Week 4(1/3)

Perceptron

Machine Learning with Python

Handong Global University Prof. Youngsup Kim idebtor@gmail.com

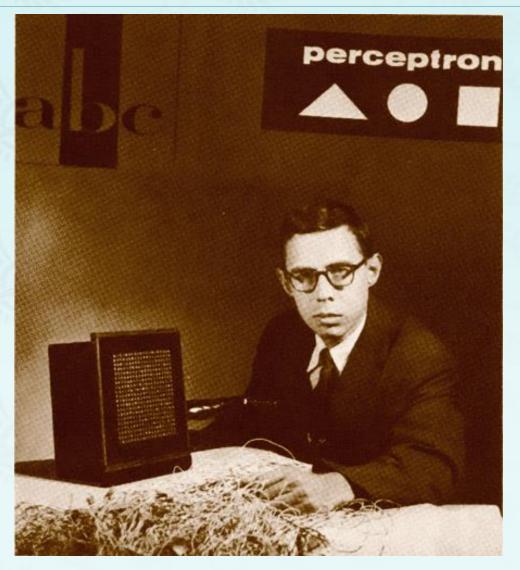
Perceptron

Goals

Understanding Perceptron

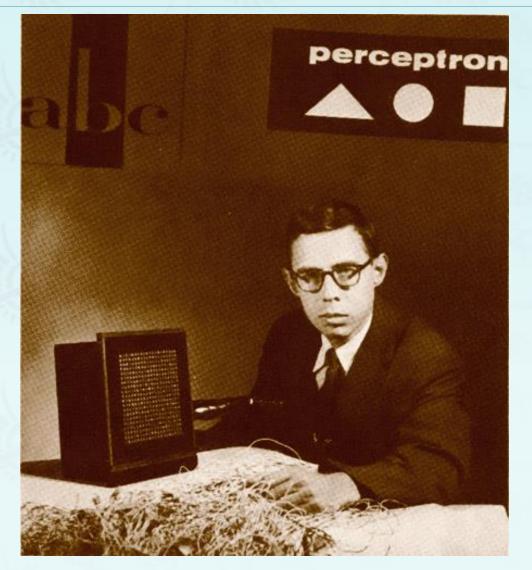
Content

- Perceptron Overview
- Perceptron Binary Classification
- Perceptron Learning
- Overfitting and Underfitting



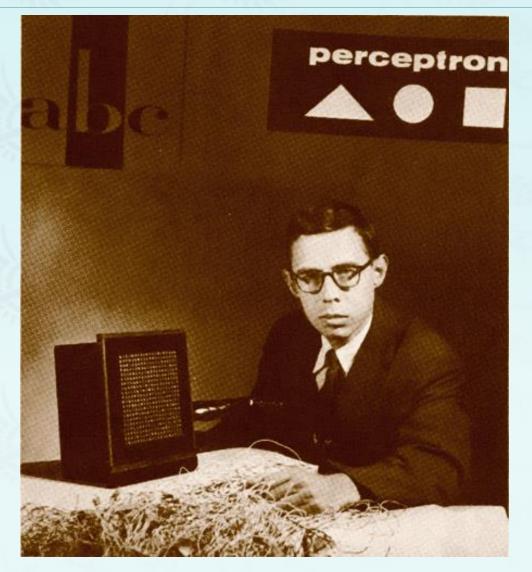
Frank Rosenblatt(출처: Arvin Calspan Advanced Technology Center; Hecht-Nielsen, R. Neurocomputing)

- Artificial Neuron → Neuron, Node, Perceptron
- Perceptron → The First Artificial Neural Network
 - Frank Rosenblatt, 1957
 - Cornell Aeronautical Laboratory



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마크 1 퍼셉트론 (출처: Arvin Calspan Advanced Technology Center; Hecht-Nielsen, R. Neurocomputing)

ARCHIVES

NEW NAVY DEVICE LEARNS BY DOING; Psychologist Shows Embryo of Computer Designed to Read and Grow Wiser

JULY 8, 1958











WASHINGTON, July 7 (UPI) -- The Navy revealed the embryo of an electronic computer today that it expects will be able to walk, talk, see, write, reproduce itself and be conscious of its existence.

