
CBSE MATH

Made Simple

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Introduction

This book links high school coordinate geometry to linear algebra and matrix analysis through solved problems.

Chapter 1

Vectors

1.1. 2023

1.1.1 In what ratio, does x -axis divide the line segment joinin the points

$\mathbf{A}(3, 6)$ and $\mathbf{B}(-12, -3)$?

(a) $1 : 2$

(b) $1 : 4$

(c) $4 : 1$

(d) $2 : 1$

1.1.2 The distance between the point $(0, 2\sqrt{5})$ and $(-2\sqrt{5}, 0)$ is

(a) $2\sqrt{10}$ units

(b) $4\sqrt{10}$ units

(c) $2\sqrt{20}$ units

(d) 0 units

1.1.3 If $(-5, 3)$ and $(5, 3)$ are two vetices of an equilateral triangle, then co-ordinates of the third vertex, given that origin lies inside the triangle

(take $\sqrt{3} = 1.7$)

1.1.4 Show that the points $(-2, 3)$, $(8, 3)$ and $(6, 7)$ are the vertices of right-angled triangle

1.1.5 If $\mathbf{Q} = (0, 1)$ is equidistant from $\mathbf{P} = (5, -3)$ and $\mathbf{R} = (x, 6)$, find the value of x .

1.1.6 The distance of the point $(-6, 8)$ from origin is :

- (a) 6
- (b) -6
- (c) 8
- (d) 10

1.1.7 The points $(-4, 0)$, $(4, 0)$ and $(0, 3)$ are the vertices of a :

- (a) right triangle
- (b) isosceles triangle
- (c) equilateral triangle
- (d) scalene triangle

1.2. 2022

1.2.1. \vec{a} and \vec{b} are two unit vectors such that

$$\left| 2\vec{a} + 3\vec{b} \right| = \left| 3\vec{a} - 2\vec{b} \right|. \quad (1.2.1.1)$$

Find the angle between \vec{a} and \vec{b} .

1.2.2. If \vec{a} and \vec{b} are two vectors such that

$$\vec{a} = \hat{i} - \hat{j} + \hat{k} \quad (1.2.2.1)$$

and

$$\vec{b} = 2\hat{i} - \hat{j} - 3\hat{k} \quad (1.2.2.2)$$

then find the vector \vec{c} , given that

$$\vec{a} \times \vec{c} = \vec{b} \quad (1.2.2.3)$$

and

$$\vec{a} \cdot \vec{c} = 4. \quad (1.2.2.4)$$

1.2.3.

$$If \left| \vec{a} \times \vec{b} \right|^2 + \left| \vec{a} \cdot \vec{b} \right|^2 = 400 \quad (1.2.3.1)$$

and

$$\left| \vec{b} \right| = 5 \quad (1.2.3.2)$$

find the value of $|\vec{a}|$.

1.2.4. If

$$\vec{a} = \hat{i} + \hat{j} + \hat{k}, \vec{a} \cdot \vec{b} = 1 \quad (1.2.4.1)$$

and

$$\vec{a} \times \vec{b} = \hat{j} - \hat{k} \quad (1.2.4.2)$$

, then find $|\vec{b}|$

1.2.5. If

$$|\vec{a}| = 3, |\vec{b}| = 2\sqrt{3} \quad (1.2.5.1)$$

and

$$\vec{a} \cdot \vec{b} = 6, \quad (1.2.5.2)$$

then find the value of $|\vec{a} \times \vec{b}|$.

1.2.6. $|\vec{a}| = 8, |\vec{b}| = 3$ and $\vec{a} \cdot \vec{b} = 12\sqrt{3}$, then the value of $|\vec{a} \times \vec{b}|$ is

(a) 24

(b) 144

(c) 2

(d) 12

1.2.7. If

$$\vec{a} = 2\hat{i} + \hat{j} + 3\hat{k}, \hat{b} = -\hat{i} + 2\hat{j} + \hat{k} \quad (1.2.7.1)$$

and

$$\vec{c} = 3\hat{i} + \hat{j} + 2\hat{k} \quad (1.2.7.2)$$

, then find $\vec{a} \cdot (\vec{b} \times \vec{c})$.

