0	0
5	0	0	0	0	0	0	0	0
:	0	0	0	0	0	0	0	0
25	0	0	0	0	0	0	0	0

Each edge will be represented as a triplet (i, j, k). The set of edges in the adjacency matrix above is

$$E = \{\langle 0, 1, 10 \rangle, \langle 1, 2, 2 \rangle, \langle 1, 3, 5 \rangle, \langle 2, 5, 3 \rangle, \langle 2, 25, 5 \rangle, \langle 3, 4, 21 \rangle\}.$$

If the above adjacency matrix were made to be *undirected*, it would be reflected along the diagonal.

```
0
         1
                               25
            2
                3
                    4
                        5 ...
0
    0
        10 0
                        0
                0
                    0
                           0
                               0
1
        0
            2
                        0
                           0
                               0
    10
                    0
2
        2
    0
            0
                0
                    0
                      3
                           0
                               5
3
        5
            0
                0
                    21
                      0
                           0
                               0
     0
4
    0
        0 0
               21
                    0
                      0 0
                               0
5
    0
         0
            3
                0
                    0
                       0
                          0
                               0
            0
                0
                        0
                           0
                               0
    0
         0
                    0
25
   [ 0
            5
                0
                    0
                           0
                               0
```

We will create a graph ADT based on this struct definition:

We elect to use an adjacency matrix with set maximum dimensions. This is both to simplify the abstraction and also due to the computational complexity of solving the Traveling Salesman Problem (TSP) with depth-first search (DFS), which is discussed in §5. The VERTICES macro will be defined and supplied to you in vertices.h. In this header file, there is another macro START_VERTEX which defines the origin vertex of the shortest Hamiltonian path we will be searching for. You may not modify this file. The struct definition of a graph *must* go in graph.c. The following subsections define the interface for the graph ADT.

```
vertices.h

1 #ifndef __VERTICES_H__
2 #define __VERTICES_H__
3

4 #define START_VERTEX 0 // Starting (origin) vertex.
5 #define VERTICES 26 // Maximum vertices in graph.
6
7 #endif
```

3.1 Graph *graph_create(uint32_t vertices, bool undirected)

The constructor for a graph. It is through this constructor in which a graph can be specified to be undirected. Make sure each cell of the adjacency matrix, matrix, is set to zero. Also make sure that each index of the visited array is initialized as false to reflect that no vertex has been visited yet. The vertices field reflects the number of vertices in the graph.

3.2 void graph_delete(Graph **G)

The destructor for a graph. Remember to set the pointer G to NULL.

3.3 uint32_t graph_vertices(Graph *G)

Return the number of vertices in the graph.

Adds an edge of weight k from vertex i to vertex j. If the graph is undirected, add an edge, also with weight k from j to i. Return true if both vertices are within bounds and the edge(s) are successfully added and false otherwise.

3.5 bool graph_has_edge(Graph *G, uint32_t i, uint32_t j)

Return true if vertices i and j are within bounds and there exists an edge from i to j. Remember: an edge exists if it has a non-zero, positive weight. Return false otherwise.

3.6 uint32_t graph_edge_weight(Graph *G, uint32_t i, uint32_t j)

Return the weight of the edge from vertex i to vertex j. If either i or j aren't within bounds, or if an edge doesn't exist, return 0.

3.7 bool graph_visited(Graph *G, uint32_t v)

Return true if vertex v has been visited and false otherwise.

3.8 void graph_mark_visited(Graph *G, uint32_t v)

If vertex v is within bounds, mark v as visited.

3.9 void graph_mark_unvisited(Graph *G, uint32_t v)

If vertex v is within bounds, mark v as unvisited.

3.10 void graph_print(Graph *G)

A debug function you will want to write to make sure your graph ADT works as expected.

4 Depth-first Search

Again it might have been the American tendency in travel. One goes, not so much to see but to tell afterward.

—John Steinbeck, Travels with Charley: In Search of Amerca

We need a methodical procedure for searching through the graph. Once we have examined a vertex,

we do not want to do so again—we don't want Denver going through cities where he has already been (he has been known to wear out his welcome: charming women and fighting men).