ARCHIVES

1958

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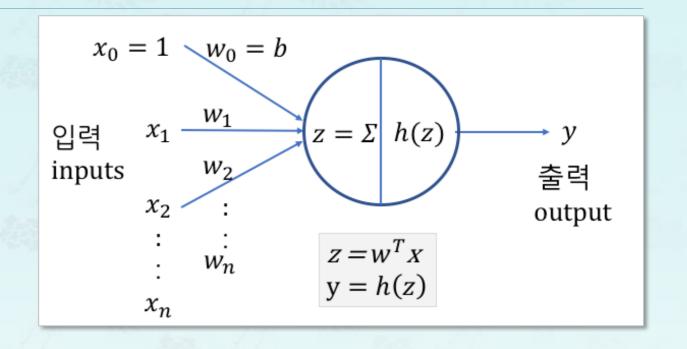




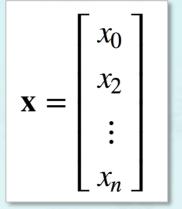


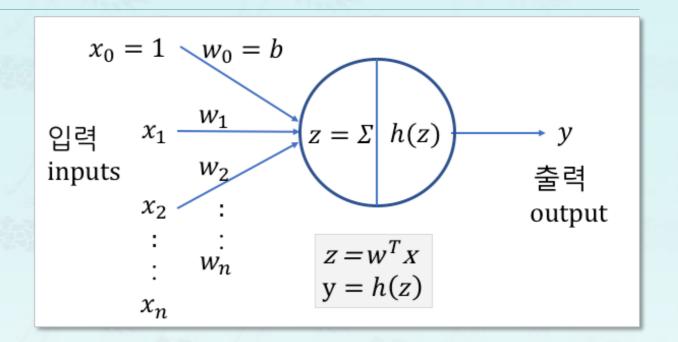


WASHINGTON, July 7 (UPI) -- The Navy revealed the embryo of an electronic computer today that it expects will be able to walk, talk, see, write, reproduce itself and be conscious of its existence.



input x



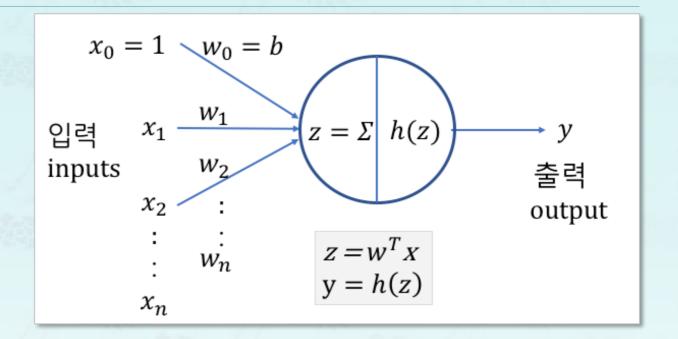


input x

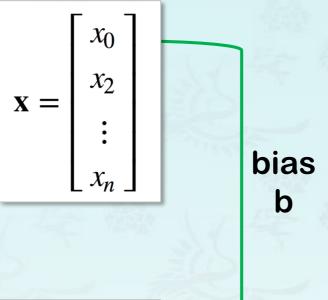
$$\mathbf{x} = \begin{bmatrix} x_0 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

weight w

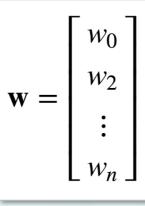
$$\mathbf{w} = \begin{bmatrix} w_0 \\ w_2 \\ \vdots \\ w_n \end{bmatrix}$$