1.2.8. $\vec{a}, \vec{b}, \vec{c}$ and \vec{d} are four non-zeros vectors such that $\vec{a} \times \vec{b} = \vec{c} \times \vec{d}$ and

$$\vec{a} \times \vec{c} = 4\vec{b} \times \vec{d} \quad (1.2.8.1)$$

, then show that $(\vec{a} - 2\vec{d})$ is parallel to $(2\vec{b} - \vec{c})$ where

$$\vec{a} \neq 2\vec{d}, \vec{c} \neq 2\vec{b} \quad (1.2.8.2)$$

1.2.9. If

$$\vec{a} = \hat{i} + \hat{j} + \hat{k}, \vec{a} \cdot \vec{b} = 1 \quad (1.2.9.1)$$

and

$$\vec{a} \times \vec{b} = \hat{j} - \hat{k}, \quad (1.2.9.2)$$

then find $\left| \vec{b} \right|$

1.2.10. If \vec{a} and \vec{b} are two vectors such that

$$\left| \vec{a} + \vec{b} \right| = \left| \vec{b} \right|, \quad (1.2.10.1)$$

then prove that $(\vec{a} + 2\vec{b})$ is perpendicular to \vec{a} .

1.2.11. If \vec{a} and \vec{b} are unit vectors and θ is the angle between them , then prove that \sin

$$\frac{\theta}{2} = \frac{1}{2} \left| \vec{a} - \vec{b} \right| \quad (1.2.11.1)$$

1.2.12. If \vec{a} and \vec{b} are two unit vectors such that and θ is the angle between them, then prove that

$$\sin \frac{\theta}{2} = \frac{1}{2} \left| \vec{a} - \vec{b} \right| \quad (1.2.12.1)$$

1.2.13. If

$$\vec{a} = 2\hat{i} + y\hat{j} + \hat{k} \quad (1.2.13.1)$$

and

$$\vec{b} = \hat{i} + 2\hat{j} + 3\hat{k} \quad (1.2.13.2)$$

are two vectors for which the vector $(\vec{a} + \vec{b})$ is perpendicular to the

vector $(\vec{a} - \vec{b})$ then find all the possible values of y .

1.2.14. Write the projection of the vector $(\vec{b} + \vec{c})$ on the vector \vec{a} , where

$$\vec{a} = 2\hat{i} - 2\hat{j} + \hat{k}, \vec{b} = \hat{i} + 2\hat{j} - 2\hat{k} \quad (1.2.14.1)$$

and

$$\vec{c} = 2\hat{i} - \hat{j} + 4\hat{k}. \quad (1.2.14.2)$$

1.2.15. If

$$\vec{a} = 2\hat{i} - \hat{j} + \hat{k}, \vec{b} = \hat{i} + \hat{j} - 2\hat{k} \quad (1.2.15.1)$$

and

$$\vec{c} = \hat{i} + 3\hat{j} - \hat{k} \quad (1.2.15.2)$$

and the projection of vector $\vec{c} + \lambda\vec{b}$ on vector \vec{a} is $2\sqrt{6}$, find the value of λ .

1.2.16. If $\vec{a} = 2\hat{i} + \hat{j} + 3\hat{k}, \vec{b} = -\hat{i} + 2\hat{j} + \hat{k}$ and

$$\vec{c} = 3\hat{i} + \hat{j} + 2\hat{k} \quad (1.2.16.1)$$

, then find $\vec{a} \cdot (\vec{b} \times \vec{c})$.

1.2.17. If

$$\vec{a} = 2\hat{i} - \hat{j} + 2\hat{k} \quad (1.2.17.1)$$

and

$$\vec{b} = 5\hat{i} - 3\hat{j} - 4\hat{k} \quad (1.2.17.2)$$

, then find the ratio $\frac{\text{projection of vector } \vec{a} \text{ on vector } \vec{b}}{\text{projection of vector } \vec{b} \text{ on vector } \vec{a}}$

1.2.18. Show that the three vectors $2\hat{i} - \hat{j} + \hat{k}$, $\hat{i} - 3\hat{j} - 5\hat{k}$, and $3\hat{i} - 4\hat{j} - 4\hat{k}$ form the vertices of a right-angled triangle. If $\vec{a} = 2\hat{i} + 2\hat{j} + 3\hat{k}$, $\vec{b} = -\hat{i} + 2\hat{j} + \hat{k}$ and

$$\vec{c} = 3\hat{i} + \hat{j} \quad (1.2.18.1)$$

are such that the vector $(\vec{a} + \lambda \vec{b})$ is perpendicular to vector \vec{c} , then find the value of λ .