Depth-first search (DFS) first marks the vertex v as having been visited, then it iterates through all of the edges $\langle v, w \rangle$, recursively calling itself starting at w if w has not already been visited.

```
1 procedure DFS(G,v):
2    label v as visited
3    for all edges from v to w in G.adjacentEdges(v) do
4        if vertex w is not labeled as visited then
5            recursively call DFS(G,w)
6    label v as unvisited
```

Finding a Hamiltonian path then reduces to:

- 1. Using DFS to find paths that pass through all vertices, and
- 2. There is an edge from the last vertex to the first. The solutions to the Traveling Salesman Problem are then the shortest found Hamiltonian paths.

5 Computational Complexity

Many a trip continues long after movement in time and space have ceased. I remember a man in Salinas who in his middle years traveled to Honolulu and back, and that journey continued for the rest of his life. We could watch him in his rocking chair on his front porch, his eyes squinted, half-closed, endlessly traveling to Honolulu.

-John Steinbeck, Travels with Charley: In Search of Amerca

How long will this take? The answer is, it will take a very long time if there are a large number of vertices. The running time of the simplest algorithm is O(n!) and there is no known algorithm that runs in less than $O(2^n)$ time. In fact, the TSP has been shown to be NP-hard, which means that it is as difficult as any problem in the class NP (you will learn more about this in CSE 104: Computability and Computational Complexity). Basically, it means that it can be solved in polynomial time if you have a magical computer that at each if-statement is takes both branches every time (creating a copy of the computer for each such branch).

6 Representing Paths

We find after years of struggle that we do not take a trip; a trip takes us.

—John Steinbeck, Travels with Charley: In Search of Amerca

Given that vertices are added to and removed from the traveled path in a stack-like manner, we decide to abstract a path as follows:

```
1 struct Path {
2   Stack *vertices; // The vertices comprising the path.
3   uint32_t length; // The total length of the path.
4 };
```

The following subsections define for the interface for the path ADT.

6.1 Path *path_create(void)

The constructor for a path. Set vertices as a freshly created stack that can hold up to VERTICES number of vertices. Initialize length to be 0. The length field will track the length of the path. In other words, it holds the sum of the edge weights between consecutive vertices in the vertices stack.

6.2 void path_delete(Path **p)

The destructor for a path. Remember to set the pointer p to NULL.

```
6.3 bool path_push_vertex(Path *p, uint32_t v, Graph *G)
```

Pushes vertex v onto path p. The length of the path is *increased* by the edge weight connecting the vertex at the top of the stack and v. Return true if the vertex was successfully pushed and false otherwise.

```
6.4 bool path_pop_vertex(Path *p, uint32_t *v, Graph *G)
```

Pops the vertices stack, passing the popped vertex back through the pointer v. The length of the path is *decreased* by the edge weight connecting the vertex at the top of the stack and the popped vertex. Return true if the vertex was successfully popped and false otherwise.

```
6.5 uint32_t path_vertices(Path *p)
```

Returns the number of vertices in the path.

```
6.6 uint32_t path_length(Path *p)
```

Returns the length of the path.

```
6.7 void path_copy(Path *dst, Path *src)
```

Assuming that the destination path dst is properly initialized, makes dst a copy of the source path src. This will require making a copy of the vertices stack as well as the length of the source path.

```
6.8 void path_print(Path *p, FILE *outfile, char *cities[])
```

Prints out a path to outfile using fprintf(). Requires a call to stack_print(), as defined in §7.10, in order to print out the contents of the vertices stack.

7 Stacks, Revisited

If you have some respect for people as they are, you can be more effective in helping them to become better than they are.

—John W. Gardner

You will use the stack that you implemented for assignment 3 with slight modifications. If there were any problems with your stack for that assignment, make sure to fix them for this assignment. Here is the modified stack interface for this assignment.

```
1 struct Stack {
2    uint32_t top;
3    uint32_t capacity;
4    uint32_t *items;
5 };
```

7.1 Stack *stack_create(uint32_t capacity)

The constructor function for a Stack. The top of a stack should be initialized to 0. The capacity of a stack is set to the specified capacity. The specified capacity also indicates the number of items to allocate memory for, the items in which are held in the dynamically allocated array items.