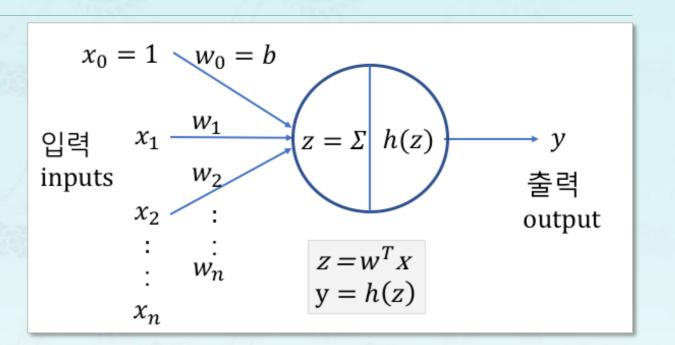


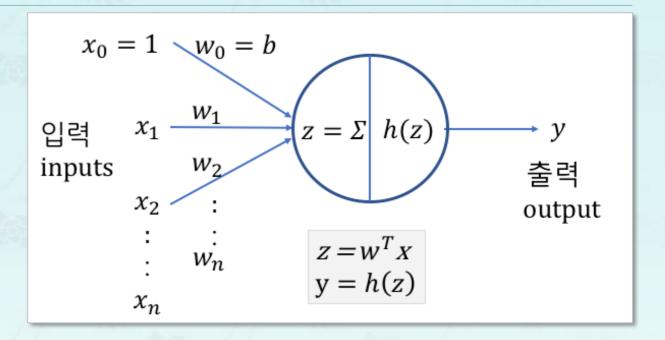
input x



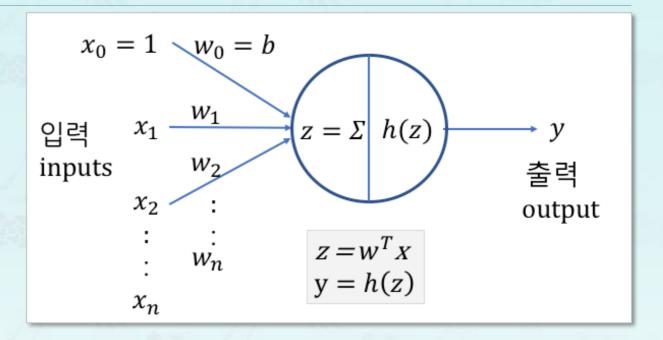
weight w



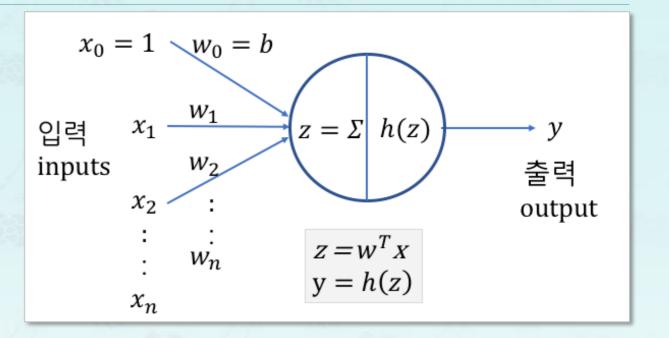




$$z = w_0 x_0 + w_1 w_1 + ... + w_n x_n$$



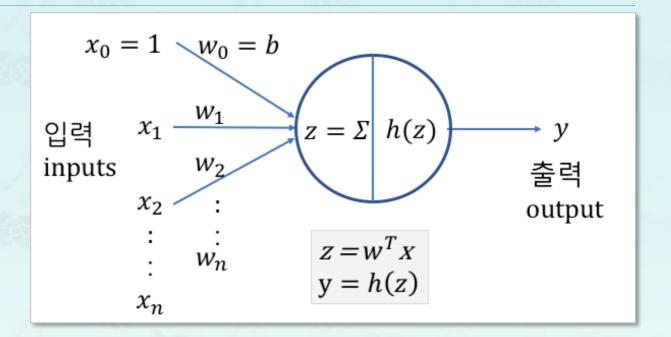
$$z = w_0 x_0 + w_1 w_1 + \dots + w_n x_n$$
$$= \sum_{j=0}^{n} x_j w_j$$



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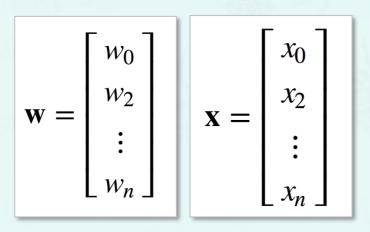
$$= \mathbf{w}^T \mathbf{x}$$

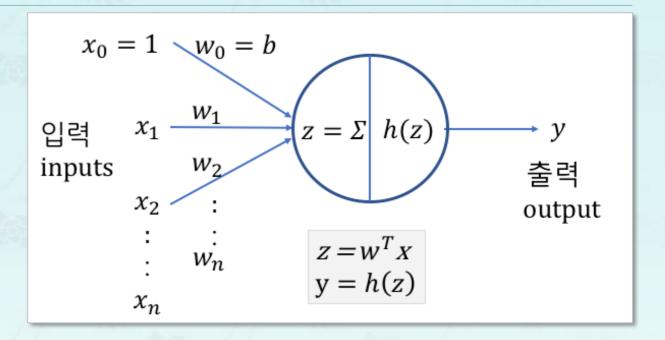


$$z = w_0 x_0 + w_1 w_1 + \dots + w_n x_n$$

$$= \sum_{j=0}^{n} x_j w_j$$

$$= \mathbf{w}^T \mathbf{x}$$





- net input z example:
 - 1. input x = [0, 1, 2, 3]
 - 2. weight w = [0..1]
 - 3. Compute net input z.

```
x = np.array([0, 1, 2, 3])
w = np.array([0, 0.1, 0.2, 0.3])
z = np.dot(x, w)
print(z)

Solution(1)
```

- net input z example:
 - 1. input x = [0, 1, 2, 3]
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Solution(1)
```

- net input z example:
 - 1. input x = [0, 1, 2, 3]
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```
import numpy as np
x = np.array(np.arange(4))
w = np.array(np.random.random(4))
z = np.dot(w, x)
print(z)

1.329056653793057 Solution(2)
```

net input z

$$z = w_0 x_0 + w_1 w_1 + \dots + w_n x_n$$
$$= \sum_{j=0}^{n} x_j w_j$$
$$= \mathbf{w}^T \mathbf{x}$$