1.2.19. If \vec{a} , \vec{b} and \vec{c} are the position vectors of the points $\mathbf{A}(2, 3, -4)$, $\mathbf{B}(3, -4, -5)$ and $\mathbf{C}(3, 2, -3)$ and respectively, then $|\vec{a} + \vec{b} + \vec{c}|$ is equal to

(a) $\sqrt{113}$

(b) $\sqrt{185}$

(c) $\sqrt{203}$

(d) $\sqrt{209}$

1.2.20. A circle has its center at $(4, 4)$. If one end of a diameter is $(4, 0)$, then find the coordinates of the other end.

1.2.21. Find the values λ , for which the distance of point $(2, 1, \lambda)$ from plane

$$3x + 5y + 4z = 11 \quad (1.2.21.1)$$

is $2\sqrt{2}$ units.

1.2.22. Find the coordinates of the point where the line through $(3, 4, 1)$ crosses the ZX-plane

1.2.23. Using vectors, find the area of the triangle with vertices $\mathbf{A}(-1, 0, -2)$, $\mathbf{B}(0, 2, 1)$ and $\mathbf{C}(-1, 4, 1)$

1.2.24. Using integration, find the area of triangle region whose vertices are $(2, 0)$, $(4, 5)$ and $(1, 4)$.

1.2.25. The distance between the points $(0, 0)$ and $(a - b, a + b)$ is

(a) $2\sqrt{ab}$

(b) $\sqrt{2a^2 + ab}$

(c) $2\sqrt{a^2 + b^2}$

(d) $\sqrt{2a^2 + 2b^2}$

1.2.26. The value of m which makes the point $(0, 0)$, $(2m, -4)$ and $(3, 6)$ collinear, is _____

1.2.27. If a line makes 60° and 45° angles with the positive directions of X-axis and z-axis respectively, then find the angle that it makes with the

positive direction of y-axis. Hence, write the direction cosines of the line.

1.2.28. The Cartesian equation of a line AB is :

$$\frac{2x-1}{12} = \frac{y+2}{2} = \frac{z-3}{3} \quad (1.2.28.1)$$

1.2.29. Find the direction cosines of a line parallel to line AB .

1.2.30. Find the direction cosines of a line whose cartesian equation is given as

$$3x + 1 = 6y - 2 = 1 - z. \quad (1.2.30.1)$$

1.2.31. A vector of magnitude 9 units in the direction of the vector $-2\hat{i} - \hat{j} + 2\hat{k}$ is _____

1.2.32. The two adjacent sides of a parallelogram are represented by $2\hat{i} - 4\hat{j} - 5\hat{k}$ and $\hat{i} + 2\hat{j} + 3\hat{k}$. Find the unit vectors parallel to its diagonals. Using the diagonal vectors, find the area of the parallelogram also.

1.2.33. The two adjacent sides of a parallelogram are represented by vectors $2\hat{i} - 4\hat{j} + 5\hat{k}$ and $\hat{i} - 2\hat{j} - 3\hat{k}$. Find the unit vector parallel to one of its diagonals. Also, find the area of the parallelogram.

1.2.34. If

$$\vec{a} = \vec{i} + 2\vec{j} + 3\vec{k} \quad (1.2.34.1)$$

and

$$\vec{b} = 2\hat{i} + 4\hat{j} - 5\hat{k} \quad (1.2.34.2)$$

represent two adjacent sides of a parallelogram, then find the unit vector parallel to the diagonal of the parallelogram

1.2.35. Find the area of the quadrilateral $ABCD$ whose vertices are $\mathbf{A}(-4, -3)$, $\mathbf{B}(3, -1)$, $\mathbf{C}(0, 5)$ and $\mathbf{D}(-4, 2)$

1.2.36. If the points $\mathbf{A}(2, 0)$, $\mathbf{B}(6, 1)$, and $\mathbf{C}(p, q)$ form a triangle of area 12sq. units (positive only) and

$$2p + q = 10, \quad (1.2.36.1)$$

then find the values of p and q .