7.2 void stack_delete(Stack **s)

The destructor function for a stack. Remember to set the pointer s to NULL.

7.3 bool stack_empty(Stack *s)

Return true if the stack is empty and false otherwise.

7.4 bool stack_full(Stack *s)

Return true if the stack is full and false otherwise.

7.5 uint32_t stack_size(Stack *s)

Return the number of items in the stack.

7.6 bool stack_push(Stack *s, uint32_t x)

If the stack is full prior to pushing the item x, return false to indicate failure. Otherwise, push the item and return true to indicate success.

7.7 bool stack_peek(Stack *s, uint32_t *x)

Peeking into a stack is synonymous with querying a stack about the element at the top of the stack. If the stack is empty prior to peeking into it, return false to indicate failure.

```
7.8 bool stack_pop(Stack *s, uint32_t *x)
```

If the stack is empty prior to popping it, return false to indicate failure. Otherwise, pop the item, set the value in the memory x is pointing to as the popped item, and return true to indicate success.

```
7.9 void stack_copy(Stack *dst, Stack *src)
```

Assuming that the destination stack dst is properly initialized, make dst a copy of the source stack src. This means making the *contents* of dst->items the same as src->items. The top of dst should also match the top of src.

```
7.10 void stack_print(Stack *s, FILE *outfile, char *cities[])
```

Prints out the contents of the stack to outfile using fprintf(). Working through each vertex in the stack starting from the *bottom*, print out the name of the city each vertex corresponds to. This function will be given to aid you.

```
1 void stack_print(Stack *s, FILE *outfile, char *cities[]) {
2    for (uint32_t i = 0; i < s->top; i += 1) {
3        fprintf(outfile, "%s", cities[s->items[i]]);
4        if (i + 1 != s->top) {
5            fprintf(outfile, " -> ");
6            }
7        }
8        fprintf(outfile, "\n");
9    }
```

8 Command-line Options

Attitude is a choice. Happiness is a choice. Optimism is a choice. Kindness is a choice. Giving is a choice. Respect is a choice. Whatever choice you make makes you. Choose wisely.

-Roy T. Bennett, The Light in the Heart

Your program must support any combination of the following command-line options.

• -h: Prints out a help message describing the purpose of the graph and the command-line options it accepts, exiting the program afterwards. Refer to the reference program in the resources repo for an idea of what to print.

- -v: Enables verbose printing. If enabled, the program prints out *all* Hamiltonian paths found as well as the total number of recursive calls to dfs().
- -u: Specifies the graph to be undirected.
- -i infile: Specify the input file path containing the cities and edges of a graph. If not specified, the default input should be set as stdin.
- -o outfile: Specify the output file path to print to. If not specified, the default output should be set as stdout.

9 Reading An Input Graph

It behooves a man who wants to see wonders sometimes to go out of his way.

—John Mandeville, The Travels of Sir John Mandeville

We will be storing graphs in specially formatted files. Here is an example:

```
$ cat mythical.graph
4
Asgard
Elysium
Olympus
Shangri-La
0 3 5
3 2 4
2 1 10
1 0 2
```

The first line of a graph file is the number of vertices, or cities, in the graph. Assuming n is the number of vertices, the next n lines of the file are the names of the cities. Each line after that is an edge. It is to be scanned in as a triplet $\langle i, j, k \rangle$ and interpreted as an edge from vertex i to vertex j with weight k.

10 Specifics

The gladdest moment in human life, methinks, is a departure into unknown lands.

—Sir Richard Burton

Here are the specifics for your program implementation.

1. Parse command-line options with looped calls to getopt(). This should be familiar from assignments 2 and 3.

- 2. Scan in the first line from the input. This will be the number of vertices, or cities, that will be in the graph. Print an error if the number specified is greater than VERTICES, the macro defined in vertices.h.
- 3. Assuming the number of specified vertices is *n*, read the next *n* lines from the input using fgets(). Each line is the name of a city. Save the name of each city to an array. You will want to either make use of strdup() from <string.h> or implement your own strdup() function. If the line is malformed, print an error and exit the program. Note: using fgets() will leave in the newline character at the end, so you will manually have to change it to the null character to remove it.
- 4. Create a new graph G, making it undirected if specified.
- 5. Scan the input line by line using fscanf() until the end-of-file is reached. Add each edge to *G*. If the line is malformed, print an error and exit the program.
- 6. Create two paths. One will be for tracking the current traveled path and the other for tracking the shortest found path.
- 7. Starting from the origin vertex, defined by the macro START_VERTEX in vertices.h, perform a depth-first search on *G* to find the shortest Hamiltonian path. Here is an example function prototype that you may use as the recursive depth-first function:

The parameter v is the vertex that you are currently on. The currently traversed path is maintained with curr. The shortest found path is tracked with shortest. The array of city names is cities. Finally, outfile is the output to print to.

8. After the search, print out the length of the shortest path found, the path itself (remember to return back to the origin), and the number of calls to dfs().

```
$ ./tsp < mythical.graph
Path length: 21
Path: Asgard -> Shangri-La -> Olympus -> Elysium -> Asgard
Total recursive calls: 4
```

If the verbose command-line option was enabled, print out all the Hamiltonian paths that were found as well. It is recommended that you print out the paths as you find them.

```
$ ./tsp -v < ucsc.graph
Path length: 7
Path: Cowell -> Stevenson -> Merrill -> Cowell
Path length: 6
Path: Cowell -> Merrill -> Stevenson -> Cowell
Path length: 6
Path: Cowell -> Merrill -> Stevenson -> Cowell
Total recursive calls: 5
```

11 Deliverables

Travel isn't always pretty. It isn't always comfortable. Sometimes it hurts, it even breaks your heart. But that's okay. The journey changes you; it should change you. It leaves marks on your memory, on your consciousness, on your heart, and on your body. You take something with you. Hopefully, you leave something good behind.

—Anthony Bourdain

- 1. Your program, called tsp, *must* have the following source and header files:
 - vertices.h defines macros regarding vertices.
 - graph.h specifies the interface to the graph ADT.
 - graph.c implements the graph ADT.
 - stack.h specifies the interface to the stack ADT.
 - stack.c implements the stack ADT.
 - path.h specifies the interface to the path ADT.
 - path.c implements the path ADT.
 - tsp.c contains main() and *may* contain any other functions necessary to complete the assignment.

You can have other source and header files, but *do not try to be overly clever*. You may not modify any of the supplied header files.

- 2. Makefile: This is a file that will allow the grader to type make or make all to compile your program.
 - CC=clang must be specified.
 - CFLAGS=-Wall -Wextra -Werror -Wpedantic must be included.
 - make should build your program, as should make all.
 - make clean must remove all files that are compiler generated.
 - make format should format all your source code, including the header files.
- 3. Your code must pass scan-build cleanly.
- 4. README.md: This *must* be in *Markdown*. This must describe your program briefly, its usage, and how to build it using your Makefile.
- 5. DESIGN.pdf: This *must* be a PDF. The design document should contain answers to the pre-lab questions at the beginning and describe your design for your program with enough detail that a sufficiently knowledgeable programmer would be able to replicate your implementation. This does not mean copying your entire program in verbatim. You should instead describe how your program works with supporting pseudo-code.

12 Supplemental Readings

One of the reasons people stop learning is that they become less and less willing to risk failure. you learn, the more places you'll go.

-John W. Gardner

- The C Programming Language by Kernighan & Ritchie
 - Chapter 4 §4.10
 - Chapter 7 \$7.4-7.8
- Introduction to Algorithms by T. Cormen, C. Leiserson, R. Rivest, & C. Stein
 - Chapter 10 §10.1
 - Chapter 35 §35.2

13 Submission

A man who procrastinates in his choosing will inevitably have his choice made for him by circumstance.

—Hunter S. Thompson, The Proud Highway

Refer back to asgn0 for the steps on how to submit your assignment through git. Remember: *add, commit,* and *push*! Your assignment is turned in *only* after you have pushed *and* submitted the commit ID on Canvas. If you forget to push, you have not turned in your assignment and you will get a *zero*. "I forgot to push" is not a valid excuse. It is *highly* recommended to commit and push your changes *often*.



Fhewhqccydw yd S yi byau wylydw q cedauo q sxqydiqm.