- 1. input x = [0, 1, 2, 3]
- 2. weight w = [0..1]
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- Thoughts on Solution(2):

```
import numpy as np
x = np.array(np.arange(4))
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1.329056653793057 Solution(2)
```

Solution(2)

net input z

1.329056653793057

$$z = w_0 x_0 + w_1 w_1 + \dots + w_n x_n$$

$$= \sum_{j=0}^{n} x_j w_j$$

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- 3. Compute net input z.
- Thoughts on Solution(2):

```
import numpy as np
x = np.array(np.arange(4))
w = np.array(np.random.random(4))
z = np.dot(w.T, x)
print(z)

1.4781818847304011 Solution(3)
```

net input z

$$z = w_0 x_0 + w_1 w_1 + \dots + w_n x_n$$
$$= \sum_{j=0}^{n} x_j w_j$$
$$= \mathbf{w}^T \mathbf{x}$$

import numpy as np np.random.seed(0) x = np.array(np.arange(4)) w = np.array(np.random.random(4)) z = np.dot(w, x) print(z)

3.5553656675063983 Solution(2A)

- 1. input x = [0, 1, 2, 3]
- 2. weight w = [0..1]
- 3. Compute net input z.
- Thoughts on Solution(2):

```
import numpy as np
np.random.seed(0)
x = np.array(np.arange(4))
w = np.array(np.random.random(4))
z = np.dot(w.T, x)
print(z)

3.5553656675063983 Solution(3A)
```

net input z

$$z = w_0 x_0 + w_1 w_1 + \dots + w_n x_n$$

$$= \sum_{j=0}^{n} x_j w_j$$

$$= \mathbf{w}^T \mathbf{x}$$

net input z example:

- 1. input x = [0, 1, 2, 3]
- 2. weight w = [0..1]
- 3. Compute net input z.
- Thoughts on Solution(2):

```
print('x.shape={}, w.shape{}, w.T.shape{}'.
    format(x.shape, w.shape, w.T.shape))
```

x.shape=(4,), w.shape(4,), w.T.shape(4,)

- •

net input z

$$z = w_0 x_0 + w_1 w_1 + \dots + w_n x_n$$

$$= \sum_{j=0}^{n} x_j w_j$$

$$= \mathbf{w}^T \mathbf{x}$$

net input z example:

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print('x.shape={}, w.shape{}, w.T.shape{}'.
    format(x.shape, w.shape, w.T.shape))
```

x.shape=(4,), w.shape(4,), w.T.shape(4,)

- •

- input x, w:
 - row vector(행 벡터)
 - shape n x 1 or (n, 1)

$$\mathbf{x} = \begin{bmatrix} x_0 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} \quad \mathbf{w}$$

$$\mathbf{w} = \begin{bmatrix} w_0 \\ w_2 \\ \vdots \\ w_n \end{bmatrix}$$

- net input z example:
 - 1. input x = [0, 1, 2, 3]
 - 2. weight w = [0..1]
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- Thoughts on Solution(2):

- input x, w:
 - row vector(행 벡터)
 - shape n x 1 or (n, 1)

$$\mathbf{x} = \begin{bmatrix} x_0 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

$$\mathbf{w} = \begin{bmatrix} w_0 \\ w_2 \\ \vdots \\ w_n \end{bmatrix}$$

- 1. input x = [0, 1, 2, 3]
- 2. weight w = [0..1]
- 3. Compute net input z.
- Thoughts on Solution(2):

```
np.random.seed(0)
x = np.array(np.arange(4)).reshape(4,1)
w = np.array(np.random.random(4)).reshape(4,1)
z = np.dot(w.T, x) #.random((4,1)) is OK!
print(z)
[[3.55536567]]
```

```
print(x)
print(w.T)
print(z)
print('shapes: x{}, w{}, w.T{}, z{}'.
  format(x.shape, w.shape, w.T.shape, z.shape))
[[0]]
[[0.5488135  0.71518937  0.60276338  0.54488318]]
[[3.55536567]]
shapes: x(4, 1), w(4, 1), w.T(1, 4), z(1, 1)
```

```
print(x)
print(w.T)
print(z)
print('shapes: x{}, w{}, w.T{}, z{}'.
  format(x.shape, w.shape, w.T.shape, z.shape))
[[0]]
 [1]
[[0.5488135  0.71518937  0.60276338  0.54488318]]
[[3.55536567]]
shapes: x(4, 1), w(4, 1), w.T(1, 4), z(1, 1)
```