Chapter 2

Linear Forms

2.1. 2022

2.1.1. Solve the equations $x + 2y = 6$ and $2x - 5y = 12$ graphically.

2.1.2. Solve the following equations for x and y using cross-multiplication method:

$$(ax - by) + (a + 4b) = 0 \quad (2.1.2.1)$$

$$(bx + ay) + (b - 4a) = 0 \quad (2.1.2.2)$$

2.1.3. Find the co-ordinates of the point where the line $\frac{x-3}{-1} = \frac{y+4}{1} = \frac{z+5}{6}$ crosses the plane passing through the points $\left(\frac{7}{2}, 0, 0\right), (0, 7, 0), (0, 0, 7)$.

2.1.4. Electrical transmission wires which are laid down in winters are stretched tightly to accommodate expansion in summers.

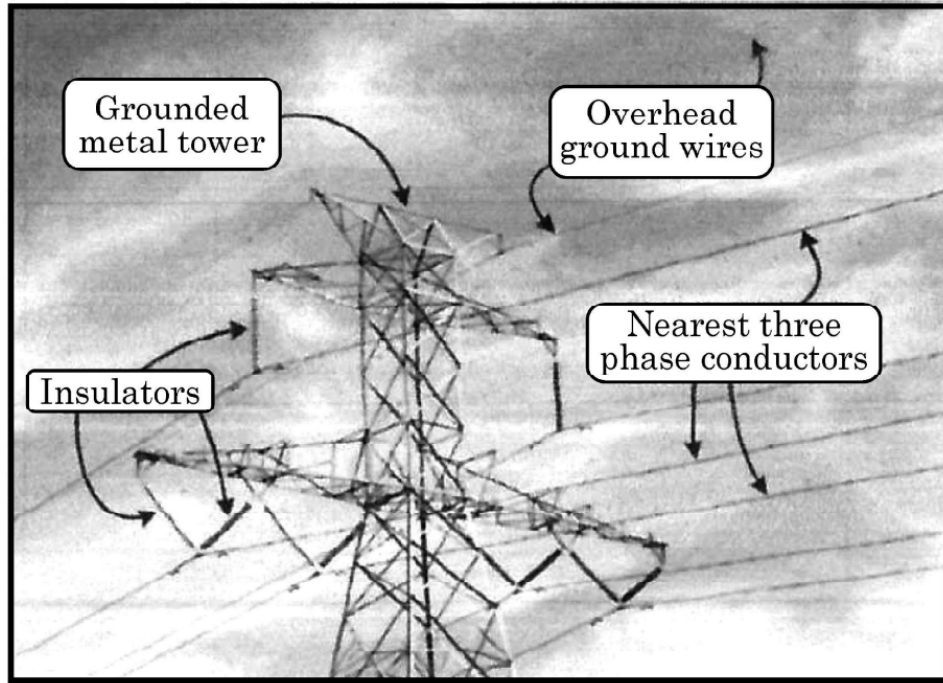


Figure 2.1.4.1: Electrical transmission wires connected to a transmission tower.

Two such wires in the figure 2.1.4.1 lie along the following lines:

$$l_1 : \frac{x+1}{3} = \frac{y-3}{-2} = \frac{z+2}{-1} \quad (2.1.4.1)$$

$$l_2 : \frac{x}{-1} = \frac{y-7}{3} = \frac{z+7}{-2} \quad (2.1.4.2)$$

Based on the given information, answer the following questions:

- (a) Are the l_1 and l_2 coplanar? Justify your answer.
- (b) Find the point of intersection of lines l_1 and l_2 .

2.1.5. Write the cartesian equation of the line PQ passing through points

P(2, 2, 1) and Q(5, 1, -2). Hence, find the y-coordinate of the point on the line PQ whose z-coordinate is -2.