```
print(x)
print(w.T)
print(z)
print('shapes: x{}, w{}, w.T{}, z{}'.
  format(x.shape, w.shape, w.T.shape, z.shape))
[[0]]
 [1]
 [2]
[[0.5488135  0.71518937  0.60276338  0.54488318]]
[[3.55536567]]
shapes: x(4, 1), w(4, 1), w.T(1, 4), z(1, 1)
```



```
print(x)
print(w.T)
print(z)
print('shapes: x{}, w{}, w.T{}, z{}'.
  format(x.shape, w.shape, w.T.shape, z.shape))
[[0]]
 [1]
 [2]
 [3]]
[[0.5488135  0.71518937  0.60276338  0.54488318]]
[[3.55536567]]
shapes: x(4, 1), w(4, 1), w.T(1, 4), z(1, 1)
```



```
z = np.dot(w.T, x).squeeze()
print(z)
```

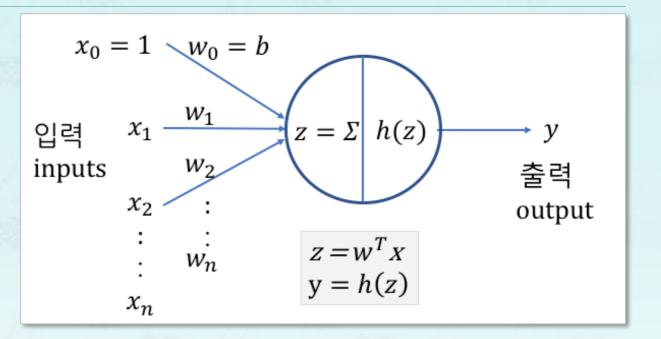
3.555365667506398

3. Perceptron Binary Classification

- Binary classification
- Linear binary classifier

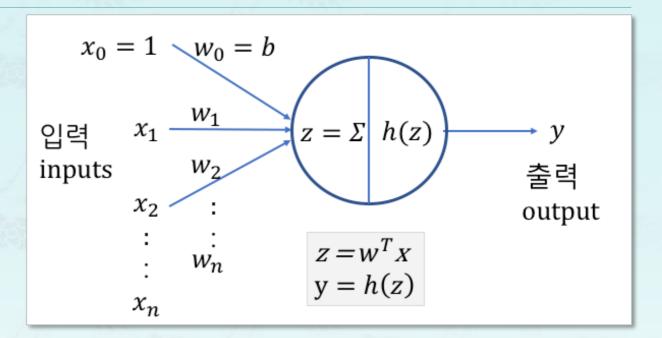
3. Perceptron Binary Classification

- input
- weight
- **?**



3. Perceptron Binary Classification

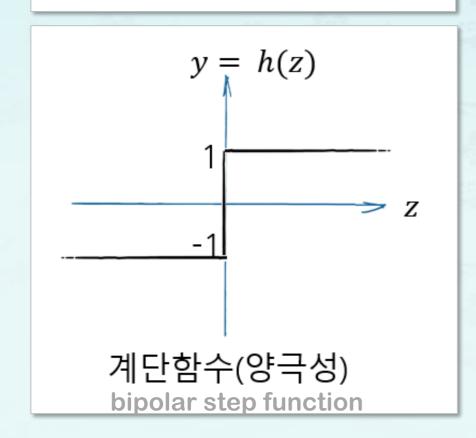
- input
- weight
- Activation Function
 - Sigmoid Function
 - Step Function
 - tanh Function
 - ReLU Function



3. Perceptron Binary Classification

 Activation Function for Binary Classification

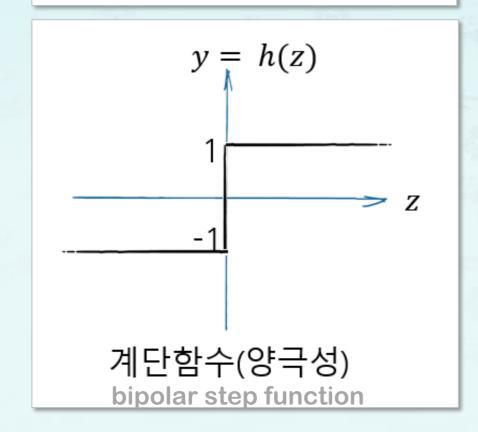
$$h(z) = \begin{cases} +1 & if \ z > 0 \\ -1 & otherwise. \end{cases}$$

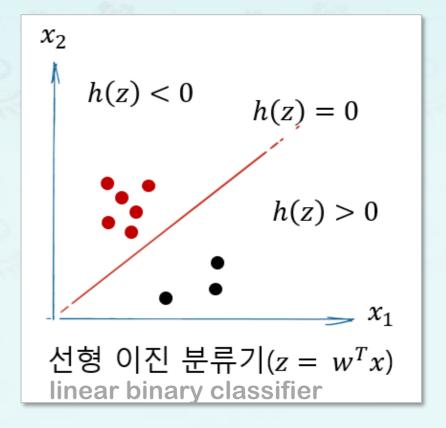


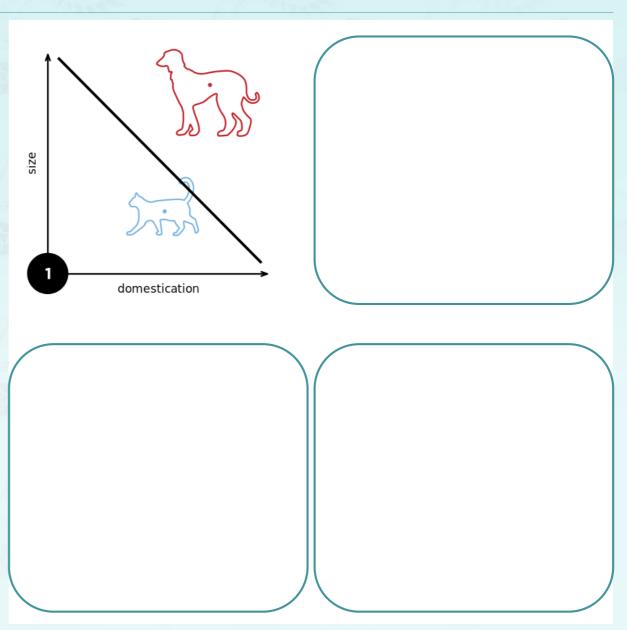
3. Perceptron Binary Classification