2.1.6. Find the distance between the lines $x = \frac{y-1}{2} = \frac{z-2}{3}$ and $x+1 = \frac{y+2}{2} = \frac{z-1}{3}$.

2.1.7. Find the shortest distance between the following lines:

$$\mathbf{r} = 3\hat{i} + 5\hat{j} + 7\hat{k} + \lambda(\hat{i} - 2\hat{j} + \hat{k}) \quad (2.1.7.1)$$

$$\mathbf{r} = (-\hat{i} - \hat{j} - \hat{k}) + \mu(7\hat{i} - 6\hat{j} + \hat{k}) \quad (2.1.7.2)$$

2.1.8. Two motorcycles A and B are running at a speed more than the allowed speed on the road (as shown in figure 2.1.8.1) represented by the following lines

$$\mathbf{r} = \lambda(\hat{i} + 2\hat{j} - \hat{k}) \quad (2.1.8.1)$$

$$\mathbf{r} = (3\hat{i} + 3\hat{j}) + \mu(2\hat{i} + \hat{j} + \hat{k}) \quad (2.1.8.2)$$

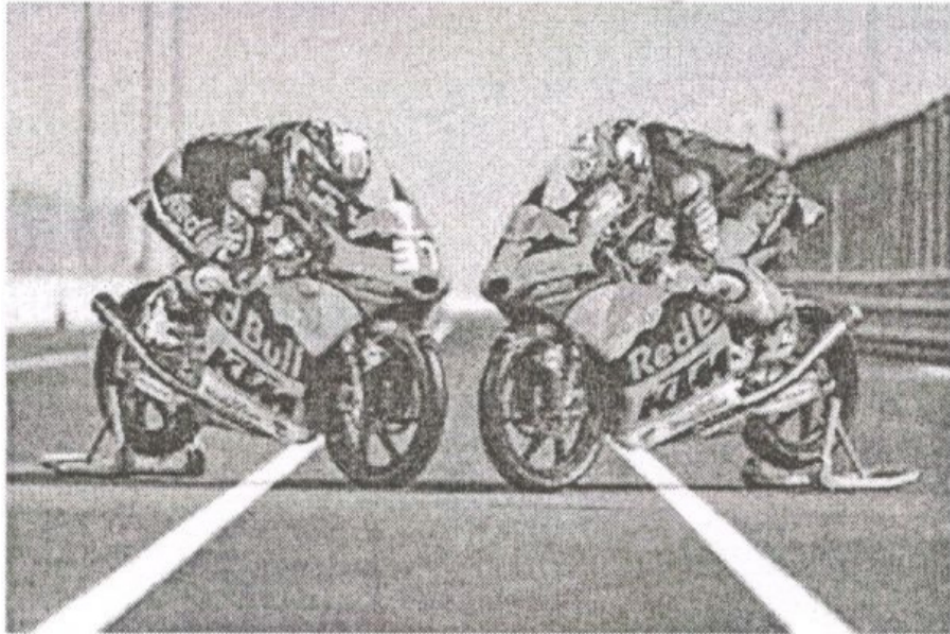


Figure 2.1.8.1: Two motorcycles moving along the road in a straight line.

Based on the following information, answer the following questions:

- (a) Find the shortest distance between the given lines.
- (b) Find a point at which the motorcycles may collide.

2.1.9. Find the shortest distance between the following lines

$$\mathbf{r} = (\lambda + 1)\hat{i} + (\lambda + 4)\hat{j} - (\lambda - 3)\hat{k} \quad (2.1.9.1)$$

$$\mathbf{r} = (3 - \mu)\hat{i} + (2\mu + 2)\hat{j} + (\mu + 6)\hat{k} \quad (2.1.9.2)$$

2.1.10. Find the shortest distance between the following lines and hence write

whether the lines are intersecting or not.

$$\frac{x-1}{2} = \frac{y+1}{3} = z, \frac{x+1}{5} = \frac{y-2}{1}, z = 2 \quad (2.1.10.1)$$

2.1.11. Find the equation of the plane passing through the points $(2, 1, 0)$, $(3, -2, -2)$ and $(1, 1, 7)$. Also, obtain its distance from the origin.

2.1.12. The foot of a perpendicular drawn from the point $(-2, -1, -3)$ on a plane is $(1, -3, 3)$. Find the equation of the plane.

2.1.13. Find the cartesian and the vector equation of a plane which passes through the point $(3, 2, 0)$ and contains the line $\frac{x-3}{1} = \frac{y-6}{5} = \frac{z-4}{4}$.

2.1.14. The distance between the planes $4x-4y+2z+5=0$ and $2x-2y+z+6=0$ is

- (a) $\frac{1}{6}$
- (b) $\frac{7}{6}$
- (c) $\frac{11}{6}$
- (d) $\frac{16}{6}$

2.1.15. Find the equation of the plane through the line of intersection of the planes

$$\mathbf{r} \cdot (\hat{i} + 3\hat{j}) + 6 = 0 \quad (2.1.15.1)$$

$$\mathbf{r} \cdot (3\hat{i} - \hat{j} - 4\hat{k}) = 0 \quad (2.1.15.2)$$

which is at a unit distance from the origin.

2.1.16. If the distance of the point $(1, 1, 1)$ from the plane $x - y + z + \lambda = 0$ is $\frac{5}{\sqrt{3}}$, find the value(s) of λ .

2.1.17. Find the distance of the point $(2, 3, 4)$ measured along the line $\frac{x-4}{3} = \frac{y+5}{6} = \frac{z+1}{2}$ from the plane $3x + 2y + 2z + 5 = 0$.

2.1.18. Find the distance of the point $P(4, 3, 2)$ from the plane determined by the points $A(-1, 6, -5)$, $B(-5, -2, 3)$ and $C(2, 4, -5)$.

2.1.19. The distance of the line

$$\mathbf{r} = (\hat{i} - \hat{j}) + \lambda(\hat{i} + 5\hat{j} + \hat{k}) \quad (2.1.19.1)$$

from the plane

$$\mathbf{r} \cdot (\hat{i} - \hat{j} + 4\hat{k}) = 5 \quad (2.1.19.2)$$

is

- (a) $\sqrt{2}$
- (b) $\frac{1}{\sqrt{2}}$
- (c) $\frac{1}{3\sqrt{2}}$
- (d) $\frac{-2}{3\sqrt{2}}$

2.1.20. Find a unit vector perpendicular to each of the vectors $(\mathbf{a} + \mathbf{b})$ and

$(\mathbf{a} - \mathbf{b})$ where

$$\mathbf{a} = \hat{i} + \hat{j} + \hat{k} \quad (2.1.20.1)$$

$$\mathbf{b} = \hat{i} + 2\hat{j} + 3\hat{k} \quad (2.1.20.2)$$

2.1.21. Find the distance of the point $(1, -2, 9)$ from the point of intersection of the line

$$\mathbf{r} = 4\hat{i} + 2\hat{j} + 7\hat{k} + \lambda(3\hat{i} + 4\hat{j} + 2\hat{k}) \quad (2.1.21.1)$$

and the plane

$$\mathbf{r} \cdot (\hat{i} - \hat{j} + \hat{k}) = 10. \quad (2.1.21.2)$$

2.1.22. Find the area bounded by the curves $y = |x - 1|$ and $y = 1$, using integration.

2.1.23. Find the coordinates of the point where the line through $(4, -3, -4)$ and $(3, -2, 2)$ crosses the plane $2x + y + z = 6$.

2.1.24. Fit a straight line trend by the method of least squares and find the trend value for the year 2008 using the data from Table 2.1.24.1:

Table 2.1.24.1: Table showing yearly trend of production of goods in lakh tonnes

Year	Production (in lakh tonnes)
2001	30
2002	35
2003	36
2004	32
2005	37
2006	40

Chapter 3

Intersection of Conics

3.1. 2022

3.1.1. Using integration, find the area of the region enclosed by the curve $y = x^2$, the x-axis and the ordinates $x = -2$ and $x = 1$.

3.1.2. Using integration, find the area of the region enclosed by line $y = \sqrt{3}x$ semi-circle $y = \sqrt{4 - x^2}$ and x-axis in first quadrant.

3.1.3. Using integration, find the area of the smaller region enclosed by the curve $4x^2 + 4y^2 = 9$ and the line $2x + 2y = 3$.