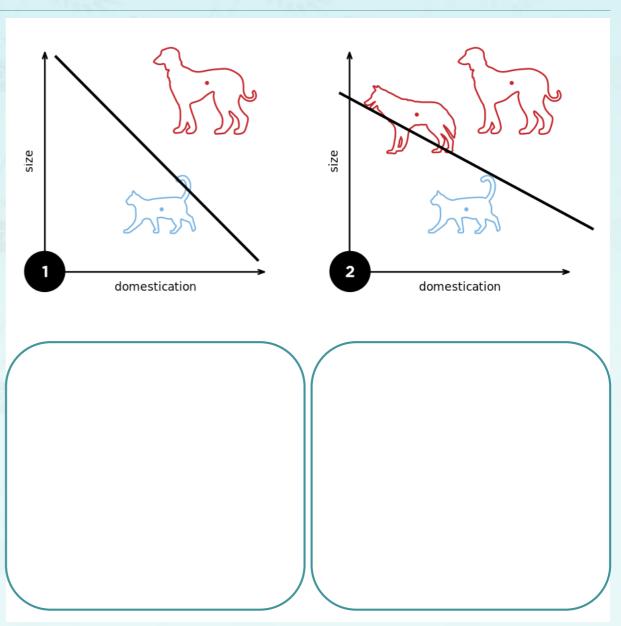
 Activation Function for Binary Classification

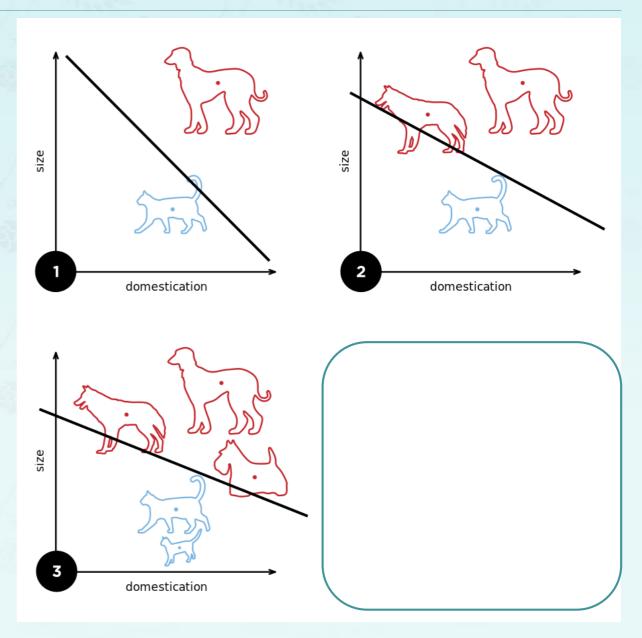
$$h(z) = \begin{cases} +1 & if \ z > 0 \\ -1 & otherwise. \end{cases}$$

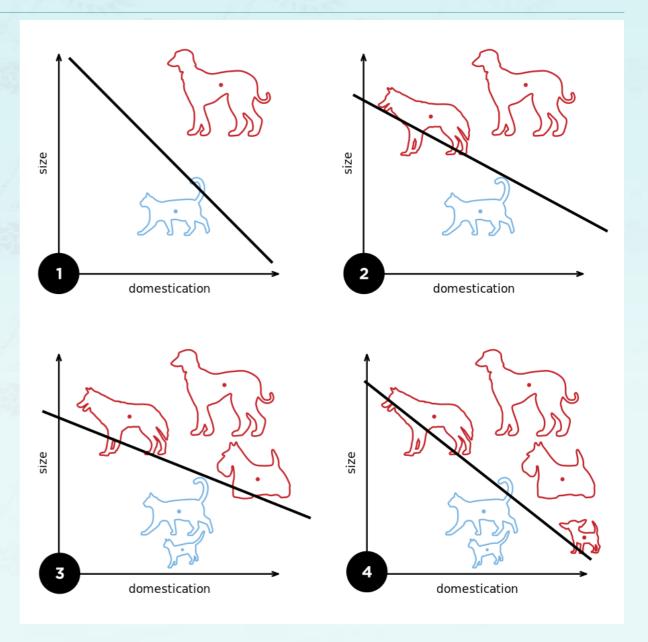












Perfect Perceptron?

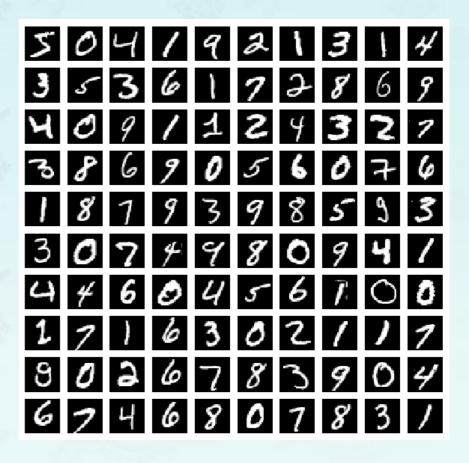
Perfect Perceptron?

Training Data:

Label:

5041921314 3536172869 4091...

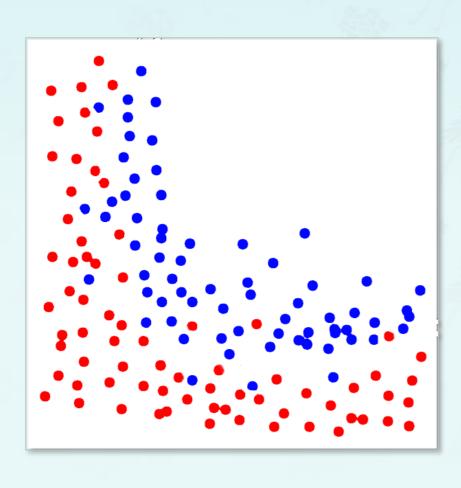
• • •

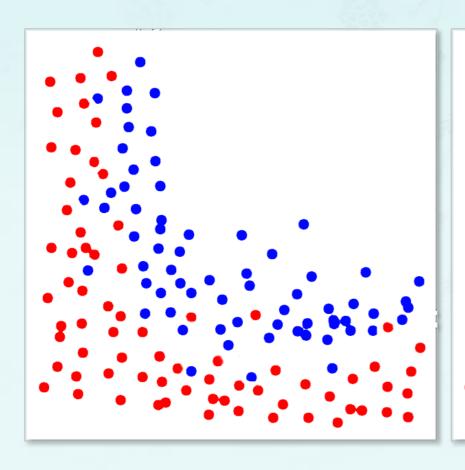


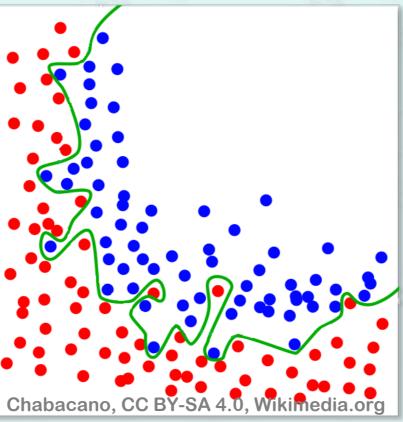


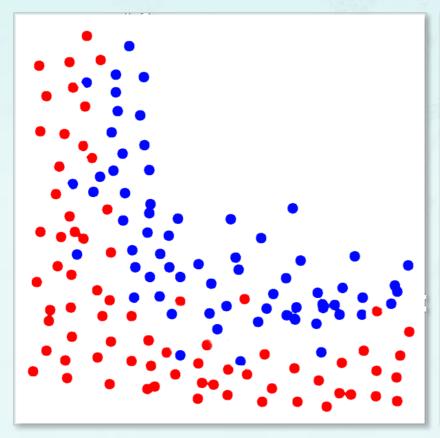
Test Data:

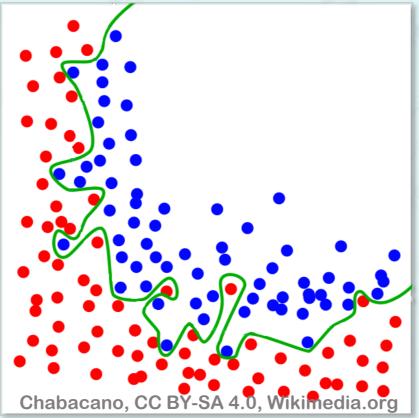
5717116302