3.1.4. If the area of the region bounded by the curve $y^2 = 4ax$ and the line $x = 4a$ is $\frac{256}{3}$ sq. units, then using integration, find the value of a , where $a > 0$.

3.1.5. Find the area of the region enclosed by the curves $y^2 = x$, $x = \frac{1}{4}$, $y = 0$ and $x = 1$, using integration.

3.1.6. If the area of the region bounded by the line $y = mx$ and the curve $x^2 = y$ is $\frac{32}{3}$ sq. units, then find the positive value of m , using integration.

- 3.1.7. If the area between the curves $x = y^2$ and $x = 4$ is divided into two equal parts by the line $x = a$, then find the value of a , using integration.
- 3.1.8. Find the area bounded by the ellipse $x^2 + 4y^2 = 16$ and the ordinates $x = 0$ and $x = 2$, using integration.
- 3.1.9. Find the area of the region $\{(x, y) : x^2 \leq y \leq x\}$, using integration

Chapter 4

Tangent And Normal

4.1. 2022

4.1.1. Draw a circle of radius 2.5 cm. Take a point **P** outside the circle at a distance of 7 cm from the center. Then construct a pair of tangents to the circle from point **P**.

4.1.2. Write the steps of construction for constructing a pair of tangents to a circle of radius 4 cm from a point **P**, at a distance of 7 cm from its center **O**.

4.1.3. In Figure 4.1.3.1, there are two concentric circles with centre **O**. If ARC and AQB are tangents to the smaller circle from the point **A** lying on the larger circle, find the length of AC , if $AQ = 5$ cm.

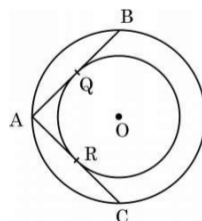


Figure 4.1.3.1: Two concentric circles with **O** as centre

- 4.1.4. In Figure 4.1.4.1, if a circle touches the side QR of $\triangle PQR$ at **S** and extended sides PQ and PR at **M** and **N**, respectively,

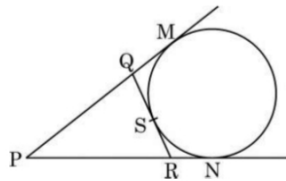


Figure 4.1.4.1: Two tangents are drawn from point **P** to the circle

prove that $PM = \frac{1}{2}(PQ + QR + PR)$

- 4.1.5. In Figure 4.1.5.1, a triangle ABC is drawn to circumscribe a circle of radius 4 cm such that the segments BD and DC into which BC is divided by the point of contact **D** are of lengths 6 cm and 8 cm respectively. If the area of $\triangle ABC$ is 84 cm^2 , find the lengths of sides AB and AC .

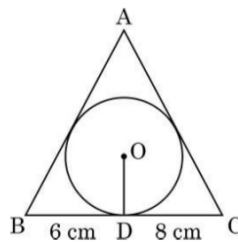


Figure 4.1.5.1: Circle with **O** as center circumscribed in triangle ABC

- 4.1.6. In Figure 4.1.6.1, PQ and PR are tangents to the circle centered at **O**. If $\angle OPR = 45^\circ$, then prove that $ORPQ$ is a square.

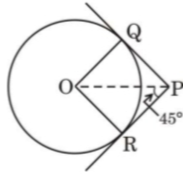


Figure 4.1.6.1: Two tangents drawn from point **P** to a circle whose centre is **O**

4.1.7. In Figure 4.1.7.1, **O** is the centre of a circle of radius 5 cm. PA and BC are tangents to the circle at **A** and **B** respectively. If OP is 13 cm, then find the length of tangents PA and BC .

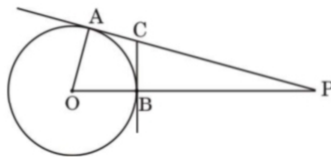


Figure 4.1.7.1: Two tangents drawn from point **C** to a circle whose centre is **O**

4.1.8. In Figure 4.1.8.1, AB is diameter of a circle centered at **O**. BC is tangent to the circle at **B. If OP bisects the chord AD and $\angle AOP = 60^\circ$, then find $m\angle C$.**

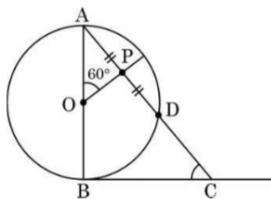


Figure 4.1.8.1: Tangent BC is drawn from point **C** to a circle whose centre is **O**

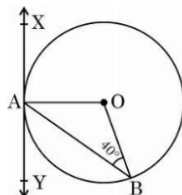


Figure 4.1.9.1: The line XAY is tangent to the circle centered at O

4.1.9. In Figure 4.1.9.1, XAY is a tangent to the circle centered at O . If $\angle ABO = 60^\circ$, then find $m\angle BAY$ and $m\angle AOB$.

4.1.10. Two concentric circles are of radii 4cm and 3 cm. Find the length of the chord of the larger circle which touches the smaller circle.

4.1.11. In Figure 4.1.11.1, a triangle ABC with $\angle B = 90^\circ$ is shown. Taking AB as diameter, a circle has been drawn intersecting AC at point P . Prove that the tangent drawn at point P bisects BC .

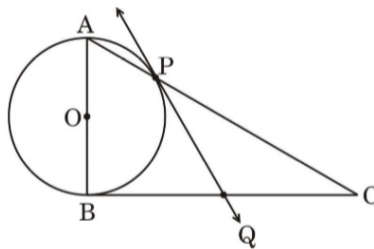


Figure 4.1.11.1: PQ is tangent to the circle centered at O . AB is the diameter and $\angle B = 90^\circ$

4.1.12. Find the equation of tangent to the curve $y = x^2 + 4x + 1$ at the point $(3, 22)$.

Chapter 5

Probability

5.1. 2022

5.2. 2023

5.2.1. Probability of happening of an event is denoted by p and probability of non-happening of the event is denoted by q . Relation between p and q is

(a) $p+q=1$

(b) $p=1, q=1$

(c) $p=q-1$

(d) $p+q+1=0$

5.2.2. A girl calculates that the probability of her winning the first prize in a lottery is 0.08. If 6000 tickets are sold, how many tickets has she bought ?

(a) 40

(b) 240

(c) 480

(d) 750

5.2.3. In a group of 20 people, 5 can't swim. If one person is selected at random, then the probability that he/sh can swim, is

(a) $\frac{3}{4}$

(b) $\frac{1}{3}$

(c) 1

(d) $\frac{1}{4}$

5.2.4. A bag contain 4 red, 3 blue and 2 yellow balls. One ball is drawn at random from the bag. Find the probability that drawn ball is

(a) red

(b) yellow

5.2.5. A bag contain 100 cards numbered 1 to 100. A card is drawn at random from the bag. What is the probability that the number on the card is a perfect cube ?

(a) $\frac{1}{20}$

(b) $\frac{3}{50}$

(c) $\frac{1}{25}$

(d) $\frac{7}{100}$

5.2.6. If three coins are tossed simultaneously, what is the probability of getting a most one trail ?

(a) $\frac{3}{8}$

(b) $\frac{4}{8}$

(c) $\frac{5}{8}$

(d) $\frac{7}{8}$

5.2.7. Two dics are thrown together. The probability of getting the difference of numbers on their upper faces equals to 3 is :

(a) $\frac{1}{9}$

(b) $\frac{2}{9}$

(c) $\frac{1}{6}$

(d) $\frac{1}{12}$

5.2.8. A card is drawn at random from a well-shuffled pack of 52 cards. The probability that the card drawn is not an ace is :

(a) $\frac{1}{13}$

(b) $\frac{9}{13}$

(c) $\frac{4}{13}$

(d) $\frac{12}{13}$

5.2.9. **Assertion (A) :** The probability that a leap year has 53 Students is $\frac{2}{7}$.

Reason (R) : The probability that a non-leap year has 53 Sundays is $\frac{5}{7}$.

- (a) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
- (b) Both Assertion (A) and Reason (R) are true and Reason (R) is not the correct explanation of Assertion (A).
- (c) Assertion (A) is true but Reason (R) is false.
- (d) Assertion (A) is false but Reason (R) is true.

Chapter 6

Construction

6.1. 2022