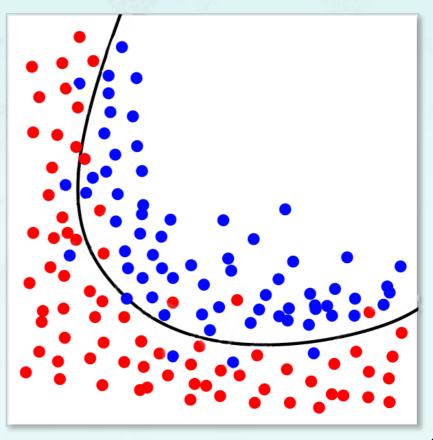




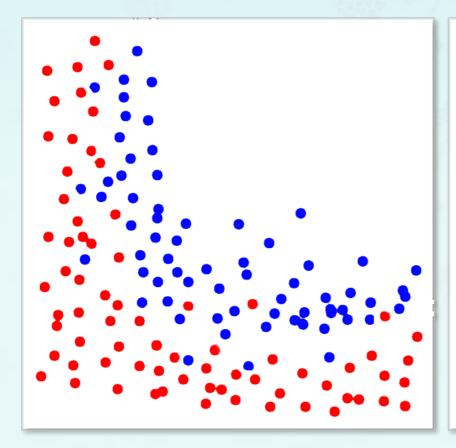


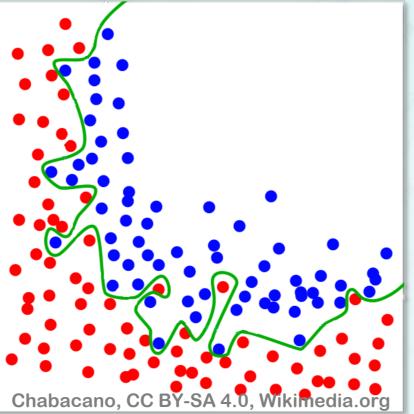


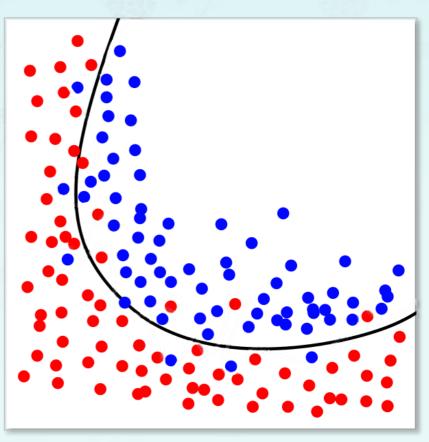




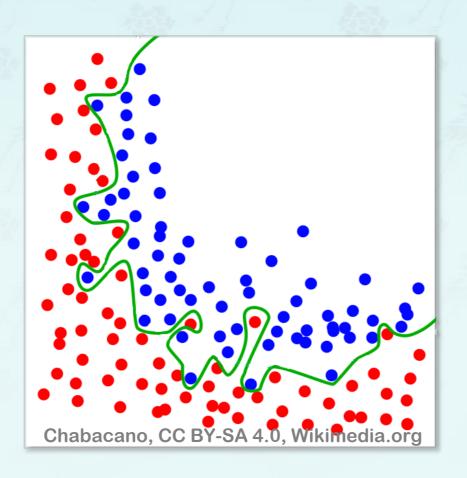
- A Better Classifier?
 - 1. Green line
 - 2. Black line







- Overfitting
- Underfitting



Perceptron

Summary

- Perceptron History
- Perceptron Structure
- Perceptron Learning
- Binary Classifier and Activation Function
- Overfitting and Underfitting

Next

4-2 Perceptron Algorithm

Week 4(1/3)

Activation Function

Machine Learning with Python

Handong Global University Prof. Youngsup Kim idebtor@gmail.com

여러분 곁에 항상 열려 있는 K-MOOC 강의실에서 만나 뵙기를 바랍니다.